### December 6, 2014 18:00

# Contents

 $\S1$  [#1] SCF 1

## 1 SCF

This is Version 1 of the Hartree-Fock theory implemented for closed shells (RHF) and open shells (UHF-DODS) calculations.

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#### NAME SCF

Perform LCAO-MO-SCF calculation on a molecule.

#### **SYNOPSIS**

double precision function scf(H, C, nbasis, nelec, nfile,
irite, damp, interp, E, HF, V, R, Rold, Ubar, eps)
integer nbasis, nelec, nfile, irite
double precision damp, E
double precision H(ARB), C(ARB), HF(ARB), V(ARB), R(ARB)
double precision Rold(ARB), Ubar(ARB), eps(ARB)

#### DESCRIPTION

Perform LCAO-MO calculation of either closed-shell RHF type or more general open-shell (real) UHF-DODS type. The method is traditional Roothan repeated diagonalizations of Hartree-Fock matrix until self-consistency is reached:

$$\mathbf{F} \cdot \mathbf{C} = \mathbf{S} \cdot \mathbf{C} \cdot \epsilon$$

#### **ARGUMENTS**

**H** Input: One-electron Hamiltonian of size (nbasis x nbasis), i.e., matrix elements of one-electron operator

C Input/Output: An initial MO matrix - it must at least orthigonalize the basis. Normally, it is simply the orthogonalization matrix  $\mathbf{S}^{-\frac{1}{2}}$ . On output the SCF C matrix is placed here.

**nbasis** Input: the number of *spatial* orbitals in the basis (i.e., half of the number of the spin-basis set functions if  $nelec \ge 0$ )

**nelec** Input: The number of electrons in the system.

**nfile** The electron-repulsion file unit.

itite Channel number for convergence information or zero if this information is not necessary.

damp Hartree-Fock damping parameter.

**interp** Interpolation parameter. If 0 no interpolation will be undertaken.

HF Output: for use as the Fock matrix

V Workspace:

R Output: Density matrix

Rold Workspace:

**Ubar** Workspace:

eps Output: orbital energies (first nelec are the occupied orbitals)

E Output: Total HF electronic energy

#### RETURNS

YES if the calculation is converged in MAX\_SCF\_ITERATIONS NO if no convergence is met. Typical usage: if ( SCF(.....) .EQ. YES ) then output successful calculation

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```
/* STRUCTURES */
"scf.f" 1 \equiv
  @\mathbf{m} YES 0
  @m NO 100
  @\mathbf{m} \ \mathsf{ERR} \ -10
  @m OK 10
  @m\ END\_OF\_FILE\ -1
  @m\ NOT\_END\_OF\_FILE\ 55
  @m LAST_BLOCK 12
  @m\ NOT\_LAST\_BLOCK\ -12
       /* OPERATIONAL CONSTANTS */
  @m ARB 1
  @m BYTES_PER_INTEGER 4
  @m LEAST_BYTE 1
  @m\ NO\_OF\_TYPES\ 20
  @m INT_BLOCK_SIZE 20
  @m MAX_BASIS_FUNCTIONS 255
  @m MAX_PRIMITIVES 1000
  @m MAX_CENTRES 50
  @m MAX_ITERATIONS 60
  @m UHF_CALCULATION 11
  @m CLOSED_SHELL_CALCULATION 21
       /* OUTPUT STREAM UNITS */
  @m ERROR_OUTPUT_UNIT 6
  @m ERI_UNIT 17
  @m MAX_ITERATIONS 50
    integer function SCF(H, C, nbasis, nelec, nfile, irite, damp, interp, E, HF, V, R, Rold, Cbar,
          epsilon, crit)
      ⟨Global SCF Declarations #2⟩
      ⟨Internal SCF Declarations #3⟩
      ⟨Select SCF Type #4⟩
      (Set initial matrices and counters #5)
      do while((icon \neq 0) \land (kount < MAX\_ITERATIONS))
        ⟨Sigle SCF iteration #6⟩
      end do
      ⟨Write the output result #7⟩
      ⟨Formats #8⟩
     return
    end
```

This code is used in section 1.

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```
\langle Global SCF Declarations 1.1 \rangle \equiv
    implicit double precision (a - h, o - z)
    integer nbasis, nelec, nfile, irite
    integer interp
    double precision H(ARB), C(ARB), HF(ARB), V(ARB), R(ARB)
    double precision Rold(ARB), Cbar(ARB)
    double precision epsilon(ARB)
    double precision E, damp, crit
This code is used in section 1.
\langle \text{Internal SCF Declarations } 1.2 \rangle \equiv
    integer scftype, kount, maxit, nocc, m, mm, i
    double precision term, turm, Rsum
    double precision zero, half
    data zero, half/0.0 \cdot 10^{+00} D, 0.5 \cdot 10^{+00} D/
This code is used in section 1.
\langle Select SCF Type 1.3 \rangle \equiv
    if (nelec > zero) then /* closed shell case */
       scftype = CLOSED\_SHELL\_CALCULATION
       nocc = abs(nelec / 2)
       m = nbasis
    else /* open shell case */
       scftype = UHF\_CALCULATION
       nocc=nelec
       m = nbasis * 2
       call spinor(H, nbasis)
       call spinor(C, nbasis)
    end if
This code is used in section 1.
\langle Set initial matrices and counters 1.4\rangle \equiv
       /* basis set size */
    m = m * m
    \mathbf{do}\ i = 1,\ mm
       R(i) = zero;
       Rold(i) = zero
    end do
    SCF = YES
    kount = 0
    icon = 100
```

