

# Modelos de Computación.

## Práctica 2.

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### Resumen

Realización de al menos cuatro computaciones manuales para cada uno de los L-programas analizados en clase de teoría.

## 1. Función Asignación

### 1.1. Computación para la entrada $X = 0$

$$(1, \langle X = 0, Z = 0, Y = 0 \rangle) \sim (2, \langle X = 0, Z = 0, Y = 0 \rangle) \sim (7, \langle X = 0, Z = 0, Y = 0 \rangle) \sim \\ (8, \langle X = 0, Z = 0, Y = 0 \rangle) \sim (12, \langle X = 0, Z = 0, Y = 0 \rangle)$$

### 1.2. Computación para la entrada $X = 1$

$$(1, \langle X = 1, Z = 0, Y = 0 \rangle) \sim (3, \langle X = 1, Z = 0, Y = 0 \rangle) \sim (4, \langle X = 0, Z = 0, Y = 0 \rangle) \sim \\ (5, \langle X = 0, Z = 0, Y = 1 \rangle) \sim (6, \langle X = 0, Z = 1, Y = 1 \rangle) \sim (1, \langle X = 0, Z = 1, Y = 1 \rangle) \sim \\ (2, \langle X = 0, Z = 1, Y = 1 \rangle) \sim (7, \langle X = 0, Z = 1, Y = 1 \rangle) \sim (9, \langle X = 0, Z = 1, Y = 1 \rangle) \sim \\ (10, \langle X = 0, Z = 0, Y = 1 \rangle) \sim (11, \langle X = 1, Z = 0, Y = 1 \rangle) \sim (7, \langle X = 1, Z = 0, Y = 1 \rangle) \sim \\ (8, \langle X = 1, Z = 0, Y = 1 \rangle) \sim (12, \langle X = 1, Z = 0, Y = 1 \rangle)$$

### 1.3. Computación para la entrada $X = 2$

$$(1, \langle X = 2, Z = 0, Y = 0 \rangle) \sim (3, \langle X = 2, Z = 0, Y = 0 \rangle) \sim (4, \langle X = 1, Z = 0, Y = 0 \rangle) \sim \\ (5, \langle X = 1, Z = 0, Y = 1 \rangle) \sim (6, \langle X = 1, Z = 1, Y = 1 \rangle) \sim (1, \langle X = 1, Z = 1, Y = 1 \rangle) \sim \\ (3, \langle X = 1, Z = 1, Y = 1 \rangle) \sim (4, \langle X = 0, Z = 1, Y = 1 \rangle) \sim (5, \langle X = 0, Z = 1, Y = 2 \rangle) \sim \\ (6, \langle X = 0, Z = 2, Y = 2 \rangle) \sim (1, \langle X = 0, Z = 2, Y = 2 \rangle) \sim (2, \langle X = 0, Z = 2, Y = 2 \rangle) \sim \\ (7, \langle X = 0, Z = 2, Y = 2 \rangle) \sim (9, \langle X = 0, Z = 2, Y = 2 \rangle) \sim (10, \langle X = 0, Z = 1, Y = 2 \rangle) \sim \\ (11, \langle X = 1, Z = 1, Y = 2 \rangle) \sim (7, \langle X = 1, Z = 1, Y = 2 \rangle) \sim (9, \langle X = 1, Z = 1, Y = 2 \rangle) \sim \\ (10, \langle X = 1, Z = 0, Y = 2 \rangle) \sim (11, \langle X = 2, Z = 0, Y = 2 \rangle) \sim (7, \langle X = 2, Z = 0, Y = 2 \rangle) \sim \\ (8, \langle X = 2, Z = 0, Y = 2 \rangle) \sim (12, \langle X = 2, Z = 0, Y = 2 \rangle)$$

