

# **Oxiflex - A Constraint Programming Solver for MiniZinc written in Rust**

Bachelor's thesis

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## **Abstract**

This thesis discusses the thesis template using some examples of the Turing Machine.

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# 1

## Introduction

# 2

## Constraint Satisfaction Problems

Constraint Satisfaction Problems (CSP) [5] are mathematical questions defined as a finite set of variables whose value must satisfy a number of constraints or limitations. When solely talking about the problem without the algorithmic finding of a solution, these are called Constraint Networks. CSPs are typical NP-complete combinatorial problems in the field of AI.

Example:

$$w = \{1, 2, 3, 4\}$$

$$y = \{1, 2, 3, 4\}$$

$$x = \{1, 2, 3\}$$

$$z = \{1, 2, 3\}$$

where:

$$w = 2 * x$$

$$w < z$$

$$y > z$$

We define variables  $w$ ,  $y$ ,  $x$  and  $z$ . Variables  $w$  and  $y$  can both have one value from  $\{1, 2, 3, 4\}$  and variables  $x$  and  $z$  can have a value from  $\{1, 2, 3\}$ . The constraints then restrict which values are valid from their respective domains. Here  $w = 2 \times x$  restrict the value of  $x$  to be double of  $w$  for example. If there are no constraints for variables, the constraints are still there but they allow every assignment. These constraints are called trivial constraints and are usually omitted.

In this example we define constraints in a mathematical notation. There are no formal restrictions on stating constraints neither by their complexity nor by the number of variables involved. To make it easier to reason about, we model constraints as binary constraint sets. Constraints are then sets of valid value pairs for two specific variables. Instead of stating the desired relation between any variables, we list all valid value pair tuples in a set. Constraint  $w < z$  then becomes  $(R_{wz} = \{(1, 2), (1, 3), (2, 3)\})$  which contains all possible value pairs for the two variables  $w$  and  $z$ .

We define Constraint Networks formally:

A (binary) constraint network is a 3-tuple  $C = \langle V, \text{dom}, (R_{uv}) \rangle$  such that:

- $V$  is a non-empty and finite set of variables,
- $\text{dom}$  is a function that assigns a non-empty and finite domain to each variable  $v \in V$ , and
- $(R_{uv})_{u,v \in V, u \neq v}$  is a family of binary relations (constraints) over  $V$  where for all  $u \neq v : R_{uv} \subseteq \text{dom}(u) \times \text{dom}(v)$

And we define our example formally:

$C = \langle V, \text{dom}, (R_{uv}) \rangle$  with

- variables:  
 $V = \{w, x, y, z\}$
- domains:  
 $\text{dom}(w) = \text{dom}(y) = \{1, 2, 3, 4\}$   
 $\text{dom}(x) = \text{dom}(z) = \{1, 2, 3\}$
- constraints:  
 $R_{wx} = \{(2, 1), (4, 2)\}$   
 $R_{wz} = \{(1, 2), (1, 3), (2, 3)\}$   
 $R_{yz} = \{(2, 1), (3, 1), (3, 2), (4, 1), (4, 2), (4, 3)\}$

The goal in CSP is then to find a Assignment that satisfies all constraints. For this simple example a possible assignment would be  $(w \mapsto 2), (x \mapsto 1), (y \mapsto 4), (z \mapsto 3)$ .

## 2.1 MiniZinc

MiniZinc [7] is a free and open-source constraint modeling language developed at and by Monash University in Australia. It allows us to express Constraint Satisfaction Problems in a mathematical notation-like way.

**MiniZinc example**

```
var 1..4: w;  
var 1..4: y;  
var 1..3: x;  
var 1..3: z;  
  
constraint w = 2 × x;  
constraint w < z;  
constraint y > z;  
  
solve satisfy;
```

MiniZinc is only the language to express a problem domain. Once a problem domain is specified in MiniZinc we can give the problem to multiple solvers to solve it each. In this way we can compare the performance of various solvers on the same problem domain. MiniZinc Domain files have the file extension `.mzn`.

MiniZinc also provides a way to parametrize a problem domain. This is a great way to scale a problem space up and see how increasing the problem space affects the solving speed. A great example for this is the Queens Problem (See Section 2.2). We define the Queens Problem domain once and can then run specific problem instances for different  $n$ . This makes it really easy to compare the solving speed for the queens problem when  $n = 8$ ,  $n = 16$  or  $n = 32$ . Files where we specify parameters for MiniZinc files are called data files and have the extension `.dzn`. We can then combine `.mzn` files with `.dzn` files to create FlatZinc files.

