

oepdev 1.0.0-alpha

Novel methods for Quantum Chemistry of Extended Molecular Aggregates

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# Chapter 1

## Main Page

### oep-dev

Generalized One-Electron Potentials: Development Platform.

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### Overview

Test various models of the intermolecular interaction that is based on the application of the **One-Electron Potentials (OEP's)** technique.

Currently, the interaction between two molecules described by the Hartree-Fock-Roothaan-Hall theory or the configuration interaction with singles theory is considered. In particular, the plugin tests the models of:

1. the Pauli exchange-repulsion interaction energy (Project II )
2. the Induction interaction energy (Project III)
3. the excitation energy transfer couplings (Project I )

against reference solutions (exact or other approximations).

Places to go:

- [https://github.com/globulion/oepdev/blob/master/doc/git/doc\\_oep\\_design.md](https://github.com/globulion/oepdev/blob/master/doc/git/doc_oep_design.md) "OEP Design"
- [https://github.com/globulion/oepdev/blob/master/doc/git/doc\\_implemented\\_models.md](https://github.com/globulion/oepdev/blob/master/doc/git/doc_implemented_models.md) "Implemented Models"
- [https://github.com/globulion/oepdev/blob/master/doc/git/doc\\_programming\\_etiquette.md](https://github.com/globulion/oepdev/blob/master/doc/git/doc_programming_etiquette.md) "Programming Etiquette"
- [Current Issues](#)

### References



## Chapter 2

# Introduction

This page introduces the user to the topic.

Now you can proceed to the [advanced section](#).





## Chapter 3

# OEP Design.

OEP (One-Electron Potential) is associated with certain quantum one-electron operator  $\hat{v}^A$  that defines the ability of molecule  $A$  to interact in a particular way with other molecules.

Technically, OEP can be understood as a **container object** (associated with the molecule in question) that stores the information about the above mentioned quantum operator. Here, it is assumed that similar OEP object is also defined for all other molecules in a molecular aggregate.

In case of interaction between molecules  $A$  and  $B$ , OEP object of molecule  $A$  interacts directly with wavefunction object of the molecule  $B$ . Defining a Solver class that handles such interaction Wavefunction class and OEP class the universal design of OEP-based approaches can be established and developed.

**Important:** OEP and Wavefunction classes should not be restricted to Hartree-Fock; in general any correlated wavefunction and derived OEP's should be allowed to work with each other.

### 3.1 OEP Classes

There are many types of OEP's, but the underlying principle is the same and independent of the type of intermolecular interaction. Therefore, the OEP's should be implemented by using a multi-level class design. In turn, this design depends on the way OEP's enter the mathematical expressions, i.e., on the types of matrix elements of the one-electron effective operator  $\hat{v}^A$ .

#### 3.1.1 Structure of possible OEP-based expressions and their unification

Structure of OEP-based mathematical expressions is listed below:

Type	Matrix Element	Comment
Type 1	$(I \hat{v}^A J)$	$I \in A, J \in B$
Type 2	$(J \hat{v}^A L)$	$J, L \in B$

In the above table,  $I$ ,  $J$  and  $K$  indices correspond to basis functions or molecular orbitals. Basis functions can be primary or auxiliary OEP-specialized density-fitting. Depending on the type of function and matrix element, there are many subtypes of resulting matrix elements that differ in their dimensionality. Examples are given below:

Matrix Element	DF-based form	ESP-based form
$(\mu \hat{v}^{A[\mu]} \sigma)$	$\sum_{I \in A} v_{\mu I}^A S_{I\sigma}$	$\sum_{\alpha \in A} q_{\alpha}^{A[\mu]} V_{\mu\sigma}^{(\alpha)}$
$(i \hat{v}^{A[i]} j)$	$\sum_{I \in A} v_{ii}^A S_{Ij}$	$\sum_{\alpha \in A} q_{\alpha}^{A[i]} V_{ij}^{(\alpha)}$

$\left(j \hat{v}^{A[i]} l\right)$	$\sum_{\mathbf{l}, \mathbf{k} \in A} S_{jl} v_{\mathbf{l}, \mathbf{k}}^{A[i]} S_{\mathbf{k}l}$	$\sum_{\alpha \in A} q_{\alpha}^{A[i]} v_{jl}^{(\alpha)}$
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In the formulae above, the OEP-part (stored by OEP instances) and the Solver-part (to be computed by the Solver) are separated. It is apparent that all OEP-parts have the form of 2nd- or 3rd-rank tensors with different class of axes (molecular orbitals, primary/auxiliary basis, atomic space). Therefore, they can be uniquely defined by a unified *tensor object* (storing double precision numbers) and unified *dimension object* storing the information of the axes classes.

In Psi4, a perfect candidate for the above is `psi4::Tensor` class declared in `psi4/libthce/thce.h`. Except from the numeric content its instances also store the information of the dimensions in a form of a vector of `psi4::Dimension` instances.

Another possibility is to use `psi::Matrix` objects, instead of `psi4::Tensor` objects, possibly putting them into a `std::vector` container in case there is more than two axes.

## Chapter 4

# List of One-Electron Potentials

Here I provide the list of OEP's that have been already derived within the scope of the OEPDev project.

### 4.1 Electrostatic Energy OEP's

For electrostatic energy calculations, OEP is simply the electrostatic potential due to nuclei and electrons.

3D form:

$$v(\mathbf{r}) = \sum_x \frac{Z_x}{|\mathbf{r} - \mathbf{r}_x|} + \sum_{\mu\nu \in A} P_{\nu\mu} \int d\mathbf{r}' \frac{\phi_\mu^*(\mathbf{r}') \phi_\nu(\mathbf{r}')}{|\mathbf{r} - \mathbf{r}'|}$$

Matrix form:

$$v_{ik} = \sum_{x \in A} Z_x V_{ik}^{(x)} + \sum_{\mu\nu \in A} P_{\nu\mu} (\mu\nu | ik)$$

### 4.2 Pauli Repulsion OEP's

The following potentials are derived for the evaluation of the Pauli repulsion energy based on Murrell's expressions.

#### 4.2.1 First-order contribution in overlap matrix expansion.

This contribution is simply the electrostatic potential coming from all nuclei and electron density except\* from electron density from molecular orbital  $i$  that interacts with the generalized overlap density between  $i$  of molecule  $A$  and  $j$  of molecule  $B$ .

3D forms:

$$v(\mathbf{r})_{S^{-1}}^{A[i]} = - \sum_{x \in A} \frac{Z_x}{|\mathbf{r} - \mathbf{r}_x|} + \sum_{\mu\nu \in A} \{D_{\nu\mu} - C_{\mu i}^* C_{\nu i}\} \int d\mathbf{r}' \frac{\phi_\mu^*(\mathbf{r}') \phi_\nu(\mathbf{r}')}{|\mathbf{r} - \mathbf{r}'|}$$

Matrix forms:

$$v_{\xi i}(S^{-1}) = \sum_{\kappa \in A} C_{i\kappa} \left\{ - \sum_{x \in A} V_{\kappa \xi}^{(x)} + \sum_{\mu \nu \in A} \{ D_{\nu \mu} - C_{\mu i}^* C_{\nu i} \} (\mu \nu | \xi \kappa) \right\}$$

#### 4.2.2 Second-order contribution in overlap matrix expansion.

To be added here!

### 4.3 Excitonic Energy Transfer OEP's

The following potentials are derived for the evaluation of the short-range EET couplings based on Fujimoto's TDFI-TI method.

#### 4.3.1 ET contributions.

3D forms:

$$\begin{aligned} v(\mathbf{r})_1^{A[\mu]} &= -C_{\mu L}^* \sum_{x \in A} \frac{Z_x}{|\mathbf{r} - \mathbf{r}_x|} + \sum_{\nu \kappa \in A} \left\{ C_{\mu L}^* D_{\nu \kappa} - \frac{1}{2} C_{\nu L}^* D_{\mu \kappa} \right\} \int d\mathbf{r}' \frac{\phi_{\nu}^*(\mathbf{r}') \phi_{\kappa}(\mathbf{r}')}{|\mathbf{r} - \mathbf{r}'|} \\ v(\mathbf{r})_2^{A[\mu]} &= C_{\kappa H} \sum_{\nu \kappa \in A} \{ 2C_{\nu L}^* C_{\mu H}^* - C_{\nu H}^* C_{\mu L}^* \} \int d\mathbf{r}' \frac{\phi_{\nu}^*(\mathbf{r}') \phi_{\kappa}(\mathbf{r}')}{|\mathbf{r} - \mathbf{r}'|} \\ v(\mathbf{r})_3^{A[\mu]} &= v(\mathbf{r})_1^{A[\mu]} + v(\mathbf{r})_2^{A[\mu]} \end{aligned}$$

Matrix forms:

$$\begin{aligned} v_{\mu \xi}(1) &= -C_{\mu L}^* \sum_{x \in A} V_{\mu \xi}^x + \sum_{\nu \kappa \in A} \left\{ C_{\mu L}^* D_{\nu \kappa} - \frac{1}{2} C_{\nu L}^* D_{\mu \kappa} \right\} (\nu \kappa | \mu \xi) \\ v_{\mu \xi}(2) &= C_{\kappa H} \sum_{\nu \kappa \in A} \{ 2C_{\nu L}^* C_{\mu H}^* - C_{\nu H}^* C_{\mu L}^* \} (\nu \kappa | \mu \xi) \\ v_{\mu \xi}(3) &= v_{\mu \xi}(1) + v_{\mu \xi}(2) \end{aligned}$$

#### 4.3.2 HT contributions.

Do be derived.

