oepdev 1.0.0-alpha

Novel methods for Quantum Chemistry of Extended Molecular Aggregates

Contents

Chapter 1

Main Page

oep-dev

Generalized One-Electron Potentials: Development Platform.

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Overview

Test various models of the intermolecular interaction that is based on the application of the **One-Electron Potentials (OEP's)** technique.

Currently, the interaction between two molecules described by the Hartree-Fock-Roothaan-Hall theory or the configuration interaction with singles theory is considered. In particular, the plugin tests the models of:

1. the Pauli exchange-repulsion interaction energy (Project II)

2. the Induction interaction energy (Project III)

3. the excitation energy transfer couplings (Project I)

against reference solutions (exact or other approximations).

Places to go:

- https://github.com/globulion/oepdev/blob/master/doc/git/doc_oep_design.md "OEP Design"

- https://github.com/globulion/oepdev/blob/master/doc/git/doc_implemented_models.md "Implemented Models"

- https://github.com/globulion/oepdev/blob/master/doc/git/doc_programming_etiquette.md "Programming Etiquette"

- Current Issues

References

[1] B. Błasiak, "One-Particle Density Matrix Polarization Susceptibility Tensors", *Submitted* **2018** XX, XXX

Chapter 2

Introduction

This page introduces the user to the topic.

Now you can proceed to the advanced section.

Chapter 3

OEP Design.

OEP (One-Electron Potential) is associated with certain quantum one-electron operator $\hat{v}^A$ that defines the ability of molecule A to interact in a particular way with other molecules.

Technically, OEP can be understood as a **container object** (associated with the molecule in question) that stores the information about the above mentioned quantum operator. Here, it is assumed that similar OEP object is also defined for all other molecules in a molecular aggregate.

In case of interaction between molecules A and B, OEP object of molecule A interacts directly with wavefunction object of the molecule B. Defining a Solver class that handles such interaction Wavefunction class and OEP class

the universal design of OEP-based approaches can be established and developed.

> **Important:** OEP and Wavefunction classes should not be restricted to Hartree-Fock; in generall any correlated wavefunction and derived OEP's should be allowed to work with each other.

3.1 OEP Classes

There are many types of OEP's, but the underlying principle is the same and independent of the type of intermolecular interaction. Therefore, the OEP's should be implemented by using a multi-level class design. In turn, this design depends on the way OEP's enter the mathematical expressions, i.e., on the types of matrix elements of the one-electron effective operator $\hat{v}^A$.

3.1.1 Structure of possible OEP-based expressions and their unification

Structure of OEP-based mathematical expressions is listed below:

Type	Matrix Element	Comment
Type 1	$\left(I\lvert\hat{v}^A\rvert J\right)$	$I \in A,\ J \in B$
Type 2	$\left(J\lvert\hat{v}^A\rvert L\right)$	$J,L \in B$

In the above table, I, J and K indices correspond to basis functions or molecular orbitals. Basis functions can be primary or auxiliary OEP-specialized density-fitting. Depending on the type of function and matrix element, there are many subtypes of resulting matrix elements that differ in their dimensionality. Examples are given below:

Matrix Element	DF-based form	ESP-based form
$\left(\mu\lvert\hat{v}^{A[\mu]}\rvert\sigma\right)$	$\sum_{\iota \in A} v^A_{\mu\iota} S_{\iota\sigma}$	$\sum_{\alpha \in A} q^{A[\mu]}_\alpha V^{(\alpha)}_{\mu\sigma}$
$\left(i\lvert\hat{v}^{A[i]}\rvert j\right)$	$\sum_{\iota \in A} v^A_{i\iota} S_{\iota j}$	$\sum_{\alpha \in A} q^{A[i]}_\alpha V^{(\alpha)}_{ij}$

| $\left(j\|\hat{v}^{A[i]}\|l\right)$ | $\sum_{\iota\kappa\in A} S_{j\iota} v^{A[i]}_{\iota\kappa} S_{\kappa l}$ | $\sum_{\alpha\in A} q^{A[i]}_{\alpha} V^{(\alpha)}_{jl}$ |

In the formulae above, the OEP-part (stored by OEP instances) and the Solver-part (to be computed by the Solver) are separated. It is apparent that all OEP-parts have the form of 2nd- or 3rd-rank tensors with different class of axes (molecular orbitals, primary/auxiliary basis, atomic space). Therefore, they can be uniquely defined by a unified *tensor object* (storing double precision numbers) and unified *dimension object* storing the information of the axes classes.

In Psi4, a perfect candidate for the above is `psi4::Tensor` class declared in `psi4/libthce/thce.h`. Except from the numeric content its instances also store the information of the dimensions in a form of a vector of `psi4::Dimension` instances.

Another possibility is to use `psi::Matrix` objects, instead of `psi4::Tensor` objects, possibly putting them into a `std::vector` container in case there is more than two axes.

Chapter 4

List of One-Electron Potentals

Here I provide the list of OEP's that have been already derived within the scope of the OEPDev project.

4.1 Electrostatic Energy OEP's

For electrostatic energy calculations, OEP is simply the electrostatic potential due to nuclei and electrons.
3D form:

$$v(\mathbf{r}) = \sum_x \frac{Z_x}{|\mathbf{r} - \mathbf{r}_x|} + \sum_{\mu\nu\in A} P_{\nu\mu} \int d\mathbf{r}' \frac{\phi_\mu^*(\mathbf{r}')\phi_\nu(\mathbf{r}')}{|\mathbf{r} - \mathbf{r}'|}$$

Matrix form:

$$v_{ik} = \sum_{x\in A} Z_x V_{ik}^{(x)} + \sum_{\mu\nu\in A} P_{\nu\mu} \left(\mu\nu|ik\right)$$

4.2 Pauli Repulsion OEP's

The following potentials are derived for the evaluation of the Pauli repulsion energy based on Murrel's expressions.

4.2.1 First-order contribution in overlap matrix expansion.

This contribution is simply the electrostatic potential coming from all nuclei and electron density except∗ from electron density from molecular orbital i that interacts with the generalized overlap density between i of molecule A and j of molecule B.
3D forms:

$$v(\mathbf{r})_{S^{-1}}^{A[i]} = -\sum_{x\in A} \frac{Z_x}{|\mathbf{r} - \mathbf{r}_x|} + \sum_{\mu\nu\in A} \left\{ D_{\nu\mu} - C_{\mu i}^* C_{\nu i} \right\} \int d\mathbf{r}' \frac{\phi_\mu^*(\mathbf{r}')\phi_\nu(\mathbf{r}')}{|\mathbf{r} - \mathbf{r}'|}$$

Matrix forms:

$$v_{\xi i}(S^{-1}) = \sum_{\kappa \in A} C_{i\kappa} \left\{ -\sum_{x \in A} V_{\kappa \xi}^{(x)} + \sum_{\mu \nu \in A} \left\{ D_{\nu \mu} - C_{\mu i}^* C_{\nu i} \right\} (\mu \nu | \xi \kappa) \right\}$$

4.2.2 Second-order contribution in overlap matrix expansion.

To be added here!

4.3 Excitonic Energy Transfer OEP's

The following potentials are derived for the evaluation of the short-range EET couplings based on Fujimoto's TDFI-TI method.

4.3.1 ET contributions.

3D forms:

$$v(\mathbf{r})_1^{A[\mu]} = -C_{\mu L}^* \sum_{x \in A} \frac{Z_x}{|\mathbf{r} - \mathbf{r}_x|} + \sum_{\nu \kappa \in A} \left\{ C_{\mu L}^* D_{\nu \kappa} - \frac{1}{2} C_{\nu L}^* D_{\mu \kappa} \right\} \int d\mathbf{r}' \frac{\phi_\nu^*(\mathbf{r}') \phi_\kappa(\mathbf{r}')}{|\mathbf{r} - \mathbf{r}'|}$$

$$v(\mathbf{r})_2^{A[\mu]} = C_{\kappa H} \sum_{\nu \kappa \in A} \left\{ 2 C_{\nu L}^* C_{\mu H}^* - C_{\nu H}^* C_{\mu L}^* \right\} \int d\mathbf{r}' \frac{\phi_\nu^*(\mathbf{r}') \phi_\kappa(\mathbf{r}')}{|\mathbf{r} - \mathbf{r}'|}$$

$$v(\mathbf{r})_3^{A[\mu]} = v(\mathbf{r})_1^{A[\mu]} + v(\mathbf{r})_1^{A[\mu]}$$

Matrix forms:

$$v_{\mu \xi}(1) = -C_{\mu L}^* \sum_{x \in A} V_{\mu \xi}^x + \sum_{\nu \kappa \in A} \left\{ C_{\mu L}^* D_{\nu \kappa} - \frac{1}{2} C_{\nu L}^* D_{\mu \kappa} \right\} (\nu \kappa | \mu \xi)$$

$$v_{\mu \xi}(2) = C_{\kappa H} \sum_{\nu \kappa \in A} \left\{ 2 C_{\nu L}^* C_{\mu H}^* - C_{\nu H}^* C_{\mu L}^* \right\} (\nu \kappa | \mu \xi)$$

$$v_{\mu \xi}(3) = v_{\mu \xi}(1) + v_{\mu \xi}(2)$$

4.3.2 HT contributions.

Do be derived.

4.3.3 CT contributions.

To be derived.

4.4 Full HF Interaction OEP's

The following potentials are derived for the evaluation of the full Hartree-Fock interaction energy based on the OEPDev equations.

Chapter 5

Density-fitting Specialized for OEP's

To get the ab-initio representation of a OEP, one can use a procedure similar to the typical density fitting or resolution of identity, both of which are nowadays widely used to compute electron-repulsion integrals (ERI's) more efficiently.

5.1 Fitting in Complete Space

An arbitrary one-electron potential of molecule A acting on any state vector associated with molecule A can be expanded in an *auxiliary space* centered on A as

$$v|i) = \sum_{\xi\eta} v|\xi)[\mathbf{S}^{-1}]_{\xi\eta}(\eta|i)$$

under the necessary assumption that the auxiliary basis set is *complete*. In a special case when the basis set is orthogonal (e.g., molecular orbitals) the above relation simplifies to

$$v|i) = \sum_{\xi} v|\xi)(\xi|i)$$

It can be easily shown that the above general and exact expansion can be obtained by performing a density fitting in the complete space. We expand the LHS of the first equation on this page in a series of the auxiliary basis functions scaled by the undetermined expansion coefficients:

$$v|i) = \sum_{\xi} G_{i\xi}|\xi)$$

which we shall refer here as to the matrix form of the OEP operator. By constructing the least-squares objective function

$$Z[\{G_{\xi}^{(i)}\}] = \int d\mathbf{r}_1 \left[v(\mathbf{r}_1)\phi_i(\mathbf{r}_1) - \sum_{\xi} G_{\xi}^{(i)} \varphi_{\xi}(\mathbf{r}_1) \right]^2$$

and requiring that

$$\frac{\partial Z[\{G_{\xi}^{(i)}\}]}{\partial G_{\mu}^{(i)}} = 0 \text{ for all } \mu$$

we find the coefficients $G_{\xi}^{(i)}$ to be

$$\mathbf{G}^{(i)} = \mathbf{v}^{(i)} \cdot \mathbf{S}^{-1}$$

where

$$v_{\eta}^{(i)} = (\eta|vi)$$
$$S_{\eta\xi} = (\eta|\xi)$$

or explitictly

$$G_{i\xi} = \sum_{\eta} [\mathbf{S}^{-1}]_{\xi\eta}(\eta|v|i)$$

identical to what we obtained from application of the resolution of identity in space spanned by non-orthogonal complete set of basis vectors.

Since matrix elements of an OEP operator in auxiliary space can be computed in the same way as the matrix elements with any other basis function, one can formally write the following identity

$$(X|v|i) = \sum_{\xi\eta} S_{X\xi} [\mathbf{S}^{-1}]_{\xi\eta} (\eta|v|i)$$

where X is an arbitrary orbital. When the other orbital does not belong to molecule A but to the (changing) environment, it is straightforward to compute the resulting matrix element, which is simply given as

$$(j_{\in B}|v^A|i_{\in A}) = \sum_{\xi} S_{j\xi} G_{i\xi}$$

where j denotes the other (environmental) basis function.

In the above equation, the OEP-part (fragment parameters for molecule A only) and the Solver-part (subject to be computed by solver on the fly) are separated. This then forms a basis for fragment-based approach to solve Quantum Chemistry problems related to the extended molecular aggregates.

5.2 Fitting in Incomplete Space

Density fitting scheme from previous section has practical disadvantage of a nearly-complete basis set being usually very large (spanned by large amount of basis set vectors). Any non-complete basis set won't work in the previous example. Since most of basis sets used in quantum chemistry do not form a complete set, it is beneficial to design a modified scheme in which it is possible to obtain the **effective** matrix elements of the OEP operator in a **incomplete** auxiliary space. This can be achieved by minimizing the following objective function

$$Z[\{G^{(i)}_\xi\}] = \iint d\mathbf{r}_1 d\mathbf{r}_2 \frac{\left[v(\mathbf{r}_1)\phi_i(\mathbf{r}_1) - \sum_\xi G^{(i)}_\xi \varphi_\xi(\mathbf{r}_1) \right] \left[v(\mathbf{r}_2)\phi_i(\mathbf{r}_2) - \sum_\xi G^{(i)}_\eta \varphi_\eta(\mathbf{r}_1) \right]}{|\mathbf{r}_1 - \mathbf{r}_2|}$$

Thus requesting that

$$\frac{\partial Z[\{G^{(i)}_\xi\}]}{\partial G^{(i)}_\mu} = 0 \text{ for all } \mu$$

we find the coefficients $G^{(i)}_\xi$ to be

$$\mathbf{G}^{(i)} = \mathbf{b}^{(i)} \cdot \mathbf{A}^{-1}$$

where

$$b^{(i)}_\eta = (\eta||vi)$$
$$A_{\eta\xi} = (\eta||\xi)$$

The symbol $||$ is to denote the operator r_{12}^{-1} and double integration over $\mathbf{r}_1$ and $\mathbf{r}_2$. Thus, it is clear that in order to use this generalized density fitting scheme one must to compute two-centre electron repulsion integrals (implemented in oepdev::ERI_1_1) as well as four-centre asymmetric electron repulsion integrals of the type $(\alpha\beta\gamma||\eta)$ (implemented in oepdev::ERI_3_1).

Chapter 6

Implemented Models

6.1   Target Properties

Detailed list of models which is to be implemented in the OEPDev project is given below:

Table 1. Models subject to be implemented and analyzed within oep-dev.

Pauli energy	Induction energy	EET Coupling
EFP2-Pauli	EFP2-Induced Dipoles	TrCAMM
Murrel et al.'s theory	Density Susceptibility	OEP-ET/HT
OEP-Murrel et al.'s		TDFI-TI
		FED
Exact (Stone's)	Exact (incl. CT)	Exact (ESD)

6.2   Target, Benchmark and Competing Models

The target models introduced in the Project shall be tested against the following benchmarks and compared with the following state-of-the-art models:

Table 2. Target models vs benchmarks and competitor models.

Target Model	Benchmarks	Competing Model
OEP-Murrel et al.'s	Murrel et al.'s	EFP2-Pauli
	Exact (Stone's)	
OEP-ET/HT + TrCAMM	Exact (ESD)	TDFI-TI
	FED	FED
	TDFI-TI	
Density Susceptibility	Exact (incl. CT)	EFP2-Induced Dipoles

Chapter 7

Contributing to oep-dev

OepDev is a plugin to Psi4.

Therefore it should follow the programming etiquette of Psi4. Also, oep-dev has additional programming tips to make the code more versatile and easy in further development. Here, I emphasise on most important aspects regarding the **programming rules**.

7.1 Main routine and libraries

Oep-dev has only *one* source file in the plugin base directory, i.e., `main.cc`. This is the main driver routine that handles the functionality of the whole OEP testing platform: specifies options for Psi4 input file and implements test routines based on the options. Other sources are stored in `MODULE/libNAME*` directories where `NAME` is the name of the library with sources and header files, whereas `MODULE` is the directory of the oep-dev module.

Things to remember:

1. **No other sources in base directory.** It is not permitted to place any new source or other files in the plugin base directory (i.e., where `main.cc` resides).

2. **Sources in library directories.** Any additional source code has to be placed in `oepdev/libNAME*` directory (either existing one or a new one; in the latter case remember to add the new `*.cc` files to `CMake-Lists.txt` in the plugin base directory.

3. **Miscellanea in special directories.** If you want to add additional documentation, put it in the `doc` directory. If you want to add graphics, put it in the `images` directory.

7.2 Header files in libraries

Header files are handy in obtaining a quick glimpse of the functionality within certain library. Each library directory should contain at least one header file in oep-dev. However, header files can be problematic if not managed properly.

Things to remember:

1. **Header preprocessor variable**. Define the preprocessor variable specyfying the existence of include of the particular header file. The format of such is

   ```
   #ifndef MODULE_LIBRARY_HEADER_h
   #define MODULE_LIBRARY_HEADER_h
   // rest of your code goes here
   #endif // MODULE_LIBRARY_HEADER_h
   ```

   Last line is the **end** of the header file. The preprocessor variables represents the directory tree `oepdev/-MODULE/LIBRARY/HEADER.h` structure (where `oepdev` is the base plugin directory). `MODULE` is the

plugin module name (e.g. `oepdev`, the name of the module directory) `LIBRARY` is the name of the library (e.g. `libutil`, should be the same as library directory name) `HEADER` is the name of the header in library directory (e.g. `diis` for `diis.h` header file)

2. **Set module namespace**. To prevent naming clashes with other modules and with Psi4 it is important to operate in separate namespace (e.g. for a module).

```
namespace MODULE {
// your code goes here
} // EndNameSpace MODULE
```

For instance, all classes and functions in `oepdev` module are implemented within the namespace of the same label. Considering addition of other local namespaces within a module can also be useful in certain cases.

7.3 Environmental variables

Defining the set of intrinsic environmental variables can help in code management and conditional compilation. The oep-dev environmental variables are defined in `include/oepdev_files.h` file. Remember also about psi4 environmental variables defined in `psi4/psifiles.h` header. As a rule, the oep-dev environmental variable should have the following format:

`OEPDEV_XXXX`

where `XXXX` is the descriptive name of variable.

7.4 Documenting the code

Code has to be documented (at best at a time it is being created). The place for documentation is always in header files. Additional documentation can be also placed in source files. Leaving a chunk of code for a production run without documentation is unacceptable.

Use Doxygen style for documentation all the time. Remember that it supports markdown which can make the documentation even more clear and easy to understand. Additionally you can create a nice `.rst` documentation file for Sphinx program. If you are coding equations, always include formulae in the documentation!

Things to remember:

1. **Descriptions of classes, structures, global functions, etc**. Each programming object should have a description.

2. **Documentation for function arguments and return object**. Usage of functions and class methods should be explained by providing the description of all arguments (use `\param` and `\return` Doxygen keywords).

3. **One-line description of class member variables**. Any class member variable should be preceded by a one-liner documentation (starting from `///`).

4. **Do not be afraid of long names in the code**. Self-documenting code is a bless!

7.5 Naming conventions

Naming is important because it helps to create more readable and clear self-documented code.

Some loose suggestions:

1. **Do not be afraid of long names in the code, but avoid redundancy**. Examples of good and bad names: good name: `get_density_matrix`; bad name: `get_matrix`. Unless there is only one type of matrix a particular objects can store, `matrix` is not a good name for a getter method. good name: `class Wavefunction`, bad name: `class WFN` good name: `int numberOfErrorVectors`, bad name: `int nvec`, bad name: `the_number_of_error_vectors` good name: `class EFPotential`, probably bad name: `class EffectiveFragmentPotential`. The latter might be understood by some people as a class that inherits from `EffectiveFragment` class. If it is not the case, compromise between abbreviation and long description is OK.

2. **Short names are OK in special situations**. In cases meaning of a particular variable is obvious and it is frequently used in the code locally, it can be named shortly. Examples are: `i` when iterating `no` number of occupied orbitals, `nv` number of virtual orbitals, etc.

3. **Clumped names for variables and dashed names for functions**. Try to distinguish between variable name like `sizeOfOEPTypeList` and a method name `get_matrix()` (neither `size_of_OEP_type_-list`, nor `getMatrix()`). This is little bit cosmetics, but helps in managing the code when it grows.

4. **Class names start from capital letter**. However, avoid only capital letters in class names, unless it is obvious. Avoid also dashes in class names (they are reserved for global functions and class methods). Examples: good name: `DIISManager`, bad name: `DIIS`. good name: `EETCouplingSolver`, bad name: `EETSolver`, very bad: `EET`.

7.6 Use Object-Oriented Programming

Try to organise your creations in objects having special relationships and data structures. Encapsulation helps in producing self-maintaining code and is much easier to use. Use:

- **factory design** for creating objects

- **container design** for designing data structures

- **polymorphysm** when dealing with various flavours of one particular feature in the data structure

Note: In Psi4, factories are frequently implemented as static methods of the base classes, for example `psi::BasisSet::build` static method. It can be followed when building object factories in oep-dev too.

Chapter 8

Advanced Usage

This page is for advanced users.

Make sure you have first read [the introduction](#).

Chapter 9

License

Chapter 10

Module Index

10.1 Modules

Here is a list of all modules:

Chapter 11

Namespace Index

11.1 Namespace List

Here is a list of all documented namespaces with brief descriptions:

Chapter 12

Hierarchical Index

12.1 Class Hierarchy

This inheritance list is sorted roughly, but not completely, alphabetically:

Chapter 13

Class Index

13.1 Class List

Here are the classes, structs, unions and interfaces with brief descriptions:

Chapter 14

File Index

14.1 File List

Here is a list of all documented files with brief descriptions:

Chapter 15

Module Documentation

15.1 The Generalized One-Electron Potentials Library

Implements the goal of this project: The Generalized One-Electron Potentials (OEP's). You will find here OEP's for computation of Pauli repulsion energy, charge-transfer energy and others.

Classes

- struct oepdev::OEPType

    Container to handle the type of One-Electron Potentials.
- class oepdev::OEPotential

    Generalized One-Electron Potential: Abstract base.
- class oepdev::ElectrostaticEnergyOEPotential

    Generalized One-Electron Potential for Electrostatic Energy.
- class oepdev::RepulsionEnergyOEPotential

    Generalized One-Electron Potential for Pauli Repulsion Energy.
- class oepdev::ChargeTransferEnergyOEPotential

    Generalized One-Electron Potential for Charge-Transfer Interaction Energy.
- class oepdev::EETCouplingOEPotential

    Generalized One-Electron Potential for EET coupling calculations.
- class oepdev::GeneralizedDensityFit

    Generalized Density Fitting Scheme. Abstract Base.
- class oepdev::SingleGeneralizedDensityFit

    Generalized Density Fitting Scheme - Single Fit.
- class oepdev::DoubleGeneralizedDensityFit

    Generalized Density Fitting Scheme - Double Fit.

15.1.1 Detailed Description

Implements the goal of this project: The Generalized One-Electron Potentials (OEP's). You will find here OEP's for computation of Pauli repulsion energy, charge-transfer energy and others.

15.2 The OEPDev Solver Library

Implementations of various solvers for molecular properties as a functions of unperturbed monomeric wavefunctions. This is the place all target OEP-based models are implemented and compared with benchmark models.

Classes

- class oepdev::OEPDevSolver

  Solver of properties of molecular aggregates. Abstract base.

- class oepdev::ElectrostaticEnergySolver

  Compute the Coulombic interaction energy between unperturbed wavefunctions.

- class oepdev::RepulsionEnergySolver

  Compute the Pauli-Repulsion interaction energy between unperturbed wavefunctions.

- class oepdev::ChargeTransferEnergySolver

  Compute the Charge-Transfer interaction energy between unperturbed wavefunctions.

15.2.1 Detailed Description

Implementations of various solvers for molecular properties as a functions of unperturbed monomeric wavefunctions. This is the place all target OEP-based models are implemented and compared with benchmark models.

15.3 The Generalized Effective Fragment Potentials Library

Implements the GEFP method, the far goal of the OEPDev project. Here you will find the containers for GEFP parameters, the density matrix susceptibility tensors and GEFP solvers.

Classes

- class oepdev::GenEffPar

  Generalized Effective Fragment Parameters. Container Class.
- class oepdev::GenEffFrag

  Generalized Effective Fragment. Container Class.
- class oepdev::GenEffParFactory

  Generalized Effective Fragment Factory. Abstract Base.
- class oepdev::PolarGEFactory

  Polarization GEFP Factory. Abstract Base.
- class oepdev::AbInitioPolarGEFactory

  Polarization GEFP Factory from First Principles. Hartree-Fock Approximation.
- class oepdev::FFAbInitioPolarGEFactory

  Polarization GEFP Factory from First Principles: Finite-Difference Model. Arbitrary level of theory.
- class oepdev::GeneralizedPolarGEFactory

  Polarization GEFP Factory with Least-Squares Parameterization.
- class oepdev::UniformEFieldPolarGEFactory

  Polarization GEFP Factory with Least-Squares Parameterization.
- class oepdev::NonUniformEFieldPolarGEFactory

  Polarization GEFP Factory with Least-Squares Parameterization.
- class oepdev::LinearUniformEFieldPolarGEFactory

  Polarization GEFP Factory with Least-Squares Parameterization.
- class oepdev::QuadraticUniformEFieldPolarGEFactory

  Polarization GEFP Factory with Least-Squares Parameterization.
- class oepdev::LinearNonUniformEFieldPolarGEFactory

  Polarization GEFP Factory with Least-Squares Parameterization.
- class oepdev::QuadraticNonUniformEFieldPolarGEFactory

  Polarization GEFP Factory with Least-Squares Parameterization.
- class oepdev::LinearGradientNonUniformEFieldPolarGEFactory

  Polarization GEFP Factory with Least-Squares Parameterization.
- class oepdev::QuadraticGradientNonUniformEFieldPolarGEFactory

  Polarization GEFP Factory with Least-Squares Parameterization.
- class oepdev::UnitaryTransformedMOPolarGEFactory

  Polarization GEFP Factory with Least-Squares Scaling of MO Space.

15.3.1 Detailed Description

Implements the GEFP method, the far goal of the OEPDev project. Here you will find the containers for GEFP parameters, the density matrix susceptibility tensors and GEFP solvers.

15.4 The Integral Package Library

Implementations of various one- and two-body integrals via McMurchie-Davidson recurrence scheme.

Classes

- class oepdev::TwoElectronInt

    General Two Electron Integral.
- class oepdev::ERI_1_1

    2-centre ERI of the form (a|O(2)|b) where O(2) = 1/r12.
- class oepdev::ERI_2_2

    4-centre ERI of the form (ab|O(2)|cd) where O(2) = 1/r12.
- class oepdev::ERI_3_1

    4-centre ERI of the form (abc|O(2)|d) where O(2) = 1/r12.
- class oepdev::TwoBodyAOInt
- class oepdev::IntegralFactory

    Extended IntegralFactory for computing integrals.
- class oepdev::PotentialInt

    Computes potential integrals.

Macros

- #define D1_INDEX(x, i, n) ((81∗(x))+(9∗(i))+(n))

    Get the index of McMurchie-Davidson-Hermite D1 coefficient stored in the `mdh_buffer_`*, that is attributed to the x Cartesian coordinate from angular momentum i of function 1, and the Hermite index n.*
- #define D2_INDEX(x, i, j, n) ((1377∗(x))+(153∗(i))+(17∗(j))+(n))

    Get the index of McMurchie-Davidson-Hermite D2 coefficient stored in the `mdh_buffer_`*, that is attributed to the x Cartesian coordinate from angular momenta i, j of function 1 and 2, and the Hermite index n.*
- #define D3_INDEX(x, i, j, k, n) ((18225∗(x))+(2025∗(i))+(225∗(j))+(25∗(k))+(n))

    Get the index of McMurchie-Davidson-Hermite D3 coefficient stored in the `mdh_buffer_`*, that is attributed to the x Cartesian coordinate from angular momenta i, j and k of function 1, 2 and 3, and the Hermite index n.*
- #define R_INDEX(n, l, m, j) ((14739∗(n))+(867∗(l))+(51∗(m))+(j))

    Get the index of McMurchie-Davidson R coefficient stored in the `mdh_buffer_R_` *from angular momenta n, l and m and the Boys index j.*

Functions

- double oepdev::d_N_n1_n2 (int N, int n1, int n2, double PA, double PB, double aP)

    Compute McMurchie-Davidson-Hermite (MDH) coefficient for binomial expansion.
- void oepdev::make_mdh_D1_coeff (int n1, double aPd, double ∗buffer)

    Compute the McMurchie-Davidson-Hermite coefficients for monomial expansion.
- void oepdev::make_mdh_D2_coeff (int n1, int n2, double aPd, double ∗PA, double ∗PB, double ∗buffer)

    Compute the McMurchie-Davidson-Hermite coefficients for binomial expansion.
- void oepdev::make_mdh_D3_coeff (int n1, int n2, int n3, double aPd, double ∗PA, double ∗PB, double ∗PC, double ∗buffer)

    Compute the McMurchie-Davidson-Hermite coefficients for trinomial expansion.
- void oepdev::make_mdh_D2_coeff_explicit_recursion (int n1, int n2, double aP, double ∗PA, double ∗PB, double ∗buffer)

    Compute the McMurchie-Davidson-Hermite coefficients for binomial expansion by explicit recursion. This function makes the same changes to buffers as oepdev::make_mdh_D2_coeff, but implements it through explicit recursion by calls to oepdev::d_N_n1_n2. Therefore, it is slightly slower. Here for debugging purposes.
- void oepdev::make_mdh_R_coeff (int N, int L, int M, double alpha, double a, double b, double c, double ∗F, double ∗buffer)

    Compute the McMurchie-Davidson R coefficients.

15.4.1 Detailed Description

Implementations of various one- and two-body integrals via McMurchie-Davidson recurrence scheme. Here, we define the primitive Gaussian type functions (GTO's)

$$\phi_i(\mathbf{r}) \equiv x_A^{n_1} y_A^{l_1} z_A^{m_1} e^{-\alpha_1 r_A^2}$$

$$\phi_j(\mathbf{r}) \equiv x_B^{n_2} y_B^{l_2} z_B^{m_2} e^{-\alpha_2 r_B^2}$$

$$\phi_k(\mathbf{r}) \equiv x_C^{n_3} y_C^{l_3} z_C^{m_3} e^{-\alpha_3 r_C^2}$$

in which $\mathbf{r}_A \equiv \mathbf{r} - \mathbf{A}$ and so on. $\mathbf{A}$ is the centre of the GTO, α_1 its exponent, whereas n_1, l_1, m_1 the Cartesian angular momenta, with the total angular momentum $\theta_1 = n_1 + l_1 + m_1$.

In OEPDev implementations, the following definition shall be in use:

$$\mathbf{P} \equiv \frac{\alpha_1 \mathbf{A} + \alpha_2 \mathbf{B}}{\alpha_1 + \alpha_2}$$

$$\mathbf{Q} \equiv \frac{\alpha_3 \mathbf{C} + \alpha_4 \mathbf{D}}{\alpha_3 + \alpha_4}$$

$$\mathbf{R} \equiv \frac{\alpha_1 \mathbf{A} + \alpha_2 \mathbf{B} + \alpha_3 \mathbf{C}}{\alpha_1 + \alpha_2 + \alpha_3}$$

$$\alpha_P \equiv \alpha_1 + \alpha_2$$

$$\alpha_Q \equiv \alpha_3 + \alpha_4$$

$$\alpha_R \equiv \alpha_1 + \alpha_2 + \alpha_3$$

The unnormalized products of primitive GTO's are denoted here as

$$[ij] \equiv \phi_i(\mathbf{r})\phi_j(\mathbf{r})$$

$$[ijk] \equiv \phi_i(\mathbf{r})\phi_j(\mathbf{r})\phi_k(\mathbf{r})$$

15.4.2 Hermite Operators

It is convenient to define

$$\Lambda_j(x_P; \alpha_P) \equiv \left(\frac{\partial}{\partial P_x}\right)^j = \alpha_P^{j/2} H_j(\sqrt{\alpha_P} x_P)$$

where $H_j(x)$ is the Hermite polynomial of order j evaluated at x. Introduction of the above Hermite operator can be used by invoking the recurrence relationship due to Hermite polynomial properties:

$$x_A \Lambda_j(x_P; \alpha_P) = j\Lambda_{j-1} + |\mathbf{P} - \mathbf{A}|_x \Lambda_j + \frac{1}{2\alpha_P}\Lambda_{j+1}$$

This can be directly used to derive very useful McMurchie-Davidson-Hermite coefficients as expansion coefficients of the polynomial expansions.

15.4.2.1 Polynomial Expansions as Hermite Series

By using the previous relation, it is possible to express the following expansions in Hermite series:

$$x_A^{n_1} = \sum_{N=0}^{n_1} d_N^{n_1} \Lambda_N(x_A; \alpha_A)$$

$$x_A^{n_1} x_B^{n_2} = \sum_{N=0}^{n_1+n_2} d_N^{n_1 n_2} \Lambda_N(x_P; \alpha_P)$$

$$x_A^{n_1} x_B^{n_2} x_C^{n_3} = \sum_{N=0}^{n_1+n_2+n_3} d_N^{n_1 n_2 n_3} \Lambda_N(x_R; \alpha_R)$$

The recurrence relationships can be easily found and they read

$$d_N^{n_1+1} = \frac{1}{2\alpha_A} d_{N-1}^{n_1} + (N+1)d_{N+1}^{n_1}$$

as well as

$$d_N^{n_1+1,n_2} = \frac{1}{2\alpha_P} d_{N-1}^{n_1 n_2} + |\mathbf{P}-\mathbf{A}|_x d_N^{n_1 n_2} + (N+1)d_{N+1}^{n_1 n_2}$$

$$d_N^{n_1,n_2+1} = \frac{1}{2\alpha_P} d_{N-1}^{n_1 n_2} + |\mathbf{P}-\mathbf{B}|_x d_N^{n_1 n_2} + (N+1)d_{N+1}^{n_1 n_2}$$

and

$$d_N^{n_1+1,n_2,n_3} = \frac{1}{2\alpha_R} d_{N-1}^{n_1 n_2 n_3} + |\mathbf{R}-\mathbf{A}|_x d_N^{n_1 n_2 n_3} + (N+1)d_{N+1}^{n_1 n_2 n_3}$$

$$d_N^{n_1,n_2+1,n_3} = \frac{1}{2\alpha_R} d_{N-1}^{n_1 n_2 n_3} + |\mathbf{R}-\mathbf{B}|_x d_N^{n_1 n_2 n_3} + (N+1)d_{N+1}^{n_1 n_2 n_3}$$

$$d_N^{n_1,n_2,n_3+1} = \frac{1}{2\alpha_R} d_{N-1}^{n_1 n_2 n_3} + |\mathbf{R}-\mathbf{C}|_x d_N^{n_1 n_2 n_3} + (N+1)d_{N+1}^{n_1 n_2 n_3}$$

respectively. The first elements are given by

$$d_0^0 = 1$$
$$d_0^{00} = 1$$
$$d_0^{000} = 1$$

By using the above formalisms, it is strightforward to express the doublet of primitive GTO's as

$$[ij] = E_{ij} \sum_{N=0}^{n_1+n_2} \sum_{L=0}^{l_1+l_2} \sum_{M=0}^{m_1+m_2} d_N^{n_1 n_2} d_L^{l_1 l_2} d_M^{m_1 m_2} \Lambda_N(x_P)\Lambda_L(y_P)\Lambda_M(z_P)e^{-\alpha_P r_P^2}$$

Analogously, the triplet of primitive GTO's is given by

$$[ijk] = E_{ijk} \sum_{N=0}^{n_1+n_2+n_3} \sum_{L=0}^{l_1+l_2+l+3} \sum_{M=0}^{m_1+m_2+m_3} d_N^{n_1 n_2 n_3} d_L^{l_1 l_2 l_3} d_M^{m_1 m_2 m_3} \Lambda_N(x_R)\Lambda_L(y_R)\Lambda_M(z_R)e^{-\alpha_R r_R^2}$$

The multiplicative constants are given by

$$E_{ij}(\alpha_1,\alpha_2) = \exp\left[-\frac{\alpha_1\alpha_2}{\alpha_1+\alpha_2}|\mathbf{A}-\mathbf{B}|^2\right]$$

$$E_{ijk}(\alpha_1,\alpha_2,\alpha_3) = \exp\left[-\frac{\alpha_1\alpha_2}{\alpha_1+\alpha_2}|\mathbf{A}-\mathbf{B}|^2\right]\exp\left[-\frac{(\alpha_1+\alpha_2)\alpha_3}{\alpha_1+\alpha_2+\alpha_3}|\mathbf{P}-\mathbf{C}|^2\right]$$

15.4.3 One-Body Integrals over Hermite Functions

The fundamental Hermite integrals that appear during computations of any kind of one-body integrals over GTO's are as follows

$$[NLM|\Theta(1)] \equiv \int d\mathbf{r}_1 \Theta(\mathbf{r}_1)\Lambda_N(x_{1P};\alpha_P)\Lambda_L(y_{1P};\alpha_P)\Lambda_M(z_{1P};\alpha_P)e^{-\alpha_P r_{1P}^2}$$

It immediately follows that the overlap, dipole, quadrupole and potential integrals are given as

$$[NLM|1] = \delta_{N0}\delta_{L0}\delta_{M0}\left(\frac{\pi}{\alpha_P}\right)^{3/2}$$

$$[NLM|x_C] = [\delta_{N1} + |\mathbf{PC}|_x\delta_{N0}]\delta_{L0}\delta_{M0}\left(\frac{\pi}{\alpha_P}\right)^{3/2}$$

$$[NLM|x_C^2] = \left[2\delta_{N2} + 2|\mathbf{PC}|_x\delta_{N1} + \left(|\mathbf{PC}|_x^2 + \frac{1}{2\alpha_P}\right)\delta_{N0}\right]\delta_{L0}\delta_{M0}\left(\frac{\pi}{\alpha_P}\right)^{3/2}$$

$$[NLM|x_C y_C] = (\delta_{N1} + |\mathbf{PC}|_x\delta_{N0})(\delta_{L1} + |\mathbf{PC}|_y\delta_{L0})\delta_{M0}\left(\frac{\pi}{\alpha_P}\right)^{3/2}$$

$$[NLM|r_C^{-1}] = \frac{2\pi}{\alpha_P}R_{NLM}$$

The coefficients R_{NLM} are discussed in separate section below.

15.4.4 Two-Body Integrals over Hermite Functions

The fundamental Hermite integrals that appear during computations of any kind of two-electron integrals over GTO's are as follows

$$[N_1L_2M_2|N_2L_2M_2] \equiv \iint d\mathbf{r}_1 d\mathbf{r}_2 \Lambda_{N_1}(x_{1P};\alpha_P)\Lambda_{L_1}(y_{1P};\alpha_P)\Lambda_{M_1}(z_{1P};\alpha_P)\Lambda_{N_2}(x_{2Q};\alpha_Q)\Lambda_{L_2}(y_{2Q};\alpha_Q)\Lambda_{M_2}(z_{2Q};\alpha_Q)e^{-\alpha_P r_{1P}^2 - \alpha_Q r_{2Q}^2}$$

The above formula dramatically reduces to the following

$$[N_1L_2M_2|N_2L_2M_2] = \lambda(-)^{N2+L2+M2}R_{N1+N2,L1+L2,M1+M2}$$

with

$$\lambda \equiv \frac{2\pi^{5/2}}{\alpha_P \alpha_Q \sqrt{\alpha_P + \alpha_Q}}$$

To compute the $R_{N1+N2,L1+L2,M1+M2}$ coefficients, the parameter T is given by

$$T = \frac{\alpha_P \alpha_Q}{\alpha_P + \alpha_Q}|\mathbf{P} - \mathbf{Q}|^2$$

15.4.5 The R(N,L,M) Coefficients

The R coefficients are defined as

$$R_{NLM} \equiv \left(\frac{\partial}{\partial a}\right)^N \left(\frac{\partial}{\partial b}\right)^L \left(\frac{\partial}{\partial c}\right)^M \int_0^1 e^{-Tu^2}\, du$$

with

$$T \equiv \alpha\left(a^2 + b^2 + c^2\right)$$

By extending the above definition to more general

$$R_{NLMj} \equiv \left(-\sqrt{\alpha}\right)^{N+L+M}(-2\alpha)^j \int_0^1 u^{N+L+M+2j}H_N(au\sqrt{\alpha})H_L(bu\sqrt{\alpha})H_M(cu\sqrt{\alpha})e^{-Tu^2}\, du$$

one can see that

$$R_{000j} = (-2\alpha)^j F_j(T)$$

The Boys function is here given by

$$F_j(T) \equiv \int_0^1 u^{2j}e^{-Tu^2}\, du$$

and its efficient implementation can be discussed elsewhere. In Psi4, `psi::Taylor_Fjt` class is used for this purpose.

Now, it is possible to show that the following recursion relationships are true:

$$R_{0,0,M+1,j} = cR_{0,0,M,j+1} + MR_{0,0,M-1,j+1}$$
$$R_{0,L+1,M,j} = bR_{0,L,M,j+1} + LR_{0,L-1,M,j+1}$$
$$R_{N+1,L,M,j} = aR_{N,L,M,j+1} + NR_{N-1,L,M,j+1}$$

This scheme is implemented in OEPDev.