§1.5 [#6]

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```
\langle \text{ Sigle SCF iteration } 1.5 \rangle \equiv
    kount = kount + 1
    E = zero;
    icon = 0
    do i = 1, mm
      HF(i) = H(i)
      E = E + R(i) * HF(i)
    enddo
    call scfGR(R, HF, m, nfile)
    \mathbf{do} \ i = 1, \ mm
      E = E + R(i) * HF(i)
    enddo
    if (scftype \equiv UHF\_CALCULATION)
      E = half * E
    write (ERROR\_OUTPUT\_UNIT, 200) E
    call gtprd(C, HF, R, m, m, m)
    call gmprd(R, C, HF, m, m, m)
    call eigen(HF, Cbar, m)
    do i = 1, m
      epsilon(i) = HF(m * (i - 1) + i)
    enddo
    call gmprd(C, Cbar, V, m, m, m)
    call scfR(V, R, m, nocc)
    Rsum = zero
    \mathbf{do}\ i = 1,\ mm
      turm = R(i) - Rold(i)
      term = dabs(turm)
      Rold(i) = R(i)
      C(i) = V(i)
      if (term > crit)
         icon=icon+1
      Rsum = Rsum + term
      if (kount < interp)
         R(i) = R(i) - damp * turm
    enddo
```

This code is used in section 1.

 $\S1.6-\S2.1$  [#7-#11] UTILITIES 6

```
⟨ Write the output result 1.6⟩ ≡
    write (ERROR_OUTPUT_UNIT, 201) Rsum, icon

if ((kount ≡ MAX_ITERATIONS) ∧ (icon ≠ 0)) then
    write (ERROR_OUTPUT_UNIT, 204)
else
    write (ERROR_OUTPUT_UNIT, 202) kount
    write (ERROR_OUTPUT_UNIT, 203) (epsilon(i), i = 1, nocc)
endif

This code is used in section 1.

⟨ Formats 1.7⟩ ≡
200: format ("□Current□Electronic□Energy□=□", f12.6)
201: format ("□Convergence□in□R□=□", f12.5, i6, "□□Changing")
202: format ("□SCF□converged□in", i4, "□iterations")
203: format ("□Orbital□Energies□", (7f10.5))
204: format ("□SCF□did□not□converged...□quitting")
This code is used in section 1.
```

### 2 UTILITIES

§2.2 [#12] spinor 7

spinor