#### 4.3.3 CT contributions.

To be derived.

### 4.4 Full HF Interaction OEP's

The following potentials are derived for the evaluation of the full Hartree-Fock interaction energy based on the OEPDev equations.

## Chapter 5

# Density-fitting Specialized for OEP's

To get the ab-initio representation of a OEP, one can use a procedure similar to the typical density fitting or resolution of identity, both of which are nowadays widely used to compute electron-repulsion integrals (ERI's) more efficiently.

### 5.1 Fitting in Complete Space

An arbitrary one-electron potential of molecule  $A$  acting on any state vector associated with molecule  $A$  can be expanded in an *auxiliary space* centered on  $A$  as

$$v|i) = \sum_{\xi\eta} v|\xi) [\mathbf{S}^{-1}]_{\xi\eta} (\eta|i)$$

under the necessary assumption that the auxiliary basis set is *complete*. In a special case when the basis set is orthogonal (e.g., molecular orbitals) the above relation simplifies to

$$v|i) = \sum_{\xi} v|\xi) (\xi|i)$$

It can be easily shown that the above general and exact expansion can be obtained by performing a density fitting in the complete space. We expand the LHS of the first equation on this page in a series of the auxiliary basis functions scaled by the undetermined expansion coefficients:

$$v|i) = \sum_{\xi} G_{i\xi} |\xi)$$

which we shall refer here as to the matrix form of the OEP operator. By constructing the least-squares objective function

$$Z[\{G_{\xi}^{(i)}\}] = \int d\mathbf{r}_1 \left[ v(\mathbf{r}_1) \phi_i(\mathbf{r}_1) - \sum_{\xi} G_{\xi}^{(i)} \varphi_{\xi}(\mathbf{r}_1) \right]^2$$

and requiring that

$$\frac{\partial Z[\{G_{\xi}^{(i)}\}]}{\partial G_{\mu}^{(i)}} = 0 \text{ for all } \mu$$

we find the coefficients  $G_{\xi}^{(i)}$  to be

$$\mathbf{G}^{(i)} = \mathbf{v}^{(i)} \cdot \mathbf{S}^{-1}$$

where

$$\begin{aligned} v_{\eta}^{(i)} &= (\eta|v|i) \\ S_{\eta\xi} &= (\eta|\xi) \end{aligned}$$

or explicitly

$$G_{i\xi} = \sum_{\eta} [\mathbf{S}^{-1}]_{\xi\eta} (\eta|v|i)$$

identical to what we obtained from application of the resolution of identity in space spanned by non-orthogonal complete set of basis vectors.

Since matrix elements of an OEP operator in auxiliary space can be computed in the same way as the matrix elements with any other basis function, one can formally write the following identity

$$(X|v|i) = \sum_{\xi\eta} S_{X\xi} [\mathbf{S}^{-1}]_{\xi\eta} (\eta|v|i)$$

where  $X$  is an arbitrary orbital. When the other orbital does not belong to molecule  $A$  but to the (changing) environment, it is straightforward to compute the resulting matrix element, which is simply given as

$$(j_{\in B}|v^A|i_{\in A}) = \sum_{\xi} S_{j\xi} G_{i\xi}$$

where  $j$  denotes the other (environmental) basis function.

In the above equation, the OEP-part (fragment parameters for molecule  $A$  only) and the Solver-part (subject to be computed by solver on the fly) are separated. This then forms a basis for fragment-based approach to solve Quantum Chemistry problems related to the extended molecular aggregates.

## 5.2 Fitting in Incomplete Space

Density fitting scheme from previous section has practical disadvantage of a nearly-complete basis set being usually very large (spanned by large amount of basis set vectors). Any non-complete basis set won't work in the previous example. Since most of basis sets used in quantum chemistry do not form a complete set, it is beneficial to design a modified scheme in which it is possible to obtain the **effective** matrix elements of the OEP operator in a **incomplete** auxiliary space. This can be achieved by minimizing the following objective function

$$Z[\{G_{\xi}^{(i)}\}] = \iint d\mathbf{r}_1 d\mathbf{r}_2 \frac{\left[ v(\mathbf{r}_1)\phi_i(\mathbf{r}_1) - \sum_{\xi} G_{\xi}^{(i)} \phi_{\xi}(\mathbf{r}_1) \right] \left[ v(\mathbf{r}_2)\phi_i(\mathbf{r}_2) - \sum_{\xi} G_{\xi}^{(i)} \phi_{\xi}(\mathbf{r}_2) \right]}{|\mathbf{r}_1 - \mathbf{r}_2|}$$

Thus requesting that

$$\frac{\partial Z[\{G_{\xi}^{(i)}\}]}{\partial G_{\mu}^{(i)}} = 0 \text{ for all } \mu$$

we find the coefficients  $G_{\xi}^{(i)}$  to be

$$\mathbf{G}^{(i)} = \mathbf{b}^{(i)} \cdot \mathbf{A}^{-1}$$

where

$$b_{\eta}^{(i)} = (\eta||vi)$$

$$A_{\eta\xi} = (\eta||\xi)$$

The symbol  $||$  is to denote the operator  $r_{12}^{-1}$  and double integration over  $\mathbf{r}_1$  and  $\mathbf{r}_2$ . Thus, it is clear that in order to use this generalized density fitting scheme one must to compute two-centre electron repulsion integrals (implemented in [oepdev::ERI\\_1\\_1](#)) as well as four-centre asymmetric electron repulsion integrals of the type  $(\alpha\beta\gamma||\eta)$  (implemented in [oepdev::ERI\\_3\\_1](#)).

## Chapter 6

# Implemented Models

### 6.1 Target Properties

Detailed list of models which is to be implemented in the OEPDev project is given below:

**Table 1.** Models subject to be implemented and analyzed within oep-dev.

Pauli energy	Induction energy	EET Coupling
EFP2-Pauli	EFP2-Induced Dipoles	TrCAMM
Murrel et al.'s theory	Density Susceptibility	OEP-ET/HT
OEP-Murrel et al.'s		TDFI-TI
		FED
Exact (Stone's)	Exact (incl. CT)	Exact (ESD)

### 6.2 Target, Benchmark and Competing Models

The target models introduced in the Project shall be tested against the following benchmarks and compared with the following state-of-the-art models:

**Table 2.** Target models vs benchmarks and competitor models.

Target Model	Benchmarks	Competing Model
OEP-Murrel et al.'s	Murrel et al.'s	EFP2-Pauli
	Exact (Stone's)	
OEP-ET/HT + TrCAMM	Exact (ESD)	TDFI-TI
	FED	FED
	TDFI-TI	
Density Susceptibility	Exact (incl. CT)	EFP2-Induced Dipoles





## Chapter 7

# Contributing to oep-dev

OepDev is a plugin to Psi4.

Therefore it should follow the programming etiquette of Psi4. Also, oep-dev has additional programming tips to make the code more versatile and easy in further development. Here, I emphasise on most important aspects regarding the **programming rules**.

### 7.1 Main routine and libraries

Oep-dev has only *one* source file in the plugin base directory, i.e., `main.cc`. This is the main driver routine that handles the functionality of the whole OEP testing platform: specifies options for Psi4 input file and implements test routines based on the options. Other sources are stored in `MODULE/libNAME*` directories where `NAME` is the name of the library with sources and header files, whereas `MODULE` is the directory of the oep-dev module.

Things to remember:

1. **No other sources in base directory.** It is not permitted to place any new source or other files in the plugin base directory (i.e., where `main.cc` resides).
2. **Sources in library directories.** Any additional source code has to be placed in `oepdev/libNAME*` directory (either existing one or a new one; in the latter case remember to add the new `*.cc` files to `CMakeLists.txt` in the plugin base directory).
3. **Miscellanea in special directories.** If you want to add additional documentation, put it in the `doc` directory. If you want to add graphics, put it in the `images` directory.