15.4.6 Function Documentation

15.4.6.1 double oepdev::d_N_n1_n2 (int *N,* int *n1,* int *n2,* double *PA,* double *PB,* double *aP*)

Compute McMurchie-Davidson-Hermite (MDH) coefficient for binomial expansion.

Parameters

N	- increment in the summation of MDH series
n1	- angular momentum of first function
n2	- angular momentum of second function
PA	- cartesian component of P-A distance
PB	- cartesian component of P-B distance
aP	- free parameter of MDH expansion

Returns

the McMurchie-Davidson-Hermite coefficient

15.4.6.2 void oepdev::make_mdh_D1_coeff (int *n1,* double *aPd,* double ∗ *buffer*)

Compute the McMurchie-Davidson-Hermite coefficients for monomial expansion.

Parameters

n1	- angular momentum of first function
aPd	- parameter equal to 0.500/Pa where Pa is exponent
buffer	- the McMurchie-Davidson-Hermite 3-dimensional array (raveled to vector): • axis 0: dimension 3 (x, y or z Cartesian component) • axis 1: dimension n1+1 (0 to n1) • axis 2: dimension n1+1 (0 to n1)

See Also

D1_INDEX

15.4.6.3 void oepdev::make_mdh_D2_coeff (int *n1,* int *n2,* double *aPd,* double ∗ *PA,* double ∗ *PB,* double ∗ *buffer*)

Compute the McMurchie-Davidson-Hermite coefficients for binomial expansion.

Parameters

n1	- angular momentum of first function
n2	- angular momentum of second function
aPd	- parameter equal to 0.500/Pa where Pa is exponent
PA	- cartesian components of P-A distance
PB	- cartesian components of P-B distance
buffer	- the McMurchie-Davidson-Hermite 4-dimensional array (raveled to vector): • axis 0: dimension 3 (x, y or z Cartesian component) • axis 1: dimension n1+1 (0 to n1) • axis 2: dimension n2+1 (0 to n2) • axis 3: dimension n1+n2+1 (0 to n1+n2)

See Also

D2_INDEX

15.4.6.4   void oepdev::make_mdh_D2_coeff_explicit_recursion (int *n1,* int *n2,* double *aP,* double ∗ *PA,* double ∗ *PB,* double ∗ *buffer*)

Compute the McMurchie-Davidson-Hermite coefficients for binomial expansion by explicit recursion. This function makes the same changes to buffers as oepdev::make_mdh_D2_coeff, but implements it through explicit recursion by calls to oepdev::d_N_n1_n2. Therefore, it is slightly slower. Here for debugging purposes.

Parameters

n1	- angular momentum of first function
n2	- angular momentum of second function
aPd	- parameter equal to 0.500/Pa where Pa is exponent
PA	- cartesian components of P-A distance
PB	- cartesian components of P-B distance
buffer	- the McMurchie-Davidson-Hermite 4-dimensional array (raveled to vector): • axis 0: dimension 3 (x, y or z Cartesian component) • axis 1: dimension n1+1 (0 to n1) • axis 2: dimension n2+1 (0 to n2) • axis 3: dimension n1+n2+1 (0 to n1+n2)

See Also

D2_INDEX

15.4.6.5   void oepdev::make_mdh_D3_coeff (int *n1,* int *n2,* int *n3,* double *aPd,* double ∗ *PA,* double ∗ *PB,* double ∗ *PC,* double ∗ *buffer*)

Compute the McMurchie-Davidson-Hermite coefficients for trinomial expansion.

Parameters

n1	- angular momentum of first function
n2	- angular momentum of second function
n3	- angular momentum of third function
aPd	- parameter equal to 0.500/Pa where Pa is exponent
PA	- cartesian components of P-A distance
PB	- cartesian components of P-B distance
PC	- cartesian components of P-C distance
buffer	- the McMurchie-Davidson-Hermite 5-dimensional array (raveled to vector): • axis 0: dimension 3 (x, y or z Cartesian component) • axis 1: dimension n1+1 (0 to n1) • axis 2: dimension n2+1 (0 to n2) • axis 3: dimension n3+1 (0 to n3) • axis 4: dimension n1+n2+n3+1 (0 to n1+n2+n3)

See Also

D3_INDEX

15.4.6.6 **void oepdev::make_mdh_R_coeff (int *N,* int *L,* int *M,* double *alpha,* double *a,* double *b,* double *c,* double $*$ *F,* double $*$ *buffer*)**

Compute the McMurchie-Davidson R coefficients.

Parameters

N	- increment in the summation of MDH series along *x* direction
L	- increment in the summation of MDH series along *y* direction
M	- increment in the summation of MDH series along *z* direction
alpha	- alpha parameter of R coefficient
a	- *x* component of PQ vector of R coefficient
b	- *y* component of PQ vector of R coefficient
c	- *z* component of PQ vector of R coefficient
F	- array of Boys function values for given alpha and PQ
buffer	- the McMurchie-Davidson 4-dimensional array (raveled to vector): • axis 0: dimension N+1 • axis 1: dimension L+1 • axis 2: dimension M+1 • axis 3: dimension N+L+M+1 (*j*-th element)

15.5 The Integral Helper Library

You will find here various iterators to go through shells while computing ERI, or iterators over ERI itself.

Classes

- class oepdev::ShellCombinationsIterator

    Iterator for Shell Combinations. Abstract Base.
- class oepdev::AOIntegralsIterator

    Iterator for AO Integrals. Abstract Base.
- class oepdev::AllAOShellCombinationsIterator_4

    Loop over all possible ERI shells in a shell quartet.
- class oepdev::AllAOShellCombinationsIterator_2

    Loop over all possible ERI shells in a shell doublet.
- class oepdev::AllAOIntegralsIterator_4

    Loop over all possible ERI within a particular shell quartet.
- class oepdev::AllAOIntegralsIterator_2

    Loop over all possible ERI within a particular shell doublet.

Typedefs

- using oepdev::SharedShellsIterator = std::shared_ptr< ShellCombinationsIterator >

    Iterator over shells as shared pointer.
- using oepdev::SharedAOIntsIterator = std::shared_ptr< AOIntegralsIterator >

    Iterator over AO integrals as shared pointer.

15.5.1 Detailed Description

You will find here various iterators to go through shells while computing ERI, or iterators over ERI itself.

15.6   The Three-Dimensional Scalar Fields Library

Handles all sorts of scalar distributions in 3D Euclidean space, such as potentials defined at particular collection of points. In this Module, you will also find handling both random and ordered points collections in a form of a G09 cube, as well as handling G09 Cube files.

Classes

- class oepdev::Points3DIterator

  Iterator over a collection of points in 3D space. Abstract base.

- class oepdev::CubePoints3DIterator

  Iterator over a collection of points in 3D space. g09 Cube-like order.

- class oepdev::RandomPoints3DIterator

  Iterator over a collection of points in 3D space. Random collection.

- class oepdev::PointsCollection3D

  Collection of points in 3D space. Abstract base.

- class oepdev::RandomPointsCollection3D

  Collection of random points in 3D space.

- class oepdev::CubePointsCollection3D

  G09 cube-like ordered collection of points in 3D space.

- class oepdev::ScalarField3D

  Scalar field in 3D space. Abstract base.

- class oepdev::ElectrostaticPotential3D

  Electrostatic potential of a molecule.

- class oepdev::OEPotential3D< T >

  Class template for OEP scalar fields.

Functions

- oepdev::OEPotential3D< T >::OEPotential3D (const int &np, const double &padding, std::shared_ptr< T > oep, const std::string &oepType)

  Construct random spherical collection of scalar field of type T.

- oepdev::OEPotential3D< T >::OEPotential3D (const int &nx, const int &ny, const int &nz, const double &px, const double &py, const double &pz, std::shared_ptr< T > oep, const std::string &oepType, psi::Options &options)

  Construct ordered 3D collection of scalar field of type T.

- virtual oepdev::OEPotential3D< T >::∼OEPotential3D ()

  Destructor.

- virtual void oepdev::OEPotential3D< T >::print () const

  Print information of the object to Psi4 output.

- virtual double oepdev::OEPotential3D< T >::compute_xyz (const double &x, const double &y, const double &z)

  Compute a value of scalar field at point (x, y, z)

15.6.1   Detailed Description

Handles all sorts of scalar distributions in 3D Euclidean space, such as potentials defined at particular collection of points. In this Module, you will also find handling both random and ordered points collections in a form of a G09 cube, as well as handling G09 Cube files.

15.6.2 Function Documentation

15.6.2.1 template<class T > **oepdev::OEPotential3D**< T >**::OEPotential3D (** const int & *np,* const double & *padding,* std::shared_ptr< T > *oep,* const std::string & *oepType* **)**

Construct random spherical collection of scalar field of type T.

The points are drawn according to uniform distrinution in 3D space.

Parameters

np	- number of points to draw
padding	- spherical padding distance (au)
oep	- OEP object of type T
oepType	- type of OEP

15.6.2.2 template<class T > **oepdev::OEPotential3D**< T >**::OEPotential3D (** const int & *nx,* const int & *ny,* const int & *nz,* const double & *px,* const double & *py,* const double & *pz,* std::shared_ptr< T > *oep,* const std::string & *oepType,* psi::Options & *options* **)**

Construct ordered 3D collection of scalar field of type T.

The points are generated according to Gaussian cube file format.

Parameters

nx	- number of points along x direction
ny	- number of points along y direction
nz	- number of points along z direction
px	- padding distance along x direction
py	- padding distance along y direction
pz	- padding distance along z direction
oep	- OEP object of type T
oepType	- type of OEP
options	- Psi4 options object

15.7 The Multipole Fitting Library

Implements methods to fit the generalized multipole moments of a generalized density distribution based on the input generalized potential scalar field. Among others, you will find here the electrostatic potential (ESP) fitting method.

Classes

- class oepdev::ESPSolver

  Charges from Electrostatic Potential (ESP). A solver-type class.

Typedefs

- using **oepdev::SharedScalarField3D** = std::shared_ptr< ScalarField3D >

15.7.1 Detailed Description

Implements methods to fit the generalized multipole moments of a generalized density distribution based on the input generalized potential scalar field. Among others, you will find here the electrostatic potential (ESP) fitting method.

15.8 The Density Functional Theory Library

Implements the OEPDev ab initio DFT methods.

Implements the OEPDev ab initio DFT methods.

15.9 The OEPDev Utilities

Contains utility functions such as printing OEPDev preambule to the output file, class for wavefunction union etc.

Classes

- class oepdev::CPHF

    CPHF solver class.
- class oepdev::DIISManager

    DIIS manager.
- struct oepdev::PerturbCharges

    Structure to hold perturbing charges.
- class oepdev::RHFPerturbed

    RHF theory under electrostatic perturbation.
- struct oepdev::ABCD

    Simple structure to hold the Fourier series expansion coefficients.
- struct oepdev::Fourier9

    Simple structure to hold the Fourier series expansion coefficients for N=4.
- class oepdev::UnitaryOptimizer

    Find the optimim unitary matrix of quadratic matrix equation.
- class oepdev::UnitaryOptimizer_4_2

    Find the optimim unitary matrix for quartic-quadratic matrix equation with trace.
- class oepdev::WavefunctionUnion

    Union of two Wavefunction objects.

Macros

- #define OEPDEV_USE_PSI4_DIIS_MANAGER 0

    Use DIIS from Psi4 (1) or OEPDev (0)?
- #define OEPDEV_MAX_AM 8

    L_max.
- #define OEPDEV_N_MAX_AM 17

    2L_max+1
- #define OEPDEV_CRIT_ERI 1e-9

    ERI criterion for E12, E34, E123 and lambda$*$EXY coefficients.
- #define OEPDEV_SIZE_BUFFER_R 250563

    *Size of R buffer (OEPDEV_N_MAX_AM$*$OEPDEV_N_MAX_AM$*$OEPDEV_N_MAX_AM$*$OEPDEV_N_MAX_AM$*$3)*
- #define OEPDEV_SIZE_BUFFER_D2 3264

    Size of D2 buffer (3$*$(OEPDEV_MAX_AM+1)$*$(OEPDEV_MAX_AM+1)$*$OEPDEV_N_MAX_AM)

Functions

- void oepdev::preambule (void)

    Print preambule for module OEPDEV.
- template$<$typename... Args$>$
    std::string oepdev::string_sprintf (const char $*$format, Args...args)

    Format string output. Example: std::string text = oepdev::string_sprinff("Test %3d, %13.5f", 5, -10.5425);.
- std::shared_ptr$<$ SuperFunctional $>$ oepdev::create_superfunctional (std::string name, Options &options)

    Set up DFT functional.

- std::shared_ptr< Molecule > oepdev::extract_monomer (std::shared_ptr< const Molecule > molecule_-dimer, int id)

    Extract molecule from dimer.

- std::shared_ptr< Wavefunction > oepdev::solve_scf (std::shared_ptr< Molecule > molecule, std::shared_-ptr< BasisSet > primary, std::shared_ptr< SuperFunctional > functional, Options &options, std::shared_-ptr< PSIO > psio)

    Solve RHF-SCF equations for a given molecule in a given basis set.

- double oepdev::average_moment (std::shared_ptr< psi::Vector > moment)

    Compute the scalar magnitude of multipole moment.

15.9.1 Detailed Description

Contains utility functions such as printing OEPDev preambule to the output file, class for wavefunction union etc.

15.9.2 Function Documentation

15.9.2.1 double oepdev::average_moment (std::shared_ptr< psi::Vector > *moment*)

Compute the scalar magnitude of multipole moment.

Parameters

moment	- multipole moment vector with unique matrix elements. Now supported only for dipole and quadrupole.

Returns

- the average multipole moment value.

The magnitudes of multipole moments are defined here as follows:

- The dipole moment magnitude is just a norm

$$|\mu| \equiv \sqrt{\mu_x^2 + \mu_y^2 + \mu_z^2}$$

- The quadrupole moment magnitude refers to the traceless moment in Buckingham convention

$$|\Theta| \equiv \sqrt{\Theta_{zz}^2 + \frac{1}{3}(\Theta_{xx} - \Theta_{yy})^2 + \frac{4}{3}(\Theta_{xy}^2 + \Theta_{xz}^2 + \Theta_{yz}^2)}$$

In the above equation, the quadrupole moment elements refer to its traceless form.

15.9.2.2 std::shared_ptr< SuperFunctional > oepdev::create_superfunctional (std::string *name,* Options & *options*)

Set up DFT functional.

Now it accepts only pure HF functional.

Parameters

name	name of the functional ("HF" is now only available)
options	psi::Options object

Returns

psi::SharedSuperFunctional object with functional.

Examples:

example_scf_perturb.cc.

15.9.2.3   std::shared_ptr< Molecule > oepdev::extract_monomer (std::shared_ptr< const Molecule > *molecule_dimer,* int *id*)

Extract molecule from dimer.

Parameters

molecule_dimer	psi::SharedMolecule object with dimer
id	index of a molecule (starts from 1)

Returns

> psi::SharedMolecule object with indicated monomer

15.9.2.4   std::shared_ptr< Wavefunction > oepdev::solve_scf (std::shared_ptr< Molecule > *molecule,* std::shared_ptr< BasisSet > *primary,* std::shared_ptr< SuperFunctional > *functional,* Options & *options,* std::shared_ptr< PSIO > *psio*)

Solve RHF-SCF equations for a given molecule in a given basis set.

Parameters

molecule	psi::SharedMolecule object with molecule
primary	shared primary basis set
functional	DFT functional
options	psi::Options object
psio	psi::PSIO object

Returns

> psi::SharedWavefunction SCF wavefunction of the molecule

15.10 The OEPDev Testing Platform Library

Testing platform at C++ level of code. You should add more tests here when developing new functionalities, theories or models.

Classes

- class oepdev::test::Test

  Manages test routines.

15.10.1 Detailed Description

Testing platform at C++ level of code. You should add more tests here when developing new functionalities, theories or models.

Chapter 16

Namespace Documentation

16.1 oepdev Namespace Reference

OEPDev module namespace.

Classes

- class GenEffPar

    Generalized Effective Fragment Parameters. Container Class.
- class GenEffFrag

    Generalized Effective Fragment. Container Class.
- class GenEffParFactory

    Generalized Effective Fragment Factory. Abstract Base.
- class PolarGEFactory

    Polarization GEFP Factory. Abstract Base.
- class AbInitioPolarGEFactory

    Polarization GEFP Factory from First Principles. Hartree-Fock Approximation.
- class FFAbInitioPolarGEFactory

    Polarization GEFP Factory from First Principles: Finite-Difference Model. Arbitrary level of theory.
- class GeneralizedPolarGEFactory

    Polarization GEFP Factory with Least-Squares Parameterization.
- class UniformEFieldPolarGEFactory

    Polarization GEFP Factory with Least-Squares Parameterization.
- class NonUniformEFieldPolarGEFactory

    Polarization GEFP Factory with Least-Squares Parameterization.
- class LinearUniformEFieldPolarGEFactory

    Polarization GEFP Factory with Least-Squares Parameterization.
- class QuadraticUniformEFieldPolarGEFactory

    Polarization GEFP Factory with Least-Squares Parameterization.
- class LinearNonUniformEFieldPolarGEFactory

    Polarization GEFP Factory with Least-Squares Parameterization.
- class QuadraticNonUniformEFieldPolarGEFactory

    Polarization GEFP Factory with Least-Squares Parameterization.
- class LinearGradientNonUniformEFieldPolarGEFactory

    Polarization GEFP Factory with Least-Squares Parameterization.
- class QuadraticGradientNonUniformEFieldPolarGEFactory

    Polarization GEFP Factory with Least-Squares Parameterization.

- class UnitaryTransformedMOPolarGEFactory

  Polarization GEFP Factory with Least-Squares Scaling of MO Space.
- class TwoElectronInt

  General Two Electron Integral.
- class ERI_1_1

  2-centre ERI of the form (a|O(2)|b) where O(2) = 1/r12.
- class ERI_2_2

  4-centre ERI of the form (ab|O(2)|cd) where O(2) = 1/r12.
- class ERI_3_1

  4-centre ERI of the form (abc|O(2)|d) where O(2) = 1/r12.
- struct OEPType

  Container to handle the type of One-Electron Potentials.
- class OEPotential

  Generalized One-Electron Potential: Abstract base.
- class ElectrostaticEnergyOEPotential

  Generalized One-Electron Potential for Electrostatic Energy.
- class RepulsionEnergyOEPotential

  Generalized One-Electron Potential for Pauli Repulsion Energy.
- class ChargeTransferEnergyOEPotential

  Generalized One-Electron Potential for Charge-Transfer Interaction Energy.
- class EETCouplingOEPotential

  Generalized One-Electron Potential for EET coupling calculations.
- class GeneralizedDensityFit

  Generalized Density Fitting Scheme. Abstract Base.
- class SingleGeneralizedDensityFit

  Generalized Density Fitting Scheme - Single Fit.
- class DoubleGeneralizedDensityFit

  Generalized Density Fitting Scheme - Double Fit.
- class TwoBodyAOInt
- class IntegralFactory

  Extended IntegralFactory for computing integrals.
- class PotentialInt

  Computes potential integrals.
- class CPHF

  CPHF solver class.
- class DIISManager

  DIIS manager.
- class ESPSolver

  Charges from Electrostatic Potential (ESP). A solver-type class.
- class ShellCombinationsIterator

  Iterator for Shell Combinations. Abstract Base.
- class AOIntegralsIterator

  Iterator for AO Integrals. Abstract Base.
- class AllAOShellCombinationsIterator_4

  Loop over all possible ERI shells in a shell quartet.
- class AllAOShellCombinationsIterator_2

  Loop over all possible ERI shells in a shell doublet.
- class AllAOIntegralsIterator_4

  Loop over all possible ERI within a particular shell quartet.
- class AllAOIntegralsIterator_2

  Loop over all possible ERI within a particular shell doublet.

- struct PerturbCharges

    Structure to hold perturbing charges.

- class RHFPerturbed

    RHF theory under electrostatic perturbation.

- class OEPDevSolver

    Solver of properties of molecular aggregates. Abstract base.

- class ElectrostaticEnergySolver

    Compute the Coulombic interaction energy between unperturbed wavefunctions.

- class RepulsionEnergySolver

    Compute the Pauli-Repulsion interaction energy between unperturbed wavefunctions.

- class ChargeTransferEnergySolver

    Compute the Charge-Transfer interaction energy between unperturbed wavefunctions.

- class Points3DIterator

    Iterator over a collection of points in 3D space. Abstract base.

- class CubePoints3DIterator

    Iterator over a collection of points in 3D space. g09 Cube-like order.

- class RandomPoints3DIterator

    Iterator over a collection of points in 3D space. Random collection.

- class PointsCollection3D

    Collection of points in 3D space. Abstract base.

- class RandomPointsCollection3D

    Collection of random points in 3D space.

- class CubePointsCollection3D

    G09 cube-like ordered collection of points in 3D space.

- class ScalarField3D

    Scalar field in 3D space. Abstract base.

- class ElectrostaticPotential3D

    Electrostatic potential of a molecule.

- class OEPotential3D

    Class template for OEP scalar fields.

- struct ABCD

    Simple structure to hold the Fourier series expansion coefficients.

- struct Fourier9

    Simple structure to hold the Fourier series expansion coefficients for N=4.

- class UnitaryOptimizer

    Find the optimim unitary matrix of quadratic matrix equation.

- class UnitaryOptimizer_4_2

    Find the optimim unitary matrix for quartic-quadratic matrix equation with trace.

- class WavefunctionUnion

    Union of two Wavefunction objects.

Typedefs

- using **SharedWavefunction** = std::shared_ptr< Wavefunction >
- using **SharedBasisSet** = std::shared_ptr< BasisSet >
- using **SharedTensor** = std::shared_ptr< Tensor >
- using **SharedMatrix** = std::shared_ptr< Matrix >
- using **SharedVector** = std::shared_ptr< Vector >
- using **SharedScalarField3D** = std::shared_ptr< ScalarField3D >
- using **SharedIntegralFactory** = std::shared_ptr< IntegralFactory >
- using **SharedTwoBodyAOInt** = std::shared_ptr< TwoBodyAOInt >

- using [SharedShellsIterator](#) = std::shared_ptr< [ShellCombinationsIterator](#) >

    Iterator over shells as shared pointer.
- using [SharedAOIntsIterator](#) = std::shared_ptr< [AOIntegralsIterator](#) >

    Iterator over AO integrals as shared pointer.
- using **SharedWavefunctionUnion** = std::shared_ptr< [WavefunctionUnion](#) >
- using **SharedOEPotential** = std::shared_ptr< [OEPotential](#) >
- using **SharedMolecule** = std::shared_ptr< Molecule >
- using **SharedSuperFunctional** = std::shared_ptr< SuperFunctional >
- using **SharedMOSpace** = std::shared_ptr< MOSpace >
- using **SharedMOSpaceVector** = std::vector< std::shared_ptr< MOSpace >>
- using **SharedIntegralTransform** = std::shared_ptr< IntegralTransform >
- using **SharedLocalizer** = std::shared_ptr< Localizer >

Functions

- **n_max_am_** (2 ∗max_am_+1)
- double [d_N_n1_n2](#) (int N, int n1, int n2, double PA, double PB, double aP)

    Compute McMurchie-Davidson-Hermite (MDH) coefficient for binomial expansion.
- void [make_mdh_D2_coeff_explicit_recursion](#) (int n1, int n2, double aP, double ∗PA, double ∗PB, double ∗buffer)

    Compute the McMurchie-Davidson-Hermite coefficients for binomial expansion by explicit recursion. This function makes the same changes to buffers as [oepdev::make_mdh_D2_coeff](#), but implements it through explicit recursion by calls to [oepdev::d_N_n1_n2](#). Therefore, it is slightly slower. Here for debugging purposes.
- void [make_mdh_D1_coeff](#) (int n1, double aPd, double ∗buffer)

    Compute the McMurchie-Davidson-Hermite coefficients for monomial expansion.
- void [make_mdh_D2_coeff](#) (int n1, int n2, double aPd, double ∗PA, double ∗PB, double ∗buffer)

    Compute the McMurchie-Davidson-Hermite coefficients for binomial expansion.
- void [make_mdh_D3_coeff](#) (int n1, int n2, int n3, double aPd, double ∗PA, double ∗PB, double ∗PC, double ∗buffer)

    Compute the McMurchie-Davidson-Hermite coefficients for trinomial expansion.
- void [make_mdh_R_coeff](#) (int N, int L, int M, double alpha, double a, double b, double c, double ∗F, double ∗buffer)

    Compute the McMurchie-Davidson R coefficients.
- constexpr std::complex< double > **operator""_i** (unsigned long long d)
- constexpr std::complex< double > **operator""_i** (long double d)
- void [preambule](#) (void)

    Print preambule for module OEPDEV.
- std::shared_ptr< SuperFunctional > [create_superfunctional](#) (std::string name, Options &options)

    Set up DFT functional.
- std::shared_ptr< Molecule > [extract_monomer](#) (std::shared_ptr< const Molecule > molecule_dimer, int id)

    Extract molecule from dimer.
- std::shared_ptr< Wavefunction > [solve_scf](#) (std::shared_ptr< Molecule > molecule, std::shared_ptr< BasisSet > primary, std::shared_ptr< SuperFunctional > functional, Options &options, std::shared_ptr< PSIO > psio)

    Solve RHF-SCF equations for a given molecule in a given basis set.
- double [average_moment](#) (std::shared_ptr< psi::Vector > moment)

    Compute the scalar magnitude of multipole moment.
- template<typename... Args>
    std::string [string_sprintf](#) (const char ∗format, Args...args)

    Format string output. Example: std::string text = oepdev::string_sprinff("Test %3d, %13.5f", 5, -10.5425);.

16.1.1   Detailed Description

OEPDev module namespace. Contains all the functionalities for the development of the Generalized One-Electroc Potentials (OEP's).

16.2   psi Namespace Reference

Psi4 package namespace.

Typedefs

- using **SharedVetor** = std::shared_ptr< Vector >
- using **SharedBasisSet** = std::shared_ptr< BasisSet >
- using **SharedMolecule** = std::shared_ptr< Molecule >
- using **SharedMatrix** = std::shared_ptr< Matrix >
- using **SharedWavefunction** = std::shared_ptr< Wavefunction >

Functions

- int read_options (std::string name, Options &options)

  Options for the OEPDev plugin.
- SharedWavefunction oepdev (SharedWavefunction ref_wfn, Options &options)

  Main routine of the OEPDev plugin.

16.2.1   Detailed Description

Psi4 package namespace. Contains all Psi4 functionalities.

16.2.2   Function Documentation

16.2.2.1   SharedWavefunction psi::oepdev (SharedWavefunction *ref_wfn,* Options & *options*)

Main routine of the OEPDev plugin.

Created with intention to test various models of the interaction energy between two molecules, described by the Hartree-Fock-Roothaan-Hall theory or the configuration interaction with singles theory.

In particular, the plugin tests the models of:

1. the Pauli repulsion and CT interaction energy (Project II)

2. the Induction interaction energy (Project III)

3. the excitation energy transfer couplings (Project I)

against benchmarks (exact or reference solutions). The list of implemented models can be found in Implemented Models .

Parameters

| *ref_wfn* | shared wavefunction of a dimer |
| *options* | psi::Options object |

Returns

    psi::SharedWavefunction (either ref_wfn or wavefunction union)

16.2.2.2   int psi::read_options (std::string *name,* Options & *options*)

Options for the OEPDev plugin.

Parameters

| *name* | name of driver function |
| *options* | psi::Options object |

Returns

    true

Chapter 17

Class Documentation

17.1 oepdev::ABCD Struct Reference

Simple structure to hold the Fourier series expansion coefficients.

```
#include <unitary_optimizer.h>
```

Public Attributes

- double **A**
- double **B**
- double **C**
- double **D**

17.1.1 Detailed Description

Simple structure to hold the Fourier series expansion coefficients.

The documentation for this struct was generated from the following file:

- oepdev/libutil/unitary_optimizer.h

17.2 oepdev::AbInitioPolarGEFactory Class Reference

Polarization GEFP Factory from First Principles. Hartree-Fock Approximation.

```
#include <gefp.h>
```

Inheritance diagram for oepdev::AbInitioPolarGEFactory:
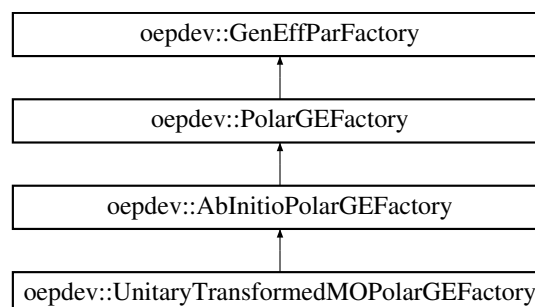
Public Member Functions

- **AbInitioPolarGEFactory** (std::shared_ptr< psi::Wavefunction > wfn, psi::Options &opt)
- virtual std::shared_ptr
  < GenEffPar > compute (void)

    Compute the density matrix susceptibility tensors.

Additional Inherited Members

17.2.1 Detailed Description

Polarization GEFP Factory from First Principles. Hartree-Fock Approximation.

Implements creation of the density matrix susceptibility tensors for which $\mathbf{X} = \mathbf{1}$. Guarantees the idempotency of the density matrix up to first-order in LCAO-MO variation. The density matrix susceptibility tensor is represented by:

$$\delta D_{\alpha\beta} = \sum_i \mathbf{B}_{\alpha\beta}^{(i;1)} \cdot \mathbf{F}(\mathbf{r}_i)$$

where $\mathbf{B}_{\alpha\beta}^{(i;1)}$ is the density matrix dipole polarizability defined for the distributed LMO site at $\mathbf{r}_i$. Its explicit form is given by

$$\mathbf{B}_{\alpha\beta}^{(i;1)} = C_{\alpha i}^{(0)} \mathbf{b}_{\beta}^{(i;1)} C_{\beta i}^{(0)} \mathbf{b}_{\alpha}^{(i;1)} - \sum_\gamma \left(D_{\alpha\gamma}^{(0)} C_{\beta i}^{(0)} + D_{\beta\gamma}^{(0)} C_{\alpha i}^{(0)} \right) \mathbf{b}_{\gamma}^{(i;1)}$$

where the susceptibility of the LCAO-MO coefficient is given by

$$b_{\alpha;w}^{(i;1)} = \frac{1}{4} \sum_u^{x,y,z} [\alpha_i]_{uw} \left[[\mathbf{L}_i]_{\text{Left}}^{-1} \right]_{u;\alpha}$$

for $w = x, y, z$. The auxiliary tensor $\mathbb{L}$ is defined as

$$\mathbb{L} = \mathbf{C}^{(0)\mathrm{T}} \cdot \mathbb{M} \cdot \left(\mathbf{1} - \mathbf{D}^{(0)} \right)$$

where $\mathbb{M}$ is the dipole integral vector of matrices in AO representation. The left inverse of the i-th element is defined as

$$[\mathbf{L}_i]_{\text{Left}}^{-1} \equiv \left[\mathbf{L}_i^{\mathrm{T}} \cdot \mathbf{L}_i \right]^{-1} \cdot \mathbf{L}_i^{\mathrm{T}}$$

Note that $\mathbf{L}_i \equiv [\mathbb{L}]_i$ is a $n \times 3$ matrix, whereas its left inverse is a $3 \times n$ matrix with n being the size of the AO basis set.

The documentation for this class was generated from the following files:

- oepdev/libgefp/gefp.h
- oepdev/libgefp/gefp_polar_abinitio.cc

17.3 oepdev::AllAOIntegralsIterator_2 Class Reference

Loop over all possible ERI within a particular shell doublet.

```
#include <integrals_iter.h>
```
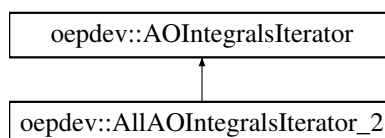
Inheritance diagram for oepdev::AllAOIntegralsIterator_2:

Public Member Functions

- AllAOIntegralsIterator_2 (const ShellCombinationsIterator ∗shellIter)

  Construct by shell iterator (const object)
- AllAOIntegralsIterator_2 (std::shared_ptr< ShellCombinationsIterator > shellIter)

  Construct by shell iterator (pointed by shared pointer)
- void first ()

  First iteration.
- void next ()

  Next iteration.
- int i () const

  Grab the current integral i index.
- int j () const

  Grab the current integral j index.
- int index () const

Additional Inherited Members

17.3.1   Detailed Description

Loop over all possible ERI within a particular shell doublet.

Constructed by providing a const reference or shared pointer to an AllAOShellCombinationsIterator object.

See Also

> AllAOShellCombinationsIterator_2

17.3.2   Constructor & Destructor Documentation

17.3.2.1   AllAOIntegralsIterator_2::AllAOIntegralsIterator_2 (const ShellCombinationsIterator ∗ shellIter)

Construct by shell iterator (const object)

Parameters

shellIter	- shell iterator object

17.3.2.2   AllAOIntegralsIterator_2::AllAOIntegralsIterator_2 (std::shared_ptr< ShellCombinationsIterator > shellIter)

Construct by shell iterator (pointed by shared pointer)

Parameters

shellIter	- shell iterator object

17.3.3   Member Function Documentation

17.3.3.1   int oepdev::AllAOIntegralsIterator_2::index (void) const `[inline],[virtual]`

Grab the current index of integral value stored in the buffer

Implements oepdev::AOIntegralsIterator.

The documentation for this class was generated from the following files:

- oepdev/libutil/integrals_iter.h
- oepdev/libutil/integrals_iter.cc

17.4 oepdev::AllAOIntegralsIterator_4 Class Reference

Loop over all possible ERI within a particular shell quartet.

```
#include <integrals_iter.h>
```
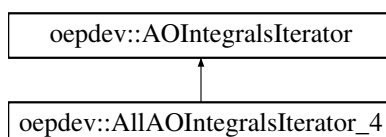
Inheritance diagram for oepdev::AllAOIntegralsIterator_4:

```
┌─────────────────────────────────┐
│  oepdev::AOIntegralsIterator     │
└─────────────────────────────────┘
                 ▲
                 │
┌─────────────────────────────────┐
│  oepdev::AllAOIntegralsIterator_4│
└─────────────────────────────────┘
```

Public Member Functions

- [AllAOIntegralsIterator_4](#) (const [ShellCombinationsIterator](#) *shellIter)

    Construct by shell iterator (const object)
- [AllAOIntegralsIterator_4](#) (std::shared_ptr< [ShellCombinationsIterator](#) > shellIter)

    Construct by shell iterator (pointed by shared pointer)
- void [first](#) ()

    First iteration.
- void [next](#) ()

    Next iteration.
- int [i](#) () const

    Grab the current integral i index.
- int [j](#) () const

    Grab the current integral j index.
- int [k](#) () const

    Grab the current integral k index.
- int [l](#) () const

    Grab the current integral l index.
- int [index](#) () const

Additional Inherited Members

17.4.1 Detailed Description

Loop over all possible ERI within a particular shell quartet.

Constructed by providing a const reference or shared pointer to an AllAOShellCombinationsIterator object.

See Also

> [AllAOShellCombinationsIterator_4](#)

17.4.2 Constructor & Destructor Documentation

17.4.2.1 AllAOIntegralsIterator_4::AllAOIntegralsIterator_4 (const ShellCombinationsIterator ∗ shellIter)

Construct by shell iterator (const object)

Parameters

shellIter	- shell iterator object

17.4.2.2 AllAOIntegralsIterator_4::AllAOIntegralsIterator_4 (std::shared_ptr< ShellCombinationsIterator > *shellIter*)

Construct by shell iterator (pointed by shared pointer)

Parameters

shellIter	- shell iterator object

17.4.3 Member Function Documentation

17.4.3.1 int oepdev::AllAOIntegralsIterator_4::index (void) const `[inline]`,`[virtual]`

Grab the current index of integral value stored in the buffer

Implements oepdev::AOIntegralsIterator.

The documentation for this class was generated from the following files:

- oepdev/libutil/integrals_iter.h
- oepdev/libutil/integrals_iter.cc

17.5 oepdev::AllAOShellCombinationsIterator_2 Class Reference

Loop over all possible ERI shells in a shell doublet.

```
#include <integrals_iter.h>
```

Inheritance diagram for oepdev::AllAOShellCombinationsIterator_2:

```
┌─────────────────────────────────────────┐
│     oepdev::ShellCombinationsIterator    │
└─────────────────────────────────────────┘
                    ▲
┌─────────────────────────────────────────┐
│ oepdev::AllAOShellCombinationsIterator_2 │
└─────────────────────────────────────────┘
```

Public Member Functions

- AllAOShellCombinationsIterator_2 (SharedBasisSet bs_1, SharedBasisSet bs_2)

  Iterate over shell doublets. Construct by providing basis sets for each axis. The basis sets must be defined for the same molecule.
- AllAOShellCombinationsIterator_2 (std::shared_ptr< IntegralFactory > integrals)

  Construct by providing integral factory.
- AllAOShellCombinationsIterator_2 (const IntegralFactory &integrals)
- AllAOShellCombinationsIterator_2 (std::shared_ptr< psi::IntegralFactory > integrals)

  Construct by providing integral factory.
- AllAOShellCombinationsIterator_2 (const psi::IntegralFactory &integrals)
- void first ()

  First iteration.
- void next ()

  Next iteration.

- void compute_shell (std::shared_ptr< oepdev::TwoBodyAOInt > tei) const

    Compute ERI's for the current shell. The eris are stored in the buffer of the argument object.

- void **compute_shell** (std::shared_ptr< psi::TwoBodyAOInt > tei) const

- int P () const

    Grab the current shell P index.

- int Q () const

    Grab the current shell Q index.

Additional Inherited Members

17.5.1 Detailed Description

Loop over all possible ERI shells in a shell doublet.

Constructed by providing IntegralFactory object or shared pointers to two basis set spaces.

17.5.2 Constructor & Destructor Documentation

17.5.2.1 AllAOShellCombinationsIterator_2::AllAOShellCombinationsIterator_2 (SharedBasisSet *bs_1,* SharedBasisSet *bs_2*)

Iterate over shell doublets. Construct by providing basis sets for each axis. The basis sets must be defined for the same molecule.

Parameters

bs_1	- basis set of axis 1
bs_2	- basis set of axis 2

17.5.2.2 oepdev::AllAOShellCombinationsIterator_2::AllAOShellCombinationsIterator_2 (std::shared_ptr< **IntegralFactory** > *integrals*)

Construct by providing integral factory.

Parameters

integrals	- OepDev integral factory object

17.5.2.3 AllAOShellCombinationsIterator_2::AllAOShellCombinationsIterator_2 (const **IntegralFactory** & *integrals*)

This is an overloaded member function, provided for convenience. It differs from the above function only in what argument(s) it accepts.

17.5.2.4 AllAOShellCombinationsIterator_2::AllAOShellCombinationsIterator_2 (std::shared_ptr< psi::IntegralFactory > *integrals*)

Construct by providing integral factory.

Parameters

integrals	- Psi4 integral factory object

17.5.2.5 AllAOShellCombinationsIterator_2::AllAOShellCombinationsIterator_2 (const psi::IntegralFactory & *integrals*)

This is an overloaded member function, provided for convenience. It differs from the above function only in what argument(s) it accepts.

17.5.3 Member Function Documentation

17.5.3.1 void AllAOShellCombinationsIterator_2::compute_shell (std::shared_ptr< oepdev::TwoBodyAOInt > *tei*) const [virtual]

Compute ERI's for the current shell. The eris are stored in the buffer of the argument object.

Parameters

tei	- two electron AO integral

Implements oepdev::ShellCombinationsIterator.

The documentation for this class was generated from the following files:

- oepdev/libutil/integrals_iter.h
- oepdev/libutil/integrals_iter.cc

17.6 oepdev::AllAOShellCombinationsIterator_4 Class Reference

Loop over all possible ERI shells in a shell quartet.

```
#include <integrals_iter.h>
```

Inheritance diagram for oepdev::AllAOShellCombinationsIterator_4:

Public Member Functions

- AllAOShellCombinationsIterator_4 (SharedBasisSet bs_1, SharedBasisSet bs_2, SharedBasisSet bs_3, SharedBasisSet bs_4)

    Iterate over shell quartets. Construct by providing basis sets for each axis. The basis sets must be defined for the same molecule.
- AllAOShellCombinationsIterator_4 (std::shared_ptr< IntegralFactory > integrals)

    Construct by providing integral factory.
- AllAOShellCombinationsIterator_4 (const IntegralFactory &integrals)
- AllAOShellCombinationsIterator_4 (std::shared_ptr< psi::IntegralFactory > integrals)

    Construct by providing integral factory.
- AllAOShellCombinationsIterator_4 (const psi::IntegralFactory &integrals)
- void first ()

    Do the first iteration.
- void next ()

    Do the next iteration.
- void compute_shell (std::shared_ptr< oepdev::TwoBodyAOInt > tei) const
- void **compute_shell** (std::shared_ptr< psi::TwoBodyAOInt > tei) const

- int P () const

  Grab the current shell P index.

- int Q () const

  Grab the current shell Q index.

- int R () const

  Grab the current shell R index.

- int S () const

  Grab the current shell S index.

Additional Inherited Members

17.6.1 Detailed Description

Loop over all possible ERI shells in a shell quartet.

Constructed by providing IntegralFactory object or shared pointers to four basis set spaces.