**1.4. Computación para la entrada  $X = 3$** 

$$\begin{aligned}
&(1, < X = 3, Z = 0, Y = 0 >) \sim (3, < X = 3, Z = 0, Y = 0 >) \sim (4, < X = 2, Z = 0, Y = 0 >) \sim \\
&(5, < X = 2, Z = 0, Y = 1 >) \sim (6, < X = 2, Z = 1, Y = 1 >) \sim (1, < X = 2, Z = 1, Y = 1 >) \sim \\
&(3, < X = 2, Z = 1, Y = 1 >) \sim (4, < X = 1, Z = 1, Y = 1 >) \sim (5, < X = 1, Z = 1, Y = 2 >) \sim \\
&(6, < X = 1, Z = 2, Y = 2 >) \sim (1, < X = 1, Z = 2, Y = 2 >) \sim (3, < X = 1, Z = 2, Y = 2 >) \sim \\
&(4, < X = 0, Z = 2, Y = 2 >) \sim (5, < X = 0, Z = 2, Y = 3 >) \sim (6, < X = 0, Z = 3, Y = 3 >) \sim \\
&(1, < X = 0, Z = 3, Y = 3 >) \sim (2, < X = 0, Z = 3, Y = 3 >) \sim (7, < X = 0, Z = 3, Y = 3 >) \sim \\
&(9, < X = 0, Z = 3, Y = 3 >) \sim (10, < X = 0, Z = 2, Y = 3 >) \sim (11, < X = 1, Z = 2, Y = 3 >) \sim \\
&(7, < X = 1, Z = 2, Y = 3 >) \sim (9, < X = 1, Z = 2, Y = 3 >) \sim (10, < X = 1, Z = 1, Y = 3 >) \sim \\
&(11, < X = 2, Z = 1, Y = 3 >) \sim (7, < X = 2, Z = 1, Y = 3 >) \sim (9, < X = 2, Z = 1, Y = 3 >) \sim \\
&(10, < X = 2, Z = 0, Y = 3 >) \sim (11, < X = 3, Z = 0, Y = 3 >) \sim (7, < X = 3, Z = 0, Y = 3 >) \sim \\
&\quad (8, < X = 3, Z = 0, Y = 3 >) \sim (12, < X = 3, Z = 0, Y = 3 >)
\end{aligned}$$

**2. Función Suma****2.1. Computación para la entrada  $X_1 = 0, X_2 = 0$** 

$$\begin{aligned}
&(1, < X_1 = 0, X_2 = 0, Z = 0, Y = 0 >) \sim (2, < X_1 = 0, X_2 = 0, Z = 0, Y = 0 >) \sim \\
&(3, < X_1 = 0, X_2 = 0, Z = 0, Y = 0 >) \sim (4, < X_1 = 0, X_2 = 0, Z = 0, Y = 0 >) \sim \\
&\quad (8, < X_1 = 0, X_2 = 0, Z = 0, Y = 0 >)
\end{aligned}$$

**2.2. Computación para la entrada  $X_1 = 1, X_2 = 0$** 

$$\begin{aligned}
&(1, < X_1 = 1, X_2 = 0, Z = 0, Y = 0 >) \sim (2, < X_1 = 1, X_2 = 0, Z = 0, Y = 1 >) \sim \\
&(3, < X_1 = 1, X_2 = 0, Z = 0, Y = 1 >) \sim (4, < X_1 = 1, X_2 = 0, Z = 0, Y = 1 >) \sim \\
&\quad (8, < X_1 = 1, X_2 = 0, Z = 0, Y = 1 >)
\end{aligned}$$

**2.3. Computación para la entrada  $X_1 = 1, X_2 = 1$** 

$$\begin{aligned}
&(1, < X_1 = 1, X_2 = 1, Z = 0, Y = 0 >) \sim (2, < X_1 = 1, X_2 = 1, Z = 0, Y = 1 >) \sim \\
&(3, < X_1 = 1, X_2 = 1, Z = 1, Y = 1 >) \sim (5, < X_1 = 1, X_2 = 1, Z = 1, Y = 1 >) \sim \\
&(6, < X_1 = 1, X_2 = 1, Z = 0, Y = 1 >) \sim (7, < X_1 = 1, X_2 = 1, Z = 0, Y = 2 >) \sim \\
&(3, < X_1 = 1, X_2 = 1, Z = 0, Y = 2 >) \sim (4, < X_1 = 1, X_2 = 1, Z = 0, Y = 2 >) \sim \\
&\quad (8, < X_1 = 1, X_2 = 1, Z = 0, Y = 2 >)
\end{aligned}$$