### 7.2 Header files in libraries

Header files are handy in obtaining a quick glimpse of the functionality within certain library. Each library directory should contain at least one header file in oep-dev. However, header files can be problematic if not managed properly.

Things to remember:

1. **Header preprocessor variable.** Define the preprocessor variable specifying the existence of include of the particular header file. The format of such is

```
#ifndef MODULE_LIBRARY_HEADER_h
#define MODULE_LIBRARY_HEADER_h
// rest of your code goes here
#endif // MODULE_LIBRARY_HEADER_h
```

Last line is the **end** of the header file. The preprocessor variables represents the directory tree `oepdev/-MODULE/LIBRARY/HEADER.h` structure (where `oepdev` is the base plugin directory). `MODULE` is the

plugin module name (e.g. `oepdev`, the name of the module directory) `LIBRARY` is the name of the library (e.g. `libutil`, should be the same as library directory name) `HEADER` is the name of the header in library directory (e.g. `diis` for `diis.h` header file)

2. **Set module namespace.** To prevent naming clashes with other modules and with `Psi4` it is important to operate in separate namespace (e.g. for a module).

```
namespace MODULE {
// your code goes here
} // EndNameSpace MODULE
```

For instance, all classes and functions in `oepdev` module are implemented within the namespace of the same label. Considering addition of other local namespaces within a module can also be useful in certain cases.

## 7.3 Environmental variables

Defining the set of intrinsic environmental variables can help in code management and conditional compilation. The `oep-dev` environmental variables are defined in `include/oepdev_files.h` file. Remember also about `psi4` environmental variables defined in `psi4/psifiles.h` header. As a rule, the `oep-dev` environmental variable should have the following format:

```
OEPDEV_XXXX
```

where `XXXX` is the descriptive name of variable.

## 7.4 Documenting the code

Code has to be documented (at best at a time it is being created). The place for documentation is always in header files. Additional documentation can be also placed in source files. Leaving a chunk of code for a production run without documentation is unacceptable.

Use Doxygen style for documentation all the time. Remember that it supports markdown which can make the documentation even more clear and easy to understand. Additionally you can create a nice `.rst` documentation file for Sphinx program. If you are coding equations, always include formulae in the documentation!

Things to remember:

1. **Descriptions of classes, structures, global functions, etc.** Each programming object should have a description.
2. **Documentation for function arguments and return object.** Usage of functions and class methods should be explained by providing the description of all arguments (use `\param` and `\return` Doxygen keywords).
3. **One-line description of class member variables.** Any class member variable should be preceded by a one-liner documentation (starting from `///`).
4. **Do not be afraid of long names in the code.** Self-documenting code is a blessing!

## 7.5 Naming conventions

Naming is important because it helps to create more readable and clear self-documented code.

Some loose suggestions:

1. **Do not be afraid of long names in the code, but avoid redundancy.** Examples of good and bad names: good name: `get_density_matrix`; bad name: `get_matrix`. Unless there is only one type of matrix a particular objects can store, `matrix` is not a good name for a getter method. good name: `class Wavefunction`, bad name: `class WFN` good name: `int numberOfErrorVectors`, bad name: `int nvec`, bad name: `the_number_of_error_vectors` good name: `class EFPotential`, probably bad name: `class EffectiveFragmentPotential`. The latter might be understood by some people as a class that inherits from `EffectiveFragment` class. If it is not the case, compromise between abbreviation and long description is OK.
2. **Short names are OK in special situations.** In cases meaning of a particular variable is obvious and it is frequently used in the code locally, it can be named shortly. Examples are: `i` when iterating `no` number of occupied orbitals, `nv` number of virtual orbitals, etc.
3. **Clumped names for variables and dashed names for functions.** Try to distinguish between variable name like `sizeofOEPTypelist` and a method name `get_matrix()` (neither `size_of_OEP_type_list`, nor `getMatrix()`). This is little bit cosmetics, but helps in managing the code when it grows.
4. **Class names start from capital letter.** However, avoid only capital letters in class names, unless it is obvious. Avoid also dashes in class names (they are reserved for global functions and class methods). Examples: good name: `DIISManager`, bad name: `DIIS`. good name: `EETCouplingSolver`, bad name: `EETSolver`, very bad: `EET`.

## 7.6 Use Object-Oriented Programming

Try to organise your creations in objects having special relationships and data structures. Encapsulation helps in producing self-maintaining code and is much easier to use. Use:

- **factory design** for creating objects
- **container design** for designing data structures
- **polymorphism** when dealing with various flavours of one particular feature in the data structure

*Note:* In Psi4, factories are frequently implemented as static methods of the base classes, for example `psi::BasisSet::build` static method. It can be followed when building object factories in oep-dev too.



## Chapter 8

# Advanced Usage

This page is for advanced users.

Make sure you have first read [the introduction](#).



## Chapter 9

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## Chapter 10

# Module Index

### 10.1 Modules

Here is a list of all modules:

The Generalized One-Electron Potentials Library . . . . .	??
The OEPDev solver Library . . . . .	??
The Generalized Effective Fragment Potentials Library . . . . .	??
The Integral Package Library . . . . .	??
The Integral Helper Library . . . . .	??
The Three-Dimensional Scalar Fields Library . . . . .	??
The Multipole Fitting Library . . . . .	??
The Density Functional Theory Library . . . . .	??
The OEPDev Utilities . . . . .	??
The OEPDev Testing Platform Library . . . . .	??



# Chapter 11

## Namespace Index

### 11.1 Namespace List

Here is a list of all documented namespaces with brief descriptions:

<a href="#">oepdev</a>	OEPPDev module namespace . . . . .	??
<a href="#">psi</a>	Psi4 package namespace . . . . .	??



## Chapter 12

# Hierarchical Index

### 12.1 Class Hierarchy

This inheritance list is sorted roughly, but not completely, alphabetically:

oepdev::ABCD . . . . .	??
oepdev::AOIntegralsIterator . . . . .	??
oepdev::AllAOIntegralsIterator_2 . . . . .	??
oepdev::AllAOIntegralsIterator_4 . . . . .	??
oepdev::CPHF . . . . .	??
CubicScalarGrid	
oepdev::CubePointsCollection3D . . . . .	??
oepdev::DIISManager . . . . .	??
enable_shared_from_this	
oepdev::OEPDevSolver . . . . .	??
oepdev::ChargeTransferEnergySolver . . . . .	??
oepdev::ElectrostaticEnergySolver . . . . .	??
oepdev::RepulsionEnergySolver . . . . .	??
oepdev::OEPotential . . . . .	??
oepdev::ChargeTransferEnergyOEPotential . . . . .	??
oepdev::EETCouplingOEPotential . . . . .	??
oepdev::ElectrostaticEnergyOEPotential . . . . .	??
oepdev::RepulsionEnergyOEPotential . . . . .	??
oepdev::PolarGEFactory . . . . .	??
oepdev::FieldScaledPolarGEFactory . . . . .	??
oepdev::MOScaledPolarGEFactory . . . . .	??
oepdev::ESPSolver . . . . .	??
oepdev::Fourier9 . . . . .	??
oepdev::GenEffFrag . . . . .	??
oepdev::GenEffPar . . . . .	??
oepdev::GenEffParFactory . . . . .	??
oepdev::PolarGEFactory . . . . .	??
IntegralFactory	
oepdev::IntegralFactory . . . . .	??
oepdev::OEType . . . . .	??
oepdev::Points3DIterator::Point . . . . .	??
oepdev::Points3DIterator . . . . .	??
oepdev::CubePoints3DIterator . . . . .	??
oepdev::RandomPoints3DIterator . . . . .	??
oepdev::PointsCollection3D . . . . .	??
oepdev::CubePointsCollection3D . . . . .	??
oepdev::RandomPointsCollection3D . . . . .	??

PotentialInt	
oepdev::PotentialInt	??
oepdev::ScalarField3D	??
oepdev::ElectrostaticPotential3D	??
oepdev::OEPotential3D< T >	??
oepdev::ShellCombinationsIterator	??
oepdev::AllAOShellCombinationsIterator_2	??
oepdev::AllAOShellCombinationsIterator_4	??
oepdev::test::Test	??
TwoBodyAOInt	
oepdev::TwoBodyAOInt	??
oepdev::TwoElectronInt	??
oepdev::ERI_1_1	??
oepdev::ERI_2_2	??
oepdev::ERI_3_1	??
oepdev::UnitaryOptimizer	??
oepdev::UnitaryOptimizer_4_2	??
Wavefunction	
oepdev::WavefunctionUnion	??