17.6.2 Constructor & Destructor Documentation

17.6.2.1 AllAOShellCombinationsIterator_4::AllAOShellCombinationsIterator_4 (SharedBasisSet *bs_1,* SharedBasisSet *bs_2,* SharedBasisSet *bs_3,* SharedBasisSet *bs_4*)

Iterate over shell quartets. Construct by providing basis sets for each axis. The basis sets must be defined for the same molecule.

Parameters

bs_1	- basis set of axis 1
bs_2	- basis set of axis 2
bs_3	- basis set of axis 3
bs_4	- basis set of axis 4

17.6.2.2 oepdev::AllAOShellCombinationsIterator_4::AllAOShellCombinationsIterator_4 (std::shared_ptr< IntegralFactory > *integrals*)

Construct by providing integral factory.

Parameters

integrals	- OepDev integral factory object

17.6.2.3 AllAOShellCombinationsIterator_4::AllAOShellCombinationsIterator_4 (const IntegralFactory & *integrals*)

This is an overloaded member function, provided for convenience. It differs from the above function only in what argument(s) it accepts.

17.6.2.4 AllAOShellCombinationsIterator_4::AllAOShellCombinationsIterator_4 (std::shared_ptr< psi::IntegralFactory > *integrals*)

Construct by providing integral factory.

Parameters

integrals	- OepDev integral factory object

17.6.2.5 AllAOShellCombinationsIterator_4::AllAOShellCombinationsIterator_4 (const psi::IntegralFactory & *integrals*)

This is an overloaded member function, provided for convenience. It differs from the above function only in what argument(s) it accepts.

17.6.3 Member Function Documentation

17.6.3.1 void AllAOShellCombinationsIterator_4::compute_shell (std::shared_ptr< oepdev::TwoBodyAOInt > *tei*) const `[virtual]`

Compute integrals in a current shell. Works both for oepdev::TwoBodyAOInt and psi::TwoBodyAOInt

Parameters

tei	- two body integral object

Implements oepdev::ShellCombinationsIterator.

The documentation for this class was generated from the following files:

- oepdev/libutil/integrals_iter.h
- oepdev/libutil/integrals_iter.cc

17.7 oepdev::AOIntegralsIterator Class Reference

Iterator for AO Integrals. Abstract Base.

```
#include <integrals_iter.h>
```

Inheritance diagram for oepdev::AOIntegralsIterator:

```
┌─────────────────────────────┐
│  oepdev::AOIntegralsIterator │
└─────────────────────────────┘
              ▲
      ┌───────┴───────┐
┌──────────────────────────────┐ ┌──────────────────────────────┐
│ oepdev::AllAOIntegralsIterator_2 │ │ oepdev::AllAOIntegralsIterator_4 │
└──────────────────────────────┘ └──────────────────────────────┘
```
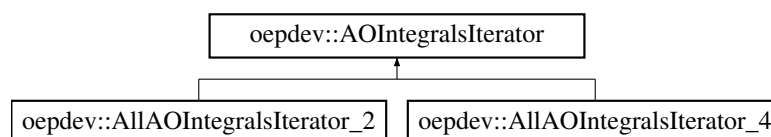
Public Member Functions

- AOIntegralsIterator ()

  Base Constructor.
- virtual ∼AOIntegralsIterator ()

  Base Destructor.
- virtual void first (void)=0

  Do the first iteration.
- virtual void next (void)=0

  Do the next iteration.
- virtual int i (void) const

  Grab i-th index.
- virtual int j (void) const

Grab j-th index.

- virtual int k (void) const

    Grab k-th index.

- virtual int l (void) const

    Grab l-th index.

- virtual int index (void) const =0

    Grab index in the integral buffer.

- virtual bool is_done (void)

    Returns the status of an iterator.

Static Public Member Functions

- static std::shared_ptr
    < AOIntegralsIterator > build (const ShellCombinationsIterator ∗shellIter, std::string mode="ALL")
- static std::shared_ptr
    < AOIntegralsIterator > build (std::shared_ptr< ShellCombinationsIterator > shellIter, std::string mode="A-
    LL")

Protected Attributes

- bool done

    The status of an iterator.

17.7.1   Detailed Description

Iterator for AO Integrals. Abstract Base.

17.7.2   Member Function Documentation

17.7.2.1   std::shared_ptr< **AOIntegralsIterator** > **AOIntegralsIterator::build (** const **ShellCombinationsIterator** ∗ *shellIter,* std::string *mode =* "ALL" **)** [static]

Build AO integrals iterator from current state of iterator over shells

Parameters

shellIter	- iterator over shells - either "ALL" or "UNIQUE" (iterate over all or unique integrals)

Returns

iterator over AO integrals

17.7.2.2   std::shared_ptr< **AOIntegralsIterator** > **AOIntegralsIterator::build (** std::shared_ptr< **ShellCombinationsIterator** > *shellIter,* std::string *mode =* "ALL" **)** [static]

This is an overloaded member function, provided for convenience. It differs from the above function only in what argument(s) it accepts.

The documentation for this class was generated from the following files:

- oepdev/libutil/integrals_iter.h
- oepdev/libutil/integrals_iter.cc

17.8 oepdev::ChargeTransferEnergyOEPotential Class Reference

Generalized One-Electron Potential for Charge-Transfer Interaction Energy.

`#include <oep.h>`
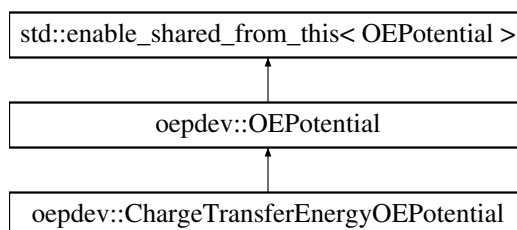
Inheritance diagram for oepdev::ChargeTransferEnergyOEPotential:

```
┌─────────────────────────────────────────────┐
│   std::enable_shared_from_this< OEPotential > │
└─────────────────────────────────────────────┘
                        ▲
                        │
┌─────────────────────────────────────────────┐
│              oepdev::OEPotential              │
└─────────────────────────────────────────────┘
                        ▲
                        │
┌─────────────────────────────────────────────┐
│    oepdev::ChargeTransferEnergyOEPotential    │
└─────────────────────────────────────────────┘
```

Public Member Functions

- **ChargeTransferEnergyOEPotential** (SharedWavefunction wfn, SharedBasisSet auxiliary, Options &options)
- **ChargeTransferEnergyOEPotential** (SharedWavefunction wfn, Options &options)
- virtual void compute (const std::string &oepType) override

    Compute matrix forms of all OEP's within a specified OEP type.

- virtual void compute_3D (const std::string &oepType, const double &x, const double &y, const double &z, double &v) override

    Compute value of potential in point x, y, z and save at v.

- virtual void **print_header** () const override

Additional Inherited Members

17.8.1 Detailed Description

Generalized One-Electron Potential for Charge-Transfer Interaction Energy.

Contains the following OEP types:

- `Otto-Ladik.V1` - DF-based term

- `Otto-Ladik.V2` - ESP-based term

- `Otto-Ladik.V3` - ESP-based term

The documentation for this class was generated from the following files:

- oepdev/liboep/oep.h
- oepdev/liboep/oep.cc

17.9 oepdev::ChargeTransferEnergySolver Class Reference

Compute the Charge-Transfer interaction energy between unperturbed wavefunctions.

`#include <solver.h>`

Inheritance diagram for oepdev::ChargeTransferEnergySolver:

std::enable_shared_from_this< OEPDevSolver >

↑

oepdev::OEPDevSolver

↑

oepdev::ChargeTransferEnergySolver
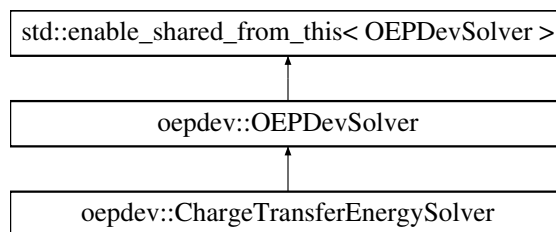
Public Member Functions

- **ChargeTransferEnergySolver** (SharedWavefunctionUnion wfn_union)
- virtual double compute_oep_based (const std::string &method="DEFAULT")

    Compute property by using OEP's.

- virtual double compute_benchmark (const std::string &method="DEFAULT")

    Compute property by using benchmark method.

Additional Inherited Members

17.9.1 Detailed Description

Compute the Charge-Transfer interaction energy between unperturbed wavefunctions.

The implemented methods are shown below

Keyword	Method Description
Benchmark Methods	
`OTTO_LADIK`	∗Default∗. CT energy at HF level from Otto and Ladik (1975).
`EFP2`	CT energy at HF level from EFP2 model.
OEP-Based Methods	
`OTTO_LADIK`	∗Default∗. OEP-based Otto-Ladik expressions.

Table 17.1: Methods available in the Solver

In order to construct this solver, **always** use the `OEPDevSolver::build` static factory method.

Below the detailed description of the implemented equations is given for each of the above provided methods. In the formulae across, it is assumed that the orbitals are real. The Coulomb notation for electron repulsion integrals (ERI's) is adopted; i.e,

$$(ac|bd) = \iint d\mathbf{r}_1 d\mathbf{r}_2 \phi_a(\mathbf{r}_1)\phi_c(\mathbf{r}_1)\frac{1}{r_{12}}\phi_b(\mathbf{r}_2)\phi_d(\mathbf{r}_2)$$

Greek subscripts denote basis set orbitals whereas Italic subscripts denote the occupied molecular orbitals.

The CT energy between molecules *A* and *B* is given by

$$E^{\mathrm{CT}} = E^{\mathrm{A^+B^-}} + E^{\mathrm{A^-B^+}}$$

Benchmark Methods

CT energy at HF level by Otto and Ladik (1975).

For a closed-shell system, CT energy equation of Otto and Ladik becomes

$$E^{A^+B^-} \approx 2 \sum_{i \in A}^{\text{Occ}_A} \sum_{n \in B}^{\text{Vir}_B} \frac{V_{in}^2}{\varepsilon_i - \varepsilon_n}$$

where

$$V_{in} = V_{in}^B + 2 \sum_{j \in B}^{\text{Occ}_B} (in|jj) - \sum_{k \in A}^{\text{Occ}_A} S_{kn} \left\{ V_{ik}^B + 2 \sum_{j \in B}^{\text{Occ}_B} (ik|jj) \right\}$$
$$- \sum_{j \in B}^{\text{Occ}_B} \left[S_{ij} \left\{ V_{nj}^A + 2 \sum_{k \in A}^{\text{Occ}_A} (1 - \delta_{ik})(nj|kk) \right\} - (nj|ij) \right] + \sum_{k \in A}^{\text{Occ}_A} \sum_{j \in B}^{\text{Occ}_B} S_{kj}(1 - \delta_{ik})(ik|nj)$$

and analogously the twin term.

CT energy at HF level by EFP2.

In EFP2 method, CT energy is given as

$$E^{A^+B^-} \approx 2 \sum_{i \in A}^{\text{Occ}_A} \sum_{n \in B}^{\text{Vir}_B} \frac{V_{in}^2}{F_{ii} - T_{nn}}$$

where

$$V_{in}^2 = \frac{V_{in}^B - \sum_{m \in A}^{\text{All}_A} V_{im} S_{mn}^B}{1 - \sum_{m \in A}^{\text{All}_A} S_{mn}^2} \left\{ V_{in}^B - \sum_{m \in A}^{\text{All}_A} V_{im}^B S_{mn} + \sum_{j \in B}^{\text{Occ}_B} S_{ij} \left(T_{nj} - \sum_{m \in A}^{\text{All}_A} S_{nm} T_{mj} \right) \right\}$$

and analogously the twin term.

OEP-Based Methods

OEP-Based Otto-Ladik's theory

After introducing OEP's, the original Otto-Ladik's theory is reformulated *without* approximation as

$$E^{A^+B^-} \approx 2 \sum_{i \in A}^{\text{Occ}_A} \sum_{n \in B}^{\text{Vir}_B} \frac{\left(V_{in}^{\text{DF}} + V_{in}^{\text{ESP,A}} + V_{in}^{\text{ESP,B}} \right)^2}{\varepsilon_i - \varepsilon_n}$$

where

$$V_{in}^{\text{DF}} = \sum_{\eta \in B}^{\text{Aux}_B} S_{i\eta} G_{\eta n}^B$$

$$V_{in}^{\text{ESP,A}} = \sum_{k \in A}^{\text{Occ}_A} \sum_{j \in B}^{\text{Occ}_B} S_{kj} \sum_{x \in A} V_{nj}^{(x)} q_{ik}^{(x)}$$

$$V_{in}^{\text{ESP,B}} = - \sum_{k \in A}^{\text{Occ}_A} S_{kn} V_{ik}^B$$

The OEP matrix for density fitted part is given by

$$G_{\eta n}^B = \sum_{\eta' \in B}^{\text{Aux}_B} [\mathbf{S}^{-1}]_{\eta \eta'} \left\{ V_{\eta' n}^B + \sum_{j \in B}^{\text{Occ}_B} \left[2(\eta' n|jj) - (\eta' j|nj) \right] \right\}$$

The OEP ESP-A charges are fit to reproduce the OEP potential

$$v_{ik}^A(\mathbf{r}) \equiv (1-\delta_{ik}) \int \frac{\phi_i(\mathbf{r}')\phi_k(\mathbf{r}')}{|\mathbf{r}-\mathbf{r}'|}\, d\mathbf{r}' - \delta_{ik} \left(\sum_{x\in A} \frac{-Z_x}{|\mathbf{r}-\mathbf{r}_x|} + 2 \sum_{k\in A}^{\mathrm{Occ_A}} \int \frac{\phi_k(\mathbf{r}')\phi_k(\mathbf{r}')}{|\mathbf{r}-\mathbf{r}'|}\, d\mathbf{r}' - 2 \int \frac{\phi_i(\mathbf{r}')\phi_i(\mathbf{r}')}{|\mathbf{r}-\mathbf{r}'|}\, d\mathbf{r}' \right)$$

so that

$$v_{ik}^A(\mathbf{r}) \cong \sum_{x\in A} \frac{q_{ik}^{(x)}}{|\mathbf{r}-\mathbf{r}_x|}$$

The OEP ESP-B charges are fit to reproduce the electrostatic potential of molecule *B* (they are standard ESP charges).

17.9.2 Member Function Documentation

17.9.2.1 double ChargeTransferEnergySolver::compute_benchmark (const std::string & *method =* `"DEFAULT"`) `[virtual]`

Compute property by using benchmark method.

Each solver object has one `DEFAULT` benchmark method

Parameters

method	- benchmark method

Implements oepdev::OEPDevSolver.

17.9.2.2 double ChargeTransferEnergySolver::compute_oep_based (const std::string & *method =* `"DEFAULT"`) `[virtual]`

Compute property by using OEP's.

Each solver object has one `DEFAULT` OEP-based method.

Parameters

method	- flavour of OEP model

Implements oepdev::OEPDevSolver.

The documentation for this class was generated from the following files:

- oepdev/libutil/solver.h
- oepdev/libutil/solver.cc

17.10 oepdev::CPHF Class Reference

CPHF solver class.

```
#include <cphf.h>
```

Public Member Functions

- CPHF (SharedWavefunction ref_wfn, Options &options)

  Constructor.
- ∼CPHF ()

  Desctructor.
- void compute (void)

    run the calculations

- void print (void) const

    print to output file

- int nocc (void) const

    get the number of occupied orbitals

- std::shared_ptr< Wavefunction > wfn (void) const

    grab the wavefunction

- Options & options (void) const

    grab the Psi4 options

- std::shared_ptr< Matrix > polarizability (void) const

    retrieve the molecular (total) polarizability

- std::shared_ptr< Matrix > polarizability (int i) const

    retrieve the i-th orbital-associated polarizability

- std::shared_ptr< Matrix > polarizability (int i, int j) const

    retrieve the charge-transfer polarizability associated with orbitals i and j

- std::shared_ptr< Matrix > X (int x) const

    retrieve the X operator O-V perturbation matrix in AO basis for x-th component

- std::shared_ptr< Vector > lmo_centroid (int i) const

    retrieve the i-th orbital (LMO) centroid

- std::shared_ptr< Localizer > localizer (void) const

    retrieve the orbital localizer

Protected Attributes

- std::shared_ptr
  < psi::Wavefunction > _wfn

    Wavefunction object.

- std::shared_ptr< Localizer > _localizer

    Orbital localizer.

- const int _no

    Number of occupied orbitals.

- const int _nv

    Number of virtual orbitals.

- const int _nn

    Number of basis functions.

- long int _memory

    Memory.

- int _maxiter

    Maximum number of iterations.

- double _conv

    CPHF convergence threshold.

- bool _with_diis

    whether use DIIS or not

- const int _diis_dim

    Size of subspace.

- std::shared_ptr< BasisSet > _primary

    Primary Basis Set.

- std::shared_ptr< Matrix > _cocc

    Occupied orbitals.

- std::shared_ptr< Matrix > _cvir

Virtual orbitals.

- std::shared_ptr< Vector > _eps_occ

    Occupied orbital energies.

- std::shared_ptr< Vector > _eps_vir

    Virtual orbital energies.

- std::vector< std::shared_ptr
  < oepdev::DIISManager > > _diis

    the DIIS managers for each perturbation operator x, y and z

- Options & _options

    Options.

- std::shared_ptr< Matrix > _molecularPolarizability

    Total (molecular) polarizability tensor.

- std::vector< std::shared_ptr
  < Vector > > _orbitalCentroids

    LMO centroids.

- std::vector< std::shared_ptr
  < Matrix > > _orbitalPolarizabilities

    orbital-associated polarizability tensors

- std::vector< std::vector
  < std::shared_ptr< Matrix > > > _orbitalChargeTransferPolarizabilities

    orbital-orbital charge-transfer polarizability tensors

- std::vector< std::shared_ptr
  < Matrix > > _X_OV_ao_matrices

    Perturbation X Operator O->V matrices in AO basis.

17.10.1 Detailed Description

CPHF solver class.

Solves CPHF equations (now only for RHF wavefunction). Computes molecular and polarizabilities associated with the localized molecular orbitals (LMO).

Note

Useful options:

- `CPHF_CONVER` - convergence of CPHF. Default: `1e-8` (au)

- `CPHF_CONVER` - maximum numberof iterations. Default: `50`

- `CPHF_DIIS` - wheather use DIIS or not. Default: `true`

- `CPHF_DIIS_DIM` - dimension of iterative subspace. Default: `3`

- `CPHF_LOCALIZE` - localize the molecular orbitals? Default: `true`

- `CPHF_LOCALIZER` - set orbital localization method. Available: `BOYS` and `PIPEK_MEZEY`. Default: `BOYS`

17.10.2 Constructor & Destructor Documentation

17.10.2.1 oepdev::CPHF::CPHF (SharedWavefunction *ref_wfn,* Options & *options*)

Constructor.

Parameters

ref_wfn	reference HF wavefunction
options	set of Psi4 options

The documentation for this class was generated from the following files:

- oepdev/libutil/cphf.h
- oepdev/libutil/cphf.cc

17.11 oepdev::CubePoints3DIterator Class Reference

Iterator over a collection of points in 3D space. g09 Cube-like order.

```
#include <space3d.h>
```

Inheritance diagram for oepdev::CubePoints3DIterator:

```
oepdev::Points3DIterator
          ▲
oepdev::CubePoints3DIterator
```
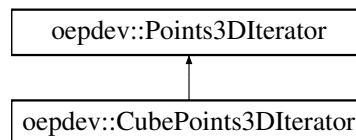
Public Member Functions

- **CubePoints3DIterator** (const int &nx, const int &ny, const int &nz, const double &dx, const double &dy, const double &dz, const double &ox, const double &oy, const double &oz)
- virtual void first ()

    Initialize first iteration.
- virtual void next ()

    Step to next iteration.

Protected Attributes

- const int **nx_**
- const int **ny_**
- const int **nz_**
- const double **dx_**
- const double **dy_**
- const double **dz_**
- const double **ox_**
- const double **oy_**
- const double **oz_**
- int **ii_**
- int **jj_**
- int **kk_**

Additional Inherited Members

17.11.1 Detailed Description

Iterator over a collection of points in 3D space. g09 Cube-like order.

Note: Always create instances by using static factory method from Points3DIterator. Do not use constructor of this class.

The documentation for this class was generated from the following files:

- oepdev/libutil/space3d.h
- oepdev/libutil/space3d.cc

17.12 oepdev::CubePointsCollection3D Class Reference

G09 cube-like ordered collection of points in 3D space.

```
#include <space3d.h>
```

Inheritance diagram for oepdev::CubePointsCollection3D:

```
┌────────────────────────────┐  ┌────────────────────────────┐
│  oepdev::PointsCollection3D │  │      CubicScalarGrid       │
└────────────────────────────┘  └────────────────────────────┘
              ▲                              ▲
              └──────────────┬───────────────┘
              ┌──────────────────────────────┐
              │ oepdev::CubePointsCollection3D │
              └──────────────────────────────┘
```
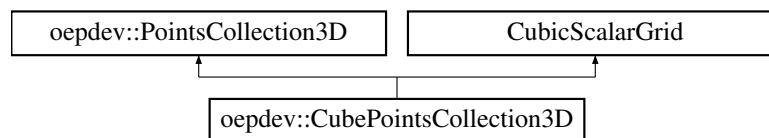
Public Member Functions

- **CubePointsCollection3D** (Collection collectionType, const int &nx, const int &ny, const int &nz, const double &px, const double &py, const double &pz, psi::SharedBasisSet bs, psi::Options &options)
- virtual void print () const
    Print the information to Psi4 output file.
- virtual void **write_cube_file** (psi::SharedMatrix v, const std::string &name)

Additional Inherited Members

17.12.1 Detailed Description

G09 cube-like ordered collection of points in 3D space.

Note: Do not use constructors of this class explicitly. Instead, use static factory methods of the superclass to create instances.

The documentation for this class was generated from the following files:

- oepdev/libutil/space3d.h
- oepdev/libutil/space3d.cc

17.13 oepdev::DIISManager Class Reference

DIIS manager.

```
#include <diis.h>
```

Public Member Functions

- DIISManager (int dim, int na, int nb)
- ~DIISManager ()

Destructor.

- void put (const std::shared_ptr< const Matrix > &error, const std::shared_ptr< const Matrix > &vector)
- void compute (void)
- void update (std::shared_ptr< Matrix > &other)

17.13.1 Detailed Description

DIIS manager.

Instance can interact directly with the process of solving vector quantities in iterative manner. One needs to pass the dimensions of solution vector as well as the DIIS subspace size. The iterative procedure requires providing the current vector and also an estimate of the error vector. The updated DIIS vector can be copied to an old vector through the Instance.

17.13.2 Constructor & Destructor Documentation

17.13.2.1 oepdev::DIISManager::DIISManager (int *dim,* int *na,* int *nb*)

Constructor.

Parameters

dim	Size of DIIS subspace
na	Number of solution rows
nb	Number of solution columns

17.13.3 Member Function Documentation

17.13.3.1 void oepdev::DIISManager::compute (void)

Perform DIIS interpolation.

17.13.3.2 void oepdev::DIISManager::put (const std::shared_ptr< const Matrix > & *error,* const std::shared_ptr< const Matrix > & *vector*)

Put the current solution to the DIIS manager.

Parameters

error	Shared matrix with current solution error
vector	Shared matrix with current solution vector

17.13.3.3 void oepdev::DIISManager::update (std::shared_ptr< Matrix > & *other*)

Update solution vector. Pass the Shared pointer to current solution. Then it will be overriden by the updated DIIS solution.

The documentation for this class was generated from the following files:

- oepdev/libutil/diis.h
- oepdev/libutil/diis.cc

17.14   oepdev::DoubleGeneralizedDensityFit Class Reference

Generalized Density Fitting Scheme - Double Fit.

```
#include <oep_gdf.h>
```

Inheritance diagram for oepdev::DoubleGeneralizedDensityFit:
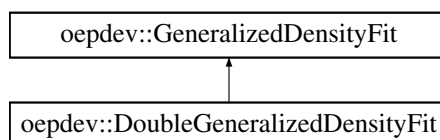
Public Member Functions

- **DoubleGeneralizedDensityFit** (std::shared_ptr< psi::BasisSet > bs_auxiliary, std::shared_ptr< psi::Basis-Set > bs_intermediate, std::shared_ptr< psi::Matrix > v_vector)
- void compute (void)

  Perform the generalized density fit.

Additional Inherited Members

17.14.1   Detailed Description

Generalized Density Fitting Scheme - Double Fit.

The density fitting map projects the OEP onto an arbitrary (not necessarily complete) auxiliary basis set space through application of the self energy minimization technique. The resulting three-electron repulsion integrals are computed by utilizing the resolution of identity in an intermediate, nearly-complete basis set space, hence performing an internal density fitting in nearly complete basis. Refer to density fitting specialized for OEP's for more details.

17.14.2   Determination of the OEP matrix

Coefficients $\mathbf{G}$ are computed by using the following relation

$$\mathbf{G} = \mathbf{A}^{-1} \cdot \mathbf{R} \cdot \mathbf{H}$$

where the intermediate projection matrix is given by

$$\mathbf{H} = \mathbf{S}^{-1} \cdot \mathbf{V}$$

In the above equations,

$$A_{\xi\xi'} = \left(\xi||\xi'\right)$$
$$R_{\xi\varepsilon} = \left(\xi||\varepsilon\right)$$
$$S_{\varepsilon\varepsilon'} = \left(\varepsilon|\varepsilon'\right)$$
$$V^{\varepsilon i} = \left(\varepsilon|\hat{v}i\right)$$

The following labeling convention is used here:

- i denotes the arbitrary state vector

- ξ denotes the auxiliary basis set element

- ε denotes the intermediate (nearly complete) basis set element

In the above, | denotes the single integration over electron coordinate, i.e.,

$$(a|b) \equiv \int d\mathbf{r}\phi_a^*(\mathbf{r})\phi_b(\mathbf{r})$$

whereas || acts as shown below:

$$(a||b) \equiv \iint d\mathbf{r}'d\mathbf{r}'' \frac{\phi_a^*(\mathbf{r}')\phi_b(\mathbf{r}'')}{|\mathbf{r}' - \mathbf{r}''|}$$

The spatial form of the potential operator $\hat{v}$ can be expressed by

$$v(\mathbf{r}) \equiv \int d\mathbf{r}' \frac{\rho(\mathbf{r}')}{|\mathbf{r}' - \mathbf{r}|}$$

with $\rho(\mathbf{r})$ being the effective one-electron density associated with $\hat{v}$.

17.14.2.1 Theory behind the double GDF scheme

In order to perform the generalized density fitting in an incomplete auxiliary basis set, one must apply the following formula:

$$\mathbf{G} = \mathbf{A}^{-1} \cdot \mathbf{B}$$

where one encounters the need of evaluation of the following *three-electron integrals*

$$B_{\xi i} = (\xi||\hat{v}i) \equiv \iiint d\mathbf{r}'d\mathbf{r}''d\mathbf{r}''' \phi_\xi^*(\mathbf{r}') \frac{1}{|\mathbf{r}' - \mathbf{r}''|} \rho(\mathbf{r}''') \frac{1}{|\mathbf{r}''' - \mathbf{r}''|} \phi_i(\mathbf{r}'')$$

Computation of all the necessery integrals of this kind is very costly and impractical for larger molecules. However, one can use the same trick that is a kernel of the OEP technique introduced in the OEPDev project, i.e., introduce the effective potential in order to get rid of one integration. This can be done by performing the generalized density fitting in the nearly complete intermediate basis

$$\hat{v}|i) \cong \sum_\varepsilon H_{\varepsilon i} |\varepsilon)$$

Note that this is done just for the sake of factorizing the triple integral and computing the OEP matrix for the incomplete auxiliary basis. Therefore, the intermediate basis set is used just for a while during density fitting and is no longer necessary later on. By inserting the above identity to the triple integral one can transform it into a sum of the two-electron integrals that are much easier to evaluate. This leads to equations given in the beginning of this section.

The documentation for this class was generated from the following files:

- oepdev/liboep/oep_gdf.h
- oepdev/liboep/oep_gdf.cc

17.15 oepdev::EETCouplingOEPotential Class Reference

Generalized One-Electron Potential for EET coupling calculations.

```
#include <oep.h>
```

Inheritance diagram for oepdev::EETCouplingOEPotential:
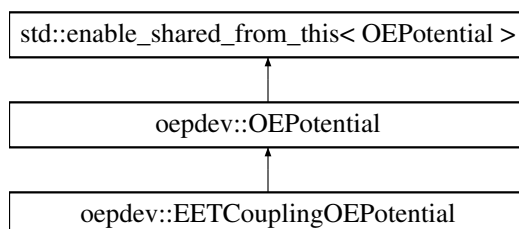
Public Member Functions

- **EETCouplingOEPotential** (SharedWavefunction wfn, SharedBasisSet auxiliary, Options &options)
- **EETCouplingOEPotential** (SharedWavefunction wfn, Options &options)
- virtual void compute (const std::string &oepType) override

    Compute matrix forms of all OEP's within a specified OEP type.

- virtual void compute_3D (const std::string &oepType, const double &x, const double &y, const double &z, double &v) override

    Compute value of potential in point x, y, z and save at v.

- virtual void **print_header** () const override

Additional Inherited Members

17.15.1 Detailed Description

Generalized One-Electron Potential for EET coupling calculations.

Contains the following OEP types:

- `Fujimoto.ET1`

- `Fujimoto.ET2`

- `Fujimoto.HT1`

- `Fujimoto.HT1`

- `Fujimoto.HT2`

- `Fujimoto.CT1`

- `Fujimoto.CT2`

The documentation for this class was generated from the following files:

- oepdev/liboep/oep.h
- oepdev/liboep/oep.cc

17.16 oepdev::ElectrostaticEnergyOEPotential Class Reference

Generalized One-Electron Potential for Electrostatic Energy.

`#include <oep.h>`

Inheritance diagram for oepdev::ElectrostaticEnergyOEPotential:
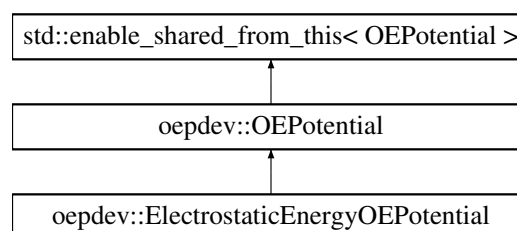
Public Member Functions

- ElectrostaticEnergyOEPotential (SharedWavefunction wfn, Options &options)

  Only ESP-based potential is worth implementing.

- virtual void compute (const std::string &oepType) override

  Compute matrix forms of all OEP's within a specified OEP type.

- virtual void compute_3D (const std::string &oepType, const double &x, const double &y, const double &z, double &v) override

  Compute value of potential in point x, y, z and save at v.

- virtual void **print_header** () const override

Additional Inherited Members

17.16.1 Detailed Description

Generalized One-Electron Potential for Electrostatic Energy.

Contains the following OEP types:

- `V`

The documentation for this class was generated from the following files:

- oepdev/liboep/oep.h
- oepdev/liboep/oep.cc

17.17 oepdev::ElectrostaticEnergySolver Class Reference

Compute the Coulombic interaction energy between unperturbed wavefunctions.

`#include <solver.h>`

Inheritance diagram for oepdev::ElectrostaticEnergySolver:

```
┌─────────────────────────────────────────────┐
│  std::enable_shared_from_this< OEPDevSolver > │
└─────────────────────────────────────────────┘
                      ▲
┌─────────────────────────────────────────────┐
│           oepdev::OEPDevSolver               │
└─────────────────────────────────────────────┘
                      ▲
┌─────────────────────────────────────────────┐
│      oepdev::ElectrostaticEnergySolver        │
└─────────────────────────────────────────────┘
```
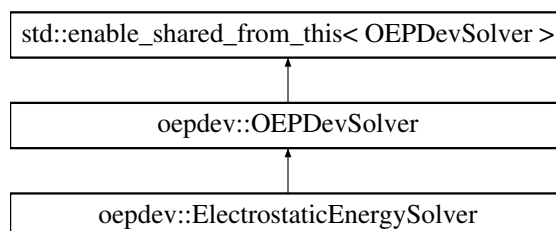
Public Member Functions

- **ElectrostaticEnergySolver** (SharedWavefunctionUnion wfn_union)
- virtual double compute_oep_based (const std::string &method="DEFAULT")

  Compute property by using OEP's.

- virtual double compute_benchmark (const std::string &method="DEFAULT")

  Compute property by using benchmark method.

Additional Inherited Members

17.17.1 Detailed Description

Compute the Coulombic interaction energy between unperturbed wavefunctions.

The implemented methods are shown in below

Keyword	Method Description
Benchmark Methods	
`AO_EXPANDED`	∗Default∗. Exact Coulombic energy from atomic orbital expansions.
`MO_EXPANDED`	Exact Coulombic energy from molecular orbital expansions
OEP-Based Methods	
`ESP_SYMMETRIZED`	∗Default∗. Coulombic energy from ESP charges interacting with nuclei and electronic density. Symmetrized with respect to monomers.

Table 17.2: Methods available in the Solver

Below the detailed description of the above methods is given.

Benchmark Methods

Exact Coulombic energy from atomic orbital expansions.

The Coulombic interaction energy is given by

$$E^{\mathrm{Coul}} = E^{\mathrm{Nuc-Nuc}} + E^{\mathrm{Nuc-El}} + E^{\mathrm{El-El}}$$

where the nuclear-nuclear repulsion energy is

$$E^{\mathrm{Nuc-Nuc}} = \sum_{x \in A} \sum_{y \in B} \frac{Z_x Z_y}{|\mathbf{r}_x - \mathbf{r}_y|}$$

the nuclear-electronic attraction energy is

$$E^{\mathrm{Nuc-El}} = \sum_{x \in A} \sum_{\lambda\sigma \in B} Z_x V_{\lambda\sigma}^{(x)} \left(D_{\lambda\sigma}^{(\alpha)} + D_{\lambda\sigma}^{(\beta)} \right) + \sum_{y \in B} \sum_{\mu\nu \in A} Z_y V_{\mu\nu}^{(y)} \left(D_{\mu\nu}^{(\alpha)} + D_{\mu\nu}^{(\beta)} \right)$$

and the electron-electron repulsion energy is

$$E^{\mathrm{El-El}} = \sum_{\mu\nu \in A} \sum_{\lambda\sigma \in B} \left\{ D_{\mu\nu}^{(\alpha)} + D_{\mu\nu}^{(\beta)} \right\} \left\{ D_{\lambda\sigma}^{(\alpha)} + D_{\lambda\sigma}^{(\beta)} \right\} (\mu\nu|\lambda\sigma)$$

In the above equations,

$$V_{\lambda\sigma}^{(x)} \equiv \int \frac{\varphi_\lambda^*(\mathbf{r}) \varphi_\sigma(\mathbf{r})}{|\mathbf{r} - \mathbf{r}_x|} d\mathbf{r}$$

Exact Coulombic energy from molecular orbital expansion.

This approach is fully equivalent to the atomic orbital expansion shown above. For the closed shell case, the Coulombic interaction energy is given by

$$E^{\mathrm{Coul}} = E^{\mathrm{Nuc-Nuc}} + E^{\mathrm{Nuc-El}} + E^{\mathrm{El-El}}$$

where the nuclear-nuclear repulsion energy is

$$E^{\text{Nuc}-\text{Nuc}} = \sum_{x \in A} \sum_{y \in B} \frac{Z_x Z_y}{|\mathbf{r}_x - \mathbf{r}_y|}$$

the nuclear-electronic attraction energy is

$$E^{\text{Nuc}-\text{El}} = 2 \sum_{i \in A} \sum_{y \in B} V_{ii}^{(y)} + 2 \sum_{j \in B} \sum_{x \in A} V_{jj}^{(x)}$$

and the electron-electron repulsion energy is

$$E^{\text{El}-\text{El}} = 4 \sum_{i \in A} \sum_{j \in B} (ii|jj)$$

OEP-Based Methods

Coulombic energy from ESP charges interacting with nuclei and electronic density.

In this approach, nuclear and electronic density of either species is approximated by ESP charges. In order to achieve symmetric expression, the interaction is computed twice (ESP of A interacting with density matrix and nuclear charges of B and vice versa) and then divided by 2. Thus,

$$E^{\text{Coul}} \approx \frac{1}{2} \left[\sum_{x \in A} \sum_{y \in B} \frac{Z_x q_y}{|\mathbf{r}_x - \mathbf{r}_y|} + \sum_{y \in B} \sum_{\mu \nu \in A} q_y V_{\mu\nu}^{(y)} \left(D_{\mu\nu}^{(\alpha)} + D_{\mu\nu}^{(\beta)} \right) + \sum_{y \in B} \sum_{x \in A} \frac{q_x Z_y}{|\mathbf{r}_x - \mathbf{r}_y|} + \sum_{x \in A} \sum_{\lambda \sigma \in B} Z_x V_{\lambda\sigma}^{(x)} \left(D_{\lambda\sigma}^{(\alpha)} + D_{\lambda\sigma}^{(\beta)} \right) \right]$$

If the basis set is large and the number of ESP centres $q_{x(y)}$ is sufficient, the sum of first two contrubutions equals the sum of the latter two contributions.

Notes:

- This solver also computes and prints the ESP-ESP point charge interaction energy,

$$E^{\text{Coul,ESP}} \approx \sum_{x \in A} \sum_{y \in B} \frac{q_x q_y}{|\mathbf{r}_x - \mathbf{r}_y|}$$

  for reference purposes.

- In order to construct this solver, **always** use the `OEPDevSolver::build` static factory method.

17.17.2 Member Function Documentation

17.17.2.1 double ElectrostaticEnergySolver::compute_benchmark (const std::string & *method* = `"DEFAULT"`) `[virtual]`

Compute property by using benchmark method.

Each solver object has one `DEFAULT` benchmark method

Parameters

method	- benchmark method

Implements oepdev::OEPDevSolver.

17.17.2.2 double ElectrostaticEnergySolver::compute_oep_based (const std::string & *method* = `"DEFAULT"`) `[virtual]`

Compute property by using OEP's.

Each solver object has one `DEFAULT` OEP-based method.

Parameters

method	- flavour of OEP model

Implements oepdev::OEPDevSolver.

The documentation for this class was generated from the following files:

- oepdev/libutil/solver.h
- oepdev/libutil/solver.cc

17.18 oepdev::ElectrostaticPotential3D Class Reference

Electrostatic potential of a molecule.

```
#include <space3d.h>
```

Inheritance diagram for oepdev::ElectrostaticPotential3D:
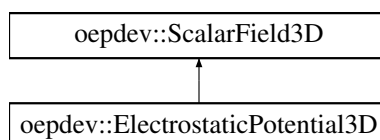
```
┌─────────────────────────────┐
│   oepdev::ScalarField3D     │
└─────────────────────────────┘
               ▲
┌─────────────────────────────┐
│ oepdev::ElectrostaticPotential3D │
└─────────────────────────────┘
```

Public Member Functions

- **ElectrostaticPotential3D** (const int &np, const double &padding, psi::SharedWavefunction wfn, psi::Options &options)
- **ElectrostaticPotential3D** (const int &nx, const int &ny, const int &nz, const double &px, const double &py, const double &pz, psi::SharedWavefunction wfn, psi::Options &options)
- virtual double compute_xyz (const double &x, const double &y, const double &z)

    Compute a value of scalar field at point (x, y, z)
- virtual void print () const

    Print information of the object to Psi4 output.

Additional Inherited Members

17.18.1 Detailed Description

Electrostatic potential of a molecule.

Computes the electrostatic potential of a molecule directly from the wavefunction. The electrostatic potential $v(\mathbf{r})$ at point $\mathbf{r}$ is computed from the following formula:

$$v(\mathbf{r}) = v_{\text{nuc}}(\mathbf{r}) + v_{\text{el}}(\mathbf{r})$$

where the nuclear and electronic contributions are defined accordingly as

$$v_{\text{nuc}}(\mathbf{r}) = \sum_x \frac{Z_x}{|\mathbf{r} - \mathbf{r}_x|}$$

$$v_{\text{el}}(\mathbf{r}) = \sum_{\mu\nu} \left\{ D_{\mu\nu}^{(\alpha)} + D_{\mu\nu}^{(\beta)} \right\} V_{\nu\mu}(\mathbf{r})$$

In the above equations, Z_x denotes the charge of xth nucleus, $D_{\mu\nu}^{(\omega)}$ is the one-particle (relaxed) density matrix element in AO basis associated with the ω electron spin, and $V_{\mu\nu}(\mathbf{r})$ is the potential one-electron integral defined

by

$$V_{\nu\mu}(\mathbf{r}) \equiv \int d\mathbf{r}' \varphi_\nu^*(\mathbf{r}') \frac{1}{|\mathbf{r} - \mathbf{r}'|} \varphi_\mu(\mathbf{r}')$$

The documentation for this class was generated from the following files:

- oepdev/libutil/space3d.h
- oepdev/libutil/space3d.cc

17.19 oepdev::ERI_1_1 Class Reference

2-centre ERI of the form (a|O(2)|b) where O(2) = 1/r12.

```
#include <eri.h>
```

Inheritance diagram for oepdev::ERI_1_1:
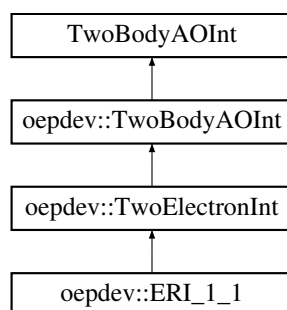
Public Member Functions

- ERI_1_1 (const IntegralFactory ∗integral, int deriv=0, bool use_shell_pairs=false)
    Constructor. Use oepdev::IntegralFactory to generate this object.
- ∼ERI_1_1 ()
    Destructor.

