

Oxiflex - A Constraint Programming Solver for MiniZinc written in Rust

Bachelor's thesis

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Abstract

This thesis discusses the thesis template using some examples of the Turing Machine.

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1

Introduction

2

Constraint Satisfaction Problems

Constraint Satisfaction Problems (CSP) are mathematical questions defined as a finite set of variables whose value must satisfy a number of constraints or limitations. When solely talking about the problem without the algorithmic finding of a solution, these are called Constraint Networks.

Example:

$$w = \{1, 2, 3, 4\}$$

$$y = \{1, 2, 3, 4\}$$

$$x = \{1, 2, 3\}$$

$$z = \{1, 2, 3\}$$

where:

$$w = 2 * x$$

$$w < z$$

$$y > z$$

We define variables w , y , x and z . Variables w and y can both have one value from $\{1, 2, 3, 4\}$ and variables x and z can have a value from $\{1, 2, 3\}$. The constraints then restrict which values are valid from their respective domains. Here $w = 2 \times x$ restrict the value of x to be double of w for example. If there are no constraints for variables, the constraints are still there but they allow every assignment. These constraints are called trivial constraints and are usually omitted.

In this example we define constraints in a mathematical notation. There are no formal restrictions on stating constraints neither by their complexity nor by the number of variables involved. To make it easier to reason about, we model constraints as binary constraint sets. Constraints are then sets of valid value pairs for two specific variables. Instead of stating the desired relation between any variables, we list all valid value pair tuples in a set. Constraint $w < z$ then becomes $(R_{wz} = \{(1, 2), (1, 3), (2, 3)\})$ which contains all possible value pairs for the two variables w and z .

We define Constraint Networks formally:

A (binary) constraint network is a 3-tuple $C = \langle V, \text{dom}, (R_{uv}) \rangle$ such that:

- V is a non-empty and finite set of variables,
- dom is a function that assigns a non-empty and finite domain to each variable $v \in V$, and
- $(R_{uv})_{u,v \in V, u \neq v}$ is a family of binary relations (constraints) over V where for all $u \neq v : R_{uv} \subseteq \text{dom}(u) \times \text{dom}(v)$

And we define our example formally:

$C = \langle V, \text{dom}, (R_{uv}) \rangle$ with

- variables:
 $V = \{w, x, y, z\}$
- domains:
 $\text{dom}(w) = \text{dom}(y) = \{1, 2, 3, 4\}$
 $\text{dom}(x) = \text{dom}(z) = \{1, 2, 3\}$
- constraints:
 $R_{wx} = \{(2, 1), (4, 2)\}$
 $R_{wz} = \{(1, 2), (1, 3), (2, 3)\}$
 $R_{yz} = \{(2, 1), (3, 1), (3, 2), (4, 1), (4, 2), (4, 3)\}$

The goal in CSP is then to find a Assignment that satisfies all constraints. For this simple example a possible assignment would be $(w \mapsto 2), (x \mapsto 1), (y \mapsto 4), (z \mapsto 3)$.

2.1 MiniZinc

MiniZinc [1] is a free and open-source constraint modeling language developed at and by Monash University in Australia. It allows us to express Constraint Satisfaction Problems in a mathematical notation-like way.

MiniZinc example

```
var 1..4: w;  
var 1..4: y;  
var 1..3: x;  
var 1..3: z;  
  
constraint w = 2 × x;  
constraint w < z;  
constraint y > z;  
  
solve satisfy;
```

MiniZinc is only the language to express a problem domain. Once a problem domain is specified in MiniZinc we can give the problem to multiple solvers to solve it each. In this way we can compare the performance of various solvers on the same problem domain. MiniZinc Domain files have the file extension `.mzn`.

MiniZinc also provides a way to parametrize a problem domain. This is a great way to scale a problem space up and see how increasing the problem space affects the solving speed. A great example for this is the Queens Problem (See Section 2.2). We define the Queens Problem domain once and can then run specific problem instances for different n . This makes it really easy to compare the solving speed for the queens problem when $n = 8$, $n = 16$ or $n = 32$. Files where we specify parameters for MiniZinc files are called data files and have the extension `.dzn`. We can then combine `.mzn` files with `.dzn` files to create FlatZinc files.

2.1.1 FlatZinc

FlatZinc is a simpler problem specification language provided by the MiniZinc package. It is designed to be used by solvers directly. MiniZinc files are translated to FlatZinc files in a pre-solving step. FlatZinc files have the file extension `.fzn`.

Translating from MiniZinc to FlatZinc maps more advanced instructions from MiniZinc to primitives supported in FlatZinc. An analogy to this translation is compiling a C program to Assembly where MiniZinc is C and FlatZinc is Assembly. FlatZinc therefore requires solvers to support a set of standard constraints called "FlatZinc builtins". Builtins need to be implemented to be a fully compatible FlatZinc solver.