## Chapter 13

# Class Index

### 13.1 Class List

Here are the classes, structs, unions and interfaces with brief descriptions:

<a href="#">oepdev::ABCD</a>	Simple structure to hold the Fourier series expansion coefficients . . . . .	??
<a href="#">oepdev::AllAOIntegralsIterator_2</a>	Loop over all possible ERI within a particular shell doublet . . . . .	??
<a href="#">oepdev::AllAOIntegralsIterator_4</a>	Loop over all possible ERI within a particular shell quartet . . . . .	??
<a href="#">oepdev::AllAOShellCombinationsIterator_2</a>	Loop over all possible ERI shells in a shell doublet . . . . .	??
<a href="#">oepdev::AllAOShellCombinationsIterator_4</a>	Loop over all possible ERI shells in a shell quartet . . . . .	??
<a href="#">oepdev::AOIntegralsIterator</a>	Iterator for AO Integrals. Abstract Base . . . . .	??
<a href="#">oepdev::ChargeTransferEnergyOEPotential</a>	Generalized One-Electron Potential for Charge-Transfer Interaction Energy . . . . .	??
<a href="#">oepdev::ChargeTransferEnergySolver</a>	Compute the Charge-Transfer interaction energy between unperturbed wavefunctions . . . . .	??
<a href="#">oepdev::CPHF</a>	CPHF solver class . . . . .	??
<a href="#">oepdev::CubePoints3DIterator</a>	Iterator over a collection of points in 3D space. g09 Cube-like order . . . . .	??
<a href="#">oepdev::CubePointsCollection3D</a>	G09 cube-like ordered collection of points in 3D space . . . . .	??
<a href="#">oepdev::DIISManager</a>	DIIS manager . . . . .	??
<a href="#">oepdev::EETCouplingOEPotential</a>	Generalized One-Electron Potential for EET coupling calculations . . . . .	??
<a href="#">oepdev::ElectrostaticEnergyOEPotential</a>	Generalized One-Electron Potential for Electrostatic Energy . . . . .	??
<a href="#">oepdev::ElectrostaticEnergySolver</a>	Compute the Coulombic interaction energy between unperturbed wavefunctions . . . . .	??
<a href="#">oepdev::ElectrostaticPotential3D</a>	Electrostatic potential of a molecule . . . . .	??
<a href="#">oepdev::ERI_1_1</a>	2-centre ERI of the form $(a O(2) b)$ where $O(2) = 1/r_{12}$ . . . . .	??
<a href="#">oepdev::ERI_2_2</a>	4-centre ERI of the form $(ab O(2) cd)$ where $O(2) = 1/r_{12}$ . . . . .	??
<a href="#">oepdev::ERI_3_1</a>	4-centre ERI of the form $(abc O(2) d)$ where $O(2) = 1/r_{12}$ . . . . .	??

<a href="#">oepdev::ESPSolver</a>	Charges from Electrostatic Potential (ESP). A solver-type class . . . . .	??
<a href="#">oepdev::FieldScaledPolarGEFactory</a>	Polarization GEFP Factory with Least-Squares Scaling of Cartesian Degrees of freedom . . .	??
<a href="#">oepdev::Fourier9</a>	Simple structure to hold the Fourier series expansion coefficients for $N=4$ . . . . .	??
<a href="#">oepdev::GenEffFrag</a>	Generalized Effective Fragment. Container Class . . . . .	??
<a href="#">oepdev::GenEffPar</a>	Generalized Effective Fragment Parameters. Container Class . . . . .	??
<a href="#">oepdev::GenEffParFactory</a>	Generalized Effective Fragment Factory. Abstract Base . . . . .	??
<a href="#">oepdev::IntegralFactory</a>	Extended <a href="#">IntegralFactory</a> for computing integrals . . . . .	??
<a href="#">oepdev::MOScaledPolarGEFactory</a>	Polarization GEFP Factory with Least-Squares Scaling of MO Space . . . . .	??
<a href="#">oepdev::OEPDevSolver</a>	Solver of properties of molecular aggregates. Abstract base . . . . .	??
<a href="#">oepdev::OEPotential</a>	Generalized One-Electron Potential: Abstract base . . . . .	??
<a href="#">oepdev::OEPotential3D&lt; T &gt;</a>	Class template for OEP scalar fields . . . . .	??
<a href="#">oepdev::OEType</a>	Container to handle the type of One-Electron Potentials . . . . .	??
<a href="#">oepdev::Points3DIterator::Point</a>	. . . . .	??
<a href="#">oepdev::Points3DIterator</a>	Iterator over a collection of points in 3D space. Abstract base . . . . .	??
<a href="#">oepdev::PointsCollection3D</a>	Collection of points in 3D space. Abstract base . . . . .	??
<a href="#">oepdev::PolarGEFactory</a>	Polarization GEFP Factory . . . . .	??
<a href="#">oepdev::PotentialInt</a>	Computes potential integrals . . . . .	??
<a href="#">oepdev::RandomPoints3DIterator</a>	Iterator over a collection of points in 3D space. Random collection . . . . .	??
<a href="#">oepdev::RandomPointsCollection3D</a>	Collection of random points in 3D space . . . . .	??
<a href="#">oepdev::RepulsionEnergyOEPotential</a>	Generalized One-Electron Potential for Pauli Repulsion Energy . . . . .	??
<a href="#">oepdev::RepulsionEnergySolver</a>	Compute the Pauli-Repulsion interaction energy between unperturbed wavefunctions . . . . .	??
<a href="#">oepdev::ScalarField3D</a>	Scalar field in 3D space. Abstract base . . . . .	??
<a href="#">oepdev::ShellCombinationsIterator</a>	Iterator for Shell Combinations. Abstract Base . . . . .	??
<a href="#">oepdev::test::Test</a>	Manages test routines . . . . .	??
<a href="#">oepdev::TwoBodyAOInt</a>	. . . . .	??
<a href="#">oepdev::TwoElectronInt</a>	General Two Electron Integral . . . . .	??
<a href="#">oepdev::UnitaryOptimizer</a>	Find the optimum unitary matrix of quadratic matrix equation . . . . .	??
<a href="#">oepdev::UnitaryOptimizer_4_2</a>	Find the optimum unitary matrix for quartic-quadratic matrix equation with trace . . . . .	??
<a href="#">oepdev::WavefunctionUnion</a>	Union of two Wavefunction objects . . . . .	??



## Chapter 14

# File Index

### 14.1 File List

Here is a list of all documented files with brief descriptions:

<a href="#">main.cc</a>	??
include/ <a href="#">oepdev_files.h</a>	??
include/doxygen/ <b>oepdev_manual.h</b>	??
include/doxygen/ <b>oepdev_modules.h</b>	??
include/doxygen/ <b>oepdev_namespaces.h</b>	??
oepdev/libgefp/ <a href="#">gefp.h</a>	??
oepdev/libints/ <a href="#">eri.h</a>	??
oepdev/libints/ <a href="#">recurr.h</a>	??
oepdev/liboep/ <a href="#">oep.h</a>	??
oepdev/libpsi/ <a href="#">integral.h</a>	??
oepdev/libpsi/ <a href="#">potential.h</a>	??
oepdev/libtest/ <a href="#">test.h</a>	??
oepdev/libutil/ <b>cp hf.h</b>	??
oepdev/libutil/ <a href="#">diis.h</a>	??
oepdev/libutil/ <a href="#">esp.h</a>	??
oepdev/libutil/ <a href="#">integrals_iter.h</a>	??
oepdev/libutil/ <a href="#">solver.h</a>	??
oepdev/libutil/ <b>space3d.h</b>	??
oepdev/libutil/ <a href="#">unitary_optimizer.h</a>	??
oepdev/libutil/ <a href="#">util.h</a>	??
oepdev/libutil/ <a href="#">wavefunction_union.h</a>	??



# Chapter 15

## Module Documentation

### 15.1 The Generalized One-Electron Potentials Library

Implements the goal of this project: The Generalized One-Electron Potentials (OEP's). You will find here OEP's for computation of Pauli repulsion energy, charge-transfer energy and others.