Protected Member Functions

- size_t compute_doublet (int, int)
    Compute ERI's between 2 shells.

Protected Attributes

- double ∗ mdh_buffer_1_
    Buffer for McMurchie-Davidson-Hermite coefficents for monomial expansion (shell 1)
- double ∗ mdh_buffer_2_
    Buffer for McMurchie-Davidson-Hermite coefficents for monomial expansion (shell 2)

17.19.1 Detailed Description

2-centre ERI of the form (a|O(2)|b) where O(2) = 1/r12.

ERI's are computed for a shell doublet (P|Q) and stored in the `target_full_` buffer, accessible through `buffer()` method:

$$\text{For each } (n_1, l_1, m_1) \in P :$$
$$\text{For each } (n_2, l_2, m_2) \in Q :$$
$$\text{ERI} = (A|B)[\{\alpha\}, \mathbf{n}, \mathbf{l}, \mathbf{m}]$$

For detailed description of the McMurchie-Davidson scheme, refer to The Integral Package Library.

17.19.2 Implementation

A set of ERI's in a shell is decontracted as

$$(A|B)[\{\alpha\}, \mathbf{n}, \mathbf{l}, \mathbf{m}] = \sum_{ij} c_i(\alpha_1) c_j(\alpha_2) (i|j)[\{\alpha\}, \mathbf{n}, \mathbf{l}, \mathbf{m}]$$

where the primitive ERI is given by

$$(i|j)[\{\alpha\}, \mathbf{n}, \mathbf{l}, \mathbf{m}] \qquad = \qquad \sum_{N_1=0}^{n_1} \sum_{L_1=0}^{l_1} \sum_{M_1=0}^{m_1} \sum_{N_2=0}^{n_2} \sum_{L_2=0}^{l_2} \sum_{M_2=0}^{m_2} d_{N_1}^{n_1} d_{L_1}^{l_1} d_{M_1}^{m_1} d_{N_2}^{n_2} d_{L_2}^{l_2} d_{M_2}^{m_2} [N_1 L_1 M_1 | N_2 L_2 M_2]$$

The documentation for this class was generated from the following files:

- oepdev/libints/eri.h
- oepdev/libints/eri.cc

17.20 oepdev::ERI_2_2 Class Reference

4-centre ERI of the form (ab|O(2)|cd) where O(2) = 1/r12.

```
#include <eri.h>
```

Inheritance diagram for oepdev::ERI_2_2:
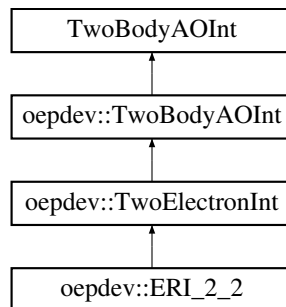
Public Member Functions

- ERI_2_2 (const IntegralFactory *integral, int deriv=0, bool use_shell_pairs=false)
    Constructor. Use oepdev::IntegralFactory to generate this object.
- ~ERI_2_2 ()
    Destructor.

Protected Member Functions

- size_t compute_quartet (int, int, int, int)
    Compute ERI's between 4 shells.

Protected Attributes

- double ∗ mdh_buffer_12_

    Buffer for McMurchie-Davidson-Hermite coefficents for binomial expansion (shells 1 and 2)
- double ∗ mdh_buffer_34_

    Buffer for McMurchie-Davidson-Hermite coefficents for binomial expansion (shells 3 and 4)

17.20.1 Detailed Description

4-centre ERI of the form $(ab|O(2)|cd)$ where $O(2) = 1/r12$.

ERI's are computed for a shell quartet $(PQ|RS)$ and stored in the `target_full_` buffer, accessible through `buffer()` method:

$$\text{For each } (n_1, l_1, m_1) \in P :$$
$$\text{For each } (n_2, l_2, m_2) \in Q :$$
$$\text{For each } (n_3, l_3, m_3) \in R :$$
$$\text{For each } (n_4, l_4, m_4) \in S :$$
$$\text{ERI} = (AB|CD)[\{\alpha\}, \mathbf{n}, \mathbf{l}, \mathbf{m}]$$

For detailed description of the McMurchie-Davidson scheme, refer to The Integral Package Library.

17.20.2 Implementation

A set of ERI's in a shell is decontracted as

$$(AB|CD)[\{\alpha\}, \mathbf{n}, \mathbf{l}, \mathbf{m}] = \sum_{ijkl} c_i(\alpha_1) c_j(\alpha_2) c_k(\alpha_3) c_l(\alpha_4) (ij|kl)[\{\alpha\}, \mathbf{n}, \mathbf{l}, \mathbf{m}]$$

where the primitive ERI is given by

$$(ij|kl)[\{\alpha\}, \mathbf{n}, \mathbf{l}, \mathbf{m}] = E_{ij}(\alpha_1, \alpha_2) E_{kl}(\alpha_3, \alpha_4)$$
$$\times \sum_{N_1=0}^{n_1+n_2} \sum_{L_1=0}^{l_1+l_2} \sum_{M_1=0}^{m_1+m_2} \sum_{N_2=0}^{n_3+n_4} \sum_{L_2=0}^{l_3+l_4} \sum_{M_2=0}^{m_3+m_4} d_{N_1}^{n_1 n_2} d_{L_1}^{l_1 l_2} d_{M_1}^{m_1 m_2} d_{N_2}^{n_3 n_4} d_{L_2}^{l_3 l_4} d_{M_2}^{m_3 m_4} [N_1 L_1 M_1 | N_2 L_2 M_2]$$

In the above equation, the multiplicative constants are given as

$$E_{ij}(\alpha_1, \alpha_2) = \exp\left[-\frac{\alpha_1 \alpha_2}{\alpha_1 + \alpha_2} |\mathbf{A} - \mathbf{B}|^2 \right]$$
$$E_{kl}(\alpha_3, \alpha_4) = \exp\left[-\frac{\alpha_3 \alpha_4}{\alpha_3 + \alpha_4} |\mathbf{C} - \mathbf{D}|^2 \right]$$

The documentation for this class was generated from the following files:

- oepdev/libints/eri.h
- oepdev/libints/eri.cc

17.21 oepdev::ERI_3_1 Class Reference

4-centre ERI of the form $(abc|O(2)|d)$ where $O(2) = 1/r12$.

```
#include <eri.h>
```

Inheritance diagram for oepdev::ERI_3_1:

```
                        ┌─────────────────────────┐
                        │      TwoBodyAOInt        │
                        └─────────────────────────┘
                                    ▲
                        ┌─────────────────────────┐
                        │   oepdev::TwoBodyAOInt   │
                        └─────────────────────────┘
                                    ▲
                        ┌─────────────────────────┐
                        │  oepdev::TwoElectronInt  │
                        └─────────────────────────┘
                                    ▲
                        ┌─────────────────────────┐
                        │     oepdev::ERI_3_1      │
                        └─────────────────────────┘
```
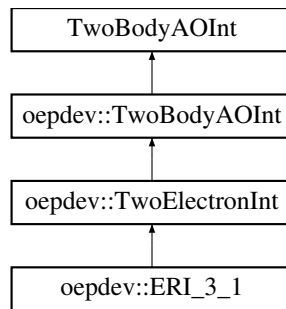
Public Member Functions

- ERI_3_1 (const IntegralFactory ∗integral, int deriv=0, bool use_shell_pairs=false)

    Constructor. Use oepdev::IntegralFactory to generate this object.
- ∼ERI_3_1 ()

    Destructor.

Protected Member Functions

- size_t compute_quartet (int, int, int, int)

    Compute ERI's between 4 shells.

Protected Attributes

- double ∗ mdh_buffer_123_

    Buffer for McMurchie-Davidson-Hermite coefficents for trinomial expansion (shells 1, 2 and 3)
- double ∗ mdh_buffer_4_

    Buffer for McMurchie-Davidson-Hermite coefficents for monomial expansion (shell 4)

17.21.1 Detailed Description

4-centre ERI of the form (abc|O(2)|d) where O(2) = 1/r12.

ERI's are computed for a shell quartet (PQR|S) and stored in the `target_full_` buffer, accessible through `buffer()` method:

$$
\text{For each } (n_1, l_1, m_1) \in P :
$$
$$
\text{For each } (n_2, l_2, m_2) \in Q :
$$
$$
\text{For each } (n_3, l_3, m_3) \in R :
$$
$$
\text{For each } (n_4, l_4, m_4) \in S :
$$
$$
\text{ERI} = (ABC|D)[\{\alpha\}, \mathbf{n}, \mathbf{l}, \mathbf{m}]
$$

For detailed description of the McMurchie-Davidson scheme, refer to The Integral Package Library.

17.21.2 Implementation

A set of ERI's in a shell is decontracted as

$$
(ABC|D)[\{\alpha\}, \mathbf{n}, \mathbf{l}, \mathbf{m}] = \sum_{ijkl} c_i(\alpha_1) c_j(\alpha_2) c_k(\alpha_3) c_l(\alpha_4) (ijk|l)[\{\alpha\}, \mathbf{n}, \mathbf{l}, \mathbf{m}]
$$

where the primitive ERI is given by

$$(ijk|l)[\{\alpha\}, \mathbf{n}, \mathbf{l}, \mathbf{m}] = E_{ijk}(\alpha_1, \alpha_2, \alpha_3)$$

$$\times \sum_{N_1=0}^{n_1+n_2+n_3} \sum_{L_1=0}^{l_1+l_2+l_3} \sum_{M_1=0}^{m_1+m_2+m_3} \sum_{N_2=0}^{n_4} \sum_{L_2=0}^{l_4} \sum_{M_2=0}^{m_4} d_{N_1}^{n_1 n_2 n_3} d_{L_1}^{l_1 l_2 l_3} d_{M_1}^{m_1 m_2 m_3} d_{N_2}^{n_4} d_{L_2}^{l_4} d_{M_2}^{m_4} [N_1 L_1 M_1 | N_2 L_2 M_2]$$

In the above equation, the multiplicative constants are given as

$$E_{ijk}(\alpha_1, \alpha_2, \alpha_3) = \exp\left[-\frac{\alpha_1 \alpha_2}{\alpha_1 + \alpha_2}|\mathbf{A} - \mathbf{B}|^2\right] \exp\left[-\frac{(\alpha_1 + \alpha_2)\alpha_3}{\alpha_1 + \alpha_2 + \alpha_3}|\mathbf{P} - \mathbf{C}|^2\right]$$

The documentation for this class was generated from the following files:

- oepdev/libints/eri.h
- oepdev/libints/eri.cc

17.22 oepdev::ESPSolver Class Reference

Charges from Electrostatic Potential (ESP). A solver-type class.

```
#include <esp.h>
```

Public Member Functions

- ESPSolver (SharedScalarField3D field)

    Construct from scalar field.
- ESPSolver (SharedScalarField3D field, psi::SharedMatrix centres)

    Construct from scalar field.
- virtual ∼ESPSolver ()

    Destructor.
- virtual psi::SharedVector charges () const

    Get the (fit) charges.
- virtual psi::SharedMatrix centres () const

    Get the charge distribution centres.
- virtual void compute ()

    Perform fitting of effective charges.

Protected Attributes

- const int nCentres_

    Number of fit centres.
- SharedScalarField3D field_

    Scalar field.
- psi::SharedVector charges_

    Charges to be fit.
- psi::SharedMatrix centres_

    Centres, at which fit charges will reside.

17.22.1 Detailed Description

Charges from Electrostatic Potential (ESP). A solver-type class.

Solves the least-squares problem to fit the generalized charges q_m, that reproduce the reference generalized potential $v^{\text{ref}}(\mathbf{r})$ supplied by the `ScalarField3D` object:

$$\int d\mathbf{r}' \left[v^{\text{ref}}(\mathbf{r}') - \sum_m \frac{q_m}{|\mathbf{r}' - \mathbf{r}_m|} \right]^2 \rightarrow \text{minimize}$$

The charges are subject to the following constraint:

$$\sum_m q_m = 0$$

Method description.

M generalized charges is found by solving the matrix equation

$$\begin{pmatrix} \mathbf{A} & 0 \\ 0 & 1 \end{pmatrix}^{-1} \cdot \begin{pmatrix} \mathbf{b} \\ 0 \end{pmatrix} = \begin{pmatrix} \mathbf{q} \\ \lambda \end{pmatrix}$$

where the $\mathbf{A}$ matrix of dimension $M \times M$ and b} vector or length M are given as

$$A_{mn} = \sum_i \frac{1}{r_{im} r_{in}}$$

$$b_m = \sum_i \frac{v^{\text{ref}}(\mathbf{r}_m)}{r_{im}}$$

In the above equation, summations run over all sample points, at which reference potential is known.

Note

Useful options:

- `ESP_PAD_SPHERE` - Padding spherical radius for random points selection. Default: `10.0` [A.U.]
- `ESP_NPOINTS_PER_ATOM` - Number of random points per atom in a molecule. Detault: `1500`
- `ESP_VDW_RADIUS_C` - The vdW radius for carbon atom. Default: `3.0` [A.U.]
- `ESP_VDW_RADIUS_H` - The vdW radius for hydrogen atom. Default: `4.0` [A.U.]
- `ESP_VDW_RADIUS_N` - The vdW radius for nitrogen atom. Default: `2.4` [A.U.]
- `ESP_VDW_RADIUS_O` - The vdW radius for oxygen atom. Default: `5.6` [A.U.]
- `ESP_VDW_RADIUS_F` - The vdW radius for fluorium atom. Default: `2.3` [A.U.]
- `ESP_VDW_RADIUS_CL` - The vdW radius for chlorium atom. Default: `2.9` [A.U.]

17.22.2 Constructor & Destructor Documentation

17.22.2.1 oepdev::ESPSolver::ESPSolver (SharedScalarField3D *field*)

Construct from scalar field.

Assume that the centres are on atoms associated with the scalar field.

Parameters

field	- oepdev scalar field object

17.22.2.2 oepdev::ESPSolver::ESPSolver (SharedScalarField3D *field,* psi::SharedMatrix *centres*)

Construct from scalar field.

Solve ESP equations for a custom set of charge distribution centres.

Parameters

field	- oepdev scalar field object
centres	- matrix with coordinates of charge distribution centres

The documentation for this class was generated from the following files:

- oepdev/libutil/esp.h
- oepdev/libutil/esp.cc

17.23 oepdev::FFAbInitioPolarGEFactory Class Reference

Polarization GEFP Factory from First Principles: Finite-Difference Model. Arbitrary level of theory.

```
#include <gefp.h>
```

Inheritance diagram for oepdev::FFAbInitioPolarGEFactory:

```
oepdev::GenEffParFactory
          ↑
oepdev::PolarGEFactory
          ↑
oepdev::FFAbInitioPolarGEFactory
```
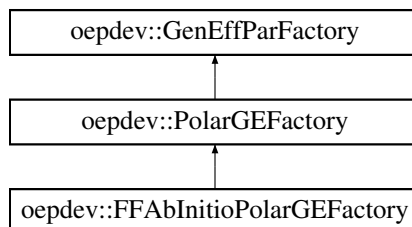
Public Member Functions

- **FFAbInitioPolarGEFactory** (std::shared_ptr< psi::Wavefunction > wfn, psi::Options &opt)
- virtual std::shared_ptr
  < GenEffPar > compute (void)
  Compute the density matrix susceptibility tensors.

Additional Inherited Members

17.23.1 Detailed Description

Polarization GEFP Factory from First Principles: Finite-Difference Model. Arbitrary level of theory.

Implements creation of the density matrix susceptibility tensors. Does not guarantee the idempotency of the density matrix in LCAO-MO variation, but for weak electric fields the idempotency is to be expected up to first order. The density matrix susceptibility tensor is represented by:

$$\delta D_{\alpha\beta} = \mathbf{B}_{\alpha\beta}^{(1)} \cdot \mathbf{F} + \mathbf{B}_{\alpha\beta}^{(2)} : \mathbf{F} \otimes \mathbf{F}$$

where $\mathbf{B}_{\alpha\beta}^{(1)}$ is the density matrix dipole polarizability defined as

$$\mathbf{B}_{\alpha\beta}^{(1)} = \frac{\partial D_{\alpha\beta}}{\partial \mathbf{F}}\Big|_{\mathbf{F}=\mathbf{0}}$$

whereas $\mathbf{B}_{\alpha\beta}^{(2)}$ is the density matrix dipole-dipole hyperpolarizability,

$$\mathbf{B}_{\alpha\beta}^{(2)} = \frac{1}{2}\frac{\partial^2 D_{\alpha\beta}}{\partial \mathbf{F} \otimes \partial \mathbf{F}}\Big|_{\mathbf{F}=\mathbf{0}}$$

The first derivative is evaluated numerically from central finite-field 3-point formula,

$$f' = \frac{f(h) - f(-h)}{2h} + \mathfrak{O}(h^2)$$

where h is the differentiation step. Second derivatives are evaluated from the following formulae:

$$f_{uu} = \frac{f(h) + f(-h) - 2f(0)}{h^2} + \mathfrak{O}(h^2)$$

$$f_{uw} = \frac{f(h,h) + f(-h,-h) + 2f(0) - f(h,0) - f(-h,0) - f(0,h) - f(0,-h)}{2h^2} + \mathfrak{O}(h^2)$$

As long as the second-order susceptibility is considered, this susceptibility model works well for uniform weak, moderate and strong electric fields.

The documentation for this class was generated from the following files:

- oepdev/libgefp/gefp.h
- oepdev/libgefp/gefp_polar_ffabinitio.cc

17.24 oepdev::Fourier9 Struct Reference

Simple structure to hold the Fourier series expansion coefficients for N=4.

```
#include <unitary_optimizer.h>
```

Public Attributes

- double **a0**
- double **a1**
- double **a2**
- double **a3**
- double **a4**
- double **b1**
- double **b2**
- double **b3**
- double **b4**

17.24.1 Detailed Description

Simple structure to hold the Fourier series expansion coefficients for N=4.

The documentation for this struct was generated from the following file:

- oepdev/libutil/unitary_optimizer.h

17.25 oepdev::GenEffFrag Class Reference

Generalized Effective Fragment. Container Class.

```
#include <gefp.h>
```

Public Member Functions

- GenEffFrag ()

    Initialize with default name of GEFP (Default)
- GenEffFrag (std::string name)

    Initialize with custom name of GEFP.
- ∼GenEffFrag ()

    Destruct.
- void rotate (std::shared_ptr< psi::Matrix > R)

    Rotate.
- void translate (std::shared_ptr< psi::Vector > T)

    Translate.
- void superimpose (std::shared_ptr< psi::Matrix > targetXYZ, std::vector< int > supList)

    Superimpose.
- void set_gefp_polarization (const std::shared_ptr< GenEffPar > &par)

    Set the Density Matrix Susceptibility Tensor Object.
- void set_dmat_dipole_polarizability (const std::vector< std::vector< std::shared_ptr< psi::Matrix >>> &susc)

    Set the Density Matrix Dipole Polarizability.
- void set_dmat_dipole_dipole_hyperpolarizability (const std::vector< std::vector< std::shared_ptr< psi::- Matrix >>> &susc)

    Set the Density Matrix Dipole-Dipole Hyperpolarizability.
- void set_dmat_quadrupole_polarizability (const std::vector< std::vector< std::shared_ptr< psi::Matrix >>> &susc)

    Set the Density Matrix Quadrupole Polarizability.
- std::shared_ptr< psi::Matrix > susceptibility (int fieldRank, int fieldGradientRank, int i, int x) const

    Grab the Density Matrix Susceptibility.
- std::vector< std::shared_ptr
  < psi::Matrix > > susceptibility (int fieldRank, int fieldGradientRank, int i) const

    Grab the Density Matrix Susceptibility.
- std::vector< std::vector
  < std::shared_ptr< psi::Matrix > > > susceptibility (int fieldRank, int fieldGradientRank) const

    Grab the Density Matrix Susceptibility.

Public Attributes

- std::map< std::string,
  std::shared_ptr< GenEffPar > > parameters

    Dictionary of All GEF Parameters.

Protected Attributes

- std::string name_

    Name of GEFP.
- std::shared_ptr< GenEffPar > densityMatrixSusceptibilityGEF_

    Density Matrix Susceptibility Tensor.
- std::shared_ptr< GenEffPar > electrostaticEnergyGEF_

    Electrostatic Energy Effective One-Electron Potential.
- std::shared_ptr< GenEffPar > repulsionEnergyGEF_

    Exchange-Repulsion Effective One-Electron Potential.
- std::shared_ptr< GenEffPar > chargeTransferEnergyGEF_

    Charge-Transfer Effective One-Electron Potential.
- std::shared_ptr< GenEffPar > EETCouplingConstantGEF_

    EET Coupling Effective One-Electron Potential.

17.25.1   Detailed Description

Generalized Effective Fragment. Container Class.

Describes the GEFP fragment that is in principle designed to work at correlated levels of theory.

17.25.2   Member Function Documentation

17.25.2.1   std::shared_ptr<psi::Matrix> oepdev::GenEffFrag::susceptibility (int *fieldRank,* int *fieldGradientRank,* int *i,* int *x*) const `[inline]`

Grab the Density Matrix Susceptibility.

Parameters

fieldRank	- power dependency with respect to the electric field
fieldGradient-Rank	- power dependency with respect to the electric field gradient
i	- id of the distributed site
x	- id of the composite Cartesian component

17.25.2.2   std::vector<std::shared_ptr<psi::Matrix> > oepdev::GenEffFrag::susceptibility (int *fieldRank,* int *fieldGradientRank,* int *i*) const `[inline]`

Grab the Density Matrix Susceptibility.

Parameters

fieldRank	- power dependency with respect to the electric field
fieldGradient-Rank	- power dependency with respect to the electric field gradient
i	- id of the distributed site

17.25.2.3   std::vector<std::vector<std::shared_ptr<psi::Matrix> > > oepdev::GenEffFrag::susceptibility (int *fieldRank,* int *fieldGradientRank*) const `[inline]`

Grab the Density Matrix Susceptibility.

Parameters

fieldRank	- power dependency with respect to the electric field
fieldGradient-Rank	- power dependency with respect to the electric field gradient

The documentation for this class was generated from the following files:

- oepdev/libgefp/gefp.h
- oepdev/libgefp/gefp.cc

17.26   oepdev::GenEffPar Class Reference

Generalized Effective Fragment Parameters. Container Class.

```
#include <gefp.h>
```

Public Member Functions

- GenEffPar (std::string name)

    Create with name of this parameter type.

- ∼GenEffPar ()

    Destruct.

- void set_susceptibility (int fieldRank, int fieldGradientRank, const std::vector< std::vector< std::shared_ptr< psi::Matrix >>> &susc)

    Set the Density Matrix Susceptibility.

- void set_dipole_polarizability (const std::vector< std::vector< std::shared_ptr< psi::Matrix >>> &susc)

    Set The Density Matrix Dipole Polarizability.

- void set_dipole_dipole_hyperpolarizability (const std::vector< std::vector< std::shared_ptr< psi::Matrix >>> &susc)

    Set The Density Matrix Dipole-Dipole Hyperpolarizability.

- void set_quadrupole_polarizability (const std::vector< std::vector< std::shared_ptr< psi::Matrix >>> &susc)

    Set The Density Matrix Quadrupole Polarizability.

- void set_centres (const std::vector< std::shared_ptr< psi::Vector >> &centres)

    Set the distributed centres' positions.

- void allocate (int fieldRank, int fieldGradientRank, int nsites, int nbf)

    Allocate the Density Matrix Susceptibility.

- void allocate_dipole_polarizability (int nsites, int nbf)

    Allocate The Density Matrix Dipole Polarizability.

- void allocate_dipole_dipole_hyperpolarizability (int nsites, int nbf)

    Allocate The Density Matrix Dipole-Dipole Hyperpolarizability.

- void allocate_quadrupole_polarizability (int nsites, int nbf)

    Allocate The Density Matrix Quadrupole Polarizability.

- bool **hasDensityMatrixDipolePolarizability** () const
- bool **hasDensityMatrixDipoleDipoleHyperpolarizability** () const
- bool **hasDensityMatrixQuadrupolePolarizability** () const
- std::shared_ptr< psi::Matrix > susceptibility (int fieldRank, int fieldGradientRank, int i, int x) const

    Grab the Density Matrix Susceptibility.

- std::vector< std::shared_ptr
  < psi::Matrix > > susceptibility (int fieldRank, int fieldGradientRank, int i) const

    Grab the Density Matrix Susceptibility.

- std::vector< std::vector
  < std::shared_ptr< psi::Matrix > > > susceptibility (int fieldRank, int fieldGradientRank) const

    Grab the Density Matrix Susceptibility.

- std::vector< std::vector
  < std::shared_ptr< psi::Matrix > > > dipole_polarizability () const

    Grab the density matrix dipole polarizability tensor.

- std::vector< std::shared_ptr
  < psi::Matrix > > dipole_polarizability (int i) const

    Grab the density matrix dipole polarizability tensor's x-th component.

- std::shared_ptr< psi::Matrix > dipole_polarizability (int i, int x) const

    Grab the density matrix dipole polarizability tensor's x-th component of the i-th distributed site.

- std::vector< std::vector
  < std::shared_ptr< psi::Matrix > > > dipole_dipole_hyperpolarizability () const

    Grab the density matrix dipole-dipole hyperpolarizability tensor.

- std::vector< std::shared_ptr
  < psi::Matrix > > dipole_dipole_hyperpolarizability (int i) const

    Grab the density matrix dipole-dipole hyperpolarizability tensor's x-th component.

- std::shared_ptr< psi::Matrix > dipole_dipole_hyperpolarizability (int i, int x) const

    Grab the density matrix dipole-dipole hyperpolarizability tensor's x-th component of the i-th distributed site.

- std::vector< std::vector
  < std::shared_ptr< psi::Matrix > > > quadrupole_polarizability () const

    Grab the density matrix quadrupole polarizability tensor.

- std::vector< std::shared_ptr
  < psi::Matrix > > quadrupole_polarizability (int i) const

    Grab the density matrix quadrupole polarizability tensor's x-th component.

- std::shared_ptr< psi::Matrix > quadrupole_polarizability (int i, int x) const

    Grab the density matrix quadrupole polarizability tensor's x-th component of the i-th distributed site.

- std::vector< std::shared_ptr
  < psi::Vector > > centres () const

    Grab the centres' positions.

- std::shared_ptr< psi::Vector > centre (int i) const

    Grab the position of the i-th distributed site.

- std::shared_ptr< psi::Matrix > compute_density_matrix (std::shared_ptr< psi::Vector > field)

    Compute the density matrix due to the uniform electric field perturbation.

- std::shared_ptr< psi::Matrix > compute_density_matrix (double fx, double fy, double fz)

    Compute the density matrix due to the uniform electric field perturbation.

- std::shared_ptr< psi::Matrix > compute_density_matrix (std::vector< std::shared_ptr< psi::Vector >> fields)

    Compute the density matrix due to the non-uniform electric field perturbation.

- std::shared_ptr< psi::Matrix > compute_density_matrix (std::vector< std::shared_ptr< psi::Vector >> fields, std::vector< std::shared_ptr< psi::Matrix >> grads)

    Compute the density matrix due to the non-uniform electric field perturbation.

Protected Attributes

- std::string name_

    The Name of Parameter Type.

- std::vector< std::vector
  < std::shared_ptr< psi::Matrix > > > densityMatrixDipolePolarizability_

    The Density Matrix Dipole Polarizability.

- std::vector< std::vector
  < std::shared_ptr< psi::Matrix > > > densityMatrixDipoleDipoleHyperpolarizability_

    The Density Matrix Dipole-Dipole Hyperpolarizability.

- std::vector< std::vector
  < std::shared_ptr< psi::Matrix > > > densityMatrixQuadrupolePolarizability_

    The Density Matrix Quadrupole Polarizability.

- std::vector< std::shared_ptr
  < psi::Vector > > distributedCentres_

    The Positions of the Distributed Centres.

- bool **hasDensityMatrixDipolePolarizability_**
- bool **hasDensityMatrixDipoleDipoleHyperpolarizability_**
- bool **hasDensityMatrixQuadrupolePolarizability_**

17.26.1 Detailed Description

Generalized Effective Fragment Parameters. Container Class.

17.26.2 Member Function Documentation

17.26.2.1 void oepdev::GenEffPar::allocate (int *fieldRank,* int *fieldGradientRank,* int *nsites,* int *nbf*) `[inline]`

Allocate the Density Matrix Susceptibility.

Parameters

fieldRank	- power dependency with respect to the electric field $\mathbf{F}$
fieldGradient-Rank	- power dependency with respect to the electric field gradient $\nabla \otimes \mathbf{F}$
nsites	- number of distributed sites
nbf	- number of basis functions in the basis set

The following susceptibilities are supported (fieldRank, fieldGradientRank):

- (1, 0) - dipole polarizability, interacts with $\mathbf{F}$

- (2, 0) - dipole-dipole hyperpolarizability, interacts with $\mathbf{F} \otimes \mathbf{F}$

- (0, 1) - quadrupole polarizability, interacts with $\nabla \otimes \mathbf{F}$

17.26.2.2   std::shared_ptr< psi::Matrix > oepdev::GenEffPar::compute_density_matrix (std::shared_ptr< psi::Vector > *field*)

Compute the density matrix due to the uniform electric field perturbation.

Parameters

field	- the uniform electric field vector (A.U.)

17.26.2.3   std::shared_ptr< psi::Matrix > oepdev::GenEffPar::compute_density_matrix (double *fx,* double *fy,* double *fz*)

Compute the density matrix due to the uniform electric field perturbation.

Parameters

fx	- *x*-th Cartesian component of the uniform electric field vector (A.U.)
fy	- *y*-th Cartesian component of the uniform electric field vector (A.U.)
fz	- *z*-th Cartesian component of the uniform electric field vector (A.U.)

17.26.2.4   std::shared_ptr< psi::Matrix > oepdev::GenEffPar::compute_density_matrix (std::vector< std::shared_ptr< psi::Vector >> *fields*)

Compute the density matrix due to the non-uniform electric field perturbation.

Parameters

fields	- the list of non-uniform electric field vector (A.U.) evaluated at the distributed DMatPol sites

17.26.2.5   std::shared_ptr< psi::Matrix > oepdev::GenEffPar::compute_density_matrix (std::vector< std::shared_ptr< psi::Vector >> *fields,* std::vector< std::shared_ptr< psi::Matrix >> *grads*)

Compute the density matrix due to the non-uniform electric field perturbation.

Parameters

fields	- the list of electric field vectors (A.U.) evaluated at the distributed DMatPol sites
grads	- the list of electric field gradient matrices (A.U.) evaluated at the distributed DMatPol sites

17.26.2.6   void oepdev::GenEffPar::set_susceptibility (int *fieldRank,* int *fieldGradientRank,* const std::vector< std::vector< std::shared_ptr< psi::Matrix >>> & *susc*)   [inline]

Set the Density Matrix Susceptibility.

Parameters

fieldRank	- power dependency with respect to the electric field $\mathbf{F}$
fieldGradient-Rank	- power dependency with respect to the electric field gradient $\nabla \otimes \mathbf{F}$
susc	- the susceptibility tensor

The following susceptibilities are supported (fieldRank, fieldGradientRank):

- (1, 0) - dipole polarizability, interacts with $\mathbf{F}$

- (2, 0) - dipole-dipole hyperpolarizability, interacts with $\mathbf{F} \otimes \mathbf{F}$

- (0, 1) - quadrupole polarizability, interacts with $\nabla \otimes \mathbf{F}$

17.26.2.7 std::shared_ptr<psi::Matrix> oepdev::GenEffPar::susceptibility (int *fieldRank,* int *fieldGradientRank,* int *i,* int *x*) const `[inline]`

Grab the Density Matrix Susceptibility.

Parameters

fieldRank	- power dependency with respect to the electric field
fieldGradient-Rank	- power dependency with respect to the electric field gradient
i	- id of the distributed site
x	- id of the composite Cartesian component

The following susceptibilities are supported (fieldRank, fieldGradientRank):

- (1, 0) - dipole polarizability, interacts with $\mathbf{F}$

- (2, 0) - dipole-dipole hyperpolarizability, interacts with $\mathbf{F} \otimes \mathbf{F}$

- (0, 1) - quadrupole polarizability, interacts with $\nabla \otimes \mathbf{F}$

The distributed sites are assumed to be atomic sites or molecular orbital centroids (depending on the polarization factory used). For the electric field, the composite Cartesian index is just an ordinary Cartesian index. For the electric field gradient and electric field squared, the composite Cartesian index is given as

$$I(x, y) = 3x + y$$

where the values of 0, 1 and 2 correspond to *x*, *y* and *z* Cartesian components, respectively. Therefore, in the latter case, there is 9 distinct composite Cartesian components.

17.26.2.8 std::vector<std::shared_ptr<psi::Matrix> > oepdev::GenEffPar::susceptibility (int *fieldRank,* int *fieldGradientRank,* int *i*) const `[inline]`

Grab the Density Matrix Susceptibility.

Parameters

fieldRank	- power dependency with respect to the electric field
fieldGradient-Rank	- power dependency with respect to the electric field gradient
i	- id of the distributed site

The following susceptibilities are supported (fieldRank, fieldGradientRank):

- (1, 0) - dipole polarizability, interacts with $\mathbf{F}$

- (2, 0) - dipole-dipole hyperpolarizability, interacts with $\mathbf{F} \otimes \mathbf{F}$

• (0, 1) - quadrupole polarizability, interacts with $\nabla \otimes \mathbf{F}$

The distributed sites are assumed to be atomic sites or molecular orbital centroids (depending on the polarization factory used).

17.26.2.9 std::vector<std::vector<std::shared_ptr<psi::Matrix> > > oepdev::GenEffPar::susceptibility (int *fieldRank,* int *fieldGradientRank*) const `[inline]`

Grab the Density Matrix Susceptibility.

Parameters

fieldRank	- power dependency with respect to the electric field
fieldGradient-Rank	- power dependency with respect to the electric field gradient

The following susceptibilities are supported (fieldRank, fieldGradientRank):

• (1, 0) - dipole polarizability, interacts with $\mathbf{F}$

• (2, 0) - dipole-dipole hyperpolarizability, interacts with $\mathbf{F} \otimes \mathbf{F}$

• (0, 1) - quadrupole polarizability, interacts with $\nabla \otimes \mathbf{F}$

The documentation for this class was generated from the following files:

• oepdev/libgefp/gefp.h
• oepdev/libgefp/gefp.cc

17.27 oepdev::GenEffParFactory Class Reference

Generalized Effective Fragment Factory. Abstract Base.

```
#include <gefp.h>
```

Inheritance diagram for oepdev::GenEffParFactory:

Public Member Functions

• GenEffParFactory (std::shared_ptr< psi::Wavefunction > wfn, psi::Options &opt)

   Construct from wavefunction and Psi4 options.
• virtual ∼GenEffParFactory ()

   Destruct.
• virtual std::shared_ptr
   < GenEffPar > compute (void)=0

   Compute the fragment parameters.
• virtual std::shared_ptr
   < psi::Wavefunction > wfn (void) const

   Grab wavefunction.
• virtual psi::Options & options (void) const

   Grab options.
• std::shared_ptr< CPHF > cphf_solver () const

   Grab the CPHF object.

Static Public Member Functions

- static std::shared_ptr
  < GenEffParFactory > build (const std::string &type, std::shared_ptr< psi::Wavefunction > wfn, psi::Options &opt)

    Build Density Matrix Susceptibility Generalized Factory.

Protected Member Functions

- virtual double random_double ()

    Draw random number.
- virtual std::shared_ptr
  < psi::Vector > draw_random_point ()

    Draw random point in 3D space, excluding the vdW region.
- virtual bool is_in_vdWsphere (double x, double y, double z) const

    Is the point inside a vdW region?

Protected Attributes

- std::shared_ptr
  < psi::Wavefunction > wfn_

    Wavefunction.
- psi::Options & options_

    Psi4 Options.
- std::default_random_engine randomNumberGenerator_

    Random number generators.
- std::uniform_real_distribution
  < double > **randomDistribution_**
- std::shared_ptr< psi::Matrix > excludeSpheres_

    Matrix with vdW sphere information.
- std::map< std::string, double > vdwRadius_

    Map with vdW radii.
- double cx_

    Centre-of-mass coordinates.
- double **cy_**
- double **cz_**
- double radius_

    Radius of padding sphere around the molecule.
- const int nbf_

    Number of basis functions.
- std::shared_ptr< CPHF > cphfSolver_

    The CPHF object.
- std::shared_ptr
  < oepdev::GenEffParFactory > abInitioPolarizationSusceptibilitiesFactory_

    Ab initio polarization susceptibility factory.

17.27.1 Detailed Description

Generalized Effective Fragment Factory. Abstract Base.

Describes the GEFP fragment that is in principle designed to work at correlated levels of theory.

17.27.2 Member Function Documentation

17.27.2.1 std::shared_ptr< oepdev::GenEffParFactory > oepdev::GenEffParFactory::build (const std::string & *type,* **std::shared_ptr< psi::Wavefunction >** *wfn,* **psi::Options &** *opt* **)** `[static]`

Build Density Matrix Susceptibility Generalized Factory.

Parameters

type	- Type of factory
wfn	- Psi4 wavefunction
opt	- Psi4 options

Available factory types:

- `POLARIZATION` - creates the polarization generalized effective fragment parameters' factory Factory subtype is specified in Psi4 options (input file).

Note

Useful options:

- `POLARIZATION` factory type:
  - `DMATPOL_TRAINING_MODE` - training mode. Default: `EFIELD`
  - `DMATPOL_NSAMPLES` - number of random samples (field or test charges sets). Default: `30`
  - `DMATPOL_FIELD_SCALE` - electric field scale factor (relevant if training mode is `EFIELD`). Default: `0.01` [au]
  - `DMATPOL_NTEST_CHARGE` - number of test charges per sample (relevant if training mode is `CHARGES`). Default: `1`
  - `DMATPOL_TEST_CHARGE` - test charge value (relevant if training mode is `CHARGES`). Default: `0.001` [au]
  - `DMATPOL_FIELD_RANK` - electric field rank. Default: `1`
  - `DMATPOL_GRADIENT_RANK` - electric field gradient rank. Default: `0`
  - `DMATPOL_TEST_FIELD_X` - test electric field in X direction. Default: `0.000` [au]
  - `DMATPOL_TEST_FIELD_Y` - test electric field in Y direction. Default: `0.000` [au]
  - `DMATPOL_TEST_FIELD_Z` - test electric field in Z direction. Default: `0.008` [au]
  - `DMATPOL_OUT_STATS` - output file name for statistical evaluation results. Default: `dmatpol.-stats.dat`
  - `DMATPOL_DO_AB_INITIO` - compute ab initio susceptibilities and evaluate statistics for it. Default: `false`
  - `DMATPOL_OUT_STATS_AB_INITIO` - output file name for statistical evaluation results of ab initio model. Default: `dmatpol.stats.abinitio.dat`

The documentation for this class was generated from the following files:

- oepdev/libgefp/gefp.h
- oepdev/libgefp/gefp.cc

17.28 oepdev::GeneralizedDensityFit Class Reference

Generalized Density Fitting Scheme. Abstract Base.

`#include <oep_gdf.h>`

Inheritance diagram for oepdev::GeneralizedDensityFit:
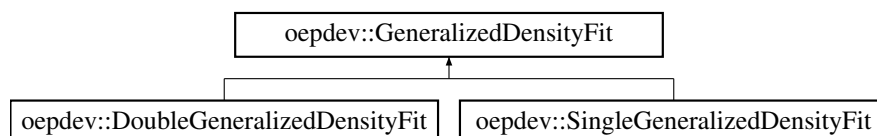
Public Member Functions

- GeneralizedDensityFit ()

    Constructor. Initializes the pointers.
- virtual ∼GeneralizedDensityFit ()

    Destructor.
- void compute (void)=0

    Perform the generalized density fit.
- std::shared_ptr< psi::Matrix > G (void) const

    Extract the $G_{\eta i}$ coefficients.

Static Public Member Functions

- static std::shared_ptr
  < GeneralizedDensityFit > **build** (std::shared_ptr< psi::BasisSet > bs_auxiliary, std::shared_ptr< psi::-
  Matrix > v_vector)
- static std::shared_ptr
  < GeneralizedDensityFit > **build** (std::shared_ptr< psi::BasisSet > bs_auxiliary, std::shared_ptr< psi::-
  BasisSet > bs_intermediate, std::shared_ptr< psi::Matrix > v_vector)

Protected Attributes

- std::shared_ptr< psi::Matrix > G_

    The OEP coefficients $G_{\eta i}$.
- std::shared_ptr< psi::Matrix > H_

    The intermediate DF coefficients for $\hat{v}|i\rangle$.
- std::shared_ptr< psi::BasisSet > bs_a_

    Basis set: auxiliary.
- std::shared_ptr< psi::BasisSet > bs_i_

    Basis set: intermediate.
- std::shared_ptr
  < psi::IntegralFactory > ints_aa_

    Integral factory: aux - aux.
- std::shared_ptr
  < psi::IntegralFactory > ints_ai_

    Integral factory: aux - int.