**2.4. Computación para la entrada  $X_1 = 3, X_2 = 0$** 

$$\begin{aligned}
&(1, < X_1 = 3, X_2 = 0, Z = 0, Y = 0 >) \sim (2, < X_1 = 3, X_2 = 0, Z = 0, Y = 3 >) \sim \\
&(3, < X_1 = 3, X_2 = 0, Z = 0, Y = 3 >) \sim (4, < X_1 = 3, X_2 = 0, Z = 0, Y = 3 >) \sim \\
&\quad (8, < X_1 = 3, X_2 = 0, Z = 0, Y = 3 >)
\end{aligned}$$

### 3. Función Resta Restringida

#### 3.1. Computación para la entrada $X_1 = 0, X_2 = 0$

$$\begin{aligned} (1, < X_1 = 0, X_2 = 0, Z = 0, Y = 0 >) &\sim (2, < X_1 = 0, X_2 = 0, Z = 0, Y = 0 >) \sim \\ (3, < X_1 = 0, X_2 = 0, Z = 0, Y = 0 >) &\sim (4, < X_1 = 0, X_2 = 0, Z = 0, Y = 0 >) \sim \\ (10, < X_1 = 0, X_2 = 0, Z = 0, Y = 0 >) \end{aligned}$$

#### 3.2. Computación para la entrada $X_1 = 1, X_2 = 0$

$$\begin{aligned} (1, < X_1 = 1, X_2 = 0, Z = 0, Y = 0 >) &\sim (2, < X_1 = 1, X_2 = 0, Z = 0, Y = 1 >) \sim \\ (3, < X_1 = 1, X_2 = 0, Z = 0, Y = 1 >) &\sim (4, < X_1 = 1, X_2 = 0, Z = 0, Y = 1 >) \sim \\ (10, < X_1 = 1, X_2 = 0, Z = 0, Y = 1 >) \end{aligned}$$

#### 3.3. Computación para la entrada $X_1 = 1, X_2 = 1$

$$\begin{aligned} (1, < X_1 = 1, X_2 = 1, Z = 0, Y = 0 >) &\sim (2, < X_1 = 1, X_2 = 1, Z = 0, Y = 1 >) \sim \\ (3, < X_1 = 1, X_2 = 1, Z = 1, Y = 1 >) &\sim (5, < X_1 = 1, X_2 = 1, Z = 1, Y = 1 >) \sim \\ (7, < X_1 = 1, X_2 = 1, Z = 1, Y = 1 >) &\sim (8, < X_1 = 1, X_2 = 1, Z = 1, Y = 0 >) \sim \\ (9, < X_1 = 1, X_2 = 1, Z = 0, Y = 0 >) &\sim (3, < X_1 = 1, X_2 = 1, Z = 0, Y = 0 >) \sim \\ (4, < X_1 = 1, X_2 = 1, Z = 0, Y = 0 >) &\sim (10, < X_1 = 1, X_2 = 1, Z = 0, Y = 0 >) \end{aligned}$$

#### 3.4. Computación para la entrada $X_1 = 3, X_2 = 1$

$$\begin{aligned} (1, < X_1 = 3, X_2 = 1, Z = 0, Y = 0 >) &\sim (2, < X_1 = 3, X_2 = 1, Z = 0, Y = 3 >) \sim \\ (3, < X_1 = 3, X_2 = 1, Z = 1, Y = 3 >) &\sim (5, < X_1 = 3, X_2 = 1, Z = 1, Y = 1 >) \sim \\ (7, < X_1 = 3, X_2 = 1, Z = 1, Y = 1 >) &\sim (8, < X_1 = 3, X_2 = 1, Z = 1, Y = 2 >) \sim \\ (9, < X_1 = 3, X_2 = 1, Z = 0, Y = 2 >) &\sim (3, < X_1 = 3, X_2 = 1, Z = 0, Y = 2 >) \sim \\ (4, < X_1 = 3, X_2 = 1, Z = 0, Y = 2 >) &\sim (10, < X_1 = 3, X_2 = 1, Z = 0, Y = 2 >) \end{aligned}$$