Simple example translated to FlatZinc

```

array [1..2] of int: x_introduced_2_ = [1,-2];
array [1..2] of int: x_introduced_3_ = [1,-1];
array [1..2] of int: x_introduced_4_ = [-1,1];
var 2..4: w:: output_var:: is_defined_var;
var 1..4: y:: output_var;
var 1..3: x:: output_var;
var 1..3: z:: output_var;
constraint int_lin_eq(x_introduced_2_,[w,x],0):: defines_var(w);
constraint int_lin_le(x_introduced_3_,[w,z],-1);
constraint int_lin_le(x_introduced_4_,[y,z],-1);
solve satisfy;

```

The translation of the variable declarations is straight forward. But our constraints are each split into two parts and translated into linear combinations. For example is constraint $w = 2 \times x$ translated to the builtin called `int_lin_eq` which is defined as follows:

int_lin_eq builtin

```

predicate int_lin_eq(array [int] of int: as,
array [int] of var int: bs,
int: c)

```

With the restriction on given parameters to the constraint.

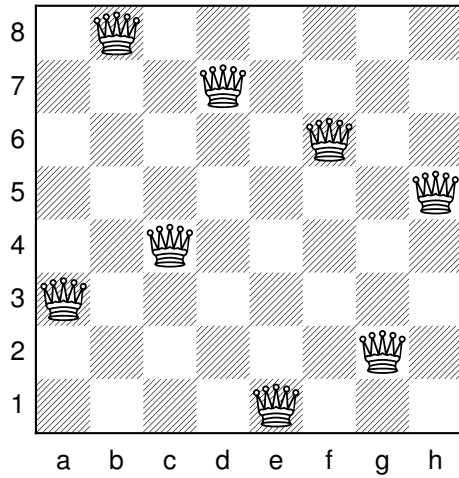
int_lin_eq builtin constraint

$$c = \sum_i as[i] \times bs[i] \quad (2.1)$$

Note that MiniZinc already does some basic level of inference. The FlatZinc variable w can only have values between 2 and 4 in the translated FlatZinc file. But in the MiniZinc file we defined w with the domain $\{1, 2, 3, 4\}$. This means MiniZinc infers that w can not be value 1 and removes it from its domain declaration. Due to the constraint $w = 2 \times x$, the variable w has to be double of x and x must have at least value 1. Therefore excluding 1 as possible value for w .

2.2 Queens Problem

Also called the Eight Queens Puzzle, the Queens Problem is an example of a classic constraint satisfaction problem that involves placing eight queens on an 8x8 chessboard in such a way that no two queens threaten each other. That is, no two queens can share the same row, column, or diagonal.



The Eighth Queens Puzzle is really good suited as an example problem domain for constraint satisfaction problems because it is easy to understand and can also easily be scaled up to increase complexity for a solver. By generalizing the problem from a fixed 8×8 grid size to an $n \times n$ grid with n queens, the problem remains the same in principle, but gets way harder to solve.

MiniZinc Model for N-Queens Problem

```
int: n;

array [1..n] of var 1..n: q;

predicate
noattack(int: i, int: j, var int: qi, var int: qj) =
qi != qj /\
qi + i != qj + j /\
qi - i != qj - j;

constraint
forall (i in 1..n, j in i+1..n) (
noattack(i, j, q[i], q[j])
);

solve satisfy;
```

This MiniZinc model defines an array of variables q where each index corresponds to a column on the chessboard and the value at each index represents the row position of the queen in that column. The constraints ensure that no two queens are on the same row, column or diagonal.

This model is from a past MiniZinc challenge by Reza Rafeh July 2005 and Peter Stuckey September 30 2006. See <https://github.com/MiniZinc/minizinc-benchmarks/blob/master/>

queens/queens.mzn for reference.

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Oxiflex

As part of this thesis we present oxiflex, a minimal constraint satisfaction problem solver from scratch for MiniZinc written in rust. Oxiflex is a FlatZinc solver that can be used as an backend to MiniZinc. This means oxiflex supports the minimal requirements for a solver to take advantage of the MiniZinc toolchain.

Oxiflex is open-source and available under the MIT license under <https://github.com/glklimmer/oxiflex>.

3.1 Rust

3.2 Dependencies

3.2.1 flatzinc

A FlatZinc parser for rust.

3.2.2 structopt

3.2.3 hyperfine

3.3 Solver

3.3.1 Naive Backtracking

3.4 Inference

3.4.1 Forward Checking

3.4.2 Arc Consistency

4

Results

Results, Graphs and stuff.

5

Conclusion

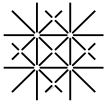
Time for some interpretation.

Bibliography

- [1] N. Nethercote, P.J. Stuckey, R. Becket, S. Brand, G.J. Duck, and G. Tack. Minizinc: Towards a standard cp modelling language. In C. Bessiere, editor, *Proceedings of the 13th International Conference on Principles and Practice of Constraint Programming*, volume 4741 of *LNCS*, pages 529–543. Springer, 2007.



Appendix



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