17.28.1 Detailed Description

Generalized Density Fitting Scheme. Abstract Base.

Performs the following map:

$$\hat{v}|i\rangle \cong \sum_{\eta} G_{\eta i} |\eta\rangle$$

where $\hat{v}$ is the effective one-electron potential (OEP) operator, $|i\rangle$ is an arbitrary state vector and $|\eta\rangle$ is an auxiliary basis vector. The coefficients $G_{\eta i}$ are stored and define the OEP acting on the state i. The mapping onto the auxiliary space can be done in two ways:

- **Single Density Fit.** This method requires the auxiliary basis set to be nearly complete.

- **Double Density Fit.** This method can be used to arbitrary auxiliary basis sets.

The documentation for this class was generated from the following files:

- oepdev/liboep/oep_gdf.h
- oepdev/liboep/oep_gdf.cc

17.29 oepdev::GeneralizedPolarGEFactory Class Reference

Polarization GEFP Factory with Least-Squares Parameterization.

`#include <gefp.h>`

Inheritance diagram for oepdev::GeneralizedPolarGEFactory:

Classes

- struct StatisticalSet

    A structure to handle statistical data.

Public Member Functions

- GeneralizedPolarGEFactory (std::shared_ptr< psi::Wavefunction > wfn, psi::Options &opt)

    Construct from Psi4 wavefunction and options.
- virtual ∼GeneralizedPolarGEFactory ()

    Destruct.
- virtual std::shared_ptr
    < GenEffPar > compute (void)

    Peform Least-Squares Fit.
- bool has_dipole_polarizability () const

    Dipole Polarizability (interacting with $\mathbf{F}$)
- bool has_dipole_dipole_hyperpolarizability () const

    Dipole-Dipole Hyperpolarizability (interacting with $\mathbf{F}^2$)
- bool has_quadrupole_polarizability () const

    Quadrupole Polarizability (interacting with $\nabla \otimes \mathbf{F}$)
- bool has_ab_initio_dipole_polarizability () const

    Ab Initio Dipole Polarizability (interacting with $\mathbf{F}$)
- double Zinit () const

    Grab initial summaric Z value.
- double Z () const

    Grab final summaric Z value.

Protected Member Functions

- void allocate (void)

    Allocate memory.
- void invert_hessian (void)

    Invert Hessian (do also the identity test)
- void compute_electric_field_sums (void)

    Compute electric field sum set.
- void compute_electric_field_gradient_sums (void)

    Compute electric field gradient sum set.
- void compute_statistics (void)

    Run the statistical evaluation of results.

- void set_distributed_centres (void)

    Set the distributed centres.
- void compute_parameters (void)

    Compute the parameters.
- void fit (void)

    Perform least-squares fit.
- void compute_ab_initio (void)

    Compute ab initio parameters.
- void save (int i, int j)

    Save susceptibility tensors associated with the i-th and j-th basis set function.
- virtual void compute_samples (void)=0

    Compute samples of density matrices and select electric field distributions.
- virtual void compute_gradient (int i, int j)=0

    Compute Gradient vector associated with the i-th and j-th basis set function.
- virtual void compute_hessian (void)=0

    Compute Hessian matrix (independent on the parameters)

Protected Attributes

- int nBlocks_

    Number of parameter blocks.
- int nSites_

    Number of distributed sites.
- int nSitesAbInitio_

    Number of distributed sites of Ab Initio model (FF - single site (com); distributed: LMO sites)
- int nParameters_

    Dimensionality of entire parameter space.
- std::vector< int > nParametersBlock_

    Dimensionality of parameter space per block.
- const int nSamples_

    Number of statistical samples.
- const double symmetryNumber_ [6]

    Symmetry number for matrix susceptibilities.
- std::shared_ptr< psi::Matrix > Gradient_

    Gradient.
- std::shared_ptr< psi::Matrix > Hessian_

    Hessian.
- std::shared_ptr< psi::Matrix > Parameters_

    Parameters.
- std::shared_ptr
  < oepdev::GenEffPar > PolarizationSusceptibilities_

    Density Matrix Susceptibility Tensors Object.
- std::shared_ptr
  < oepdev::GenEffPar > abInitioPolarizationSusceptibilities_

    Density Matrix Susceptibility Tensors Object for Ab Initio Model.
- bool hasDipolePolarizability_

    Has Dipole Polarizability?
- bool hasDipoleDipoleHyperpolarizability_

    Has Dipole-Dipole Hyperpolarizability?
- bool hasQuadrupolePolarizability_

    Has Quadrupole Polarizability?

- bool hasAbInitioDipolePolarizability_

    Has Ab Initio Dipole Polarizability?
- StatisticalSet referenceStatisticalSet_

    Reference statistical data.
- StatisticalSet referenceDpolStatisticalSet_

    Multipole reference statistical data.
- StatisticalSet modelStatisticalSet_

    Model statistical data.
- StatisticalSet abInitioModelStatisticalSet_

    Ab Initio Model statistical data.
- std::vector< std::shared_ptr
  < psi::Matrix > > VMatrixSet_

    Potential matrix set.
- std::vector< std::vector
  < std::shared_ptr< Vector > > > electricFieldSet_

    Electric field set.
- std::vector< std::vector
  < std::shared_ptr< Matrix > > > electricFieldGradientSet_

    Electric field gradient set.
- std::vector< std::vector
  < double > > electricFieldSumSet_

    Electric field sum set.
- std::vector< std::vector
  < std::shared_ptr< psi::Vector > > > electricFieldGradientSumSet_

    Electric field gradient sum set.
- std::vector< std::vector
  < std::shared_ptr< Vector > > > abInitioModelElectricFieldSet_

    Electric field set for Ab Initio Model (LMO-distributed)
- const double mField_

    Level shifters for Hessian blocks.
- double Zinit_

    Initial summaric Z value.
- double Z_

    Final summaric Z value.
- std::shared_ptr< psi::JK > jk_

    Computer of generalized JK objects.

Additional Inherited Members

17.29.1 Detailed Description

Polarization GEFP Factory with Least-Squares Parameterization.

Implements a general class of methods for the density matrix susceptibility tensors represented by:

$$\delta D_{\alpha\beta} = \sum_i \left\{ \mathbf{B}^{(10)}_{i;\alpha\beta} \cdot \mathbf{F}(\mathbf{r}_i) + \mathbf{B}^{(20)}_{i;\alpha\beta} : \mathbf{F}(\mathbf{r}_i) \otimes \mathbf{F}(\mathbf{r}_i) + \mathbf{B}^{(01)}_{i;\alpha\beta} : \nabla_i \otimes \mathbf{F}(\mathbf{r}_i) + \ldots \right\}$$

where:

- $\mathbf{B}^{(10)}_{i;\alpha\beta}$ is the density matrix dipole polarizability

- $\mathbf{B}^{(20)}_{i;\alpha\beta}$ is the density matrix dipole-dipole hyperpolarizability

- $\mathbf{B}_{i;\alpha\beta}^{(01)}$ is the density matrix quadrupole polarizability

all defined for the generalized distributed site at $\mathbf{r}_i$.

Available models:

1. Training against uniform electric fields

   - oepdev::LinearUniformEFieldPolarGEFactory - linear with respect to electric field
   - oepdev::QuadraticUniformEFieldPolarGEFactory - quadratic with respect to electric field

2. Training against non-uniform electric fields

   - oepdev::LinearNonUniformEFieldPolarGEFactory - linear with respect to electric field, distributed site model
   - oepdev::QuadraticNonUniformEFieldPolarGEFactory - quadratic with respect to electric field, distributed site model
   - oepdev::LinearGradientNonUniformEFieldPolarGEFactory - linear with respect to electric field and linear with respect to electric field gradient, distributed site model. This model does not function now.
   - oepdev::QuadraticGradientNonUniformEFieldPolarGEFactory - linear with respect to electric field and linear with respect to electric field gradient, distributed site model. This model does not function now.

For the non-linear field training, a set of point charges in each training sample is assumed. Distributed models use atomic centers as expansion points.

Determination of the generalized susceptibilities

Let $\left\{\mathbf{F}^{(1)}(\mathbf{r}), \mathbf{F}^{(2)}(\mathbf{r}), \ldots, \mathbf{F}^{(N)}(\mathbf{r}), \ldots\right\}$ be a set of $N_{\max}$ distinct and randomly sampled spatial distributions of electric field. It is assumed that the exact difference one-particle density matrices (with respect to the unperturbed state) defined as

$$\delta\overline{\mathbf{D}}^{(N)} \equiv \overline{\mathbf{D}}^{(N)} - \overline{\mathbf{D}}^{(0)}$$

are known for each sample (overline symbolizes the exact estimate). Now, for each pair of the AO indices the following parameterization is constructed:

$$\delta D^{(N)} = \sum_i^M \left\{ \sum_u^{x,y,z} s_{iu}^{[1]} F_{iu}^{(N)} + \sum_u^{x,y,z} \sum_{w<u} r_{uw} s_{iuw}^{[2]} F_{iu}^{(N)} F_{iw}^{(N)} + \ldots \right\}$$

(the Greek subscripts were omitted here for notational simplicity). In the above equation, $B_u^{(i;1)} = s_{iu}^{[1]}$ and $B_{uw}^{(i;2)} = r_{uw} s_{iuw}^{[2]}$, where r_{uw} is the symmetry factor equal to 1 for diagonal elements and 2 for off-diagonal elements of $B_{uw}^{(i;2)}$. The multiple parameter blocks ($\mathbf{s}^{[1]}$, $\mathbf{s}^{[2]}$ and so on) appear in the first power, allowing for linear least-squares regression. The square bracket superscripts denote the block of the parameter space.

To determine the optimum set, $\mathbf{s} = \begin{pmatrix} \mathbf{s}^{[1]} & \mathbf{s}^{[2]} & \cdots \end{pmatrix}^{\mathrm{T}}$, a loss function Z that is subject to the least-squares minimization, is defined as

$$Z(\mathbf{s}) = \sum_N^{N_{\max}} \left(\delta D^{(N)} - \delta\overline{D}^{(N)} \right)^2 .$$

The Hessian of Z computed with respect to the parameters is parameter-independent (constant) and generally non-singular as long as the electric fields on all distributed sites are different. Therefore, the exact solution for the optimal parameters is given by the Newton equation

$$\mathbf{s} = -\mathbf{H}^{-1} \cdot \mathbf{g} ,$$

where $\mathbf{g}$ and $\mathbf{H}$ are the gradient vector and the Hessian matrix, respectively. Note that in this case the dimensions of parameter space for the block 1 and 2 are equal to $3M$ and $6M$, respectively. The explicit forms of the gradient and Hessian up to second-order are given in the next section.

Explicit Formulae for Gradient and Hessian Blocks in Linear Regression DMS Model

The gradient vector $\mathbf{g}$ and the Hessian matrix $\mathbf{H}$ are built from blocks associated with a particular type of parameters, i.e.,

$$\mathbf{g} = \begin{pmatrix} \mathbf{g}^{[1]} \\ \mathbf{g}^{[2]} \end{pmatrix}, \quad \mathbf{H} = \begin{pmatrix} \mathbf{H}^{[11]} & \mathbf{H}^{[12]} \\ \mathbf{H}^{[21]} & \mathbf{H}^{[22]} \end{pmatrix},$$

where the block indices 1 and 2 correspond to the first- and second-order susceptibilities, respectively. Note that the second derivatives of $\delta D^{(N)}$ with respect to the adjustable parameters vanish due to the linear functional form of the parameterization formula given in the previous section. Thus, the gradient element of the r-th block and Hessian element of the (rs)-th block read

$$g^{[r]} \equiv \frac{\partial Z}{\partial s^{[r]}} = -2 \sum_N \overline{\delta D}^{(N)} \frac{\partial \left[\delta D^{(N)} \right]}{\partial s^{[r]}},$$

$$H^{[rs]} \equiv \frac{\partial^2 Z}{\partial s^{[r]} \partial s^{[s]}} = 2 \sum_N \frac{\partial \left[\delta D^{(N)} \right]}{\partial s^{[r]}} \frac{\partial \left[\delta D^{(N)} \right]}{\partial s^{[s]}}.$$

The explicit formulae for the gradient are

$$g_{ku}^{[1]} = -2 \sum_N \overline{\delta D}^{(N)} F_{ku}^{(N)},$$

$$g_{kuw}^{[2]} = -2 r_{uw} \sum_N \overline{\delta D}^{(N)} F_{ku}^{(N)} F_{kw}^{(N)}.$$

The Hessian subsequently follows to be %

$$H_{ku,lw}^{[11]} = 2 \sum_N F_{ku}^{(N)} F_{lw}^{(N)},$$

$$H_{ku,lu'w'}^{[12]} = 2 r_{u'w'} \sum_N F_{ku}^{(N)} F_{lu'}^{(N)} F_{lw'}^{(N)},$$

$$H_{kuw,lu'w'}^{[22]} = 2 r_{uw} r_{u'w'} \sum_N F_{ku}^{(N)} F_{kw}^{(N)} F_{lu'}^{(N)} F_{lw'}^{(N)}.$$

Note that due to the symmetry of the Hessian matrix, the block 21 is a transpose of the block 12. The composite indices ku and kuw are constructed from the distributed site index k and the appropriate symmetry-adapted ($w < u$) Cartesian component of a particular DMS tensor: u for the first-order, and uw for the second-order susceptibility tensor, respectively. The method described above can be easily extended to third and higher orders.

The documentation for this class was generated from the following files:

- oepdev/libgefp/gefp.h
- oepdev/libgefp/gefp_polar_base.cc

17.30 oepdev::IntegralFactory Class Reference

Extended IntegralFactory for computing integrals.

```
#include <integral.h>
```

Inheritance diagram for oepdev::IntegralFactory:
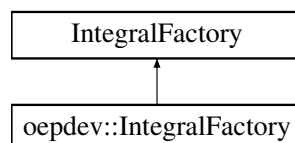
Public Member Functions

- IntegralFactory (std::shared_ptr< psi::BasisSet > bs1, std::shared_ptr< psi::BasisSet > bs2, std::shared_-ptr< psi::BasisSet > bs3, std::shared_ptr< psi::BasisSet > bs4)

  Initialize integral factory given a BasisSet for each center. Becomes (bs1 bs2 | bs3 bs4).

- IntegralFactory (std::shared_ptr< psi::BasisSet > bs1, std::shared_ptr< psi::BasisSet > bs2)

  Initialize integral factory given a BasisSet for two centres. Becomes (bs1 bs2 | bs1 bs2).

- IntegralFactory (std::shared_ptr< psi::BasisSet > bs1)

  Initialize integral factory given a BasisSet for two centres. Becomes (bs1 bs1 | bs1 bs1).

- virtual ∼IntegralFactory ()

  Destructor.

- virtual oepdev::TwoBodyAOInt ∗ eri_1_1 (int deriv=0, bool use_shell_pairs=false)

  Returns an ERI_1_1 integral object.

- virtual oepdev::TwoBodyAOInt ∗ eri_2_1 (int deriv=0, bool use_shell_pairs=false)

  Returns an ERI_2_1 integral object.

- virtual oepdev::TwoBodyAOInt ∗ eri_2_2 (int deriv=0, bool use_shell_pairs=false)

  Returns an ERI_2_2 integral object.

- virtual oepdev::TwoBodyAOInt ∗ eri_3_1 (int deriv=0, bool use_shell_pairs=false)

  Returns an ERI_3_1 integral object.

17.30.1 Detailed Description

Extended IntegralFactory for computing integrals.

In addition to integrals available in Psi4, oepdev::IntegralFactory enables to compute also:

- OEI's:

  - none at that moment

- ERI's:

  - integrals of type (a|b) - `oepdev::ERI_1_1`

  - integrals of type (ab|c) - `oepdev::ERI_2_1`

  - integrals of type (abc|d) - `oepdev::ERI_3_1`

  - integrals of type (ab|cd) - `oepdev::ERI_2_2` (also in Psi4 as `psi::ERI`)

The documentation for this class was generated from the following files:

- oepdev/libpsi/integral.h
- oepdev/libpsi/integral.cc

17.31 oepdev::LinearGradientNonUniformEFieldPolarGEFactory Class Reference

Polarization GEFP Factory with Least-Squares Parameterization.

`#include <gefp.h>`

Inheritance diagram for oepdev::LinearGradientNonUniformEFieldPolarGEFactory:

```
                    ┌─────────────────────────────────────────┐
                    │       oepdev::GenEffParFactory          │
                    └─────────────────────────────────────────┘
                                      ▲
                    ┌─────────────────────────────────────────┐
                    │        oepdev::PolarGEFactory           │
                    └─────────────────────────────────────────┘
                                      ▲
                    ┌─────────────────────────────────────────┐
                    │    oepdev::GeneralizedPolarGEFactory     │
                    └─────────────────────────────────────────┘
                                      ▲
                    ┌─────────────────────────────────────────┐
                    │  oepdev::NonUniformEFieldPolarGEFactory  │
                    └─────────────────────────────────────────┘
                                      ▲
          ┌──────────────────────────────────────────────────────────┐
          │  oepdev::LinearGradientNonUniformEFieldPolarGEFactory    │
          └──────────────────────────────────────────────────────────┘
```
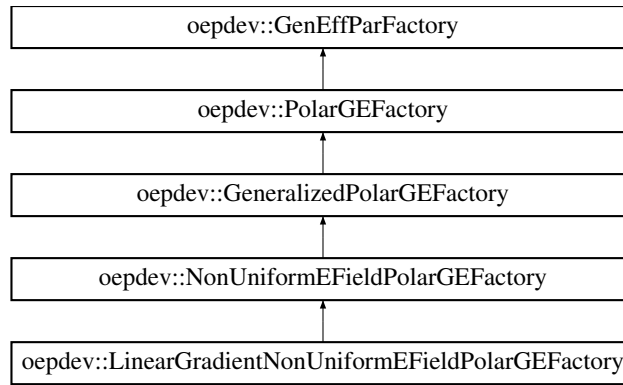
Public Member Functions

- **LinearGradientNonUniformEFieldPolarGEFactory** (std::shared_ptr< psi::Wavefunction > wfn, psi::-Options &opt)
- void compute_gradient (int i, int j)
  Compute Gradient vector associated with the i-th and j-th basis set function.
- void compute_hessian (void)
  Compute Hessian matrix (independent on the parameters)

Additional Inherited Members

17.31.1 Detailed Description

Polarization GEFP Factory with Least-Squares Parameterization.

Implements the generalized density matrix susceptibility model of the form

$$\delta D_{\alpha\beta} \approx \sum_i \left\{ \mathbf{B}_{i;\alpha\beta}^{(10)} \cdot \mathbf{F}(\mathbf{r}_i) + \mathbf{B}_{i;\alpha\beta}^{(01)} : \nabla_i \otimes \mathbf{F}(\mathbf{r}_i) \right\}$$

where:

- $\mathbf{B}_{i;\alpha\beta}^{(10)}$ is the density matrix dipole polarizability

- $\mathbf{B}_{i;\alpha\beta}^{(01)}$ is the density matrix quadrupole polarizability all defined for the distributed site at $\mathbf{r}_i$.

Note

    This model is not available now and probably will be deprecated in the future.

The documentation for this class was generated from the following files:

- oepdev/libgefp/gefp.h
- oepdev/libgefp/gefp_polar_nonuniform_field_1_grad_1.cc

17.32 oepdev::LinearNonUniformEFieldPolarGEFactory Class Reference

Polarization GEFP Factory with Least-Squares Parameterization.

```
#include <gefp.h>
```

Inheritance diagram for oepdev::LinearNonUniformEFieldPolarGEFactory:

```
                        ┌──────────────────────────────────┐
                        │      oepdev::GenEffParFactory      │
                        └──────────────────────────────────┘
                                         ▲
                        ┌──────────────────────────────────┐
                        │      oepdev::PolarGEFactory        │
                        └──────────────────────────────────┘
                                         ▲
                        ┌──────────────────────────────────┐
                        │  oepdev::GeneralizedPolarGEFactory │
                        └──────────────────────────────────┘
                                         ▲
                        ┌──────────────────────────────────┐
                        │ oepdev::NonUniformEFieldPolarGEFactory │
                        └──────────────────────────────────┘
                                         ▲
                        ┌──────────────────────────────────┐
                        │ oepdev::LinearNonUniformEFieldPolarGEFactory │
                        └──────────────────────────────────┘
```
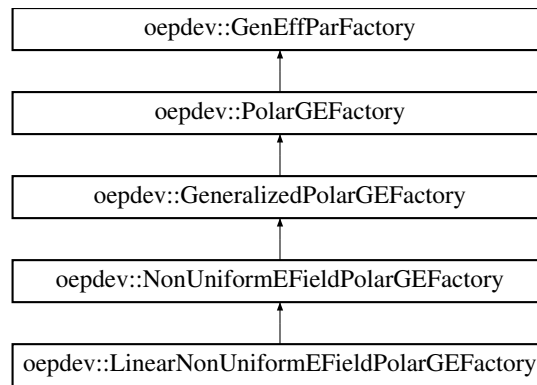
Public Member Functions

- **LinearNonUniformEFieldPolarGEFactory** (std::shared_ptr< psi::Wavefunction > wfn, psi::Options &opt)
- void compute_gradient (int i, int j)

    Compute Gradient vector associated with the i-th and j-th basis set function.

- void compute_hessian (void)

    Compute Hessian matrix (independent on the parameters)

Additional Inherited Members

17.32.1   Detailed Description

Polarization GEFP Factory with Least-Squares Parameterization.

Implements the generalized density matrix susceptibility model of the form

$$\delta D_{\alpha\beta} \approx \sum_i \mathbf{B}^{(10)}_{i;\alpha\beta} \cdot \mathbf{F}(\mathbf{r}_i)$$

where:

- $\mathbf{B}^{(10)}_{i;\alpha\beta}$ is the density matrix dipole polarizability defined for the distributed site at $\mathbf{r}_i$.

The documentation for this class was generated from the following files:

- oepdev/libgefp/gefp.h
- oepdev/libgefp/gefp_polar_nonuniform_field_1.cc

17.33   oepdev::LinearUniformEFieldPolarGEFactory Class Reference

Polarization GEFP Factory with Least-Squares Parameterization.

```
#include <gefp.h>
```

Inheritance diagram for oepdev::LinearUniformEFieldPolarGEFactory:
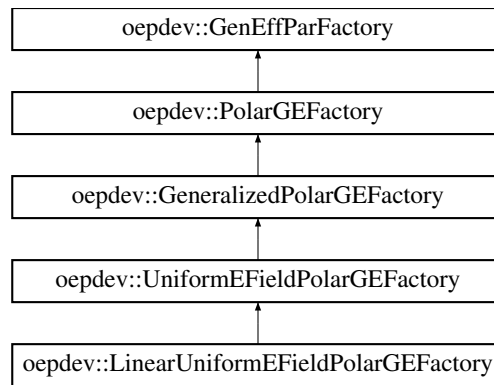
Public Member Functions

- **LinearUniformEFieldPolarGEFactory** (std::shared_ptr< psi::Wavefunction > wfn, psi::Options &opt)
- void compute_gradient (int i, int j)

    Compute Gradient vector associated with the i-th and j-th basis set function.
- void compute_hessian (void)

    Compute Hessian matrix (independent on the parameters)

Additional Inherited Members

17.33.1 Detailed Description

Polarization GEFP Factory with Least-Squares Parameterization.

Implements the generalized density matrix susceptibility model of the form

$$\delta D_{\alpha\beta} \approx \mathbf{B}_{\alpha\beta}^{(10)} \cdot \mathbf{F}$$

where:

- $\mathbf{B}_{\alpha\beta}^{(10)}$ is the density matrix dipole polarizability

The documentation for this class was generated from the following files:

- oepdev/libgefp/gefp.h
- oepdev/libgefp/gefp_polar_uniform_field_1.cc

17.34 oepdev::NonUniformEFieldPolarGEFactory Class Reference

Polarization GEFP Factory with Least-Squares Parameterization.

```
#include <gefp.h>
```

Inheritance diagram for oepdev::NonUniformEFieldPolarGEFactory:
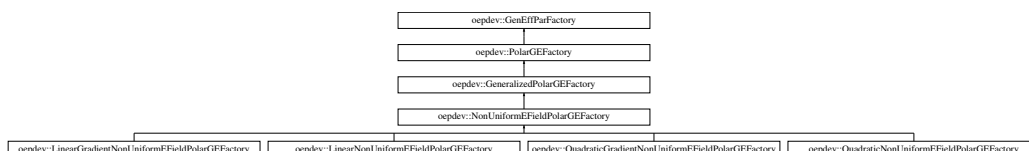
Public Member Functions

- **NonUniformEFieldPolarGEFactory** (std::shared_ptr< psi::Wavefunction > wfn, psi::Options &opt)
- void compute_samples (void)

    Compute samples of density matrices and select electric field distributions.
- virtual void compute_gradient (int i, int j)=0

    Compute Gradient vector associated with the i-th and j-th basis set function.
- virtual void compute_hessian (void)=0

    Compute Hessian matrix (independent on the parameters)

Additional Inherited Members

17.34.1 Detailed Description

Polarization GEFP Factory with Least-Squares Parameterization.

Implements a class of density matrix susceptibility models for parameterization in the non-uniform electric field generated by point charges.

The documentation for this class was generated from the following files:

- oepdev/libgefp/gefp.h
- oepdev/libgefp/gefp_polar_nonuniform_base.cc

17.35 oepdev::OEPDevSolver Class Reference

Solver of properties of molecular aggregates. Abstract base.

```
#include <solver.h>
```

Inheritance diagram for oepdev::OEPDevSolver:
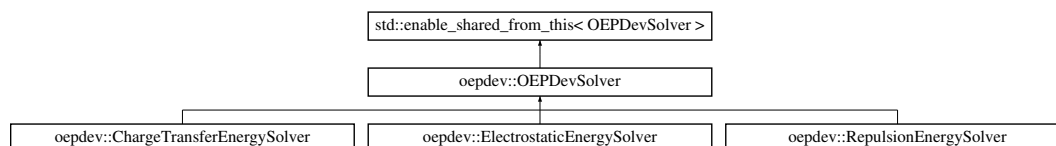
Public Member Functions

- OEPDevSolver (SharedWavefunctionUnion wfn_union)

    Take wavefunction union and initialize the Solver.
- virtual ∼OEPDevSolver ()

    Destroctor.
- virtual double compute_oep_based (const std::string &method="DEFAULT")=0

    Compute property by using OEP's.
- virtual double compute_benchmark (const std::string &method="DEFAULT")=0

    Compute property by using benchmark method.

Static Public Member Functions

- static std::shared_ptr
    < OEPDevSolver > build (const std::string &target, SharedWavefunctionUnion wfn_union)

    Build a solver of a particular property for given molecular cluster.

Protected Attributes

- SharedWavefunctionUnion wfn_union_

    Wavefunction union.

- std::vector< std::string > methods_oepBased_

    Names of all OEP-based methods implemented for a solver.

- std::vector< std::string > methods_benchmark_

    Names of all benchmark methods implemented for a solver.

17.35.1 Detailed Description

Solver of properties of molecular aggregates. Abstract base.

Uses only a wavefunction union object to initialize. Available solvers:

- `ELECTROSTATIC ENERGY`

- `REPULSION ENERGY`

- `CHARGE TRANSFER ENERGY`

17.35.2 Constructor & Destructor Documentation

17.35.2.1 OEPDevSolver::OEPDevSolver (SharedWavefunctionUnion *wfn_union*)

Take wavefunction union and initialize the Solver.

Parameters

wfn_union	- wavefunction union of isolated molecular wavefunctions

17.35.3 Member Function Documentation

17.35.3.1 std::shared_ptr< **OEPDevSolver** > OEPDevSolver::build (const std::string & *target,* SharedWavefunctionUnion *wfn_union*) `[static]`

Build a solver of a particular property for given molecular cluster.

Parameters

target	- target property
wfn_union	- wavefunction union of isolated molecular wavefunctions

Implemented target properties:

- `ELECTROSTATIC_ENERGY` - Coulombic interaction energy between unperturbed wavefunctions.

- `REPULSION_ENERGY` - Pauli repulsion interaction energy between unperturbed wavefunctions.

See Also

    ElectrostaticEnergySolver

17.35.3.2 double OEPDevSolver::compute_benchmark (const std::string & *method =* `"DEFAULT"`) `[pure virtual]`

Compute property by using benchmark method.

Each solver object has one `DEFAULT` benchmark method

Parameters

method	- benchmark method

Implemented in oepdev::ChargeTransferEnergySolver, oepdev::RepulsionEnergySolver, and oepdev::Electrostatic-EnergySolver.

17.35.3.3 double OEPDevSolver::compute_oep_based (const std::string & *method* = `"DEFAULT"`) `[pure virtual]`

Compute property by using OEP's.

Each solver object has one `DEFAULT` OEP-based method.

Parameters

method	- flavour of OEP model

Implemented in oepdev::ChargeTransferEnergySolver, oepdev::RepulsionEnergySolver, and oepdev::Electrostatic-EnergySolver.

The documentation for this class was generated from the following files:

- oepdev/libutil/solver.h
- oepdev/libutil/solver.cc

17.36   oepdev::OEPotential Class Reference

Generalized One-Electron Potential: Abstract base.

`#include <oep.h>`

Inheritance diagram for oepdev::OEPotential:
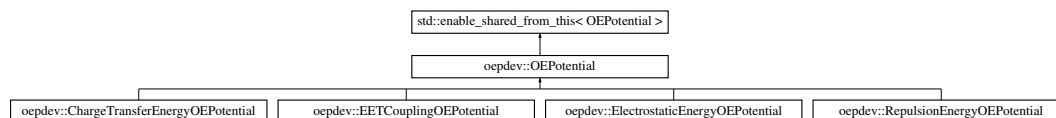
Public Member Functions

- OEPotential (SharedWavefunction wfn, Options &options)

    Fully ESP-based OEP object.
- OEPotential (SharedWavefunction wfn, SharedBasisSet auxiliary, Options &options)

    General OEP object.
- virtual ∼OEPotential ()

    Destructor.
- virtual void compute (void)

    Compute matrix forms of all OEP's within all OEP types.
- virtual void compute (const std::string &oepType)=0

    Compute matrix forms of all OEP's within a specified OEP type.
- virtual void compute_3D (const std::string &oepType, const double &x, const double &y, const double &z, double &v)=0

    Compute value of potential in point x, y, z and save at v.
- virtual void write_cube (const std::string &oepType, const std::string &fileName)

    Write potential to a cube file.

- virtual void rotate (const Matrix &rotmat)

    Rotate.
- virtual void translate (const Vector &trans)

    Translate.
- virtual void superimpose (const Matrix &refGeometry, const std::vector< int > &supList, const std::vector< int > &reordList)

    Superimpose.
- std::string name () const

    Retrieve name of this OEP.
- OEPType oep (const std::string &oepType) const

    Retrieve the potentials.
- SharedMatrix matrix (const std::string &oepType) const

    Retrieve the potentials in a matrix form.
- SharedWavefunction wfn () const

    Retrieve wavefunction object.
- void **set_name** (const std::string &name)
- virtual void **print_header** () const =0

Static Public Member Functions

- static std::shared_ptr
    < OEPotential > build (const std::string &category, SharedWavefunction wfn, Options &options)

    Build fully ESP-based OEP object.
- static std::shared_ptr
    < OEPotential > build (const std::string &category, SharedWavefunction wfn, SharedBasisSet auxiliary, Options &options)

    Build general OEP object.

Protected Attributes

- Options options_

    Psi4 options.
- SharedWavefunction wfn_

    Wavefunction.
- SharedBasisSet primary_

    Promary Basis set.
- SharedBasisSet auxiliary_

    Auxiliary Basis set.
- std::string name_

    Name of this OEP;.
- std::map< std::string, OEPType > oepTypes_

    Types of OEP's within the scope of this object.
- std::shared_ptr
    < psi::IntegralFactory > intsFactory_

    Integral factory.
- std::shared_ptr< psi::Matrix > potMat_

    Matrix of potential one-electron integrals.
- std::shared_ptr
    < psi::OneBodyAOInt > OEInt_

    One-electron integral shared pointer.
- std::shared_ptr< PotentialInt > potInt_

    One-electron potential shared pointer.

17.36.1 Detailed Description

Generalized One-Electron Potential: Abstract base.

Manages OEP's in matrix and 3D forms. Available OEP categories:

- ELECTROSTATIC ENERGY

- REPULSION ENERGY

- CHARGE TRANSFER ENERGY

- EET COUPLING CONSTANT

17.36.2 Constructor & Destructor Documentation

17.36.2.1 OEPotential::OEPotential (SharedWavefunction *wfn,* Options & *options*)

Fully ESP-based OEP object.

Parameters

wfn	- wavefunction
options	- Psi4 options

17.36.2.2 OEPotential::OEPotential (SharedWavefunction *wfn,* SharedBasisSet *auxiliary,* Options & *options*)

General OEP object.

Parameters

wfn	- wavefunction
auxiliary	- basis set for density fitting of OEP's
options	- Psi4 options

17.36.3 Member Function Documentation

17.36.3.1 std::shared_ptr< OEPotential > OEPotential::build (const std::string & *category,* SharedWavefunction *wfn,* Options & *options*) `[static]`

Build fully ESP-based OEP object.

Parameters

type	- OEP category
wfn	- wavefunction
options	- Psi4 options

17.36.3.2 std::shared_ptr< OEPotential > OEPotential::build (const std::string & *category,* SharedWavefunction *wfn,* SharedBasisSet *auxiliary,* Options & *options*) `[static]`

Build general OEP object.

Parameters

type	- OEP category
wfn	- wavefunction
auxiliary	- basis set for density fitting of OEP's
options	- Psi4 options

The documentation for this class was generated from the following files:

- oepdev/liboep/oep.h
- oepdev/liboep/oep.cc

17.37 oepdev::OEPotential3D< T > Class Template Reference

Class template for OEP scalar fields.

```
#include <space3d.h>
```

Inheritance diagram for oepdev::OEPotential3D< T >:
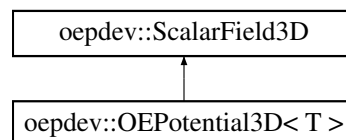
Public Member Functions

- OEPotential3D (const int &np, const double &padding, std::shared_ptr< T > oep, const std::string &oepType)

  Construct random spherical collection of scalar field of type T.

- OEPotential3D (const int &nx, const int &ny, const int &nz, const double &px, const double &py, const double &pz, std::shared_ptr< T > oep, const std::string &oepType, psi::Options &options)

  Construct ordered 3D collection of scalar field of type T.

- virtual ∼OEPotential3D ()

  Destructor.

- virtual double compute_xyz (const double &x, const double &y, const double &z)

  Compute a value of scalar field at point (x, y, z)

- virtual void print () const

  Print information of the object to Psi4 output.

Protected Attributes

- std::shared_ptr< T > oep_

  Shared pointer to the instance of class `T`

- std::string oepType_

  Descriptor of the scalar field type stored in instance of `T`

Additional Inherited Members

17.37.1 Detailed Description

template$<$**class T**$>$**class oepdev::OEPotential3D**$<$ **T** $>$

Class template for OEP scalar fields.

Used for special type of classes T that contain following public member functions:

```
class T : public std::enable_shared_from_this<T> {

  public:
    void compute_3D(const std::string& descriptor,
                    const double& x, const double& y, const double& z,
                    double& v);

    shared_ptr<psi::Wavefunction> wfn() const {return wfn_;}

};
```

with the `descriptor` of a certain scalar field type, `x`, `y`, `z` the points in 3D space in which the scalar field has to be computed and stored at `v`. Instances of `T` should store shared pointer to wavefunction object. List of classes `T` that are compatible with this class template and are currently implemented in oepdev is given below:

- `oepdev::OEPotential` abstract base (do not use derived classes as `T`)

Template parameters:

Template Parameters

T	the compatible class (e.g. `oepdev::OEPotential`)

The documentation for this class was generated from the following file:

- oepdev/libutil/space3d.h

17.38   oepdev::OEPType Struct Reference

Container to handle the type of One-Electron Potentials.

`#include <oep.h>`

Public Attributes

- std::string name

    Name of this type of OEP.
- bool is_density_fitted

    Is this OEP DF-based?
- int n

    Number of OEP's within a type.
- SharedMatrix matrix

    All OEP's of this type gathered in a matrix form.

17.38.1   Detailed Description

Container to handle the type of One-Electron Potentials.

The documentation for this struct was generated from the following file:

- oepdev/liboep/oep.h

17.39 oepdev::PerturbCharges Struct Reference

Structure to hold perturbing charges.

```
#include <scf_perturb.h>
```

Public Attributes

- std::vector< double > charges
    Vector of charge values.
- std::vector< std::shared_ptr
  < psi::Vector > > positions
    Vector of charge position vectors.

17.39.1 Detailed Description

Structure to hold perturbing charges.

The documentation for this struct was generated from the following file:

- oepdev/libutil/scf_perturb.h

17.40 oepdev::Points3DIterator::Point Struct Reference

Public Attributes

- double **x**
- double **y**
- double **z**
- int **index**

The documentation for this struct was generated from the following file:

- oepdev/libutil/space3d.h

17.41 oepdev::Points3DIterator Class Reference

Iterator over a collection of points in 3D space. Abstract base.

```
#include <space3d.h>
```

Inheritance diagram for oepdev::Points3DIterator:
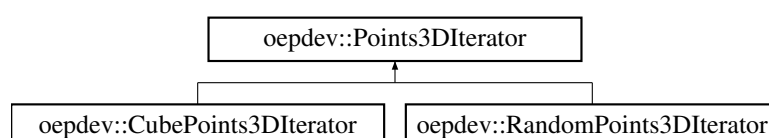
Classes

- struct Point

Public Member Functions

- Points3DIterator (const int &np)

  Plain constructor. Initializes the abstract features.
- virtual ∼Points3DIterator ()

  Destructor.
- virtual bool is_done ()

  Check if iteration is finished.
- virtual void first ()=0

  Initialize first iteration.
- virtual void next ()=0

  Step to next iteration.

- virtual double **x** () const
- virtual double **y** () const
- virtual double **z** () const
- virtual int **index** () const

Static Public Member Functions

- static shared_ptr
  < Points3DIterator > build (const int &nx, const int &ny, const int &nz, const double &dx, const double &dy, const double &dz, const double &ox, const double &oy, const double &oz)

  Build G09 Cube collection iterator.
- static shared_ptr
  < Points3DIterator > build (const int &np, const double &radius, const double &cx, const double &cy, const double &cz)

  Build random collection iterator.
- static shared_ptr
  < Points3DIterator > build (const int &np, const double &pad, psi::SharedMolecule mol)

  Build random collection iterator.

Protected Attributes

- const int np_

  Number of points.
- bool done_

  Status of the iterator.
- int index_

  Current index.

- Point **current_**

17.41.1 Detailed Description

Iterator over a collection of points in 3D space. Abstract base.

Points3DIterators are constructed either as iterators over:

- a random collections or

- an ordered (g09 cube-like) collections. **Note:** Always create instances by using static factory methods.

17.41.2 Constructor & Destructor Documentation

17.41.2.1 oepdev::Points3DIterator::Points3DIterator (const int & *np*)

Plain constructor. Initializes the abstract features.

Parameters

np	- number of points this iterator is constructed for

17.41.3 Member Function Documentation

17.41.3.1 std::shared_ptr< **Points3DIterator** > oepdev::Points3DIterator::build (const int & *nx,* const int & *ny,* const int & *nz,* const double & *dx,* const double & *dy,* const double & *dz,* const double & *ox,* const double & *oy,* const double & *oz*) `[static]`

Build G09 Cube collection iterator.

The points are generated according to Gaussian cube file format.

Parameters

nx	- number of points along x direction
ny	- number of points along y direction
nz	- number of points along z direction
dx	- spacing distance along x direction
dy	- spacing distance along y direction
dz	- spacing distance along y direction
ox	- coordinate x of cube origin
oy	- coordinate y of cube origin
oz	- coordinate z of cube origin

17.41.3.2 std::shared_ptr< **Points3DIterator** > oepdev::Points3DIterator::build (const int & *np,* const double & *radius,* const double & *cx,* const double & *cy,* const double & *cz*) `[static]`

Build random collection iterator.

The points are drawn according to uniform distrinution in 3D space.

Parameters

np	- number of points to draw
radius	- sphere radius inside which points are to be drawn
cx	- coordinate x of sphere's centre
cy	- coordinate y of sphere's centre
cz	- coordinate z of sphere's centre

17.41.3.3 shared_ptr< **Points3DIterator** > oepdev::Points3DIterator::build (const int & *np,* const double & *pad,* psi::SharedMolecule *mol*) `[static]`

Build random collection iterator.

The points are drawn according to uniform distrinution in 3D space enclosing a molecule given. All drawn points lie outside the van der Waals volume.

Parameters

np	- number of points to draw
pad	- radius padding of a minimal sphere enclosing the molecule
mol	- Psi4 molecule object

The documentation for this class was generated from the following files:

- oepdev/libutil/space3d.h
- oepdev/libutil/space3d.cc

17.42 oepdev::PointsCollection3D Class Reference

Collection of points in 3D space. Abstract base.