### 4. Función Producto

#### 4.1. Computación para la entrada $X_1 = 0, X_2 = 0$

$$\begin{aligned} (1, < X_1 = 0, X_2 = 0, Z_1 = 0, Z_2 = 0, Y = 0 >) &\sim (2, < X_1 = 0, X_2 = 0, Z_1 = 0, Z_2 = 0, Y = 0 >) \sim \\ (3, < X_1 = 0, X_2 = 0, Z_1 = 0, Z_2 = 0, Y = 0 >) &\sim (8, < X_1 = 0, X_2 = 0, Z_1 = 0, Z_2 = 0, Y = 0 >) \end{aligned}$$

#### 4.2. Computación para la entrada $X_1 = 1, X_2 = 0$

$$\begin{aligned} (1, < X_1 = 1, X_2 = 0, Z_1 = 0, Z_2 = 0, Y = 0 >) &\sim (2, < X_1 = 1, X_2 = 0, Z_1 = 0, Z_2 = 0, Y = 0 >) \sim \\ (3, < X_1 = 1, X_2 = 0, Z_1 = 0, Z_2 = 0, Y = 0 >) &\sim (8, < X_1 = 1, X_2 = 0, Z_1 = 0, Z_2 = 0, Y = 0 >) \end{aligned}$$

**4.3. Computación para la entrada  $X_1 = 1, X_2 = 1$** 

$$\begin{aligned}
(1, < X_1 = 1, X_2 = 1, Z_1 = 0, Z_2 = 0, Y = 0 >) \sim (2, < X_1 = 1, X_2 = 1, Z_1 = 0, Z_2 = 1, Y = 0 >) \sim \\
(4, < X_1 = 1, X_2 = 1, Z_1 = 0, Z_2 = 1, Y = 0 >) \sim (5, < X_1 = 1, X_2 = 1, Z_1 = 0, Z_2 = 0, Y = 0 >) \sim \\
(6, < X_1 = 1, X_2 = 1, Z_1 = 1, Z_2 = 0, Y = 0 >) \sim (7, < X_1 = 1, X_2 = 1, Z_1 = 1, Z_2 = 0, Y = 1 >) \sim \\
(2, < X_1 = 1, X_2 = 1, Z_1 = 1, Z_2 = 0, Y = 1 >) \sim (3, < X_1 = 1, X_2 = 1, Z_1 = 1, Z_2 = 0, Y = 1 >) \sim \\
(8, < X_1 = 1, X_2 = 1, Z_1 = 1, Z_2 = 0, Y = 1 >)
\end{aligned}$$

**4.4. Computación para la entrada  $X_1 = 0, X_2 = 1$** 

$$\begin{aligned}
(1, < X_1 = 0, X_2 = 1, Z_1 = 0, Z_2 = 0, Y = 0 >) \sim (2, < X_1 = 0, X_2 = 1, Z_1 = 0, Z_2 = 1, Y = 0 >) \sim \\
(4, < X_1 = 0, X_2 = 1, Z_1 = 0, Z_2 = 1, Y = 0 >) \sim (5, < X_1 = 0, X_2 = 1, Z_1 = 0, Z_2 = 0, Y = 0 >) \sim \\
(6, < X_1 = 0, X_2 = 1, Z_1 = 0, Z_2 = 0, Y = 0 >) \sim (7, < X_1 = 0, X_2 = 1, Z_1 = 0, Z_2 = 0, Y = 0 >) \sim \\
(2, < X_1 = 0, X_2 = 1, Z_1 = 0, Z_2 = 0, Y = 0 >) \sim (3, < X_1 = 0, X_2 = 1, Z_1 = 0, Z_2 = 0, Y = 0 >) \sim \\
(8, < X_1 = 0, X_2 = 1, Z_1 = 0, Z_2 = 0, Y = 0 >)
\end{aligned}$$