#### Classes

- struct [oepdev::OEPTType](#)  
*Container to handle the type of One-Electron Potentials.*
- class [oepdev::OEPotential](#)  
*Generalized One-Electron Potential: Abstract base.*
- class [oepdev::ElectrostaticEnergyOEPotential](#)  
*Generalized One-Electron Potential for Electrostatic Energy.*
- class [oepdev::RepulsionEnergyOEPotential](#)  
*Generalized One-Electron Potential for Pauli Repulsion Energy.*
- class [oepdev::ChargeTransferEnergyOEPotential](#)  
*Generalized One-Electron Potential for Charge-Transfer Interaction Energy.*
- class [oepdev::EETCouplingOEPotential](#)  
*Generalized One-Electron Potential for EET coupling calculations.*

#### 15.1.1 Detailed Description

Implements the goal of this project: The Generalized One-Electron Potentials (OEP's). You will find here OEP's for computation of Pauli repulsion energy, charge-transfer energy and others.

## 15.2 The OEPDev solver Library

Implementations of various solvers for molecular properties as a functions of unperturbed monomeric wavefunctions. This is the place all target OEP-based models are implemented and compared with benchmark models.

### Classes

- class [oepdev::OEPDevSolver](#)  
*Solver of properties of molecular aggregates. Abstract base.*
- class [oepdev::ElectrostaticEnergySolver](#)  
*Compute the Coulombic interaction energy between unperturbed wavefunctions.*
- class [oepdev::RepulsionEnergySolver](#)  
*Compute the Pauli-Repulsion interaction energy between unperturbed wavefunctions.*
- class [oepdev::ChargeTransferEnergySolver](#)  
*Compute the Charge-Transfer interaction energy between unperturbed wavefunctions.*

### 15.2.1 Detailed Description

Implementations of various solvers for molecular properties as a functions of unperturbed monomeric wavefunctions. This is the place all target OEP-based models are implemented and compared with benchmark models.

## 15.3 The Generalized Effective Fragment Potentials Library

Implements the GEFP method, the far goal of the OEPDev project. Here you will find the containers for GEFP parameters, the density matrix susceptibility tensors and GEFP solvers.

### Classes

- class [oepdev::GenEffPar](#)  
*Generalized Effective Fragment Parameters. Container Class.*
- class [oepdev::GenEffFrag](#)  
*Generalized Effective Fragment. Container Class.*
- class [oepdev::GenEffParFactory](#)  
*Generalized Effective Fragment Factory. Abstract Base.*
- class [oepdev::PolarGEFactory](#)  
*Polarization GEFP Factory.*
- class [oepdev::MOScaledPolarGEFactory](#)  
*Polarization GEFP Factory with Least-Squares Scaling of MO Space.*
- class [oepdev::FieldScaledPolarGEFactory](#)  
*Polarization GEFP Factory with Least-Squares Scaling of Cartesian Degrees of freedom.*

### 15.3.1 Detailed Description

Implements the GEFP method, the far goal of the OEPDev project. Here you will find the containers for GEFP parameters, the density matrix susceptibility tensors and GEFP solvers.

## 15.4 The Integral Package Library

Implementations of various one- and two-body integrals via McMurchie-Davidson recurrence scheme.

### Classes

- class `oepdev::TwoElectronInt`  
*General Two Electron Integral.*
- class `oepdev::ERI_1_1`  
*2-centre ERI of the form  $(a|O(2)|b)$  where  $O(2) = 1/r^{12}$ .*
- class `oepdev::ERI_2_2`  
*4-centre ERI of the form  $(ab|O(2)|cd)$  where  $O(2) = 1/r^{12}$ .*
- class `oepdev::ERI_3_1`  
*4-centre ERI of the form  $(abc|O(2)|d)$  where  $O(2) = 1/r^{12}$ .*
- class `oepdev::TwoBodyAOInt`
- class `oepdev::IntegralFactory`  
*Extended `IntegralFactory` for computing integrals.*
- class `oepdev::PotentialInt`  
*Computes potential integrals.*

### Macros

- `#define D1_INDEX(x, i, n) ((81*(x))+(9*(i))+(n))`  
*Get the index of McMurchie-Davidson-Hermite D1 coefficient stored in the `mdh_buffer_`, that is attributed to the x Cartesian coordinate from angular momentum i of function 1, and the Hermite index n.*
- `#define D2_INDEX(x, i, j, n) ((1377*(x))+(153*(i))+(17*(j))+(n))`  
*Get the index of McMurchie-Davidson-Hermite D2 coefficient stored in the `mdh_buffer_`, that is attributed to the x Cartesian coordinate from angular momenta i, j of function 1 and 2, and the Hermite index n.*
- `#define D3_INDEX(x, i, j, k, n) ((18225*(x))+(2025*(i))+(225*(j))+(25*(k))+(n))`  
*Get the index of McMurchie-Davidson-Hermite D3 coefficient stored in the `mdh_buffer_`, that is attributed to the x Cartesian coordinate from angular momenta i, j and k of function 1, 2 and 3, and the Hermite index n.*
- `#define R_INDEX(n, l, m, j) ((14739*(n))+(867*(l))+(51*(m))+(j))`  
*Get the index of McMurchie-Davidson R coefficient stored in the `mdh_buffer_R_` from angular momenta n, l and m and the Boys index j.*

### Functions

- double `oepdev::d_N_n1_n2` (int N, int n1, int n2, double PA, double PB, double aP)  
*Compute McMurchie-Davidson-Hermite (MDH) coefficient for binomial expansion.*
- void `oepdev::make_mdh_D1_coeff` (int n1, double aPd, double \*buffer)  
*Compute the McMurchie-Davidson-Hermite coefficients for monomial expansion.*
- void `oepdev::make_mdh_D2_coeff` (int n1, int n2, double aPd, double \*PA, double \*PB, double \*buffer)  
*Compute the McMurchie-Davidson-Hermite coefficients for binomial expansion.*
- void `oepdev::make_mdh_D3_coeff` (int n1, int n2, int n3, double aPd, double \*PA, double \*PB, double \*PC, double \*buffer)  
*Compute the McMurchie-Davidson-Hermite coefficients for trinomial expansion.*
- void `oepdev::make_mdh_D2_coeff_explicit_recursion` (int n1, int n2, double aP, double \*PA, double \*PB, double \*buffer)  
*Compute the McMurchie-Davidson-Hermite coefficients for binomial expansion by explicit recursion. This function makes the same changes to buffers as `oepdev::make_mdh_D2_coeff`, but implements it through explicit recursion by calls to `oepdev::d_N_n1_n2`. Therefore, it is slightly slower. Here for debugging purposes.*
- void `oepdev::make_mdh_R_coeff` (int N, int L, int M, double alpha, double a, double b, double c, double \*F, double \*buffer)  
*Compute the McMurchie-Davidson R coefficients.*

### 15.4.1 Detailed Description

Implementations of various one- and two-body integrals via McMurchie-Davidson recurrence scheme. Here, we define the primitive Gaussian type functions (GTO's)

$$\begin{aligned}\phi_i(\mathbf{r}) &\equiv x_A^{n_1} y_A^{l_1} z_A^{m_1} e^{-\alpha_1 r_A^2} \\ \phi_j(\mathbf{r}) &\equiv x_B^{n_2} y_B^{l_2} z_B^{m_2} e^{-\alpha_2 r_B^2} \\ \phi_k(\mathbf{r}) &\equiv x_C^{n_3} y_C^{l_3} z_C^{m_3} e^{-\alpha_3 r_C^2}\end{aligned}$$

in which  $\mathbf{r}_A \equiv \mathbf{r} - \mathbf{A}$  and so on.  $\mathbf{A}$  is the centre of the GTO,  $\alpha_1$  its exponent, whereas  $n_1, l_1, m_1$  the Cartesian angular momenta, with the total angular momentum  $\theta_1 = n_1 + l_1 + m_1$ .

In OEPDev implementations, the following definition shall be in use:

$$\begin{aligned}\mathbf{P} &\equiv \frac{\alpha_1 \mathbf{A} + \alpha_2 \mathbf{B}}{\alpha_1 + \alpha_2} \\ \mathbf{Q} &\equiv \frac{\alpha_3 \mathbf{C} + \alpha_4 \mathbf{D}}{\alpha_3 + \alpha_4} \\ \mathbf{R} &\equiv \frac{\alpha_1 \mathbf{A} + \alpha_2 \mathbf{B} + \alpha_3 \mathbf{C}}{\alpha_1 + \alpha_2 + \alpha_3} \\ \alpha_P &\equiv \alpha_1 + \alpha_2 \\ \alpha_Q &\equiv \alpha_3 + \alpha_4 \\ \alpha_R &\equiv \alpha_1 + \alpha_2 + \alpha_3\end{aligned}$$

The unnormalized products of primitive GTO's are denoted here as

$$\begin{aligned}[ij] &\equiv \phi_i(\mathbf{r}) \phi_j(\mathbf{r}) \\ [ijk] &\equiv \phi_i(\mathbf{r}) \phi_j(\mathbf{r}) \phi_k(\mathbf{r})\end{aligned}$$

### 15.4.2 Hermite Operators

It is convenient to define

$$\Lambda_j(x_P; \alpha_P) \equiv \left( \frac{\partial}{\partial P_x} \right)^j = \alpha_P^{j/2} H_j(\sqrt{\alpha_P} x_P)$$

where  $H_j(x)$  is the Hermite polynomial of order  $j$  evaluated at  $x$ . Introduction of the above Hermite operator can be used by invoking the recurrence relationship due to Hermite polynomial properties:

$$x_A \Lambda_j(x_P; \alpha_P) = j \Lambda_{j-1} + |\mathbf{P} - \mathbf{A}|_x \Lambda_j + \frac{1}{2\alpha_P} \Lambda_{j+1}$$

This can be directly used to derive very useful McMurchie-Davidson-Hermite coefficients as expansion coefficients of the polynomial expansions.