### 2.1.1 FlatZinc

FlatZinc is a simpler problem specification language provided by the MiniZinc package. It is designed to be used by solvers directly. MiniZinc files are translated to FlatZinc files in a pre-solving step. FlatZinc files have the file extension `.fzn`.

Translating from MiniZinc to FlatZinc maps more advanced instructions from MiniZinc to primitives supported in FlatZinc. An analogy to this translation is compiling a C program to Assembly where MiniZinc is C and FlatZinc is Assembly. FlatZinc therefore requires solvers to support a set of standard constraints called "FlatZinc builtins". Builtins need to be implemented to be a fully compatible FlatZinc solver.



## Simple example translated to FlatZinc

```

array [1..2] of int: x_introduced_2_ = [1,-2];
array [1..2] of int: x_introduced_3_ = [1,-1];
array [1..2] of int: x_introduced_4_ = [-1,1];
var 2..4: w:: output_var:: is_defined_var;
var 1..4: y:: output_var;
var 1..3: x:: output_var;
var 1..3: z:: output_var;
constraint int_lin_eq(x_introduced_2_,[w,x],0):: defines_var(w);
constraint int_lin_le(x_introduced_3_,[w,z],-1);
constraint int_lin_le(x_introduced_4_,[y,z],-1);
solve satisfy;

```

The translation of the variable declarations is straight forward. But our constraints are each split into two parts and translated into linear combinations. For example is constraint  $w = 2 \times x$  translated to the builtin called `int_lin_eq` which is defined as follows:

## int\_lin\_eq builtin

```

predicate int_lin_eq(array [int] of int: as,
array [int] of var int: bs,
int: c)

```

With the restriction on given parameters to the constraint.

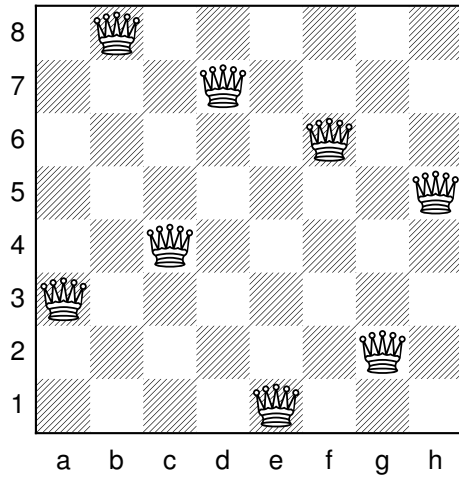
## int\_lin\_eq builtin constraint

$$c = \sum_i as[i] \times bs[i] \quad (2.1)$$

Note that MiniZinc already does some basic level of inference. The FlatZinc variable  $w$  can only have values between 2 and 4 in the translated FlatZinc file. But in the MiniZinc file we defined  $w$  with the domain  $\{1, 2, 3, 4\}$ . This means MiniZinc infers that  $w$  can not be value 1 and removes it from its domain declaration. Due to the constraint  $w = 2 \times x$ , the variable  $w$  has to be double of  $x$  and  $x$  must have at least value 1. Therefore excluding 1 as possible value for  $w$ .

## 2.2 Queens Problem

Also called the Eight Queens Puzzle, the Queens Problem is an example of a classic constraint satisfaction problem that involves placing eight queens on an 8x8 chessboard in such a way that no two queens threaten each other. That is, no two queens can share the same row, column, or diagonal.



The Eighth Queens Puzzle is really good suited as an example problem domain for constraint satisfaction problems because it is easy to understand and can also easily be scaled up to increase complexity for a solver. By generalizing the problem from a fixed  $8 \times 8$  grid size to an  $n \times n$  grid with  $n$  queens, the problem remains the same in principle, but gets way harder to solve. See the following example of the queens problem in minizinc [10].

#### MiniZinc Model for N-Queens Problem

```
int: n;

array [1..n] of var 1..n: q;

predicate
noattack(int: i, int: j, var int: qi, var int: qj) =
qi != qj /\
qi + i != qj + j /\
qi - i != qj - j;

constraint
forall (i in 1..n, j in i+1..n) (
noattack(i, j, q[i], q[j])
);

solve satisfy;
```

This MiniZinc model defines an array of variables  $q$  where each index corresponds to a column on the chessboard and the value at each index represents the row position of the queen in that column. The constraints ensure that no two queens are on the same row, column or diagonal.