```
"scf.f" 2.2 \equiv
     subroutine spinor(H, m)
       double precision H(*)
       integer m
       double precision zero
       \mathbf{integer}\ i,\, j,\, ij,\, ji,\, ip,\, jp,\, ijp,\, ijd,\, nl,\, n
       data zero/0.0 \cdot 10^{+00} D/
       n = 2 * m;
       nl = m + 1
       do i = 1, m
         do j = 1, m
           ij = m * (j-1) + i;
           ip = i + m;
           jp = j + m
           ijp = n * (jp - 1) + ip;
           H(ijp) = H(ij)
         end\ do
       end do
       do i = 1, m
         do j = 1, m
           ip = i + m;
           jp = j + m;
           ijp = n * (jp - 1) + ip
            ijd = n * (j-1) + i;
           H(ijd) = H(ijp)
         end do
       end do
       \mathbf{do}\ i=1,\ m
         \mathbf{do}\ j = nl,\ n
           ij = n * (j-1) + i;
           ji = n * (i - 1) + j
           H(ij) = zero
           H(ji) = zero
         end do
       end do
       return
     end
```

 $n: \underline{2.2}.$ 

*nbasis*: 1, 1.1, 1.3.

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*abs*: 1.3. ARB:  $\underline{1}$ , 1.1.  $BYTES\_PER\_INTEGER: 1.$ *C*: <u>1.1</u>. Cbar: 1, 1.1, 1.5.  $CLOSED\_SHELL\_CALCULATION: 1, 1.3.$ crit: 1, 1.1, 1.5.*dabs*: 1.5.  $damp\colon \ 1,\,\underline{1.1},\,1.5.$ *E*: <u>1.1</u>. eigen: 1.5. $END\_OF\_FILE$ :  $\underline{1}$ . epsilon:  $1, \underline{1.1}, 1.5, 1.6.$  $ERI_{-}UNIT: \underline{1}.$ ERR:  $\underline{1}$ .  $ERROR\_OUTPUT\_UNIT$ :  $\underline{1}$ , 1.5, 1.6. gmprd: 1.5.gtprd: 1.5.H: 1.1, 2.2. $half: \underline{1.2}, 1.5.$ HF: 1, 1.1, 1.5.i: 1.2, 2.2.icon: 1, 1.4, 1.5, 1.6.  $ij: \underline{2.2}.$  $ijd: \underline{2.2}.$ ijp: 2.2. $INT\_BLOCK\_SIZE$ :  $\underline{1}$ . interp:  $1, \underline{1.1}, 1.5$ .  $ip: \underline{2.2}.$ irite:  $1, \underline{1.1}$ . j: 2.2.  $ji: \underline{2.2}.$  $jp: \underline{2.2}.$ kount: 1, <u>1.2</u>, 1.4, 1.5, 1.6.  $LAST\_BLOCK$ : 1.  $LEAST\_BYTE$ : 1. m: 1.2, 2.2. $MAX\_BASIS\_FUNCTIONS$ :  $\underline{1}$ .  $MAX\_CENTRES$ : 1.  $MAX\_ITERATIONS$ :  $\underline{1}$ , 1.6.  $MAX\_PRIMITIVES$ : 1. maxit: 1.2. $mm: \ \underline{1.2}, \ 1.4, \ 1.5.$ 

§2.3 [#13] INDEX 9

```
nelec: 1, 1.1, 1.3.
nfile: 1, 1.1, 1.5.
nl: 2.2.
NO: 1.
NO_OF_TYPES: 1.
nocc: 1.2, 1.3, 1.5, 1.6.
NOT_END_OF_FILE: 1.
NOT_LAST_BLOCK: 1.

R: 1.1.
Rold: 1, 1.1, 1.4, 1.5.
Rsum: 1.2, 1.5, 1.6.

SCF: 1, 1.4.
scfGR: 1.5.
```

scfR: 1.5. scftype: 1.2, 1.3, 1.5. spinor: 1.3, 2.2.

 $term: \ \underline{1.2}, \ 1.5. \\ turm: \ \underline{1.2}, \ 1.5.$ 

 $UHF\_CALCULATION: \underline{1}, 1.3, 1.5.$ 

V:  $\underline{1.1}$ .

while: 1.

YES:  $\underline{1}$ , 1.4.

 $zero\colon \ \ \underline{1.2},\ 1.3,\ 1.4,\ 1.5,\ \underline{2.2}.$ 

```
\label{eq:continuous} $$\left\langle \text{ Formats } 1.7 \right\rangle$ Used in section 1. $$\left\langle \text{ Global SCF Declarations } 1.1 \right\rangle$ Used in section 1. $$\left\langle \text{ Internal SCF Declarations } 1.2 \right\rangle$ Used in section 1. $$\left\langle \text{ Select SCF Type } 1.3 \right\rangle$ Used in section 1. $$\left\langle \text{ Set initial matrices and counters } 1.4 \right\rangle$ Used in section 1. $$\left\langle \text{ Sigle SCF iteration } 1.5 \right\rangle$ Used in section 1. $$\left\langle \text{ Write the output result } 1.6 \right\rangle$ Used in section 1. $$
```

COMMAND LINE: "fweave -C3 scf.web".

WEB FILE: "scf.web". CHANGE FILE: (none).

GLOBAL LANGUAGE: FORTRAN.