#### 15.4.2.1 Polynomial Expansions as Hermite Series

By using the previous relation, it is possible to express the following expansions in Hermite series:

$$\begin{aligned}x_A^{n_1} &= \sum_{N=0}^{n_1} d_N^{n_1} \Lambda_N(x_A; \alpha_A) \\ x_A^{n_1} x_B^{n_2} &= \sum_{N=0}^{n_1+n_2} d_N^{n_1 n_2} \Lambda_N(x_P; \alpha_P) \\ x_A^{n_1} x_B^{n_2} x_C^{n_3} &= \sum_{N=0}^{n_1+n_2+n_3} d_N^{n_1 n_2 n_3} \Lambda_N(x_R; \alpha_R)\end{aligned}$$

The recurrence relationships can be easily found and they read

$$d_N^{n_1+1} = \frac{1}{2\alpha_A} d_{N-1}^{n_1} + (N+1) d_{N+1}^{n_1}$$

as well as

$$d_N^{n_1+1, n_2} = \frac{1}{2\alpha_P} d_{N-1}^{n_1 n_2} + |\mathbf{P} - \mathbf{A}|_x d_N^{n_1 n_2} + (N+1) d_{N+1}^{n_1 n_2}$$

$$d_N^{n_1, n_2+1} = \frac{1}{2\alpha_P} d_{N-1}^{n_1 n_2} + |\mathbf{P} - \mathbf{B}|_x d_N^{n_1 n_2} + (N+1) d_{N+1}^{n_1 n_2}$$

and

$$d_N^{n_1+1, n_2, n_3} = \frac{1}{2\alpha_R} d_{N-1}^{n_1 n_2 n_3} + |\mathbf{R} - \mathbf{A}|_x d_N^{n_1 n_2 n_3} + (N+1) d_{N+1}^{n_1 n_2 n_3}$$

$$d_N^{n_1, n_2+1, n_3} = \frac{1}{2\alpha_R} d_{N-1}^{n_1 n_2 n_3} + |\mathbf{R} - \mathbf{B}|_x d_N^{n_1 n_2 n_3} + (N+1) d_{N+1}^{n_1 n_2 n_3}$$

$$d_N^{n_1, n_2, n_3+1} = \frac{1}{2\alpha_R} d_{N-1}^{n_1 n_2 n_3} + |\mathbf{R} - \mathbf{C}|_x d_N^{n_1 n_2 n_3} + (N+1) d_{N+1}^{n_1 n_2 n_3}$$

respectively. The first elements are given by

$$d_0^0 = 1$$

$$d_0^{00} = 1$$

$$d_0^{000} = 1$$

By using the above formalisms, it is straightforward to express the doublet of primitive GTO's as

$$[ij] = E_{ij} \sum_{N=0}^{n_1+n_2} \sum_{L=0}^{l_1+l_2} \sum_{M=0}^{m_1+m_2} d_N^{n_1 n_2} d_L^{l_1 l_2} d_M^{m_1 m_2} \Lambda_N(x_P) \Lambda_L(y_P) \Lambda_M(z_P) e^{-\alpha_P r_P^2}$$

Analogously, the triplet of primitive GTO's is given by

$$[ijk] = E_{ijk} \sum_{N=0}^{n_1+n_2+n_3} \sum_{L=0}^{l_1+l_2+l_3} \sum_{M=0}^{m_1+m_2+m_3} d_N^{n_1 n_2 n_3} d_L^{l_1 l_2 l_3} d_M^{m_1 m_2 m_3} \Lambda_N(x_R) \Lambda_L(y_R) \Lambda_M(z_R) e^{-\alpha_R r_R^2}$$

The multiplicative constants are given by

$$E_{ij}(\alpha_1, \alpha_2) = \exp \left[ -\frac{\alpha_1 \alpha_2}{\alpha_1 + \alpha_2} |\mathbf{A} - \mathbf{B}|^2 \right]$$

$$E_{ijk}(\alpha_1, \alpha_2, \alpha_3) = \exp \left[ -\frac{\alpha_1 \alpha_2}{\alpha_1 + \alpha_2} |\mathbf{A} - \mathbf{B}|^2 \right] \exp \left[ -\frac{(\alpha_1 + \alpha_2) \alpha_3}{\alpha_1 + \alpha_2 + \alpha_3} |\mathbf{P} - \mathbf{C}|^2 \right]$$

### 15.4.3 One-Body Integrals over Hermite Functions

The fundamental Hermite integrals that appear during computations of any kind of one-body integrals over GTO's are as follows

$$[NLM|\Theta(1)] \equiv \int d\mathbf{r}_1 \Theta(\mathbf{r}_1) \Lambda_N(x_{1P}; \alpha_P) \Lambda_L(y_{1P}; \alpha_P) \Lambda_M(z_{1P}; \alpha_P) e^{-\alpha_P r_{1P}^2}$$

It immediately follows that the overlap, dipole, quadrupole and potential integrals are given as

$$[NLM|1] = \delta_{N0} \delta_{L0} \delta_{M0} \left( \frac{\pi}{\alpha_P} \right)^{3/2}$$

$$[NLM|x_C] = [\delta_{N1} + |\mathbf{P}\mathbf{C}|_x \delta_{N0}] \delta_{L0} \delta_{M0} \left( \frac{\pi}{\alpha_P} \right)^{3/2}$$

$$[NLM|x_C^2] = \left[ 2\delta_{N2} + 2|\mathbf{P}\mathbf{C}|_x \delta_{N1} + \left( |\mathbf{P}\mathbf{C}|_x^2 + \frac{1}{2\alpha_P} \right) \delta_{N0} \right] \delta_{L0} \delta_{M0} \left( \frac{\pi}{\alpha_P} \right)^{3/2}$$

$$[NLM|x_C y_C] = (\delta_{N1} + |\mathbf{P}\mathbf{C}|_x \delta_{N0}) (\delta_{L1} + |\mathbf{P}\mathbf{C}|_y \delta_{L0}) \delta_{M0} \left( \frac{\pi}{\alpha_P} \right)^{3/2}$$

$$[NLM|r_C^{-1}] = \frac{2\pi}{\alpha_P} R_{NLM}$$



The coefficients  $R_{NLM}$  are discussed in separate section below.

### 15.4.4 Two-Body Integrals over Hermite Functions

The fundamental Hermite integrals that appear during computations of any kind of two-electron integrals over GTO's are as follows

$$[N_1 L_1 M_1 | N_2 L_2 M_2] \equiv \iint d\mathbf{r}_1 d\mathbf{r}_2 \Lambda_{N_1}(x_{1P}; \alpha_P) \Lambda_{L_1}(y_{1P}; \alpha_P) \Lambda_{M_1}(z_{1P}; \alpha_P) \Lambda_{N_2}(x_{2Q}; \alpha_Q) \Lambda_{L_2}(y_{2Q}; \alpha_Q) \Lambda_{M_2}(z_{2Q}; \alpha_Q) e^{-\alpha_P r_{1P}^2 - \alpha_Q r_{2Q}^2}$$

The above formula dramatically reduces to the following

$$[N_1 L_1 M_1 | N_2 L_2 M_2] = \lambda (-)^{N_2+L_2+M_2} R_{N_1+N_2, L_1+L_2, M_1+M_2}$$

with

$$\lambda \equiv \frac{2\pi^{5/2}}{\alpha_P \alpha_Q \sqrt{\alpha_P + \alpha_Q}}$$

To compute the  $R_{N_1+N_2, L_1+L_2, M_1+M_2}$  coefficients, the parameter  $T$  is given by

$$T = \frac{\alpha_P \alpha_Q}{\alpha_P + \alpha_Q} |\mathbf{P} - \mathbf{Q}|^2$$

### 15.4.5 The R(N,L,M) Coefficients

The  $R$  coefficients are defined as

$$R_{NLM} \equiv \left( \frac{\partial}{\partial a} \right)^N \left( \frac{\partial}{\partial b} \right)^L \left( \frac{\partial}{\partial c} \right)^M \int_0^1 e^{-Tu^2} du$$

with

$$T \equiv \alpha (a^2 + b^2 + c^2)$$

By extending the above definition to more general

$$R_{NLMj} \equiv (-\sqrt{\alpha})^{N+L+M} (-2\alpha)^j \int_0^1 u^{N+L+M+2j} H_N(au\sqrt{\alpha}) H_L(bu\sqrt{\alpha}) H_M(cu\sqrt{\alpha}) e^{-Tu^2} du$$

one can see that

$$R_{000j} = (-2\alpha)^j F_j(T)$$

The Boys function is here given by

$$F_j(T) \equiv \int_0^1 u^{2j} e^{-Tu^2} du$$

and its efficient implementation can be discussed elsewhere. In Psi4, `psi::Taylor_Fjt` class is used for this purpose.