# 3

## Solving Constraint Satisfaction Problems

Constraints satisfaction problems on finite domains are typically solved using a form of search. We search for a solution to the constraint network by trying out all possible values until a solution is found. That is, a valid assignment of all variables with a value of their respective domain satisfying all constraints within the constraint network.

### 3.1 Naive Backtracking

Backtracking is a technique used to search a problem space for potential solutions [2]. It systematically organizes the search process by attempting to extend a partial solution step-by-step. If an extension of the current partial solution proves unfeasible at any stage, the algorithm "backtracks" to a previous, shorter partial solution and tries a different path. This method is particularly useful in solving constraint satisfaction problems, as demonstrated by the algorithm called NaiveBacktracking.

```
function NaiveBacktracking)
   $\langle V, \text{dom}, (R_{uv}) \rangle := C$ 
  if  $\alpha$  is inconsistent with  $C$ :
    return inconsistent

  if  $\alpha$  is a total assignment:
    return  $\alpha$ 

  select some variable  $v$  for which  $\alpha$  is not defined
  for each  $d \in \text{dom}(v)$  in some order:
     $\alpha' := \alpha \cup \{v \mapsto d\}$ 
     $\alpha'' := \text{NaiveBacktracking}(C, \alpha')$ 
    if  $\alpha'' \neq \text{inconsistent}$ :
      return  $\alpha''$ 

  return inconsistent
```

Input: constraint network  $C$  and partial assignment  $\alpha$  for  $C$ . On first invocation of Naive-Backtracking we pass an empty assignment  $\alpha = \emptyset$ .

Result: Total assignment (solution) of  $C$  or **inconsistent**.

This algorithm corresponds to Depth First Search (DFS). It assigns values to variables from their domains to form a partial assignment. This process continues until either all variables are assigned and a solution is found, or a constraint is violated. If a constraint is violated, the algorithm backtracks and tries a different value from the domain until a solution is found. If all possible assignments violate constraints, there is no solution. Finding a total assignment, that is an partial assignment that gives each variable a valid value from its domain, is finding a solution.

Backtracking is far from the best way to solve CSPs.

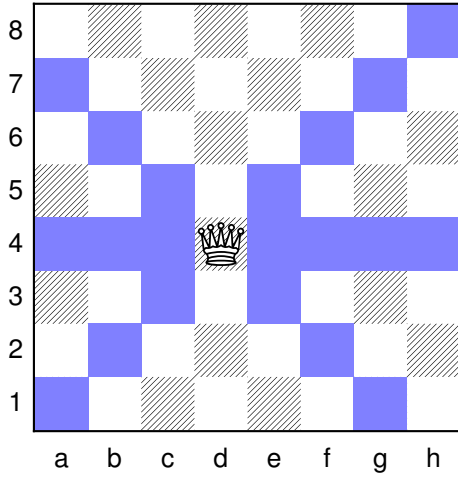
### 3.1.1 Variable Ordering

Backtracking in general does not specify in which order the search is done. For constraint satisfaction problems we want to assign critical variables early. Critical variables are variables that thighten the search space the most by their assignment. This can be done in multiple ways:

- **static order**  
Fixed order defined prior to search
- **dynamic order**  
Order depends on current search state and is calculated after each assignment

## 3.2 Inference

Inference allows us to modify our constraint network by thightening the constraint network. Thightening works by excluding values from domains of variables that we know are not possible. For example in the Queens Problem (See 2.2) if we place a Queen on  $d4$ , we can exclude the value 4 from all other files (chess term for column). We can also exclude all diagonally positioned squares like  $a1$ ,  $b2$ ,  $c3$  and so forth. See 3.2 for reference. Note that we do not need to do anything with the file the queen is on because we modeled the file to be a variable to solve for and a variable can only have one value anyways.