`#include <space3d.h>`

Inheritance diagram for oepdev::PointsCollection3D:
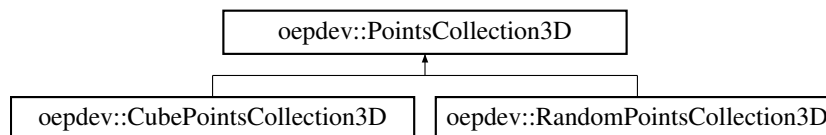
Public Types

- enum Collection { **Random**, **Cube** }

    Public descriptior of collection type.

Public Member Functions

- PointsCollection3D (Collection collectionType, int &np)

    Initialize abstract features.
- **PointsCollection3D** (Collection collectionType, const int &np)
- virtual ∼PointsCollection3D ()

    Destructor.
- virtual int npoints () const

    Get the number of points.
- virtual shared_ptr
  < Points3DIterator > points_iterator () const

    Get the iterator over this collection of points.
- virtual Collection get_type () const

    Get the collection type.
- virtual void print () const =0

    Print the information to Psi4 output file.

Static Public Member Functions

- static shared_ptr
  < PointsCollection3D > build (const int &npoints, const double &radius, const double &cx=0.0, const double &cy=0.0, const double &cz=0.0)

    Build random collection of points.
- static shared_ptr
  < PointsCollection3D > build (const int &npoints, const double &padding, psi::SharedMolecule mol)

    Build random collection of points.
- static shared_ptr
  < PointsCollection3D > build (const int &nx, const int &ny, const int &nz, const double &px, const double &py, const double &pz, psi::SharedBasisSet bs, psi::Options &options)

    Build G09 Cube collection of points.

Protected Attributes

- const int np_

  Number of points.

- Collection collectionType_

  Collection type.

- shared_ptr< Points3DIterator > pointsIterator_

  iterator over points collection

17.42.1   Detailed Description

Collection of points in 3D space. Abstract base.

Create random or ordered (g09 cube-like) collections of points in 3D space.

Note: Always create instances by using static factory methods.

17.42.2   Constructor & Destructor Documentation

17.42.2.1   oepdev::PointsCollection3D::PointsCollection3D (Collection *collectionType,* int & *np*)

Initialize abstract features.

Parameters

np	- number of points to be created

17.42.3   Member Function Documentation

17.42.3.1   std::shared_ptr< PointsCollection3D > oepdev::PointsCollection3D::build (const int & *npoints,* const double & *radius,* const double & *cx =* 0.0*,* const double & *cy =* 0.0*,* const double & *cz =* 0.0) `[static]`

Build random collection of points.

Points uniformly span a sphere.

Parameters

npoints	- number of points to draw
radius	- sphere radius inside which points are to be drawn
cx	- coordinate x of sphere's centre
cy	- coordinate y of sphere's centre
cz	- coordinate z of sphere's centre

17.42.3.2   std::shared_ptr< PointsCollection3D > oepdev::PointsCollection3D::build (const int & *npoints,* const double & *padding,* psi::SharedMolecule *mol*) `[static]`

Build random collection of points.

Points uniformly span space inside a sphere enclosing a molecule. exluding the van der Waals volume.

Parameters

np	- number of points to draw

padding	- radius padding of a minimal sphere enclosing the molecule
mol	- Psi4 molecule object

17.42.3.3 std::shared_ptr< PointsCollection3D > oepdev::PointsCollection3D::build (const int & *nx,* const int & *ny,* const int & *nz,* const double & *px,* const double & *py,* const double & *pz,* psi::SharedBasisSet *bs,* psi::Options & *options*) `[static]`

Build G09 Cube collection of points.

The points span a parallelpiped according to Gaussian cube file format.

Parameters

nx	- number of points along x direction
ny	- number of points along y direction
nz	- number of points along z direction
px	- padding distance along x direction
py	- padding distance along y direction
pz	- padding distance along z direction
bs	- Psi4 basis set object
options	- Psi4 options object

The documentation for this class was generated from the following files:

- oepdev/libutil/space3d.h
- oepdev/libutil/space3d.cc

17.43 oepdev::PolarGEFactory Class Reference

Polarization GEFP Factory. Abstract Base.

```
#include <gefp.h>
```

Inheritance diagram for oepdev::PolarGEFactory:

Public Member Functions

- PolarGEFactory (std::shared_ptr< psi::Wavefunction > wfn, psi::Options &opt)

    Construct from Psi4 options.
- virtual ~PolarGEFactory ()

    Destruct.
- virtual std::shared_ptr
  < GenEffPar > compute (void)=0

    Compute the density matrix susceptibility tensors.

Protected Member Functions

- std::shared_ptr< psi::Vector > draw_field ()

    Randomly draw electric field value.

- double draw_charge ()

    Randomly draw charge value.
- std::shared_ptr
  < oepdev::RHFPerturbed > perturbed_state (const std::shared_ptr< psi::Vector > &field)

    Solve SCF equations to find perturbed state due to uniform electric field.
- std::shared_ptr
  < oepdev::RHFPerturbed > perturbed_state (const std::shared_ptr< psi::Vector > &pos, const double
  &charge)

    Solve SCF equations to find perturbed state due to point charge.
- std::shared_ptr
  < oepdev::RHFPerturbed > perturbed_state (const std::shared_ptr< psi::Matrix > &charges)

    Solve SCF equations to find perturbed state due to set of point charges.
- std::shared_ptr< psi::Vector > field_due_to_charges (const std::shared_ptr< psi::Matrix > &charges, const
  double &x, const double &y, const double &z)

    Evaluate electric field at point (x,y,z) due to point charges.
- std::shared_ptr< psi::Vector > **field_due_to_charges** (const std::shared_ptr< psi::Matrix > &charges, const
  std::shared_ptr< psi::Vector > &pos)
- std::shared_ptr< psi::Matrix > field_gradient_due_to_charges (const std::shared_ptr< psi::Matrix >
  &charges, const double &x, const double &y, const double &z)

    Evaluate electric field gradient at point (x,y,z) due to point charges.
- std::shared_ptr< psi::Matrix > **field_gradient_due_to_charges** (const std::shared_ptr< psi::Matrix >
  &charges, const std::shared_ptr< psi::Vector > &pos)

Additional Inherited Members

17.43.1 Detailed Description

Polarization GEFP Factory. Abstract Base.

Basic interface for the polarization density matrix susceptibility parameters.

The documentation for this class was generated from the following files:

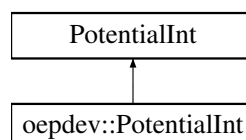- oepdev/libgefp/gefp.h
- oepdev/libgefp/gefp_polar_base.cc

17.44 oepdev::PotentialInt Class Reference

Computes potential integrals.

```
#include <potential.h>
```

Inheritance diagram for oepdev::PotentialInt:

Public Member Functions

- PotentialInt (std::vector< psi::SphericalTransform > &st, std::shared_ptr< psi::BasisSet > bs1, std::shared-
  _ptr< psi::BasisSet > bs2, int deriv=0)

Constructor. Initialize identically like in psi::PotentiIlnt.

- PotentialInt (std::vector< psi::SphericalTransform > &st, std::shared_ptr< psi::BasisSet > bs1, std::shared-_ptr< psi::BasisSet > bs2, std::shared_ptr< psi::Matrix > Qxyz, int deriv=0)

    Constructor. Takes an arbitrary collection of charges.

- PotentialInt (std::vector< psi::SphericalTransform > &, std::shared_ptr< psi::BasisSet >, std::shared_ptr< psi::BasisSet >, const double &x, const double &y, const double &z, const double &q=1.0, int deriv=0)

    Constructor. Computes potential for one point x, y, z for a test particle of charge q.

- void set_charge_field (const double &x, const double &y, const double &z, const double &q=1.0)

    Mutator. Set the charge field to be a x, y, z point of charge q.

17.44.1 Detailed Description

Computes potential integrals.

17.44.2 Constructor & Destructor Documentation

17.44.2.1 oepdev::PotentialInt::PotentialInt (std::vector< psi::SphericalTransform > & *st,* std::shared_ptr< psi::BasisSet > *bs1,* std::shared_ptr< psi::BasisSet > *bs2,* int *deriv =* 0)

Constructor. Initialize identically like in psi::PotentiIlnt.

Parameters

st	- Spherical transform object
bs1	- basis set for first space
bs2	- basis set for second space
deriv	- derivative level

17.44.2.2 oepdev::PotentialInt::PotentialInt (std::vector< psi::SphericalTransform > & *st,* std::shared_ptr< psi::BasisSet > *bs1,* std::shared_ptr< psi::BasisSet > *bs2,* std::shared_ptr< psi::Matrix > *Qxyz,* int *deriv =* 0)

Constructor. Takes an arbitrary collection of charges.

Parameters

st	- Spherical transform object
bs1	- basis set for first space
bs2	- basis set for second space
Qxyz	- matrix with charges and their positions
deriv	- derivative level

17.44.2.3 oepdev::PotentialInt::PotentialInt (std::vector< psi::SphericalTransform > & *st,* std::shared_ptr< psi::BasisSet > *bs1,* std::shared_ptr< psi::BasisSet > *bs2,* const double & *x,* const double & *y,* const double & *z,* const double & *q* = 1.0, int *deriv =* 0)

Constructor. Computes potential for one point x, y, z for a test particle of charge q.

Parameters

st	- Spherical transform object
bs1	- basis set for first space

bs2	- basis set for second space
x	- x coordinate of q
y	- y coordinate of q
z	- z coordinate of q
q	- value of the probe charge
deriv	- derivative level

17.44.3 Member Function Documentation

17.44.3.1 void oepdev::PotentialInt::set_charge_field (const double & *x,* const double & *y,* const double & *z,* const double & *q* = 1.0)

Mutator. Set the charge field to be a x, y, z point of charge q.

Parameters

x	- x coordinate of q
y	- y coordinate of q
z	- z coordinate of q
q	- value of the probe charge

The documentation for this class was generated from the following files:

- oepdev/libpsi/potential.h
- oepdev/libpsi/potential.cc

17.45 oepdev::QuadraticGradientNonUniformEFieldPolarGEFactory Class Reference

Polarization GEFP Factory with Least-Squares Parameterization.

```
#include <gefp.h>
```

Inheritance diagram for oepdev::QuadraticGradientNonUniformEFieldPolarGEFactory:
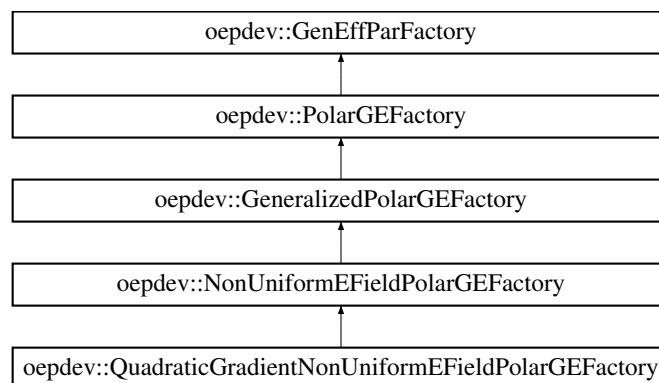
Public Member Functions

- **QuadraticGradientNonUniformEFieldPolarGEFactory** (std::shared_ptr< psi::Wavefunction > wfn, psi::-Options &opt)
- void compute_gradient (int i, int j)

    Compute Gradient vector associated with the i-th and j-th basis set function.
- void compute_hessian (void)

    Compute Hessian matrix (independent on the parameters)

Additional Inherited Members

17.45.1 Detailed Description

Polarization GEFP Factory with Least-Squares Parameterization.

Implements the generalized density matrix susceptibility model of the form

$$\delta D_{\alpha\beta} \approx \sum_i \left\{ \mathbf{B}_{i;\alpha\beta}^{(10)} \cdot \mathbf{F}(\mathbf{r}_i) + \mathbf{B}_{i;\alpha\beta}^{(20)} : \mathbf{F} \otimes \mathbf{F}(\mathbf{r}_i) + \mathbf{B}_{i;\alpha\beta}^{(01)} : \nabla_i \otimes \mathbf{F}(\mathbf{r}_i) \right\}$$

where:

- $\mathbf{B}_{i;\alpha\beta}^{(10)}$ is the density matrix dipole polarizability

- $\mathbf{B}_{i;\alpha\beta}^{(20)}$ is the density matrix dipole-dipole hyperpolarizability

- $\mathbf{B}_{i;\alpha\beta}^{(01)}$ is the density matrix quadrupole polarizability all defined for the distributed site at $\mathbf{r}_i$.

Note

This model is not available now and probably will be deprecated in the future.

The documentation for this class was generated from the following files:

- oepdev/libgefp/gefp.h
- oepdev/libgefp/gefp_polar_nonuniform_field_2_grad_1.cc

17.46 oepdev::QuadraticNonUniformEFieldPolarGEFactory Class Reference

Polarization GEFP Factory with Least-Squares Parameterization.

```
#include <gefp.h>
```

Inheritance diagram for oepdev::QuadraticNonUniformEFieldPolarGEFactory:
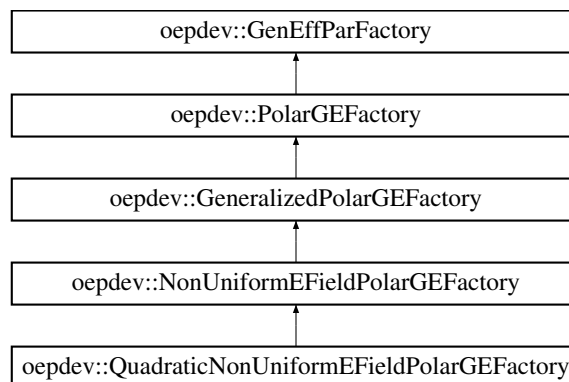
Public Member Functions

- **QuadraticNonUniformEFieldPolarGEFactory** (std::shared_ptr< psi::Wavefunction > wfn, psi::Options &opt)
- void compute_gradient (int i, int j)

    Compute Gradient vector associated with the i-th and j-th basis set function.
- void compute_hessian (void)

    Compute Hessian matrix (independent on the parameters)

Additional Inherited Members

17.46.1   Detailed Description

Polarization GEFP Factory with Least-Squares Parameterization.

Implements the generalized density matrix susceptibility model of the form

$$\delta D_{\alpha\beta} \approx \sum_{i} \left\{ \mathbf{B}_{i;\alpha\beta}^{(10)} \cdot \mathbf{F}(\mathbf{r}_i) + \mathbf{B}_{i;\alpha\beta}^{(20)} : \mathbf{F}(\mathbf{r}_i) \otimes \mathbf{F}(\mathbf{r}_i) \right\}$$

where:

- $\mathbf{B}_{i;\alpha\beta}^{(10)}$ is the density matrix dipole polarizability

- $\mathbf{B}_{i;\alpha\beta}^{(20)}$ is the density matrix dipole-dipole hyperpolarizability all defined for the distributed site at $\mathbf{r}_i$.

The documentation for this class was generated from the following files:

- oepdev/libgefp/gefp.h
- oepdev/libgefp/gefp_polar_nonuniform_field_2.cc

17.47   oepdev::QuadraticUniformEFieldPolarGEFactory Class Reference

Polarization GEFP Factory with Least-Squares Parameterization.

```
#include <gefp.h>
```

Inheritance diagram for oepdev::QuadraticUniformEFieldPolarGEFactory:
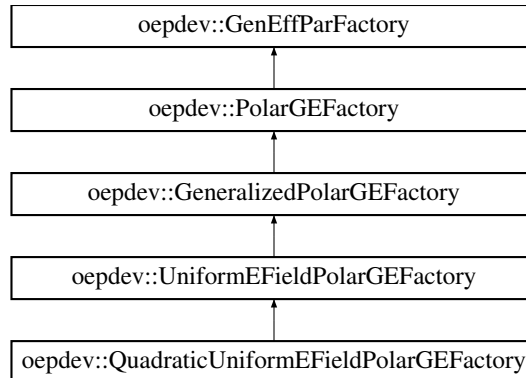
Public Member Functions

- **QuadraticUniformEFieldPolarGEFactory** (std::shared_ptr< psi::Wavefunction > wfn, psi::Options &opt)
- void compute_gradient (int i, int j)

     Compute Gradient vector associated with the i-th and j-th basis set function.

- void compute_hessian (void)

     Compute Hessian matrix (independent on the parameters)

Additional Inherited Members

17.47.1   Detailed Description

Polarization GEFP Factory with Least-Squares Parameterization.

Implements the generalized density matrix susceptibility model of the form

$$\delta D_{\alpha\beta} \approx \mathbf{B}_{\alpha\beta}^{(10)} \cdot \mathbf{F} + \mathbf{B}_{\alpha\beta}^{(20)} : \mathbf{F} \otimes \mathbf{F}$$

where:

- $\mathbf{B}_{\alpha\beta}^{(10)}$ is the density matrix dipole polarizability

- $\mathbf{B}_{\alpha\beta}^{(20)}$ is the density matrix dipole-dipole hyperpolarizability

The documentation for this class was generated from the following files:

- oepdev/libgefp/gefp.h
- oepdev/libgefp/gefp_polar_uniform_field_2.cc

17.48 oepdev::RandomPoints3DIterator Class Reference

Iterator over a collection of points in 3D space. Random collection.

```
#include <space3d.h>
```

Inheritance diagram for oepdev::RandomPoints3DIterator:

```
┌─────────────────────────────┐
│  oepdev::Points3DIterator   │
└─────────────────────────────┘
              ▲
┌─────────────────────────────┐
│ oepdev::RandomPoints3DIterator │
└─────────────────────────────┘
```
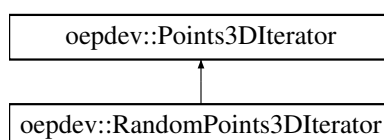
Public Member Functions

- **RandomPoints3DIterator** (const int &np, const double &radius, const double &cx, const double &cy, const double &cz)
- **RandomPoints3DIterator** (const int &np, const double &pad, psi::SharedMolecule mol)
- virtual void first ()
    Initialize first iteration.
- virtual void next ()
    Step to next iteration.

Protected Member Functions

- virtual double **random_double** ()
- virtual void **draw_random_point** ()
- virtual bool **is_in_vdWsphere** (double x, double y, double z) const

Protected Attributes

- double **cx_**
- double **cy_**
- double **cz_**
- double **radius_**
- double **r_**
- double **phi_**

- double **theta_**
- double **x_**
- double **y_**
- double **z_**
- psi::SharedMatrix **excludeSpheres_**
- std::map< std::string, double > **vdwRadius_**
- std::default_random_engine **randomNumberGenerator_**
- std::uniform_real_distribution
  < double > **randomDistribution_**

Additional Inherited Members

17.48.1 Detailed Description

Iterator over a collection of points in 3D space. Random collection.

Note: Always create instances by using static factory method from Points3DIterator. Do not use constructors of this class.

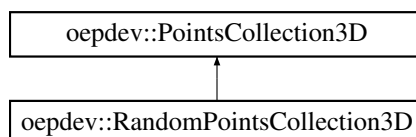The documentation for this class was generated from the following files:

- oepdev/libutil/space3d.h
- oepdev/libutil/space3d.cc

17.49 oepdev::RandomPointsCollection3D Class Reference

Collection of random points in 3D space.

```
#include <space3d.h>
```

Inheritance diagram for oepdev::RandomPointsCollection3D:

```
┌─────────────────────────────────┐
│   oepdev::PointsCollection3D     │
└─────────────────────────────────┘
                 ▲
                 │
┌─────────────────────────────────┐
│ oepdev::RandomPointsCollection3D │
└─────────────────────────────────┘
```

Public Member Functions

- **RandomPointsCollection3D** (Collection collectionType, const int &npoints, const double &radius, const double &cx, const double &cy, const double &cz)
- **RandomPointsCollection3D** (Collection collectionType, const int &npoints, const double &padding, psi::-SharedMolecule mol)
- virtual void print () const

  Print the information to Psi4 output file.

Additional Inherited Members

17.49.1 Detailed Description

Collection of random points in 3D space.

Note: Do not use constructors of this class explicitly. Instead, use static factory methods of the superclass to create instances.

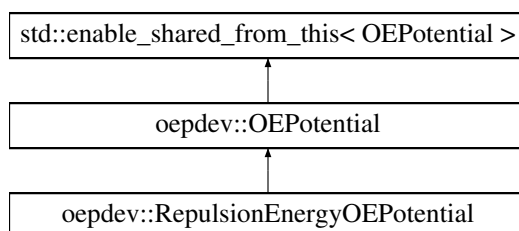The documentation for this class was generated from the following files:

- oepdev/libutil/space3d.h
- oepdev/libutil/space3d.cc

17.50 oepdev::RepulsionEnergyOEPotential Class Reference

Generalized One-Electron Potential for Pauli Repulsion Energy.

```
#include <oep.h>
```

Inheritance diagram for oepdev::RepulsionEnergyOEPotential:

```
┌─────────────────────────────────────────────┐
│  std::enable_shared_from_this< OEPotential >  │
└─────────────────────────────────────────────┘
                      ▲
┌─────────────────────────────────────────────┐
│            oepdev::OEPotential                │
└─────────────────────────────────────────────┘
                      ▲
┌─────────────────────────────────────────────┐
│     oepdev::RepulsionEnergyOEPotential        │
└─────────────────────────────────────────────┘
```

Public Member Functions

- **RepulsionEnergyOEPotential** (SharedWavefunction wfn, SharedBasisSet auxiliary, Options &options)
- **RepulsionEnergyOEPotential** (SharedWavefunction wfn, Options &options)
- virtual void compute (const std::string &oepType) override

    Compute matrix forms of all OEP's within a specified OEP type.

- virtual void compute_3D (const std::string &oepType, const double &x, const double &y, const double &z, double &v) override

    Compute value of potential in point x, y, z and save at v.

- virtual void **print_header** () const override

Additional Inherited Members

17.50.1 Detailed Description

Generalized One-Electron Potential for Pauli Repulsion Energy.

Contains the following OEP types:

- `Murrell-etal.S1`

- `Otto-Ladik.S2`

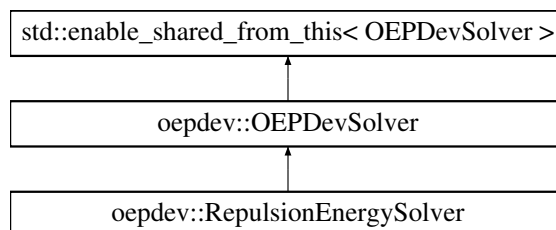The documentation for this class was generated from the following files:

- oepdev/liboep/oep.h
- oepdev/liboep/oep.cc

17.51 oepdev::RepulsionEnergySolver Class Reference

Compute the Pauli-Repulsion interaction energy between unperturbed wavefunctions.

```
#include <solver.h>
```

Inheritance diagram for oepdev::RepulsionEnergySolver:

Public Member Functions

- **RepulsionEnergySolver** (SharedWavefunctionUnion wfn_union)
- virtual double compute_oep_based (const std::string &method="DEFAULT")

    Compute property by using OEP's.
- virtual double compute_benchmark (const std::string &method="DEFAULT")

    Compute property by using benchmark method.

Additional Inherited Members

17.51.1 Detailed Description

Compute the Pauli-Repulsion interaction energy between unperturbed wavefunctions.

The implemented methods are shown below *Note:*

Keyword	Method Description
Benchmark Methods	
HAYES_STONE	∗Default∗. Pauli Repulsion energy at HF level from Hayes and Stone (1984).
DENSITY_BASED	Pauli Repulsion energy at HF level from Mandado and Hermida-Ramon (2012).
MURRELL_ETAL	Approximate Pauli Repulsion energy at HF level from Murrell et al (1967).
OTTO_LADIK	Approximate Pauli Repulsion energy at HF level from Otto and Ladik (1975).
EFP2	Approximate Pauli Repulsion energy at HF level from EFP2 model.
OEP-Based Methods	
MURRELL_ETAL_MIX	∗Default∗. OEP-Murrell et al's: S1 term via DF-OEP, S2 term via ESP-OEP.
MURRELL_ETAL_ESP	OEP-Murrell et al's: S1 and S2 via ESP-OEP

Table 17.3: Methods available in the Solver

- This solver also computes and prints the exchange energy at HF level (formulae are given below) for reference purposes.

- In order to construct this solver, **always** use the `OEPDevSolver::build` static factory method.

Below the detailed description of the implemented equations is given for each of the above provided methods. In the formulae across, it is assumed that the orbitals are real. The Coulomb notation for electron repulsion integrals (ERI's) is adopted; i.e,

$$(ac|bd) = \iint d\mathbf{r}_1 d\mathbf{r}_2 \phi_a(\mathbf{r}_1)\phi_c(\mathbf{r}_1)\frac{1}{r_{12}}\phi_b(\mathbf{r}_2)\phi_d(\mathbf{r}_2)$$

Greek subscripts denote basis set orbitals whereas Italic subscripts denote the occupied molecular orbitals.

Benchmark Methods

Pauli Repulsion energy at HF level by Hayes and Stone (1984).

For a closed-shell system, equation of Hayes and Stone (1984) becomes

$$E^{\text{Rep}} = 2\sum_{kl}\left(V_{kl}^A + V_{kl}^B + T_{kl}\right)\left[[\mathbf{S}^{-1}]_{lk} - \delta_{lk}\right] + \sum_{klmn}(kl|mn)\left\{2[\mathbf{S}^{-1}]_{kl}[\mathbf{S}^{-1}]_{mn} - [\mathbf{S}^{-1}]_{kn}[\mathbf{S}^{-1}]_{lm} - 2\delta_{kl}\delta_{mn} + \delta_{kn}\delta_{lm}\right\}$$

where $\mathbf{S}$ is the overlap matrix between the doubly-occupied orbitals. The exact, pure exchange energy is for a closed shell case given as

$$E^{\text{Ex,pure}} = -2\sum_{a\in A}\sum_{b\in B}(ab|ba)$$

Similarity transformation of molecular orbitals does not affect the resulting energies. The overall exchange-repulsion interaction energy is then (always net repulsive)

$$E^{\text{Ex-Rep}} = E^{\text{Ex,pure}} + E^{\text{Rep}}$$

Repulsion energy of Mandado and Hermida-Ramon (2011)

At the Hartree-Fock level, the exchange-repulsion energy from the density-based scheme of Mandado and Hermida-Ramon (2011) is fully equivalent to the method by Hayes and Stone (1984). However, density-based method enables to compute exchange-repulsion energy at any level of theory. It is derived based on the Pauli deformation density matrix,

$$\Delta\mathbf{D}^{\text{Pauli}} \equiv \mathbf{D}^{oo} - \mathbf{D}$$

where $\mathbf{D}^{oo}$ and $\mathbf{D}$ are the density matrix formed from mutually orthogonal sets of molecular orbitals within the entire aggregate (formed by symmetric orthogonalization of MO's) and the density matrix of the unperturbed system (that can be understood as a Hadamard sum $\mathbf{D} \equiv \mathbf{D}^A \oplus \mathbf{D}^B$).

At HF level, the Pauli deformation density matrix is given by

$$\Delta\mathbf{D}^{\text{Pauli}} = \mathbf{C}\left[\mathbf{S}^{-1} - \mathbf{1}\right]\mathbf{C}^\dagger$$

whereas the density matrix constructed from mutually orthogonal orbitals is

$$\mathbf{D}^{oo} = \mathbf{C}\mathbf{S}^{-1}\mathbf{C}^\dagger$$

In the above equations, $\mathbf{S}$ is the overlap matrix between doubly occupied molecular orbitals of the entire aggregate.

Here, the expressions for the exchange-repulsion energy at any level of theory are shown for the case of open-shell system. The net repulsive energy is given as

$$E^{\text{Ex-Rep}} = E^{\text{Rep},1} + E^{\text{Rep},2} + E^{\text{Ex}}$$

where the one- and two-electron part of the repulsion energy is

$$E^{\text{Rep},1} = E^{\text{Rep,Kin}} + E^{\text{Rep,Nuc}}$$
$$E^{\text{Rep},2} = E^{\text{Rep,el}-\Delta} + E^{\text{Rep},\Delta-\Delta}$$

The kinetic and nuclear contributions are

$$E^{\text{Rep,Kin}} = 2 \sum_{\alpha\beta \in A,B} \Delta D^{\text{Pauli}}_{\alpha\beta} T_{\alpha\beta}$$

$$E^{\text{Rep,Nuc}} = 2 \sum_{\alpha\beta \in A,B} \Delta D^{\text{Pauli}}_{\alpha\beta} \sum_{z \in A,B} V^{(z)}_{\alpha\beta}$$

whereas the electron-deformation and deformation-deformation interaction contributions are

$$E^{\text{Rep,el}-\Delta} = 4 \sum_{\alpha\beta\gamma\delta \in A,B} \Delta D^{\text{Pauli}}_{\alpha\beta} D_{\gamma\delta} (\alpha\beta|\gamma\delta)$$

$$E^{\text{Rep},\Delta-\Delta} = 2 \sum_{\alpha\beta\gamma\delta \in A,B} \Delta D^{\text{Pauli}}_{\alpha\beta} \Delta D^{\text{Pauli}}_{\gamma\delta} (\alpha\beta|\gamma\delta)$$

The associated exchange energy is given by

$$E^{\text{Ex}} = - \sum_{\alpha\beta\gamma\delta \in A,B} \left[D^{oo}_{\alpha\delta} D^{oo}_{\beta\gamma} - D^{A}_{\alpha\delta} D^{A}_{\beta\gamma} - D^{B}_{\alpha\delta} D^{B}_{\beta\gamma} \right] (\alpha\beta|\gamma\delta)$$

It is important to emphasise that, although, at HF level, the particular 'repulsive' and 'exchange' energies computed by using either Hayes and Stone or Mandado and Hermida-Ramon methods are not equal to each other, they sum up to exactly the same exchange-repulsion energy, $E^{\text{Ex}-\text{Rep}}$. Therefore, these methods at HF level are fully equivalent but the nature of partitioning of repulsive and exchange parts is different. It is also noted that the orbital localization does *not* affect the resulting energies, as opposed to the few approximate methods described below (Otto-Ladik and EFP2 methods).

Approximate Pauli Repulsion energy at HF level from Murrell et al.

By expanding the overlap matrix in a Taylor series one can show that the Pauli repulsion energy is approximately given as

$$E^{\text{Rep}} = E^{\text{Rep}}(\mathscr{O}(S)) + E^{\text{Rep}}(\mathscr{O}(S^2))$$

where the first-order term is

$$E^{\text{Rep}}(\mathscr{O}(S)) = -2 \sum_{a \in A} \sum_{b \in B} S_{ab} \left\{ V^{A}_{ab} + \sum_{c \in A} [2(ab|cc) - (ac|bc)] + V^{B}_{ab} + \sum_{d \in B} [2(ab|dd) - (ad|bd)] \right\}$$

whereas the second-order term is

$$E^{\text{Rep}}(\mathscr{O}(S^2)) = 2 \sum_{a \in A} \sum_{b \in B} S_{ab} \left\{ \sum_{c \in A} S_{bc} \left[V^{B}_{ac} + 2 \sum_{d \in B} (ac|dd) \right] + \sum_{d \in B} S_{ad} \left[V^{A}_{bd} + 2 \sum_{x \in A} (bd|cc) \right] - \sum_{c \in A} \sum_{d \in B} S_{cd}(ac|bd) \right\}$$

Thus derived repulsion energy is invariant with respect to transformation of molecular orbitals, similarly as Hayes--Stone's method and density-based method. By using OEP technique, the above theory can be exactly re-cast *without* any further approximations.

Approximate Pauli Repulsion energy at HF level from Otto and Ladik (1975).

The Pauli repulsion energy is approximately given as

$$E^{\text{Rep}} = E^{\text{Rep}}(\mathscr{O}(S)) + E^{\text{Rep}}(\mathscr{O}(S^2))$$

where the first-order term is

$$E^{\text{Rep}}(\mathscr{O}(S)) = -2 \sum_{a \in A} \sum_{b \in B} S_{ab} \left\{ V^{A}_{ab} + 2 \sum_{c \in A} (ab|cc) - (ab|aa) + V^{B}_{ab} + 2 \sum_{d \in B} (ab|dd) - (ab|bb) \right\}$$

whereas the second-order term is

$$E^{\text{Rep}}(\mathscr{O}(S^2)) = 2 \sum_{a \in A} \sum_{b \in B} S^2_{ab} \left\{ V^{B}_{aa} + V^{A}_{bb} + 2 \sum_{c \in A} (cc|bb) + 2 \sum_{d \in B} (aa|dd) - (aa|bb) \right\}$$

Thus derived repulsion energy is *not* invariant with respect to transformation of molecular orbitals, in contrast to Hayes-Stone's method and density-based method. It was shown that good results are obtained when using localized molecular orbitals, whereas using canonical molecular orbitals brings poor results. By using OEP technique, the above theory can be exactly re-cast *without* any further approximations.

Approximate Pauli Repulsion energy at HF level from Jensen and Gordon (1996).

The Pauli repulsion energy used within the EFP2 approach is approximately given as

$$E^{\mathrm{Rep}} = E^{\mathrm{Rep}}(\mathscr{O}(S)) + E^{\mathrm{Rep}}(\mathscr{O}(S^2))$$

where the first-order term is

$$E^{\mathrm{Rep}}(\mathscr{O}(S)) = -2\sum_{a\in A}\sum_{b\in B} S_{ab}\left\{\sum_{c\in A} F_{ac}^A S_{cb} + \sum_{d\in B} F_{bd}^B S_{da} - 2T_{ab}\right\}$$

whereas the second-order term is

$$E^{\mathrm{Rep}}(\mathscr{O}(S^2)) = 2\sum_{a\in A}\sum_{b\in B} S_{ab}^2\left\{\sum_{x\in A}\frac{-Z_x}{R_{xb}} + \sum_{y\in B}\frac{-Z_y}{R_{ya}} + \sum_{c\in A}\frac{2}{R_{bc}} + \sum_{d\in B}\frac{2}{R_{ad}} - \frac{1}{R_{ab}}\right\}$$

Thus derived repulsion energy is *not* invariant with respect to transformation of molecular orbitals, in contrast to Hayes-Stone's method and density-based method. It was shown that good results are obtained when using localized molecular orbitals, whereas using canonical molecular orbitals brings poor results.

In EFP2, exchange energy is approximated by spherical Gaussian approximation (SGO). The result of this is the following formula for the exchange energy:

$$E^{\mathrm{Ex}} \approx -4\sum_{a\in A}\sum_{b\in B}\sqrt{\frac{-2\ln|S_{ab}|}{\pi}}\frac{S_{ab}^2}{R_{ab}}$$

In all the above formulas, R_{ij} are distances between position vectors of *i*th and *j*th point. The LMO centroids are defined by

$$\mathbf{r}_a = (a|\mathbf{r}|a)$$

where *a* denotes the occupied molecular orbital.

OEP-Based Methods

The Murrell et al's theory of Pauli repulsion for S-1 term and the Otto-Ladik's theory for S-2 term is here re-cast by introducing OEP's. The S-1 term is expressed via DF-OEP, whereas the S-2 term via ESP-OEP.

S-1 term (Murrell et al.)

The OEP reduction without any approximations leads to the following formula

$$E^{\mathrm{Rep}}(\mathscr{O}(S^1)) = -2\sum_{a\in A}\sum_{b\in B} S_{ab}\left\{\sum_{\xi\in A} S_{b\xi} G_{\xi a}^A + \sum_{\eta\in B} S_{a\eta} G_{\eta b}^B\right\}$$

where the OEP matrices are given as

$$G_{\xi a}^A = \sum_{\xi'\in A}[\mathbf{S}^{-1}]_{\xi\xi'}\sum_{\alpha\in A}\left\{C_{\alpha a}V_{\alpha\xi'}^A + \sum_{\mu\nu\in A}\left[2C_{\alpha a}D_{\mu\nu} - C_{\nu a}D_{\alpha\mu}\right](\alpha\xi'|\mu\nu)\right\}$$

and analogously for molecule *B*. Here, the nuclear attraction integrals are denoted by $V_{\alpha\xi'}^A$.

S-2 term (Otto-Ladik)

After the OEP reduction, this contribution under Otto-Ladik approximation has the following form:

$$E^{\mathrm{Rep}}(\mathscr{O}(S^2)) = 2\sum_{a\in A}\sum_{b\in B} S_{ab}^2\left\{\sum_{x\in A} q_{xa}V_{bb}^{(x)} + \sum_{y\in B} q_{yb}V_{aa}^{(y)}\right\}$$

where the ESP charges associated with each occupied molecular orbital reproduce the *effective potential* of molecule in question, i.e.,

$$\sum_{x \in A} \frac{q_{xa}}{|\mathbf{r} - \mathbf{r}_x|} \cong v_a^A(\mathbf{r})$$

where the potential is given by

$$v_a^A(\mathbf{r}) = \sum_{x \in A} \frac{-Z_x}{|\mathbf{r} - \mathbf{r}_x|} + 2 \sum_{c \in A} \int \frac{\phi_c(\mathbf{r}')\phi_c(\mathbf{r}')}{|\mathbf{r} - \mathbf{r}'|} \, d\mathbf{r}' - \frac{1}{2} \int \frac{\phi_a(\mathbf{r}')\phi_a(\mathbf{r}')}{|\mathbf{r} - \mathbf{r}'|} \, d\mathbf{r}'$$

17.51.2 Member Function Documentation

17.51.2.1 double RepulsionEnergySolver::compute_benchmark (const std::string & *method* = `"DEFAULT"`) `[virtual]`

Compute property by using benchmark method.

Each solver object has one `DEFAULT` benchmark method

Parameters

method	- benchmark method

Implements [oepdev::OEPDevSolver](#).

17.51.2.2 double RepulsionEnergySolver::compute_oep_based (const std::string & *method* = `"DEFAULT"`) `[virtual]`

Compute property by using OEP's.

Each solver object has one `DEFAULT` OEP-based method.

Parameters

method	- flavour of OEP model

Implements [oepdev::OEPDevSolver](#).

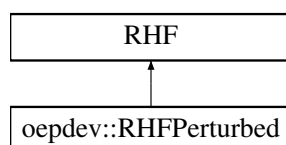The documentation for this class was generated from the following files:

- oepdev/libutil/[solver.h](#)
- oepdev/libutil/solver.cc

17.52 oepdev::RHFPerturbed Class Reference

RHF theory under electrostatic perturbation.

`#include <scf_perturb.h>`

Inheritance diagram for oepdev::RHFPerturbed:

Public Member Functions

- RHFPerturbed (std::shared_ptr< psi::Wavefunction > ref_wfn, std::shared_ptr< psi::SuperFunctional > functional)

    Build from wavefunction and superfunctional.

- RHFPerturbed (std::shared_ptr< psi::Wavefunction > ref_wfn, std::shared_ptr< psi::SuperFunctional > functional, psi::Options &options, std::shared_ptr< psi::PSIO > psio)

    Build from wavefunction and superfunctional + options and psio.

- virtual ∼RHFPerturbed ()

    Clear memory.

- virtual double compute_energy ()

    Compute total energy.

- virtual void set_perturbation (std::shared_ptr< psi::Vector > field)

    Perturb the system with external electric field.

- virtual void set_perturbation (const double &fx, const double &fy, const double &fz)

    This is an overloaded member function, provided for convenience. It differs from the above function only in what argument(s) it accepts.

- virtual void set_perturbation (std::shared_ptr< psi::Vector > position, const double &charge)

    Perturb the system with a point charge.

- virtual void set_perturbation (const double &rx, const double &ry, const double &rz, const double &charge)

    This is an overloaded member function, provided for convenience. It differs from the above function only in what argument(s) it accepts.

- std::shared_ptr< psi::Matrix > Vpert () const

    Get a copy of the perturbation potential one-electron matrix.

- double nuclear_interaction_energy () const

    Get the interaction energy of the nuclei with the perturbing potential.

Protected Member Functions

- virtual void perturb_Hcore ()

    Add the electrostatic perturbation to the Hcore matrix.

Protected Attributes

- std::shared_ptr< psi::Vector > perturbField_

    Perturbing electric field.

- std::shared_ptr< PerturbCharges > perturbCharges_

    Perturbing charges.

- std::shared_ptr< psi::Matrix > Vpert_

    Perturbation potential one-electron matrix.

- double nuclearInteractionEnergy_

    Electrostatic interaction energy due to nuclei.

17.52.1 Detailed Description

RHF theory under electrostatic perturbation.

Compute RHF wavefunction under the following conditions:

- external uniform electric field

- set of point charges The mixed conditions can also be used.

Theory

The electrostatic perturbation is here understood as a distribution of external (generally non-uniform) electric field. It is assumed that this perturbation is one-electron in nature. Therefore, the one-electron Hamiltonian is changed according to the following

$$\mathbf{H}^{\text{core}} \rightarrow \mathbf{H}^{\text{core}} + \sum_n q_n \mathbf{V}^{(n)} - \mathbb{M} \cdot \mathbf{F}$$

where q_n is the external classical point charge, $\mathbf{V}^{(n)}$ is the associated matrix of potential integrals, $\mathbb{M}$ is the vector of dipole integrals and $\mathbf{F}$ is an external uniform electric field. The total energy is then computed by performing an SCF procedure on the above one-electron Hamiltonian. The contribution due to nuclei is included, i.e.,

$$E_{\text{Nuc}} \rightarrow E_{\text{Nuc}-\text{Nuc}} + \sum_{In} \frac{q_n Z_I}{r_{In}} - \mu_{\text{Nuc}} \cdot \mathbf{F}$$

where μ_{Nuc} is the nuclear dipole moment and Z_I is the atomic number of the Ith nucleus. It is added in the nuclear repulsion energy $E_{\text{Nuc}-\text{Nuc}}$ (note that the resulting energy can be negative as well depending on the electric field direction and configuration of point charges.