Now, it is possible to show that the following recursion relationships are true:

$$R_{0,0,M+1,j} = cR_{0,0,M,j+1} + MR_{0,0,M-1,j+1}$$

$$R_{0,L+1,M,j} = bR_{0,L,M,j+1} + LR_{0,L-1,M,j+1}$$

$$R_{N+1,L,M,j} = aR_{N,L,M,j+1} + NR_{N-1,L,M,j+1}$$

This scheme is implemented in OEPDev.

### 15.4.6 Function Documentation

#### 15.4.6.1 double oepdev::d\_N\_n1\_n2 ( int N, int n1, int n2, double PA, double PB, double aP )

Compute McMurchie-Davidson-Hermite (MDH) coefficient for binomial expansion.

## Parameters

<i>N</i>	- increment in the summation of MDH series
<i>n1</i>	- angular momentum of first function
<i>n2</i>	- angular momentum of second function
<i>PA</i>	- cartesian component of P-A distance
<i>PB</i>	- cartesian component of P-B distance
<i>aP</i>	- free parameter of MDH expansion

## Returns

the McMurchie-Davidson-Hermite coefficient

15.4.6.2 `void oepdev::make_mdh_D1_coeff ( int n1, double aPd, double * buffer )`

Compute the McMurchie-Davidson-Hermite coefficients for monomial expansion.

## Parameters

<i>n1</i>	- angular momentum of first function
<i>aPd</i>	- parameter equal to 0.500/ <i>Pa</i> where <i>Pa</i> is exponent
<i>buffer</i>	- the McMurchie-Davidson-Hermite 3-dimensional array (raveled to vector): <ul style="list-style-type: none"> <li>• axis 0: dimension 3 (x, y or z Cartesian component)</li> <li>• axis 1: dimension <i>n1</i>+1 (0 to <i>n1</i>)</li> <li>• axis 2: dimension <i>n1</i>+1 (0 to <i>n1</i>)</li> </ul>

## See Also

[D1\\_INDEX](#)

15.4.6.3 `void oepdev::make_mdh_D2_coeff ( int n1, int n2, double aPd, double * PA, double * PB, double * buffer )`

Compute the McMurchie-Davidson-Hermite coefficients for binomial expansion.

## Parameters

<i>n1</i>	- angular momentum of first function
<i>n2</i>	- angular momentum of second function
<i>aPd</i>	- parameter equal to 0.500/ <i>Pa</i> where <i>Pa</i> is exponent
<i>PA</i>	- cartesian components of P-A distance
<i>PB</i>	- cartesian components of P-B distance
<i>buffer</i>	- the McMurchie-Davidson-Hermite 4-dimensional array (raveled to vector): <ul style="list-style-type: none"> <li>• axis 0: dimension 3 (x, y or z Cartesian component)</li> <li>• axis 1: dimension <i>n1</i>+1 (0 to <i>n1</i>)</li> <li>• axis 2: dimension <i>n2</i>+1 (0 to <i>n2</i>)</li> <li>• axis 3: dimension <i>n1</i>+<i>n2</i>+1 (0 to <i>n1</i>+<i>n2</i>)</li> </ul>

## See Also

[D2\\_INDEX](#)

15.4.6.4 `void oepdev::make_mdh_D2_coeff_explicit_recursion ( int n1, int n2, double aP, double * PA, double * PB, double * buffer )`

Compute the McMurchie-Davidson-Hermite coefficients for binomial expansion by explicit recursion. This function makes the same changes to buffers as `oepdev::make_mdh_D2_coeff`, but implements it through explicit recursion by calls to `oepdev::d_N_n1_n2`. Therefore, it is slightly slower. Here for debugging purposes.

#### Parameters

<i>n1</i>	- angular momentum of first function
<i>n2</i>	- angular momentum of second function
<i>aPd</i>	- parameter equal to 0.500/ <i>Pa</i> where <i>Pa</i> is exponent
<i>PA</i>	- cartesian components of P-A distance
<i>PB</i>	- cartesian components of P-B distance
<i>buffer</i>	- the McMurchie-Davidson-Hermite 4-dimensional array (raveled to vector): <ul style="list-style-type: none"> <li>• axis 0: dimension 3 (x, y or z Cartesian component)</li> <li>• axis 1: dimension <i>n1</i>+1 (0 to <i>n1</i>)</li> <li>• axis 2: dimension <i>n2</i>+1 (0 to <i>n2</i>)</li> <li>• axis 3: dimension <i>n1</i>+<i>n2</i>+1 (0 to <i>n1</i>+<i>n2</i>)</li> </ul>

#### See Also

[D2\\_INDEX](#)

15.4.6.5 `void oepdev::make_mdh_D3_coeff ( int n1, int n2, int n3, double aPd, double * PA, double * PB, double * PC, double * buffer )`

Compute the McMurchie-Davidson-Hermite coefficients for trinomial expansion.

#### Parameters

<i>n1</i>	- angular momentum of first function
<i>n2</i>	- angular momentum of second function
<i>n3</i>	- angular momentum of third function
<i>aPd</i>	- parameter equal to 0.500/ <i>Pa</i> where <i>Pa</i> is exponent
<i>PA</i>	- cartesian components of P-A distance
<i>PB</i>	- cartesian components of P-B distance
<i>PC</i>	- cartesian components of P-C distance
<i>buffer</i>	- the McMurchie-Davidson-Hermite 5-dimensional array (raveled to vector): <ul style="list-style-type: none"> <li>• axis 0: dimension 3 (x, y or z Cartesian component)</li> <li>• axis 1: dimension <i>n1</i>+1 (0 to <i>n1</i>)</li> <li>• axis 2: dimension <i>n2</i>+1 (0 to <i>n2</i>)</li> <li>• axis 3: dimension <i>n3</i>+1 (0 to <i>n3</i>)</li> <li>• axis 4: dimension <i>n1</i>+<i>n2</i>+<i>n3</i>+1 (0 to <i>n1</i>+<i>n2</i>+<i>n3</i>)</li> </ul>

#### See Also

[D3\\_INDEX](#)

15.4.6.6 `void oepdev::make_mdh_R_coeff ( int N, int L, int M, double alpha, double a, double b, double c, double * F,  
double * buffer )`

Compute the McMurchie-Davidson R coefficients.

## Parameters

<i>N</i>	- increment in the summation of MDH series along x direction
<i>L</i>	- increment in the summation of MDH series along y direction
<i>M</i>	- increment in the summation of MDH series along z direction
<i>alpha</i>	- alpha parameter of R coefficient
<i>a</i>	- x component of PQ vector of R coefficient
<i>b</i>	- y component of PQ vector of R coefficient
<i>c</i>	- z component of PQ vector of R coefficient
<i>F</i>	- array of Boys function values for given alpha and PQ
<i>buffer</i>	- the McMurchie-Davidson 4-dimensional array (raveled to vector): <ul style="list-style-type: none"> <li>• axis 0: dimension N+1</li> <li>• axis 1: dimension L+1</li> <li>• axis 2: dimension M+1</li> <li>• axis 3: dimension N+L+M+1 (<i>j</i>-th element)</li> </ul>

## 15.5 The Integral Helper Library

You will find here various iterators to go through shells while computing ERI, or iterators over ERI itself.