By removing impossible values from the remaining domains, we can tighten the resulting constraint network and have a smaller search space. We adjust our NaiveBacktracking approach by applying inference after each assignment of a variable. See the following for the NaiveBacktracking algorithm.

```
function BacktrackingWithInference( $C, \alpha$ )
```

```
   $\langle V, \text{dom}, (R_{uv}) \rangle := C$ 
```

```
  if  $\alpha$  is inconsistent with  $C$ :
```

```
    return inconsistent
```

```
  if  $\alpha$  is a total assignment:
```

```
    return  $\alpha$ 
```

```
   $C' := \langle V, \text{dom}', (R'_{uv}) \rangle := \text{copy of } C$ 
```

```
  apply inference to  $C'$ 
```

```
  if  $\text{dom}'(v) \neq \emptyset$  for all variables  $v$ :
```

```
    select some variable  $v$  for which  $\alpha$  is not defined
```

```
    for each  $d \in \text{copy of } \text{dom}'(v)$  in some order:
```

```
       $\alpha' := \alpha \cup \{v \mapsto d\}$ 
```

```
       $\text{dom}'(v) := \{d\}$ 
```

```
       $\alpha'' := \text{BacktrackingWithInference}(C', \alpha')$ 
```

```
      if  $\alpha'' \neq \text{inconsistent}$ :
```

```
        return  $\alpha''$ 
```

```
  return inconsistent
```

Note that we now have to copy the constraint network after each assignment which can introduce significant overhead for simple problems. The coping is needed because we still have to backtrack if we find an inconsistent assignment. When backtracking we have to

restore the domain for each variable again because it is possible that the domain had values that are possible again after backtracking.

### 3.2.1 Forward Checking

We start with a simple inference method called Forward Checking [3]. See the following algorithm.

```
function ForwardChecking( $C, \alpha$ )
  for each  $v \in$  unassigned variables in  $\alpha$ :
    for each constraint:
      if any  $d \in \text{dom}(v)$  in conflict:  $\text{dom}(v) = \text{dom}(v) \setminus d$ 
```

Forward checking is basically looking ahead in the future to see which values can be excluded from search after an assignment. By looking ahead we can omit the backtracking part that would result by finding a dead end. We check each value for each variable with the new assignment and remove all values that are not possible anymore from their respective domain.

### 3.2.2 Arc Consistency

Arc consistency excludes all impossible values from all domains of all variables in a given constraint network. Originally developed for vision problems [12] arc consistency is the generalization of forward checking. Forward checking enforces arc consistency for all variables with respect to the just assigned variable. Arc consistency does this for all variables. This makes forward checking a special case of arc consistency. See the following for formal definition.

#### Definition: Arc Consistent

Let  $C = \langle V, \text{dom}, (R_{uv}) \rangle$  be a constraint network.

- The variable  $v \in V$  is arc consistent with respect to another variable  $v' \in V$ , if for every value  $d \in \text{dom}(v)$  there exists a value  $d' \in \text{dom}(v')$  with  $\langle d, d' \rangle \in R_{vv'}$ .
- The constraint network  $C$  is arc consistent, if every variable  $v \in V$  is arc consistent with respect to every other variable  $v' \in V$ .

Note that for a variable pair the definition is not symmetrical. That means if  $v$  is arc consistent with respect to  $v'$ ,  $v'$  does not have to be arc consistent with respect to  $v$ .

#### 3.2.2.1 Enforcing Arc Consistency

There are multiple algorithms to enforce arc consistency [4] [1]. The simplest is called AC-1. It works by making use of a function called revise. The following function revise ensures arc consistency in one direction between two variables.

**function** revise( $C, v, v'$ ):

```

 $\langle V, \text{dom}, (R_{uv}) \rangle := C$ 
for each  $d \in \text{dom}(v)$ :
  if there is no  $d' \in \text{dom}(v')$  with  $\langle d, d' \rangle \in R_{vv'}$ :
    remove  $d$  from  $\text{dom}(v)$ 

```

The following algorithm AC-1 goes over each constraint and applies revise in both directions to each variable pair for each constraint until there was no change within its iteration of using revise.

**function** AC-1( $C$ ):

```

 $\langle V, \text{dom}, (R_{uv}) \rangle := C$ 
repeat
  for each nontrivial constraint  $R_{uv}$ :
    revise( $C, u, v$ )
    revise( $C, v, u$ )
until no domain has changed in this iteration

```

Building on AC-1, AC-3 tries to save redundant checks made by AC-1. Instead of just going over all constraints over and over, we go at least over all constraint once and revise variable pairs again only if needed. In AC-3 this can be achieved by using a queue. See the following for reference.