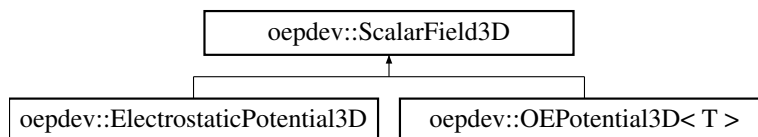The documentation for this class was generated from the following files:

- oepdev/libutil/scf_perturb.h
- oepdev/libutil/scf_perturb.cc

17.53 oepdev::ScalarField3D Class Reference

Scalar field in 3D space. Abstract base.

```
#include <space3d.h>
```

Inheritance diagram for oepdev::ScalarField3D:

Public Member Functions

- ScalarField3D (const int &np, const double &pad, psi::SharedWavefunction wfn, psi::Options &options)
    Construct potential on random grid by providing wavefunction.
- ScalarField3D (const int &nx, const int &ny, const int &nz, const double &px, const double &py, const double &pz, std::shared_ptr< psi::Wavefunction > wfn, psi::Options &options)
    Construct potential on cube grid by providing wavefunction.
- virtual ~ScalarField3D ()
    Destructor.
- virtual int npoints () const
    Get the number of points at which the scalar field is defined.
- virtual std::shared_ptr
    < PointsCollection3D > points_collection () const
    Get the collection of points.
- virtual std::shared_ptr
    < psi::Matrix > data () const
    Get the data matrix in a form { [x, y, z, f(x, y, z)] }.

- virtual std::shared_ptr
  < psi::Wavefunction > wfn () const
    Get the wavefunction.
- virtual bool is_computed () const
    Get the information if data is already computed or not.
- virtual void compute ()
    Compute the scalar field in each point from the point collection.
- virtual double compute_xyz (const double &x, const double &y, const double &z)=0
    Compute a value of scalar field at point (x, y, z)
- virtual void write_cube_file (const std::string &name)
    Write the cube file (only for Cube collections, otherwise does nothing)
- virtual void print () const =0
    Print information of the object to Psi4 output.

Static Public Member Functions

- static shared_ptr< ScalarField3D > build (const std::string &type, const int &np, const double &pad, psi::-
  SharedWavefunction wfn, psi::Options &options)
    Build scalar field of random points.
- static shared_ptr< ScalarField3D > build (const std::string &type, const int &nx, const int &ny, const int &nz,
  const double &px, const double &py, const double &pz, psi::SharedWavefunction wfn, psi::Options &options)
    Build scalar field of points on a g09-cube grid.

Protected Attributes

- std::shared_ptr
  < PointsCollection3D > pointsCollection_
    Collection of points at which the scalar field is to be computed.
- std::shared_ptr< psi::Matrix > data_
    The data matrix in a form { [x, y, z, f(x, y, z)] }.
- std::shared_ptr
  < psi::Wavefunction > wfn_
    Wavefunction.
- psi::Matrix geom_
    Geometry of a molecule.
- std::shared_ptr
  < psi::IntegralFactory > fact_
    Integral factory.
- std::shared_ptr< psi::Matrix > pot_
    Matrix of potential one-electron integrals.
- std::shared_ptr
  < psi::OneBodyAOInt > oneInt_
    One-electron integral shared pointer.
- std::shared_ptr< PotentialInt > potInt_
    One-electron potential shared pointer.
- std::shared_ptr< psi::BasisSet > primary_
    Basis set.
- int nbf_
    Number of basis functions.
- bool isComputed_
    Has data already computed?

17.53.1 Detailed Description

Scalar field in 3D space. Abstract base.

Create scalar field defined at points distributed randomly or as an ordered g09 cube-like collection. Currently implemented scalar fields are:

- Electrostatic potential - computes electrostatic potential (requires wavefunction)

- Template of generic classes - compute custom scalar fields (requires generic object that is able to compute the field in 3D space)

Note: Always create instances by using static factory methods `build`. The following types of scalar field are currently implemented:

- `ELECTROSTATIC POTENTIAL`

17.53.2 Member Function Documentation

17.53.2.1 std::shared_ptr< **ScalarField3D** > oepdev::ScalarField3D::build (const std::string & *type,* const int & *np,* const double & *pad,* psi::SharedWavefunction *wfn,* psi::Options & *options*) `[static]`

Build scalar field of random points.

Parameters

type	- type of scalar field
np	- number of points
pad	- radius padding of a minimal sphere enclosing the molecule
wfn	- Psi4 Wavefunction containing the molecule
options	- Psi4 options

17.53.2.2 std::shared_ptr< **ScalarField3D** > oepdev::ScalarField3D::build (const std::string & *type,* const int & *nx,* const int & *ny,* const int & *nz,* const double & *px,* const double & *py,* const double & *pz,* psi::SharedWavefunction *wfn,* psi::Options & *options*) `[static]`

Build scalar field of points on a g09-cube grid.

Parameters

type	- type of scalar field
nx	- number of points along x direction
ny	- number of points along y direction
nz	- number of points along z direction
px	- padding distance along x direction
py	- padding distance along y direction
pz	- padding distance along z direction
wfn	- Psi4 Wavefunction containing the molecule
options	- Psi4 options

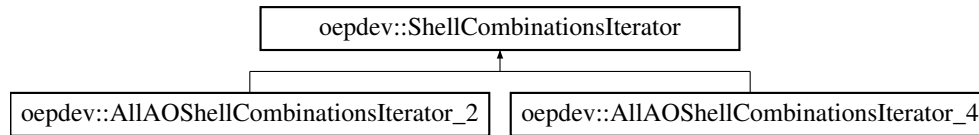The documentation for this class was generated from the following files:

- oepdev/libutil/space3d.h
- oepdev/libutil/space3d.cc

17.54 oepdev::ShellCombinationsIterator Class Reference

Iterator for Shell Combinations. Abstract Base.

```
#include <integrals_iter.h>
```

Inheritance diagram for oepdev::ShellCombinationsIterator:

Public Member Functions

- ShellCombinationsIterator (int nshell)

    Constructor.
- virtual ~ShellCombinationsIterator ()

    Destructor.
- virtual void first (void)=0

    First iteration.
- virtual void next (void)=0

    Next iteration.
- virtual std::shared_ptr
    < psi::BasisSet > bs_1 (void) const

    Grab the basis set of axis 1.
- virtual std::shared_ptr
    < psi::BasisSet > bs_2 (void) const

    Grab the basis set of axis 2.
- virtual std::shared_ptr
    < psi::BasisSet > bs_3 (void) const

    Grab the basis set of axis 3.
- virtual std::shared_ptr
    < psi::BasisSet > bs_4 (void) const

    Grab the basis set of axis 4.
- virtual int P (void) const

    Grab the current shell P index.
- virtual int Q (void) const

    Grab the current shell Q index.
- virtual int R (void) const

    Grab the current shell R index.
- virtual int S (void) const

    Grab the current shell S index.
- virtual bool is_done (void)

    Return status of an iterator.
- virtual const int nshell (void) const

    Return number of shells this iterator is for.
- virtual std::shared_ptr
    < AOIntegralsIterator > ao_iterator (std::string mode="ALL") const

- virtual void compute_shell (std::shared_ptr< oepdev::TwoBodyAOInt > tei) const =0
- virtual void **compute_shell** (std::shared_ptr< psi::TwoBodyAOInt > tei) const =0

Static Public Member Functions

- static std::shared_ptr
  < ShellCombinationsIterator > build (const IntegralFactory &ints, std::string mode="ALL", int nshell=4)

  Build shell iterator from oepdev::IntegralFactory.
- static std::shared_ptr
  < ShellCombinationsIterator > build (std::shared_ptr< IntegralFactory > ints, std::string mode="ALL", int nshell=4)

  This is an overloaded member function, provided for convenience. It differs from the above function only in what argument(s) it accepts.
- static std::shared_ptr
  < ShellCombinationsIterator > build (const psi::IntegralFactory &ints, std::string mode="ALL", int nshell=4)

  Build shell iterator from psi::IntegralFactory.
- static std::shared_ptr
  < ShellCombinationsIterator > build (std::shared_ptr< psi::IntegralFactory > ints, std::string mode="ALL", int nshell=4)

  This is an overloaded member function, provided for convenience. It differs from the above function only in what argument(s) it accepts.

Protected Attributes

- SharedBasisSet bs_1_

  Basis set of axis 1.
- SharedBasisSet bs_2_

  Basis set of axis 2.
- SharedBasisSet bs_3_

  Basis set of axis 3.
- SharedBasisSet bs_4_

  Basis set of axis 4.
- const int nshell_

  Number of shells this iterator is for.
- bool done

  Status of an iterator.

17.54.1 Detailed Description

Iterator for Shell Combinations. Abstract Base.

Date

2018/03/01 17:22:00

17.54.2 Constructor & Destructor Documentation

17.54.2.1 ShellCombinationsIterator::ShellCombinationsIterator (int *nshell*)

Constructor.

Parameters

nshell	- number of shells this iterator is for

17.54.3 Member Function Documentation

17.54.3.1 std::shared_ptr< **AOIntegralsIterator** > ShellCombinationsIterator::ao_iterator (std::string *mode* = "ALL") const [virtual]

Make an AO integral iterator based on current shell

Parameters

mode	- either "ALL" or "UNIQUE" (iterate over all or unique integrals)

Returns

iterator over AO integrals

17.54.3.2 std::shared_ptr< **ShellCombinationsIterator** > ShellCombinationsIterator::build (const **IntegralFactory &** *ints,* std::string *mode* = "ALL"*,* int *nshell* = 4) [static]

Build shell iterator from oepdev::IntegralFactory.

Parameters

ints	- integral factory
mode	- mode of iteration (either ALL or UNIQUE)
nshell	- number of shells to iterate through

Returns

shell iterator

Examples:

example_integrals_iter.cc.

17.54.3.3 std::shared_ptr< **ShellCombinationsIterator** > ShellCombinationsIterator::build (const **psi::IntegralFactory &** *ints,* std::string *mode* = "ALL"*,* int *nshell* = 4) [static]

Build shell iterator from psi::IntegralFactory.

Parameters

ints	- integral factory
mode	- mode of iteration (either ALL or UNIQUE)
nshell	- number of shells to iterate through

Returns

shell iterator

17.54.3.4 void ShellCombinationsIterator::compute_shell (std::shared_ptr< **oepdev::TwoBodyAOInt** > *tei*) const [pure virtual]

Compute integrals in a current shell. Works both for oepdev::TwoBodyAOInt and psi::TwoBodyAOInt

Parameters

tei	- two body integral object

Implemented in oepdev::AllAOShellCombinationsIterator_2, and oepdev::AllAOShellCombinationsIterator_4.

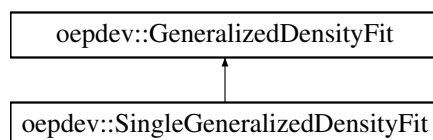The documentation for this class was generated from the following files:

- oepdev/libutil/integrals_iter.h
- oepdev/libutil/integrals_iter.cc

17.55 oepdev::SingleGeneralizedDensityFit Class Reference

Generalized Density Fitting Scheme - Single Fit.

```
#include <oep_gdf.h>
```

Inheritance diagram for oepdev::SingleGeneralizedDensityFit:

Public Member Functions

- **SingleGeneralizedDensityFit** (std::shared_ptr< psi::BasisSet > bs_auxiliary, std::shared_ptr< psi::Matrix > v_vector)
- void compute (void)

   Perform the generalized density fit.

Additional Inherited Members

17.55.1 Detailed Description

Generalized Density Fitting Scheme - Single Fit.

The density fitting map projects the OEP onto the auxiliary, nearly complete basis set space through application of the resolution of identity. Refer to density fitting in complete space for more details.

17.55.2 Determination of the OEP matrix

Coefficients $\mathbf{G}$ are computed by using the following relation

$$\mathbf{G}^{(i)} = \mathbf{v}^{(i)} \cdot \mathbf{S}^{-1}$$

where

$$S_{\xi\eta} = (\xi|\eta)$$
$$v_{\xi}^{(i)} = (\xi|\hat{v}i)$$

In the above, | denotes the single integration over electron coordinate, i.e.,

$$(a|b) \equiv \int d\mathbf{r}\phi_a^*(\mathbf{r})\phi_b(\mathbf{r})$$

whereas the spatial form of the potential operator $\hat{v}$ can be expressed by

$$v(\mathbf{r}) \equiv \int d\mathbf{r}' \frac{\rho(\mathbf{r}')}{|\mathbf{r}' - \mathbf{r}|}$$

with $\rho(\mathbf{r})$ being the effective one-electron density associated with $\hat{v}$.

The documentation for this class was generated from the following files:

- oepdev/liboep/oep_gdf.h
- oepdev/liboep/oep_gdf.cc

17.56 oepdev::GeneralizedPolarGEFactory::StatisticalSet Struct Reference

A structure to handle statistical data.

```
#include <gefp.h>
```

Public Attributes

- std::vector< double > InducedInteractionEnergySet
    Interaction energy set.
- std::vector< std::shared_ptr
  < psi::Matrix > > DensityMatrixSet
    Density matrix set.
- std::vector< std::shared_ptr
  < psi::Vector > > InducedDipoleSet
    Induced dipole moment set.
- std::vector< std::shared_ptr
  < psi::Vector > > InducedQuadrupoleSet
    Induced quadrupole moment set.
- std::vector< std::shared_ptr
  < psi::Matrix > > JKMatrixSet
    Sum of J and K matrix set.

17.56.1 Detailed Description

A structure to handle statistical data.

The documentation for this struct was generated from the following file:

- oepdev/libgefp/gefp.h

17.57 oepdev::test::Test Class Reference

Manages test routines.

```
#include <test.h>
```

Public Member Functions

- Test (std::shared_ptr< psi::Wavefunction > wfn, psi::Options &options)
    Construct the tester.

- ∼Test ()

    Destructor.

- double run (void)

    Pefrorm the test.

Protected Member Functions

- double test_basic (void)

    Test the basic functionalities of OEPDev.

- double test_cphf (void)

    Test the CPHF method.

- double test_dmatPol (void)

    Test the density matrix susceptibility (X = 1)

- double test_dmatPolX (void)

    Test the density matrix susceptibility.

- double test_eri_1_1 (void)

    Test the oepdev::ERI_1_1 class against psi::ERI.

- double test_eri_2_2 (void)

    Test the oepdev::ERI_2_2 class against psi::ERI.

- double test_eri_3_1 (void)

    Test the oepdev::ERI_3_1 class against psi::ERI.

- double test_unitaryOptimizer (void)

    Test the oepdev::UnitaryOptimizer class.

- double test_unitaryOptimizer_4_2 (void)

    Test the oepdev::UnitaryOptimizer_4_2 class.

- double test_scf_perturb (void)

    Test the oepdev::RHFPerturbed class.

Protected Attributes

- std::shared_ptr
  < psi::Wavefunction > wfn_

    Wavefunction object.

- psi::Options & options_

    Psi4 Options.

17.57.1   Detailed Description

Manages test routines.

The documentation for this class was generated from the following files:

- oepdev/libtest/test.h
- oepdev/libtest/test.cc

17.58 oepdev::TwoBodyAOInt Class Reference

Inheritance diagram for oepdev::TwoBodyAOInt:
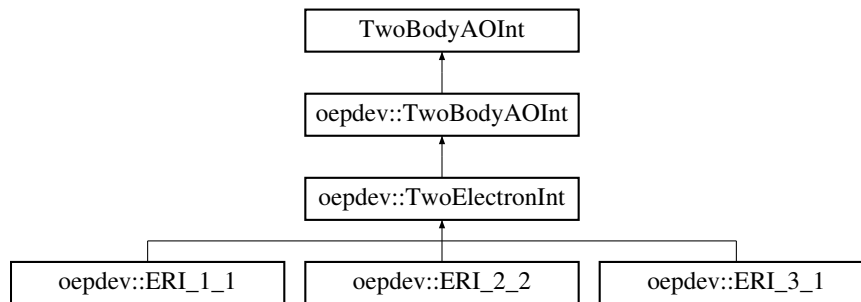
Public Member Functions

- virtual void [compute](#) (std::shared_ptr< psi::Matrix > &result, int ibs1=0, int ibs2=2)

    Compute two-body two-centre integral and put it into matrix.
- virtual void [compute](#) (psi::Matrix &result, int ibs1=0, int ibs2=2)
- virtual size_t **compute_shell** (int, int, int, int)=0
- virtual size_t **compute_shell** (int, int, int)=0
- virtual size_t **compute_shell** (int, int)=0
- virtual size_t **compute_shell_deriv1** (int, int, int, int)=0
- virtual size_t **compute_shell_deriv2** (int, int, int, int)=0
- virtual size_t **compute_shell_deriv1** (int, int, int)=0
- virtual size_t **compute_shell_deriv2** (int, int, int)=0
- virtual size_t **compute_shell_deriv1** (int, int)=0
- virtual size_t **compute_shell_deriv2** (int, int)=0

Protected Member Functions

- **TwoBodyAOInt** (const [IntegralFactory](#) ∗intsfactory, int deriv=0)
- **TwoBodyAOInt** (const [TwoBodyAOInt](#) &rhs)

17.58.1 Member Function Documentation

17.58.1.1 void oepdev::TwoBodyAOInt::compute (std::shared_ptr< psi::Matrix > & *result,* int *ibs1 =* 0, int *ibs2 =* 2) `[virtual]`

Compute two-body two-centre integral and put it into matrix.

Parameters

result	- matrix where to store (i∥j) two-body integrals
ibs1	- first basis set axis
ibs2	- second basis set axis

17.58.1.2 void oepdev::TwoBodyAOInt::compute (psi::Matrix & *result,* int *ibs1 =* 0, int *ibs2 =* 2) `[virtual]`

This is an overloaded member function, provided for convenience. It differs from the above function only in what argument(s) it accepts.

The documentation for this class was generated from the following files:

- oepdev/libpsi/integral.h
- oepdev/libpsi/integral.cc

17.59 oepdev::TwoElectronInt Class Reference

General Two Electron Integral.

```
#include <eri.h>
```

Inheritance diagram for oepdev::TwoElectronInt:
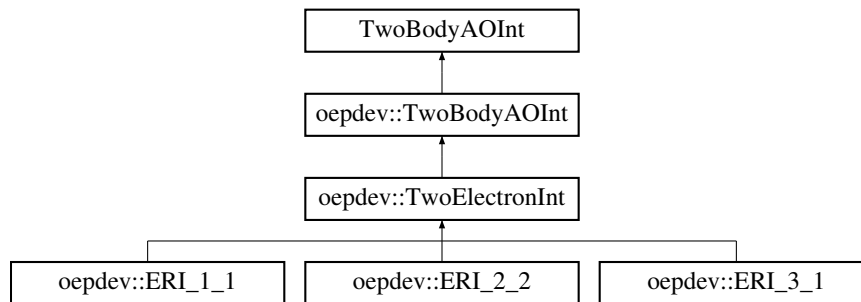
Public Member Functions

- **TwoElectronInt** (const IntegralFactory ∗integral, int deriv, bool use_shell_pairs)
- virtual size_t compute_shell (int, int)

  Compute ERI's between 2 shells. Result is stored in buffer.
- virtual size_t compute_shell (int, int, int)

  Compute ERI's between 3 shells. Result is stored in buffer.
- virtual size_t compute_shell (int, int, int, int)

  Compute ERI's between 4 shells. Result is stored in buffer.
- virtual size_t compute_shell (const psi::AOShellCombinationsIterator &)
- virtual size_t compute_shell_deriv1 (int, int)

  Compute first derivatives of ERI's between 2 shells.
- virtual size_t compute_shell_deriv2 (int, int)

  Compute second derivatives of ERI's between 2 shells.
- virtual size_t compute_shell_deriv1 (int, int, int)

  Compute first derivatives of ERI's between 3 shells.
- virtual size_t compute_shell_deriv2 (int, int, int)

  Compute second derivatives of ERI's between 3 shells.
- virtual size_t compute_shell_deriv1 (int, int, int, int)

  Compute first derivatives of ERI's between 4 shells.
- virtual size_t compute_shell_deriv2 (int, int, int, int)

  Compute second derivatives of ERI's between 4 shells.

Protected Member Functions

- int get_cart_am (int am, int n, int x)

  Get the angular momentum per Cartesian component.
- double get_R (int N, int L, int M)

  Get the (N,L,M)th McMurchie-Davidson coefficient.
- virtual size_t compute_doublet (int, int)

Computes the ERI's between three shells.

- virtual size_t compute_triplet (int, int, int)

    Computes the ERI's between three shells.

- virtual size_t compute_quartet (int, int, int, int)

    Computes the ERI's between four shells.

Protected Attributes

- const int max_am_

    Maximum angular momentum.

- const int n_max_am_

    Maximum number of angular momentum functions.

- psi::Fjt ∗ fjt_

    Computes the fundamental: Boys function value at T for degree v.

- bool use_shell_pairs_

    Should we use shell pair information?

- const double cartMap_ [60]

    Map of Cartesian components per each am.

- const double df_ [8]

    Double factorial array.

- double ∗ mdh_buffer_R_

    Buffer for the McMurchie-Davidson-Hermite R coefficents.

17.59.1 Detailed Description

General Two Electron Integral.

Implements the McMurchie-Davidson recursive scheme for all integral types. The integral can be defined for any number of Gaussian centres, thus it is not limited to 2-by-2 four-centre ERI. Currently implemented subtypes are:

- oepdev::ERI_1_1 - 2-centre electron-repulsion integral (i|j)

- oepdev::ERI_2_2 - 4-centre electron-repulsion integral (ij|kl)

- oepdev::ERI_3_1 - 4-centre electron-repulsion integral (ijk|l)

See Also

    The Integral Package Library

17.59.2 Member Function Documentation

17.59.2.1 size_t oepdev::TwoElectronInt::compute_shell (const psi::AOShellCombinationsIterator & *shellIter*)
    `[virtual]`

Compute ERIs between 4 shells. Result is stored in buffer. Only for use with ERI_2_2 and the same basis sets, otherwise shell pairs won't be compatible.

The documentation for this class was generated from the following files:

- oepdev/libints/eri.h
- oepdev/libints/eri.cc

17.60 oepdev::UniformEFieldPolarGEFactory Class Reference

Polarization GEFP Factory with Least-Squares Parameterization.

```
#include <gefp.h>
```

Inheritance diagram for oepdev::UniformEFieldPolarGEFactory:
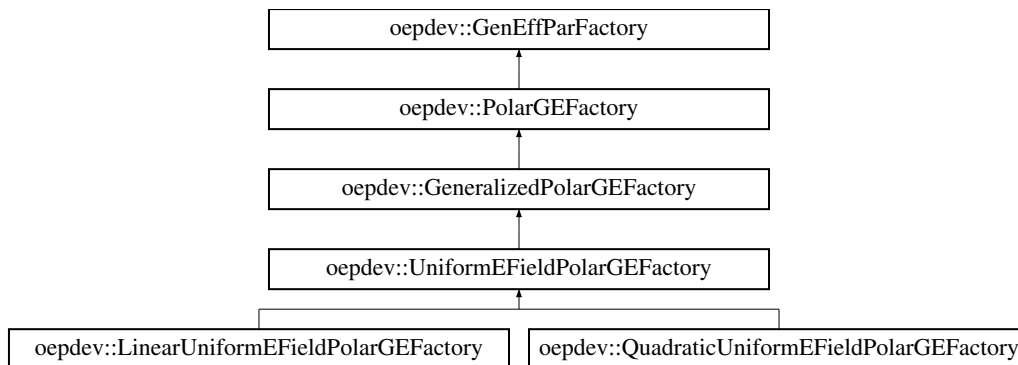
Public Member Functions

- **UniformEFieldPolarGEFactory** (std::shared_ptr< psi::Wavefunction > wfn, psi::Options &opt)
- void compute_samples (void)

  Compute samples of density matrices and select electric field distributions.

- virtual void compute_gradient (int i, int j)=0

  Compute Gradient vector associated with the i-th and j-th basis set function.

- virtual void compute_hessian (void)=0

  Compute Hessian matrix (independent on the parameters)

Additional Inherited Members

17.60.1 Detailed Description

Polarization GEFP Factory with Least-Squares Parameterization.

Implements a class of density matrix susceptibility models for parameterization in the uniform electric field.

The documentation for this class was generated from the following files:

- oepdev/libgefp/gefp.h
- oepdev/libgefp/gefp_polar_uniform_base.cc

17.61 oepdev::UnitaryOptimizer Class Reference

Find the optimim unitary matrix of quadratic matrix equation.

```
#include <unitary_optimizer.h>
```

Public Member Functions

- UnitaryOptimizer (double ∗R, double ∗P, int n, double conv=1.0e-6, int maxiter=100, bool verbose=true)

  Create from R and P matrices and optimization options.

- [UnitaryOptimizer](std::shared_ptr< psi::Matrix > R, std::shared_ptr< psi::Vector > P, double conv=1.0e-6, int maxiter=100, bool verbose=true)

    Create from R and P matrices and optimization options.

- [∼UnitaryOptimizer]()

    Clear memory.

- bool [maximize]()

    Run the minimization.

- bool [minimize]()

    Run the maximization.

- std::shared_ptr< psi::Matrix > [X]()

    Get the unitary matrix (solution)

- double ∗ [get_X]() const

    Get the unitary matrix (pointer to solution)

- double [Z]()

    Get the actual value of Z function.

- bool [success]() const

    Get the status of the optimization.

Protected Member Functions

- [UnitaryOptimizer](int n, double conv, int maxiter, bool verbose)

    Initialize the basic memory.

- void [common_init_]()

    Prepare the optimizer.

- void [run_](const std::string &opt)

    Run the optimization (intermediate interface)

- void [optimize_](const std::string &opt)

    Run the optimization (inner interface)

- void [refresh_]()

    Restore the initial state of the optimizer.

- void [update_conv_]()

    Update the convergence.

- void [update_iter_]()

    Update the iterates.

- void [update_Z_]()

    Update Z value.

- void [update_RP_]()

    Uptade R and P matrices.

- void [update_X_]()

    Update the solution matrix X.

- double [eval_Z_](double ∗[X], double ∗R, double ∗P)

    Evaluate the objective Z function.

- double **eval_Z_** ()
- double [eval_dZ_](double g, double ∗R, double ∗P, int i, int j)

    Evaluate the change in Z.

- double [eval_Z_trial_](int i, int j, double gamma)

    Evaluate the trial Z value.

- void [form_X0_]()

    Create identity matrix.

- void [form_X_](int i, int j, double gamma)

Form unitary matrix X (store in buffer Xnew_)

- void form_next_X_ (const std::string &opt)

  Form the next unitary matrix X.

- ABCD get_ABCD_ (int i, int j)

  Retrieve ABCD parameters for root search.

- void find_roots_boyd_ (const ABCD &abcd)

  Solve for all roots of equation A∗sin(g) + B∗cos(g) + C∗sin(2∗g) + D∗cos(2∗g) = 0 -> implements Boyd's method.

- double find_root_halley_ (double x0, const ABCD &abcd)

  Solve for root of equation A∗sin(g) + B∗cos(g) + C∗sin(2∗g) + D∗cos(2∗g) = 0 -> implements Halley's method.

- double find_gamma_ (const ABCD &abcd, int i, int j, const std::string &opt)

  Compute gamma from roots of base equations.

- bool lt_ (double a, double b)

  less-than function

- bool gt_ (double a, double b)

  greater-than function

- double func_0_ (double g, const ABCD &abcd)

  Function f(gamma) = d(dZ)/dgamma.

- double func_1_ (double g, const ABCD &abcd)

  Gradient of f(gamma)

- double func_2_ (double g, const ABCD &abcd)

  Hessian of f(gamma) - used only for Halley method (not implemented since Boyd method is more suitable here)

- std::shared_ptr< psi::Matrix > psi_X_ ()

  Form the Psi4 matrix with the transformation matrix.

Protected Attributes

- const int n_

  Dimension of the problem.

- const double conv_

  Convergence.

- const int maxiter_

  Maximum number of iterations.

- const bool verbose_

  Verbose mode.

- double ∗ R_

  R matrix.

- double ∗ P_

  P vector.

- double ∗ R0_

  Reference R matrix.

- double ∗ P0_

  Reference P vector.

- double ∗ X_

  X Matrix (accumulated solution)

- double ∗ W_

  Work place.

- double ∗ Xold_

  Temporary X matrix.

- double ∗ Xnew_

  Temporary X matrix.

- int niter_

    Current number of iterations.
- double S_ [4]

    Current solutions.
- double Zinit_

    Initial Z value.
- double Zold_

    Old Z value.
- double Znew_

    New Z value.
- double conv_current_

    Current convergence.
- bool success_

    Status of optimization.

17.61.1 Detailed Description

Find the optimim unitary matrix of quadratic matrix equation.

The objective function of the orthogonal matrix $\mathbf{X}$

$$Z(\mathbf{X}) \equiv \sum_{ijkl} X_{ij} X_{kl} R_{jl} - \sum_{ij} X_{ij} P_j$$

is optimized by using the Jacobi iteration algorithm. In the above equation, $\mathbf{R}$ is a square, general real matrix of size $N \times N$ whereas $\mathbf{P}$ is a real vector of length N.

Algorithm.

Optimization of $\mathbf{X}$ is factorized into a sequence of 2-dimensional rotations with one real parameter γ:

$$\mathbf{X}^{\text{New}} = \mathbf{U}(\gamma) \cdot \mathbf{X}^{\text{Old}}$$

where

$$\mathbf{U}(\gamma) \equiv \begin{pmatrix} \ddots & & & & \\ & \cos(\gamma) & \cdots & \sin(\gamma) & \\ & \vdots & \ddots & \vdots & \\ & -\sin(\gamma) & \cdots & \cos(\gamma) & \\ & & & & \ddots \end{pmatrix}$$

is the Jacobi transformation matrix constructed for the Ith and Jth element from the entire N-dimensional set. For the sake of algirithmic simplicity, every iteration after $\mathbf{U}(\gamma)$ has been formed, $\mathbf{X}^{\text{Old}}$ is for a while assumed to be an identity matrix and the $\mathbf{R}$ matrix and $\mathbf{P}$ vector are transformed according to the following formulae

$$\mathbf{R} \to \mathbf{U}\mathbf{R}\mathbf{U}^T$$
$$\mathbf{P} \to \mathbf{U}\mathbf{P}$$

The full transformation matrix is accumulated in the memory buffer until convergence.

In each iteration, the optimum angle γ is found as follows: First, the roots of the finite Fourier series

$$A\sin(\gamma) + B\cos(\gamma) + C\sin(2\gamma) + D\cos(2\gamma) = 0$$

are found. In the above equations, the expansion coefficients are given as

$$A = P_I + P_J - \sum_{k \neq I,J} (R_{Ik} + R_{Jk} + R_{kI} + R_{kJ})$$

$$B = P_I - P_J - \sum_{k \neq I,J} (R_{Ik} - R_{Jk} + R_{kI} - R_{kJ})$$

$$C = -2(R_{IJ} + R_{JI})$$

$$D = -2(R_{II} - R_{JJ})$$

and I, J are the chosen indices in the Jacobi iteration subspace. The roots are evaluated by applying the Boyd's method[1], in which they are given as

$$\gamma_n = \Re\left[-i\ln(\lambda_n)\right]$$

where λ_n is an eivenvalue of the following 4 by 4 complex matrix:

$$\begin{pmatrix} 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \\ -\frac{D+iC}{D-iC} & -\frac{B+iC}{D-iC} & 0 & -\frac{B-iC}{D-iC} \end{pmatrix}$$

Once the four roots of the Fourier series equation are found, one solution out of four is chosen which satisfies the global optimum condition, i.e., the largest increase/decrease in the objective function given by

$$\delta Z = A(1 - \cos(\gamma)) + B\sin(\gamma) + C\sin^2(\gamma) + \frac{D}{2}\sin(2\gamma)$$

The discrimination between the minimae/maximae is performed based on the evaluation of the Hessian of Z with respect to γ,

$$\frac{\partial^2 Z}{\partial \gamma^2} = A\cos(\gamma) - B\sin(\gamma) + 2C\cos(2\gamma) - 2D\sin(2\gamma)$$

All the $N(N-1)/2$ unique pairs of molecular orbitals are checked and the optimal set of γ, I, J is chosen to construct $\mathbf{X}^{\text{New}}$.

References:

[1] Boyd, J.P.; J. Eng. Math. (2006) 56, pp. 203-219

17.61.2 Constructor & Destructor Documentation

17.61.2.1 oepdev::UnitaryOptimizer::UnitaryOptimizer (double ∗ *R,* double ∗ *P,* int *n,* double *conv =* `1.0e-6`*,* int *maxiter =* `100`*,* bool *verbose =* `true`)

Create from R and P matrices and optimization options.

Parameters

R	- $\mathbf{R}$ matrix
P	- $\mathbf{P}$ vector
n	- dimensionality of the problem (N)
conv	- convergence in the Z function
maxiter	- maximum number of iterations
verbose	- whether print information of iteration process or not Sets up the optimizer.

17.61.2.2 oepdev::UnitaryOptimizer::UnitaryOptimizer (std::shared_ptr< psi::Matrix > *R,* std::shared_ptr< psi::Vector > *P,* double *conv =* `1.0e-6`*,* int *maxiter =* `100`*,* bool *verbose =* `true`)

Create from R and P matrices and optimization options.

Parameters

R	- $\mathbf{R}$ matrix
P	- $\mathbf{P}$ vector
conv	- convergence in the Z function
maxiter	- maximum number of iterations
verbose	- whether print information of iteration process or not Sets up the optimizer.

17.61.2.3 oepdev::UnitaryOptimizer::UnitaryOptimizer (int *n,* double *conv,* int *maxiter,* bool *verbose*) `[protected]`

Initialize the basic memory.

Parameters

n	- dimensionality of the problem (N)
conv	- convergence in the Z function
maxiter	- maximum number of iterations
verbose	- whether print information of iteration process or not Sets up the optimizer.

The documentation for this class was generated from the following files:

- oepdev/libutil/unitary_optimizer.h
- oepdev/libutil/unitary_optimizer.cc

17.62   oepdev::UnitaryOptimizer_4_2 Class Reference

Find the optimim unitary matrix for quartic-quadratic matrix equation with trace.

```
#include <unitary_optimizer.h>
```

Public Member Functions

- UnitaryOptimizer_4_2 (double ∗R, double ∗P, int n, double conv=1.0e-6, int maxiter=100, bool verbose=true)

  Create from R and P matrices and optimization options.

- ∼UnitaryOptimizer_4_2 ()

  Clear memory.

- bool maximize ()

  Run the minimization.

- bool minimize ()

  Run the maximization.

- std::shared_ptr< psi::Matrix > X ()

  Get the unitary matrix (solution)

- double ∗ get_X () const

  Get the unitary matrix (pointer to solution)

- double Z ()

  Get the actual value of Z function.

- bool success () const

  Get the status of the optimization.

Protected Member Functions

- UnitaryOptimizer_4_2 (int n, double conv, int maxiter, bool verbose)

    Initialize the basic memory.
- void common_init_ ()

    Prepare the optimizer.
- void run_ (const std::string &opt)

    Run the optimization (intermediate interface)
- void optimize_ (const std::string &opt)

    Run the optimization (inner interface)
- void refresh_ ()

    Restore the initial state of the optimizer.
- void update_conv_ ()

    Update the convergence.
- void update_iter_ ()

    Update the iterates.
- void update_Z_ ()

    Update Z value.
- void update_RP_ ()

    Uptade R and P matrices.
- void update_X_ ()

    Update the solution matrix X.
- double eval_Z_ (double ∗X, double ∗R, double ∗P)

    Evaluate the objective Z function.
- double **eval_Z_** ()
- double eval_dZ_ (double g, double ∗R, double ∗P, int I, int J)

    Evaluate the change in Z.
- double eval_Z_trial_ (int I, int J, double gamma)

    Evaluate the trial Z value.
- void form_X0_ ()

    Create identity matrix.
- void form_X_ (int I, int J, double gamma)

    Form unitary matrix X (store in buffer Xnew_)
- void form_next_X_ (const std::string &opt)

    Form the next unitary matrix X.
- Fourier9 get_fourier_ (int I, int J)

    Retrieve ABCD parameters for root search.
- void find_roots_boyd_ (const Fourier9 &abcd)

    Solve for all roots of equation A∗sin(g) + B∗cos(g) + C∗sin(2∗g) + D∗cos(2∗g) = 0 -> implements Boyd's method.
- double find_root_halley_ (double x0, const Fourier9 &abcd)

    Solve for root of equation A∗sin(g) + B∗cos(g) + C∗sin(2∗g) + D∗cos(2∗g) = 0 -> implements Halley's method.
- double find_gamma_ (const Fourier9 &abcd, int i, int j, const std::string &opt)

    Compute gamma from roots of base equations.
- bool lt_ (double a, double b)

    less-than function
- bool gt_ (double a, double b)

    greater-than function
- std::shared_ptr< psi::Matrix > psi_X_ ()

    Form the Psi4 matrix with the transformation matrix.

Protected Attributes

- const int n_

    Dimension of the problem.
- const double conv_

    Convergence.
- const int maxiter_

    Maximum number of iterations.
- const bool verbose_

    Verbose mode.
- double ∗ R_

    R tensor.
- double ∗ P_

    P tensor.
- double ∗ R0_

    Reference R tensor.
- double ∗ P0_

    Reference P tensor.
- double ∗ X_

    X Matrix (accumulated solution)
- double ∗ W_

    Work place.
- double ∗ Xold_

    Temporary X matrix.
- double ∗ Xnew_

    Temporary X matrix.
- int niter_

    Current number of iterations.
- double S_ [8]

    Current solutions.
- double Zinit_

    Initial Z value.
- double Zold_

    Old Z value.
- double Znew_

    New Z value.
- double conv_current_

    Current convergence.
- bool success_

    Status of optimization.

17.62.1 Detailed Description

Find the optimim unitary matrix for quartic-quadratic matrix equation with trace.

The objective function of the orthogonal matrix $\mathbf{X}$

$$Z(\mathbf{X}) \equiv \sum_{ijklmn} X_{ki}X_{lj}X_{mi}X_{nj}R_{ijklmn} + \sum_{ijk} X_{ji}X_{ki}P_{ijk}$$

is optimized by using the Jacobi iteration algorithm. In the above equation, $\mathbf{R}$ is a general real sixth-rank tensor of size N^6 whereas $\mathbf{P}$ is a general real third-rank tensor of size N^3.

Algorithm.

Optimization of $\mathbf{X}$ is factorized into a sequence of 2-dimensional rotations with one real parameter γ:

$$\mathbf{X}^{\text{New}} = \mathbf{X}^{\text{Old}} \cdot \mathbf{U}(\gamma)$$

where

$$\mathbf{U}(\gamma) \equiv \begin{pmatrix} \ddots & & & & \\ & \cos(\gamma) & \cdots & \sin(\gamma) & \\ & \vdots & \ddots & \vdots & \\ & -\sin(\gamma) & \cdots & \cos(\gamma) & \\ & & & & \ddots \end{pmatrix}$$

is the Jacobi transformation matrix constructed for the Ith and Jth element from the entire N-dimensional set. For the sake of algirithmic simplicity, every iteration after $\mathbf{U}(\gamma)$ has been formed, $\mathbf{X}^{\text{Old}}$ is for a while assumed to be an identity matrix and the $\mathbf{R}$ as well as $\mathbf{P}$ tensors are transformed according to the following formulae

$$R_{ijklmn} \rightarrow \sum_{k'l'm'n'} R_{ijk'l'm'n'} X_{k'k} X_{l'l} X_{m'm} X_{n'n}$$

$$P_{ijk} \rightarrow \sum_{j'k'} P_{ij'k'} X_{j'j} X_{k'k}$$

The full transformation matrix is accumulated in the memory buffer until convergence.

In each iteration, the optimum angle γ is found as follows: First, the roots of the finite Fourier series

$$a_0 + \sum_{p=1}^{4} \left\{ a_p \cos(px) + b_p \sin(px) \right\} = 0$$

are found. In the above equations, the expansion coefficients are calculated analytically as a function of I, J - the chosen indices in the Jacobi iteration subspace. The roots are evaluated by applying the Boyd's method[1], in which they are given as

$$\gamma_n = \Re\left[-i \ln(\lambda_n) \right]$$

where λ_n is an eivenvalue of the following 8 by 8 complex matrix:

$$\begin{pmatrix} 0 & 1 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 1 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 1 & 0 \\ -\frac{a_4 + ib_4}{a_4 - ib_4} & -\frac{a_3 + ib_3}{a_4 - ib_4} & -\frac{a_2 + ib_2}{a_4 - ib_4} & -\frac{a_1 + ib_1}{a_4 - ib_4} & -\frac{2a_0}{a_4 - ib_4} & -\frac{a_1 - ib_1}{a_4 - ib_4} & -\frac{a_2 - ib_2}{a_4 - ib_4} & -\frac{a_3 - ib_3}{a_4 - ib_4} \end{pmatrix}$$

Once the eight roots of the Fourier series equation are found, one solution out of eight is chosen which satisfies the global optimum condition, i.e., the largest increase/decrease in the objective function given by

$$\delta Z = Z(\mathbf{U}(\gamma)) - Z(\mathbf{1})$$

The Hessian is not computed. All the $N(N-1)/2$ unique pairs of molecular orbitals are checked and the optimal set of γ, I, J is chosen to construct $\mathbf{X}^{\text{New}}$.