**function** AC-3( $C$ ):

```

 $\langle V, \text{dom}, (R_{uv}) \rangle := C$ 
queue :=  $\emptyset$ 
for each nontrivial constraint  $R_{uv}$ :
  insert  $\langle u, v \rangle$  into queue
  insert  $\langle v, u \rangle$  into queue

while queue  $\neq \emptyset$ :
  remove an arbitrary element  $\langle u, v \rangle$  from queue
  revise( $C, u, v$ )
  if  $\text{dom}(u)$  changed in the call to revise:
    for each  $w \in V \setminus \{u, v\}$  where  $R_{wu}$  is nontrivial:
      insert  $\langle w, u \rangle$  into queue

```

# 4

## Oxiflex

As part of this thesis we present **oxiflex**, a minimal constraint satisfaction problem solver from scratch for MiniZinc written in Rust. Oxiflex is a FlatZinc solver that can be used as an backend to MiniZinc. This means oxiflex supports the minimal requirements for a solver to take advantage of the MiniZinc toolchain. The idea is to have a minimal solver and exactly measure the impact of various improvements on it like forward checking or arc consistency.

Oxiflex is open-source and available under the MIT license under <https://github.com/glklimmer/oxiflex>.

### 4.1 Rust

Rust [6] is a general purpose systems programming language focused on safety and performance. It achieves these goals without using a garbage collector by ensuring memory safety through a system of ownership with strict compile-time checks enforced by the borrow checker. This makes Rust particularly well-suited for creating performance-critical applications like CSP solvers where control over resources is crucial. This makes Rust an ideal choice for developing oxiflex.

### 4.2 Dependencies

This work depends on previous work by others. This section highlights the components used by oxiflex.

#### 4.2.1 flatzinc

The library flatzinc [11] is a FlatZinc parser for Rust. It parses the FlatZinc format into Rust structures and variables.



### 4.2.2 structopt

The library structopt [8] is utilized to parse command-line arguments in oxiflex. This library simplifies setting up custom commands and options for oxiflex.

### 4.2.3 hyperfine

The library hyperfine [9] is a command-line benchmarking tool. We use hyperfine to measure and compare the performance of different solver strategies and optimizations.

## 4.3 Architecture

There are three main parts of oxiflex.

- parser
- model
- solver

### 4.3.1 parser

Using flatzinc 4.2.1 oxiflex reads an FlatZinc `.fzn` file and collects all parts needed to then construct a constraint satisfaction network. These include a list for parameters, variables and constraints. In order to also output the solution after solving the problem, MiniZinc makes use of annotations on FlatZinc elements. Variables that are needed for the output are annotated as `output_var`. There are two possible output annotations in FlatZinc: `output_var` and `output_array`.

### 4.3.2 model

After parsing the FlatZinc file into Rust structures that can be used directly, oxiflex starts to build useful structures to solve any given problem. This is where oxiflex creates a model containing variables with their respective domains and constraints. Models use HashMaps to keep track of its variables and their respective domains. This allows for constant access time to domains to either read or modify them after inference (3.2) for example. Constraints are saved by the model as a list (In rust this is a pointer, capacity, length triplet). Usually when checking if constraints are violated we either want all constraints or all constraints related to a variable. For this reason an additional HashMap is created that uses variable ids as key and points to a list in the heap. In rust this can be done by using reference counting. This results in two ways to access constraints. One that is just a list to iterate over all constraint and a hashmap to get all constraints that use a specific variable.

### 4.3.3 Limitations

There are some limitations due to time constraints that currently limit oxiflex as a universal MiniZinc solver.

Only binary constraints are supported. The reason for this is that the theory used to implement oxiflex is based on binary constraints. Therefore it made sense to also just support them at first.

Not all FlatZinc builtins are supported. The idea is to implement just the needed builtins for any given interesting problem domain.

## 4.4 Solver

### 4.4.1 Value Ordering

Oxiflex is able to use dynamic ordering of variables (not values) during search based on the number of constraints.

### 4.4.2 Forward Checking

### 4.4.3 Arc Consistency

# 5

## Results

Results, Graphs and stuff.

# 6

## Conclusion

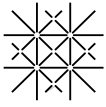
Time for some interpretation.

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## **Appendix**



## Declaration on Scientific Integrity

(including a Declaration on Plagiarism and Fraud)

Translation from German original

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