References:

[1] Boyd, J.P.; J. Eng. Math. (2006) 56, pp. 203-219

17.62.2 Constructor & Destructor Documentation

17.62.2.1 oepdev::UnitaryOptimizer_4_2::UnitaryOptimizer_4_2 (double ∗ R, double ∗ P, int n, double *conv* = `1.0e-6`**, int *maxiter* =** `100`**, bool *verbose* =** `true` **)**

Create from R and P matrices and optimization options.

Parameters

R	- **R** tensor (flattened row-wise)
P	- **P** tensor (flattened row-wise)
n	- dimensionality of the problem (N)
conv	- convergence in the Z function
maxiter	- maximum number of iterations
verbose	- whether print information of iteration process or not Sets up the optimizer.

17.62.2.2   oepdev::UnitaryOptimizer_4_2::UnitaryOptimizer_4_2 (int *n*, double *conv*, int *maxiter*, bool *verbose*)
```
[protected]
```

Initialize the basic memory.

Parameters

n	- dimensionality of the problem (N)
conv	- convergence in the Z function
maxiter	- maximum number of iterations
verbose	- whether print information of iteration process or not Sets up the optimizer.

The documentation for this class was generated from the following files:

- oepdev/libutil/unitary_optimizer.h
- oepdev/libutil/unitary_optimizer.cc

17.63   oepdev::UnitaryTransformedMOPolarGEFactory Class Reference

Polarization GEFP Factory with Least-Squares Scaling of MO Space.

```
#include <gefp.h>
```

Inheritance diagram for oepdev::UnitaryTransformedMOPolarGEFactory:
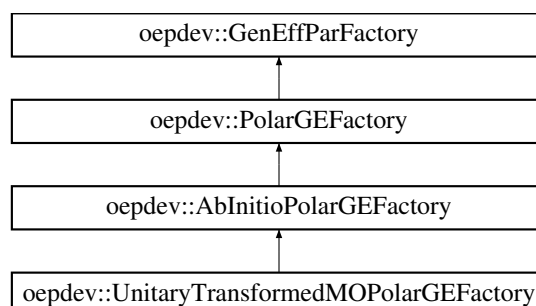
Public Member Functions

- UnitaryTransformedMOPolarGEFactory (std::shared_ptr< psi::Wavefunction > wfn, psi::Options &opt)

    Construct from CPHF object and Psi4 options.
- virtual ~UnitaryTransformedMOPolarGEFactory ()

    Destruct.
- std::shared_ptr< GenEffPar > compute (void)

    Pefrom Least-Squares Fit.

Additional Inherited Members

17.63.1 Detailed Description

Polarization GEFP Factory with Least-Squares Scaling of MO Space.

Implements creation of the density matrix susceptibility tensors for which $\mathbf{X} \neq \mathbf{1}$. Guarantees the idempotency of the density matrix up to first-order in LCAO-MO variation.

Note

> This method does not give better results than the X=1 method and is extremely time and memory consuming. Therefore, it is placed here only for future reference about solving unitary optimization problem in case it occurs.

The documentation for this class was generated from the following files:

- oepdev/libgefp/gefp.h
- oepdev/libgefp/gefp_polar_abinitio.cc

17.64 oepdev::WavefunctionUnion Class Reference

Union of two Wavefunction objects.

```
#include <wavefunction_union.h>
```

Inheritance diagram for oepdev::WavefunctionUnion:
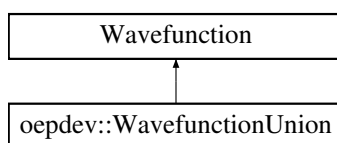
Public Member Functions

- WavefunctionUnion (SharedWavefunction ref_wfn, Options &options)

    Constructor.
- virtual ∼WavefunctionUnion ()

    Destructor.
- virtual double compute_energy ()

    Compute Energy (now blank)
- virtual double nuclear_repulsion_interaction_energy ()

    Compute Nuclear Repulsion Energy between unions.
- void localize_orbitals ()

    Localize Molecular Orbitals.
- void transform_integrals ()

    Transform Integrals (2- and 4-index transformations)
- int l_nmo (int n) const

    Get number of molecular orbitals of the ∗n∗th fragment.
- int l_nso (int n) const

    Get number of symmetry orbitals of the ∗n∗th fragment.
- int l_ndocc (int n) const

    Get number of doubly occupied orbitals of the ∗n∗th fragment.

- int l_nvir (int n) const

    Get number of virtual orbitals of the ∗n∗th fragment.

- int l_nalpha (int n) const

    Get the number of the alpha electrons of the ∗n∗th fragment.

- int l_nbeta (int n) const

    Get the number of the beta electrons of the ∗n∗th fragment.

- int l_nbf (int n) const

    Get number of basis functions of the ∗n∗th fragment.

- int l_noffs_ao (int n) const

    Get the basis set offset of the ∗n∗th fragment.

- double l_energy (int n) const

    Get the reference energy of the ∗n∗th fragment.

- SharedMolecule l_molecule (int n) const

    Get the molecule object of the ∗n∗th fragment.

- SharedBasisSet l_primary (int n) const

    Get the primary basis set object of the ∗n∗th fragment.

- SharedBasisSet l_auxiliary (int n) const

    Get the auxiliary basis set object of the ∗n∗th fragment.

- SharedWavefunction l_wfn (int n) const

    Get the wavefunction object of the ∗n∗th fragment.

- SharedMOSpace l_mospace (int n, const std::string &label) const

    Get the MO space named `label` *(either* `OCC` *or* `VIR`*) of the ∗n∗th fragment.*

- SharedLocalizer l_localizer (int n) const

    Get the orbital localizer object of the ∗n∗th fragment.

- SharedIntegralTransform integrals (void) const

    Get the integral transform object of the entire union.

- bool has_localized_orbitals (void) const

    If union got its molecular orbital localized or not.

- SharedBasisSet primary (void) const

    Get the primary basis set for the entire union.

- SharedMOSpace mospace (const std::string &label) const

    Get the MO space named `label` *(either* `OCC` *or* `VIR`*)*

- SharedMatrix Ca_subset (const std::string &basis="SO", const std::string &subset="ALL")
- SharedMatrix Cb_subset (const std::string &basis="SO", const std::string &subset="ALL")
- SharedMatrix C_subset_helper (SharedMatrix C, const Dimension &noccpi, SharedVector epsilon, const std-::string &basis, const std::string &subset)

    Helpers for Ca_ and Cb_ matrix transformers.

- SharedVector epsilon_subset_helper (SharedVector epsilon, const Dimension &noccpi, const std::string &ba-sis, const std::string &subset)

    Helper for epsilon transformer.

- void print_header (void)

    Print information about this wavefunction union.

- void print_mo_integrals (void)

    Print the MO ingegrals.

Protected Attributes

- int nIsolatedMolecules_

    Number of isolated molecules.
- SharedWavefunction dimer_wavefunction_

    The wavefunction for a dimer (electrons relaxed in the field of monomers)
- SharedIntegralTransform integrals_

    Integral transform object (2- and 4-index transformations)
- bool hasLocalizedOrbitals_

    whether orbitals of the union were localized (or not)
- std::map< const std::string, SharedMOSpace > mospacesUnion_

    Dictionary of MO spaces for the entire union (`OCC` and `VIR`)
- std::vector< SharedMolecule > l_molecule_

    List of molecules.
- std::vector< SharedBasisSet > l_primary_

    List of primary basis functions per molecule.
- std::vector< SharedBasisSet > l_auxiliary_

    List of auxiliary basis functions per molecule.
- std::vector< SharedWavefunction > l_wfn_

    List of original isolated wavefunctions (electrons unrelaxed)
- std::vector< std::string > l_name_

    List of names of isolated wavefunctions.
- std::vector< int > l_nbf_

    List of basis function numbers per molecule.
- std::vector< int > l_nmo_

    List of numbers of molecular orbitals (MO's) per molecule.
- std::vector< int > l_nso_

    List of numbers of SO's per molecule.
- std::vector< int > l_ndocc_

    List of numbers of doubly occupied orbitals per molecule.
- std::vector< int > l_nvir_

    List of numbers of virtual orbitals per molecule.
- std::vector< int > l_noffs_ao_

    List of basis set offsets per molecule.
- std::vector< double > l_energy_

    List of energies of isolated wavefunctions.
- std::vector< double > l_efzc_

    List of frozen-core energies per isolated wavefunction.
- std::vector< bool > l_density_fitted_

    List of information per wfn whether it was obtained using DF or not.
- std::vector< int > l_nalpha_

    List of numbers of alpha electrons per isolated wavefunction.
- std::vector< int > l_nbeta_

    List of numbers of beta electrons per isolated wavefunction.
- std::vector< int > l_nfrzc_

    List of numbers of frozen-core orbitals per isolated molecule.
- std::vector< SharedLocalizer > l_localizer_

    List of orbital localizers.
- std::vector< std::map< const std::string, SharedMOSpace > > l_mospace_

    List of dictionaries of MO spaces.

17.64.1 Detailed Description

Union of two Wavefunction objects.

The WavefunctionUnion is the union of two unperturbed Wavefunctions.

Notes:

1. Works only for C1 symmetry! Therefore `this->nirrep() = 1`.

2. Does not set `reference_wavefunction_`

3. Sets `oeprop_` for the union of uncoupled molecules

4. Performs Hadamard sums on `H_`, `Fa_`, `Da_`, `Ca_` and `S_` based on uncoupled wavefunctions.

5. Since it is based on shallow copy of the original Wavefunction, it **changes** contents of this wavefunction. Reallocate and copy if you want to keep the original wavefunction.

Warnings:

1. Gradients, Hessians and frequencies are not touched, hence they are **wrong**!

2. Lagrangian (if present) is not touched, hence its **wrong**!

3. Ca/Cb and epsilon subsets were reimplemented from psi::Wavefunction to remove sorting of orbitals. However, the corresponding member functions are not virtual in psi::Wavefunction. This could bring problems when upcasting.

The following variables are *shallow* copies of variables inside the Wavefunction object, that is created for the *whole* molecule cluster:

- `basissets_` (DF/RI/F12/etc basis sets)_
- `basisset_` (ORBITAL basis set)
- `sobasisset_` (Primary basis set for SO integrals)
- `AO2SO_` (AO2SO conversion matrix (AO in rows, SO in cols)
- `molecule_` (Molecule that this wavefunction is run on)
- `options_` (Options object)
- `psio_` (PSI file access variables)
- `integral_` (Integral factory)
- `factory_` (Matrix factory for creating standard sized matrices)
- `memory_` (How much memory you have access to)
- `nalpha_`, `nbeta_` (Total alpha and beta electrons)
- `nfrzc_` (Total frozen core orbitals)
- `doccpi_` (Number of doubly occupied per irrep)
- `soccpi_` (Number of singly occupied per irrep)
- `frzcpi_` (Number of frozen core per irrep)
- `frzvpi_` (Number of frozen virtuals per irrep)
- `nalphapi_` (Number of alpha electrons per irrep)
- `nbetapi_` (Number of beta electrons per irrep)

- `nsopi_` (Number of so per irrep)

- `nmopi_` (Number of mo per irrep)

- `nso_` (Total number of SOs)

- `nmo_` (Total number of MOs)

- `nirrep_` (Number of irreps; must be equal to 1 due to symmetry reasons)

- `same_a_b_dens_` and `same_a_b_orbs_` The rest is altered so that the Wavefunction parameters reflect a cluster of non-interacting (uncoupled, isolated, unrelaxed) molecular electron densities.

17.64.2 Constructor & Destructor Documentation

17.64.2.1 oepdev::WavefunctionUnion::WavefunctionUnion (SharedWavefunction *ref_wfn,* Options & *options*)

Constructor.

Provide wavefunction with molecule containing at least 2 fragments.

Parameters

ref_wfn	- reference wavefunction
options	- Psi4 options

17.64.3 Member Function Documentation

17.64.3.1 SharedMatrix oepdev::WavefunctionUnion::Ca_subset (const std::string & *basis =* `"SO"`*,* const std::string & *subset =* `"ALL"`)

Return a subset of the Ca matrix in a desired basis

Parameters

basis	the symmetry basis to use AO, SO
subset	the subset of orbitals to return ALL, ACTIVE, FROZEN, OCC, VIR, FROZEN_OCC, ACTIVE_OCC, ACTIVE_VIR, FROZEN_VIR

Returns

the matrix in Pitzer order in the desired basis

17.64.3.2 SharedMatrix oepdev::WavefunctionUnion::Cb_subset (const std::string & *basis =* `"SO"`*,* const std::string & *subset =* `"ALL"`)

Return a subset of the Cb matrix in a desired basis

Parameters

basis	the symmetry basis to use AO, SO
subset	the subset of orbitals to return ALL, ACTIVE, FROZEN, OCC, VIR, FROZEN_OCC, ACTIVE_OCC, ACTIVE_VIR, FROZEN_VIR

Returns

the matrix in Pitzer order in the desired basis

The documentation for this class was generated from the following files:

- oepdev/libutil/wavefunction_union.h
- oepdev/libutil/wavefunction_union.cc

Chapter 18

File Documentation

18.1   include/oepdev_files.h File Reference

Macros

- #define OEPDEV_USE_PSI4_DIIS_MANAGER 0

    Use DIIS from Psi4 (1) or OEPDev (0)?

- #define OEPDEV_MAX_AM 8

    L_max.

- #define OEPDEV_N_MAX_AM 17

    2L_max+1

- #define OEPDEV_CRIT_ERI 1e-9

    ERI criterion for E12, E34, E123 and lambda∗EXY coefficients.

- #define OEPDEV_SIZE_BUFFER_R 250563

    Size of R buffer (OEPDEV_N_MAX_AM∗OEPDEV_N_MAX_AM∗OEPDEV_N_MAX_AM∗OEPDEV_N_MAX_AM∗3)

- #define OEPDEV_SIZE_BUFFER_D2 3264

    Size of D2 buffer (3∗(OEPDEV_MAX_AM+1)∗(OEPDEV_MAX_AM+1)∗OEPDEV_N_MAX_AM)

18.2 main.cc File Reference

```
#include <cstdlib>
#include <cstdio>
#include <string>
#include "psi4/psi4-dec.h"
#include "psi4/psifiles.h"
#include "psi4/libdpd/dpd.h"
#include "include/oepdev_files.h"
#include "psi4/libparallel/parallel.h"
#include "psi4/liboptions/liboptions.h"
#include "psi4/libpsio/psio.h"
#include "psi4/libpsio/psio.hpp"
#include "psi4/libmints/molecule.h"
#include "psi4/libmints/wavefunction.h"
#include "psi4/libmints/basisset.h"
#include "psi4/libfunctional/superfunctional.h"
#include "oepdev/libutil/util.h"
#include "oepdev/libutil/cphf.h"
#include "oepdev/libutil/wavefunction_union.h"
#include "oepdev/libutil/integrals_iter.h"
#include "oepdev/libutil/space3d.h"
#include "oepdev/libutil/esp.h"
#include "oepdev/libutil/solver.h"
#include "oepdev/liboep/oep.h"
#include "oepdev/libpsi/potential.h"
#include "oepdev/libgefp/gefp.h"
#include "psi4/libtrans/mospace.h"
#include "psi4/libtrans/integraltransform.h"
#include "oepdev/libints/eri.h"
#include "oepdev/libpsi/integral.h"
#include "oepdev/libtest/test.h"
```

Namespaces

- psi

    Psi4 package namespace.

Typedefs

- using **SharedMolecule** = std::shared_ptr< Molecule >
- using **SharedSuperFunctional** = std::shared_ptr< SuperFunctional >
- using **SharedWavefunction** = std::shared_ptr< Wavefunction >
- using **SharedVector** = std::shared_ptr< Vector >
- using **SharedMatrix** = std::shared_ptr< Matrix >
- using **SharedBasisSet** = std::shared_ptr< BasisSet >
- using **SharedUnion** = std::shared_ptr< oepdev::WavefunctionUnion >
- using **SharedPSIO** = std::shared_ptr< PSIO >
- using **SharedCPHF** = std::shared_ptr< oepdev::CPHF >
- using **SharedMOSpace** = std::shared_ptr< MOSpace >
- using **SharedIntegralTransform** = std::shared_ptr< IntegralTransform >
- using **SharedIntegralFactory** = std::shared_ptr< IntegralFactory >
- using **SharedTwoBodyAOInt** = std::shared_ptr< TwoBodyAOInt >
- using **SharedMOSpaceVector** = std::vector< std::shared_ptr< MOSpace >>

- using **intVector** = std::vector< int >
- using **SharedLocalizer** = std::shared_ptr< Localizer >
- using **SharedOEPotential** = std::shared_ptr< oepdev::OEPotential >
- using **SharedField3D** = std::shared_ptr< oepdev::ScalarField3D >
- using **SharedGEFPFactory** = std::shared_ptr< oepdev::GenEffParFactory >
- using **SharedGEFPParameters** = std::shared_ptr< oepdev::GenEffPar >

Functions

- int psi::read_options (std::string name, Options &options)

    Options for the OEPDev plugin.
- SharedWavefunction psi::oepdev (SharedWavefunction ref_wfn, Options &options)

    Main routine of the OEPDev plugin.

18.3   oepdev/libgefp/gefp.h File Reference

```
#include <vector>
#include <string>
#include <random>
#include <cmath>
#include "psi4/libmints/wavefunction.h"
#include "psi4/libmints/matrix.h"
#include "psi4/libmints/vector.h"
#include "psi4/libmints/vector3.h"
#include "../liboep/oep.h"
#include "../libutil/util.h"
#include "../libutil/cphf.h"
#include "../libutil/scf_perturb.h"
```

Classes

- class oepdev::GenEffPar

    Generalized Effective Fragment Parameters. Container Class.
- class oepdev::GenEffFrag

    Generalized Effective Fragment. Container Class.
- class oepdev::GenEffParFactory

    Generalized Effective Fragment Factory. Abstract Base.
- class oepdev::PolarGEFactory

    Polarization GEFP Factory. Abstract Base.
- class oepdev::AbInitioPolarGEFactory

    Polarization GEFP Factory from First Principles. Hartree-Fock Approximation.
- class oepdev::FFAbInitioPolarGEFactory

    Polarization GEFP Factory from First Principles: Finite-Difference Model. Arbitrary level of theory.
- class oepdev::GeneralizedPolarGEFactory

    Polarization GEFP Factory with Least-Squares Parameterization.
- struct oepdev::GeneralizedPolarGEFactory::StatisticalSet

    A structure to handle statistical data.
- class oepdev::UniformEFieldPolarGEFactory

    Polarization GEFP Factory with Least-Squares Parameterization.
- class oepdev::NonUniformEFieldPolarGEFactory

Polarization GEFP Factory with Least-Squares Parameterization.

- class oepdev::LinearUniformEFieldPolarGEFactory

    Polarization GEFP Factory with Least-Squares Parameterization.

- class oepdev::QuadraticUniformEFieldPolarGEFactory

    Polarization GEFP Factory with Least-Squares Parameterization.

- class oepdev::LinearNonUniformEFieldPolarGEFactory

    Polarization GEFP Factory with Least-Squares Parameterization.

- class oepdev::QuadraticNonUniformEFieldPolarGEFactory

    Polarization GEFP Factory with Least-Squares Parameterization.

- class oepdev::LinearGradientNonUniformEFieldPolarGEFactory

    Polarization GEFP Factory with Least-Squares Parameterization.

- class oepdev::QuadraticGradientNonUniformEFieldPolarGEFactory

    Polarization GEFP Factory with Least-Squares Parameterization.

- class oepdev::UnitaryTransformedMOPolarGEFactory

    Polarization GEFP Factory with Least-Squares Scaling of MO Space.

Namespaces

- oepdev

    OEPDev module namespace.

18.4 oepdev/libints/eri.h File Reference

```
#include "psi4/libpsi4util/exception.h"
#include "psi4/libmints/integral.h"
#include "psi4/libmints/basisset.h"
#include "psi4/libmints/fjt.h"
#include "../libpsi/integral.h"
#include "recurr.h"
```

Classes

- class oepdev::TwoElectronInt

    General Two Electron Integral.

- class oepdev::ERI_1_1

    2-centre ERI of the form (a|O(2)|b) where O(2) = 1/r12.

- class oepdev::ERI_2_2

    4-centre ERI of the form (ab|O(2)|cd) where O(2) = 1/r12.

- class oepdev::ERI_3_1

    4-centre ERI of the form (abc|O(2)|d) where O(2) = 1/r12.

Namespaces

- oepdev

    OEPDev module namespace.

18.5 oepdev/libints/recurr.h File Reference

Namespaces

- oepdev

    OEPDev module namespace.

Macros

- #define D1_INDEX(x, i, n) ((81∗(x))+(9∗(i))+(n))

    Get the index of McMurchie-Davidson-Hermite D1 coefficient stored in the `mdh_buffer_`*, that is attributed to the x Cartesian coordinate from angular momentum i of function 1, and the Hermite index n.*

- #define D2_INDEX(x, i, j, n) ((1377∗(x))+(153∗(i))+(17∗(j))+(n))

    Get the index of McMurchie-Davidson-Hermite D2 coefficient stored in the `mdh_buffer_`*, that is attributed to the x Cartesian coordinate from angular momenta i, j of function 1 and 2, and the Hermite index n.*

- #define D3_INDEX(x, i, j, k, n) ((18225∗(x))+(2025∗(i))+(225∗(j))+(25∗(k))+(n))

    Get the index of McMurchie-Davidson-Hermite D3 coefficient stored in the `mdh_buffer_`*, that is attributed to the x Cartesian coordinate from angular momenta i, j and k of function 1, 2 and 3, and the Hermite index n.*

- #define R_INDEX(n, l, m, j) ((14739∗(n))+(867∗(l))+(51∗(m))+(j))

    Get the index of McMurchie-Davidson R coefficient stored in the `mdh_buffer_R_` *from angular momenta n, l and m and the Boys index j.*

Functions

- double oepdev::d_N_n1_n2 (int N, int n1, int n2, double PA, double PB, double aP)

    Compute McMurchie-Davidson-Hermite (MDH) coefficient for binomial expansion.

- void oepdev::make_mdh_D1_coeff (int n1, double aPd, double ∗buffer)

    Compute the McMurchie-Davidson-Hermite coefficients for monomial expansion.

- void oepdev::make_mdh_D2_coeff (int n1, int n2, double aPd, double ∗PA, double ∗PB, double ∗buffer)

    Compute the McMurchie-Davidson-Hermite coefficients for binomial expansion.

- void oepdev::make_mdh_D3_coeff (int n1, int n2, int n3, double aPd, double ∗PA, double ∗PB, double ∗PC, double ∗buffer)

    Compute the McMurchie-Davidson-Hermite coefficients for trinomial expansion.

- void oepdev::make_mdh_D2_coeff_explicit_recursion (int n1, int n2, double aP, double ∗PA, double ∗PB, double ∗buffer)

    Compute the McMurchie-Davidson-Hermite coefficients for binomial expansion by explicit recursion. This function makes the same changes to buffers as oepdev::make_mdh_D2_coeff, but implements it through explicit recursion by calls to oepdev::d_N_n1_n2. Therefore, it is slightly slower. Here for debugging purposes.

- void oepdev::make_mdh_R_coeff (int N, int L, int M, double alpha, double a, double b, double c, double ∗F, double ∗buffer)

    Compute the McMurchie-Davidson R coefficients.

18.6 oepdev/liboep/oep.h File Reference

```
#include <cstdio>
#include <string>
#include <vector>
#include <map>
#include "psi4/libparallel/parallel.h"
#include "psi4/liboptions/liboptions.h"
#include "psi4/libmints/wavefunction.h"
#include "psi4/libmints/basisset.h"
#include "psi4/libmints/matrix.h"
#include "psi4/libmints/vector.h"
#include "psi4/libthce/thce.h"
#include "psi4/libcubeprop/csg.h"
#include "../libutil/space3d.h"
```

Classes

- struct oepdev::OEPType

  Container to handle the type of One-Electron Potentials.

- class oepdev::OEPotential

  Generalized One-Electron Potential: Abstract base.

- class oepdev::ElectrostaticEnergyOEPotential

  Generalized One-Electron Potential for Electrostatic Energy.

- class oepdev::RepulsionEnergyOEPotential

  Generalized One-Electron Potential for Pauli Repulsion Energy.

- class oepdev::ChargeTransferEnergyOEPotential

  Generalized One-Electron Potential for Charge-Transfer Interaction Energy.

- class oepdev::EETCouplingOEPotential

  Generalized One-Electron Potential for EET coupling calculations.

Namespaces

- oepdev

  OEPDev module namespace.

Typedefs

- using **oepdev::SharedWavefunction** = std::shared_ptr< Wavefunction >
- using **oepdev::SharedBasisSet** = std::shared_ptr< BasisSet >
- using **oepdev::SharedTensor** = std::shared_ptr< Tensor >
- using **oepdev::SharedMatrix** = std::shared_ptr< Matrix >
- using **oepdev::SharedVector** = std::shared_ptr< Vector >

18.7 oepdev/liboep/oep_gdf.h File Reference

```
#include <cstdio>
#include <string>
#include "psi4/liboptions/liboptions.h"
#include "psi4/libmints/wavefunction.h"
#include "psi4/libmints/basisset.h"
#include "psi4/libmints/matrix.h"
#include "psi4/libmints/vector.h"
```

Classes

- class oepdev::GeneralizedDensityFit

    Generalized Density Fitting Scheme. Abstract Base.

- class oepdev::SingleGeneralizedDensityFit

    Generalized Density Fitting Scheme - Single Fit.

- class oepdev::DoubleGeneralizedDensityFit

    Generalized Density Fitting Scheme - Double Fit.

Namespaces

- oepdev

    OEPDev module namespace.

18.8 oepdev/libpsi/integral.h File Reference

```
#include "psi4/libmints/integral.h"
#include "psi4/libmints/basisset.h"
#include "psi4/libmints/matrix.h"
```

Classes

- class oepdev::TwoBodyAOInt
- class oepdev::IntegralFactory

    Extended IntegralFactory for computing integrals.

Namespaces

- oepdev

    OEPDev module namespace.

18.9   oepdev/libpsi/potential.h File Reference

```
#include <vector>
#include "psi4/psi4-dec.h"
#include "psi4/libparallel/parallel.h"
#include "psi4/liboptions/liboptions.h"
#include "psi4/libpsio/psio.h"
#include "psi4/libmints/typedefs.h"
#include "psi4/libmints/onebody.h"
#include "psi4/libmints/potential.h"
#include "psi4/libmints/sointegral_onebody.h"
#include "psi4/libmints/osrecur.h"
```

Classes

- class oepdev::PotentialInt

    Computes potential integrals.

Namespaces

- oepdev

    OEPDev module namespace.

18.10   oepdev/libtest/test.h File Reference

```
#include <vector>
#include "psi4/psi4-dec.h"
#include "psi4/libparallel/parallel.h"
#include "psi4/liboptions/liboptions.h"
#include "psi4/libpsio/psio.h"
#include "psi4/libmints/integral.h"
#include "psi4/libmints/wavefunction.h"
#include "psi4/libmints/basisset.h"
#include "psi4/libqt/qt.h"
#include "../libpsi/integral.h"
#include "../libutil/integrals_iter.h"
```

Classes

- class oepdev::test::Test

    Manages test routines.

Namespaces

- oepdev

    OEPDev module namespace.

18.11 oepdev/libutil/diis.h File Reference

```
#include <cstdio>
#include <string>
#include <vector>
#include "psi4/libparallel/parallel.h"
#include "psi4/libciomr/libciomr.h"
#include "psi4/libmints/vector.h"
#include "psi4/libmints/matrix.h"
#include "psi4/libqt/qt.h"
```

Classes

- class oepdev::DIISManager

    DIIS manager.

Namespaces

- oepdev

    OEPDev module namespace.

18.12 oepdev/libutil/esp.h File Reference

```
#include "psi4/libmints/vector.h"
#include "space3d.h"
```

Classes

- class oepdev::ESPSolver

    Charges from Electrostatic Potential (ESP). A solver-type class.

Namespaces

- psi

    Psi4 package namespace.

- oepdev

    OEPDev module namespace.

Typedefs

- using **psi::SharedVetor** = std::shared_ptr< Vector >

- using **oepdev::SharedScalarField3D** = std::shared_ptr< ScalarField3D >

18.13 oepdev/libutil/integrals_iter.h File Reference

```
#include <cstdio>
#include "psi4/libparallel/parallel.h"
#include "psi4/libmints/basisset.h"
#include "psi4/libmints/integral.h"
#include "../libpsi/integral.h"
```

Classes

- class oepdev::ShellCombinationsIterator

  Iterator for Shell Combinations. Abstract Base.
- class oepdev::AOIntegralsIterator

  Iterator for AO Integrals. Abstract Base.
- class oepdev::AllAOShellCombinationsIterator_4

  Loop over all possible ERI shells in a shell quartet.
- class oepdev::AllAOShellCombinationsIterator_2

  Loop over all possible ERI shells in a shell doublet.
- class oepdev::AllAOIntegralsIterator_4

  Loop over all possible ERI within a particular shell quartet.
- class oepdev::AllAOIntegralsIterator_2

  Loop over all possible ERI within a particular shell doublet.

Namespaces

- oepdev

  OEPDev module namespace.

Typedefs

- using **oepdev::SharedIntegralFactory** = std::shared_ptr< IntegralFactory >
- using **oepdev::SharedTwoBodyAOInt** = std::shared_ptr< TwoBodyAOInt >
- using oepdev::SharedShellsIterator = std::shared_ptr< ShellCombinationsIterator >

  Iterator over shells as shared pointer.
- using oepdev::SharedAOIntsIterator = std::shared_ptr< AOIntegralsIterator >

  Iterator over AO integrals as shared pointer.

18.14 oepdev/libutil/scf_perturb.h File Reference

```
#include "psi4/libmints/vector.h"
#include "psi4/libmints/matrix.h"
#include "psi4/libscf_solver/rhf.h"
```

Classes

- struct oepdev::PerturbCharges

  Structure to hold perturbing charges.
- class oepdev::RHFPerturbed

  RHF theory under electrostatic perturbation.

Namespaces

- oepdev

    OEPDev module namespace.

18.15 oepdev/libutil/solver.h File Reference

```
#include <cstdio>
#include <string>
#include <map>
#include "psi4/psi4-dec.h"
#include "psi4/libparallel/parallel.h"
#include "psi4/liboptions/liboptions.h"
#include "psi4/libpsio/psio.h"
#include "psi4/libmints/potential.h"
#include "psi4/libmints/integral.h"
#include "wavefunction_union.h"
#include "integrals_iter.h"
#include "../libpsi/integral.h"
#include "../liboep/oep.h"
```

Classes

- class oepdev::OEPDevSolver

    Solver of properties of molecular aggregates. Abstract base.
- class oepdev::ElectrostaticEnergySolver

    Compute the Coulombic interaction energy between unperturbed wavefunctions.
- class oepdev::RepulsionEnergySolver

    Compute the Pauli-Repulsion interaction energy between unperturbed wavefunctions.
- class oepdev::ChargeTransferEnergySolver

    Compute the Charge-Transfer interaction energy between unperturbed wavefunctions.

Namespaces

- oepdev

    OEPDev module namespace.

Typedefs

- using **oepdev::SharedWavefunctionUnion** = std::shared_ptr< WavefunctionUnion >
- using **oepdev::SharedOEPotential** = std::shared_ptr< OEPotential >

18.16 oepdev/libutil/unitary_optimizer.h File Reference

```
#include <string>
#include <complex>
#include "psi4/libmints/vector.h"
#include "psi4/libmints/matrix.h"
```

Classes

- struct [oepdev::ABCD](#)

    Simple structure to hold the Fourier series expansion coefficients.

- struct [oepdev::Fourier9](#)

    Simple structure to hold the Fourier series expansion coefficients for N=4.

- class [oepdev::UnitaryOptimizer](#)

    Find the optimim unitary matrix of quadratic matrix equation.

- class [oepdev::UnitaryOptimizer_4_2](#)

    Find the optimim unitary matrix for quartic-quadratic matrix equation with trace.

Namespaces

- [oepdev](#)

    OEPDev module namespace.

Macros

- #define **IDX**(i, j, n) ((n)$*$(i)+(j))

- #define **IDX3**(i, j, k) (n2_$*$(i)+n_$*$(j)+(k))

- #define **IDX6**(i, j, k, l, m, n) (n5_$*$(i)+n4_$*$(j)+n3_$*$(k)+n2_$*$(l)+n_$*$(m)+(n))

Functions

- constexpr std::complex$<$ double $>$ **oepdev::operator""_i** (unsigned long long d)

- constexpr std::complex$<$ double $>$ **oepdev::operator""_i** (long double d)

18.17 oepdev/libutil/util.h File Reference

```
#include <cstdio>
#include <string>
#include <cmath>
#include <map>
#include "psi4/psi4-dec.h"
#include "psi4/libparallel/parallel.h"
#include "psi4/liboptions/liboptions.h"
#include "psi4/libpsio/psio.h"
#include "psi4/libciomr/libciomr.h"
#include "psi4/libpsio/psio.hpp"
#include "psi4/libiwl/iwl.h"
#include "psi4/libqt/qt.h"
#include "psi4/libmints/molecule.h"
#include "psi4/libmints/writer.h"
#include "psi4/libmints/writer_file_prefix.h"
#include "psi4/libmints/wavefunction.h"
#include "psi4/libmints/basisset.h"
#include "psi4/libmints/vector.h"
#include "psi4/libmints/matrix.h"
#include "psi4/libmints/oeprop.h"
#include "psi4/libmints/local.h"
#include "psi4/libfunctional/superfunctional.h"
#include "psi4/libtrans/mospace.h"
#include "psi4/libtrans/integraltransform.h"
#include "psi4/libscf_solver/rhf.h"
#include "psi4/libdpd/dpd.h"
```

Namespaces

- oepdev

    OEPDev module namespace.

Typedefs

- using **oepdev::SharedMolecule** = std::shared_ptr< Molecule >
- using **oepdev::SharedSuperFunctional** = std::shared_ptr< SuperFunctional >
- using **oepdev::SharedMOSpace** = std::shared_ptr< MOSpace >
- using **oepdev::SharedMOSpaceVector** = std::vector< std::shared_ptr< MOSpace >>
- using **oepdev::SharedIntegralTransform** = std::shared_ptr< IntegralTransform >
- using **oepdev::SharedLocalizer** = std::shared_ptr< Localizer >

Functions

- void oepdev::preambule (void)

    Print preambule for module OEPDEV.

- template<typename... Args>
    std::string oepdev::string_sprintf (const char ∗format, Args...args)

    Format string output. Example: std::string text = oepdev::string_sprinff("Test %3d, %13.5f", 5, -10.5425);.

- std::shared_ptr< SuperFunctional > oepdev::create_superfunctional (std::string name, Options &options)

    Set up DFT functional.

- std::shared_ptr< Molecule > oepdev::extract_monomer (std::shared_ptr< const Molecule > molecule_-dimer, int id)

    Extract molecule from dimer.

- std::shared_ptr< Wavefunction > oepdev::solve_scf (std::shared_ptr< Molecule > molecule, std::shared_-ptr< BasisSet > primary, std::shared_ptr< SuperFunctional > functional, Options &options, std::shared_-ptr< PSIO > psio)

    Solve RHF-SCF equations for a given molecule in a given basis set.

- double oepdev::average_moment (std::shared_ptr< psi::Vector > moment)

    Compute the scalar magnitude of multipole moment.

18.18 oepdev/libutil/wavefunction_union.h File Reference

```
#include <cstdio>
#include <string>
#include <map>
#include "psi4/psi4-dec.h"
#include "psi4/libparallel/parallel.h"
#include "psi4/liboptions/liboptions.h"
#include "psi4/libpsio/psio.h"
#include "psi4/libciomr/libciomr.h"
#include "psi4/libpsio/psio.hpp"
#include "psi4/libqt/qt.h"
#include "psi4/libmints/molecule.h"
#include "psi4/libmints/writer.h"
#include "psi4/libmints/writer_file_prefix.h"
#include "psi4/libmints/wavefunction.h"
#include "psi4/libmints/basisset.h"
#include "psi4/libmints/vector.h"
#include "psi4/libmints/matrix.h"
#include "psi4/libmints/oeprop.h"
#include "psi4/libmints/local.h"
#include "psi4/libfunctional/superfunctional.h"
#include "psi4/libtrans/mospace.h"
#include "psi4/libtrans/integraltransform.h"
#include "psi4/libscf_solver/rhf.h"
#include "psi4/libdpd/dpd.h"
```

Classes

- class oepdev::WavefunctionUnion

    Union of two Wavefunction objects.

Namespaces

- oepdev

    OEPDev module namespace.

Chapter 19

Example Documentation

19.1 example_cphf.cc

Shows how to use the oepdev::CPHF solver to compute molecular and LMO-distributed polarizabilities at RHF level of theory.

```
void example_cphf(std::shared_ptr<psi::Wavefunction> wfn, psi::Options& opt){

  // build the solver
  std::shared_ptr<oepdev::CPHF> solver = std::make_shared<oepdev::CPHF>(wfn, opt);

  // run the solver to converge CPHF equations
  solver->compute();

  // print the LMO-distributed polarizabilities
  for (int i=0; i<solver->nocc(); i++) {
      solver->polarizability(i)->print();
  }

  // print the molecular polarizability
  solver->polarizability()->print();

  // grab 4th LMO-distributed polarizability and its associated LMO centroid
  psi::SharedMatrix pol_4 = solver->polarizability(3);
  psi::SharedVector rmo_4 = solver->lmo_centroid(3);
};
```

19.2 example_integrals_iter.cc

Iterations over electron repulsion integrals in AO basis. This is an example of how to use

- the oepdev::ShellCombinationsIterator class

- the oepdev::AOIntegralsIterator class.

```
void iterate(std::shared_ptr<oepdev::IntegralFactory> ints)
{
  // Prepare for direct calculation of ERI's (shell by shell)
  std::shared_ptr<psi::TwoBodyAOInt> tei(ints->eri());

  // Grab the buffer where the integrals for a current shell will be placed
  const double* buffer = tei->buffer();

  // Create iterator to go through all shell quartet combinations
  oepdev::SharedShellsIterator shellIter =
      oepdev::ShellCombinationsIterator::build(ints, "ALL", 4);

  // Iterate over shells, and then over all integrals in each shell quartet
  for (shellIter->first(); shellIter->is_done() == false; shellIter->next())
  {
      // Compute all integrals between shells in the current quartet
      shellIter->compute_shell(tei);
```

```
    // Create iterator to go through all integrals within a shell quartet
    oepdev::SharedAOIntsIterator intsIter = shellIter->ao_iterator("ALL");

    for (intsIter->first(); intsIter->is_done() == false; intsIter->next())
    {
        // Grab current (ij|kl) indices here
        int i = intsIter->i();
        int j = intsIter->j();
        int k = intsIter->k();
        int l = intsIter->l();

        // Grab the (ij|kl) integral
        double integral = buffer[intsIter->index()];
    }
  }
}
```

19.3   example_scf_perturb.cc

Perturb HF Hamiltonian with external electrostatic potential. This is an example of how to use the oepdev::RHF-Perturbed class.

```
void scf_perturb(std::shared_ptr<psi::Wavefunction> wfn, psi::Options& opt)
{
   // Set up HF superfunctional
   std::shared_ptr<psi::SuperFunctional> func = oepdev::create_superfunctional
      ("HF", opt);

   // Initialize the perturbed wavefunction
   std::shared_ptr<oepdev::RHFPerturbed> scf = std::make_shared<oepdev::RHFPerturbed>(wfn, func, opt, wfn->
      psio());

   /* Perturb the system with the uniform electric field [Fx, Fy, Fz].
      Then, add two point charges of charge qi placed at [Rxi, Ryi, Rzi].
      Provide all these values in atomic units! */
   const double Fx = 0.04, Fy = 0.05, Fz = -0.09;
   const double Rx1= 0.00, Rx2= 1.30, Rx3= -1.00;
   const double Rx1= 0.10, Rx2=-0.30, Rx3=  3.50;
   const double q1 = 0.30, q2 =-0.09;

   scf->set_perturbation(Fx, Fy, Fz);         /* set it only once, setting it again will overwrite the
      field, not add */
   scf->set_perturbation(Rx1, Ry1, Rz1, q1);
   scf->set_perturbation(Rx2, Ry2, Rz2, q2); /* more charges can be added */

   // Solve perturbed SCF equations
   scf->compute_energy();

   // Grab some data
   double energy = scf->reference_energy();      // Total energy of the system
   std::shared_ptr<psi::Matrix> Da = scf->Da();  // One-particle density matrix

   /* Note that the external field and charges perturb only one-electron Hamiltonian.*/
}
```

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