### Classes

- class [oepdev::ShellCombinationsIterator](#)  
*Iterator for Shell Combinations. Abstract Base.*
- class [oepdev::AOIntegralsIterator](#)  
*Iterator for AO Integrals. Abstract Base.*
- class [oepdev::AllAOShellCombinationsIterator\\_4](#)  
*Loop over all possible ERI shells in a shell quartet.*
- class [oepdev::AllAOShellCombinationsIterator\\_2](#)  
*Loop over all possible ERI shells in a shell doublet.*
- class [oepdev::AllAOIntegralsIterator\\_4](#)  
*Loop over all possible ERI within a particular shell quartet.*
- class [oepdev::AllAOIntegralsIterator\\_2](#)  
*Loop over all possible ERI within a particular shell doublet.*

### Typedefs

- using [oepdev::SharedShellsIterator](#) = `std::shared_ptr< ShellCombinationsIterator >`  
*Iterator over shells as shared pointer.*
- using [oepdev::SharedAOIntsIterator](#) = `std::shared_ptr< AOIntegralsIterator >`  
*Iterator over AO integrals as shared pointer.*

#### 15.5.1 Detailed Description

You will find here various iterators to go through shells while computing ERI, or iterators over ERI itself.

## 15.6 The Three-Dimensional Scalar Fields Library

Handles all sorts of scalar distributions in 3D Euclidean space, such as potentials defined at particular collection of points. In this Module, you will also find handling both random and ordered points collections in a form of a G09 cube, as well as handling G09 Cube files.

### Classes

- class [oepdev::Points3DIterator](#)  
*Iterator over a collection of points in 3D space. Abstract base.*
- class [oepdev::CubePoints3DIterator](#)  
*Iterator over a collection of points in 3D space. g09 Cube-like order.*
- class [oepdev::RandomPoints3DIterator](#)  
*Iterator over a collection of points in 3D space. Random collection.*
- class [oepdev::PointsCollection3D](#)  
*Collection of points in 3D space. Abstract base.*
- class [oepdev::RandomPointsCollection3D](#)  
*Collection of random points in 3D space.*
- class [oepdev::CubePointsCollection3D](#)  
*G09 cube-like ordered collection of points in 3D space.*
- class [oepdev::ScalarField3D](#)  
*Scalar field in 3D space. Abstract base.*
- class [oepdev::ElectrostaticPotential3D](#)  
*Electrostatic potential of a molecule.*
- class [oepdev::OEPotential3D< T >](#)  
*Class template for OEP scalar fields.*

### Functions

- [oepdev::OEPotential3D< T >::OEPotential3D](#) (const int &np, const double &padding, std::shared\_ptr< T > oep, const std::string &oepType)  
*Construct random spherical collection of scalar field of type T.*
- [oepdev::OEPotential3D< T >::OEPotential3D](#) (const int &nx, const int &ny, const int &nz, const double &px, const double &py, const double &pz, std::shared\_ptr< T > oep, const std::string &oepType, psi::Options &options)  
*Construct ordered 3D collection of scalar field of type T.*
- virtual [oepdev::OEPotential3D< T >::~~OEPotential3D](#) ()  
*Destructor.*
- virtual void [oepdev::OEPotential3D< T >::print](#) () const  
*Print information of the object to Psi4 output.*
- virtual double [oepdev::OEPotential3D< T >::compute\\_xyz](#) (const double &x, const double &y, const double &z)  
*Compute a value of scalar field at point (x, y, z)*

### 15.6.1 Detailed Description

Handles all sorts of scalar distributions in 3D Euclidean space, such as potentials defined at particular collection of points. In this Module, you will also find handling both random and ordered points collections in a form of a G09 cube, as well as handling G09 Cube files.

## 15.6.2 Function Documentation

15.6.2.1 `template<class T> oepdev::OEPotential3D< T >::OEPotential3D ( const int & np, const double & padding, std::shared_ptr< T > oep, const std::string & oepType )`

Construct random spherical collection of scalar field of type T.

The points are drawn according to uniform distribution in 3D space.

Parameters

<i>np</i>	- number of points to draw
<i>padding</i>	- spherical padding distance (au)
<i>oep</i>	- OEP object of type T
<i>oepType</i>	- type of OEP

15.6.2.2 `template<class T> oepdev::OEPotential3D< T >::OEPotential3D ( const int & nx, const int & ny, const int & nz, const double & px, const double & py, const double & pz, std::shared_ptr< T > oep, const std::string & oepType, psi::Options & options )`

Construct ordered 3D collection of scalar field of type T.

The points are generated according to Gaussian cube file format.

Parameters

<i>nx</i>	- number of points along x direction
<i>ny</i>	- number of points along y direction
<i>nz</i>	- number of points along z direction
<i>px</i>	- padding distance along x direction
<i>py</i>	- padding distance along y direction
<i>pz</i>	- padding distance along z direction
<i>oep</i>	- OEP object of type T
<i>oepType</i>	- type of OEP
<i>options</i>	- Psi4 options object



## 15.7 The Multipole Fitting Library

Implements methods to fit the generalized multipole moments of a generalized density distribution based on the input generalized potential scalar field. Among others, you will find here the electrostatic potential (ESP) fitting method.

### Classes

- class [oepdev::ESPSolver](#)  
*Charges from Electrostatic Potential (ESP). A solver-type class.*

### Typedefs

- using **oepdev::SharedScalarField3D** = std::shared\_ptr< ScalarField3D >

#### 15.7.1 Detailed Description

Implements methods to fit the generalized multipole moments of a generalized density distribution based on the input generalized potential scalar field. Among others, you will find here the electrostatic potential (ESP) fitting method.

## 15.8 The Density Functional Theory Library

Implements the OEPDev ab initio DFT methods.

Implements the OEPDev ab initio DFT methods.

## 15.9 The OEPDev Utilities

Contains utility functions such as printing OEPDev preamble to the output file, class for wavefunction union etc.

### Classes

- class `oepdev::CPHF`  
*CPHF solver class.*
- class `oepdev::DIISManager`  
*DIIS manager.*
- struct `oepdev::ABCD`  
*Simple structure to hold the Fourier series expansion coefficients.*
- struct `oepdev::Fourier9`  
*Simple structure to hold the Fourier series expansion coefficients for N=4.*
- class `oepdev::UnitaryOptimizer`  
*Find the optimum unitary matrix of quadratic matrix equation.*
- class `oepdev::UnitaryOptimizer_4_2`  
*Find the optimum unitary matrix for quartic-quadratic matrix equation with trace.*
- class `oepdev::WavefunctionUnion`  
*Union of two Wavefunction objects.*

### Macros

- `#define OEPDEV_USE_PSI4_DIIS_MANAGER 0`  
*Use DIIS from Psi4 (1) or OEPDev (0)?*
- `#define OEPDEV_MAX_AM 8`  
*L\_max.*
- `#define OEPDEV_N_MAX_AM 17`  
*2L\_max+1*
- `#define OEPDEV_CRIT_ERI 1e-9`  
*ERI criterion for E12, E34, E123 and lambda\*EXY coefficients.*
- `#define OEPDEV_SIZE_BUFFER_R 250563`  
*Size of R buffer (OEPDEV\_N\_MAX\_AM\*OEPDEV\_N\_MAX\_AM\*OEPDEV\_N\_MAX\_AM\*OEPDEV\_N\_MAX\_AM\*3)*
- `#define OEPDEV_SIZE_BUFFER_D2 3264`  
*Size of D2 buffer (3\*(OEPDEV\_MAX\_AM+1)\*(OEPDEV\_MAX\_AM+1)\*OEPDEV\_N\_MAX\_AM)*

### Functions

- void `oepdev::preamble` (void)  
*Print preamble for module OEPDEV.*
- template<typename... Args>  
std::string `oepdev::string_sprintf` (const char \*format, Args...args)  
*Format string output. Example: std::string text = oepdev::string\_sprintf("Test %3d, %13.5f", 5, -10.5425);.*
- std::shared\_ptr< SuperFunctional > `oepdev::create_superfunctional` (std::string name, Options &options)  
*Set up DFT functional.*
- std::shared\_ptr< Molecule > `oepdev::extract_monomer` (std::shared\_ptr< const Molecule > molecule\_, dimer, int id)  
*Extract molecule from dimer.*
- std::shared\_ptr< Wavefunction > `oepdev::solve_scf` (std::shared\_ptr< Molecule > molecule, std::shared\_ptr< BasisSet > primary, std::shared\_ptr< SuperFunctional > functional, Options &options, std::shared\_ptr< PSIO > psio)  
*Solve RHF-SCF equations for a given molecule in a given basis set.*

### 15.9.1 Detailed Description

Contains utility functions such as printing OEPDev preamble to the output file, class for wavefunction union etc.

### 15.9.2 Function Documentation

15.9.2.1 `std::shared_ptr< SuperFunctional > oepdev::create_superfunctional ( std::string name, Options & options )`

Set up DFT functional.

Now it accepts only pure HF functional.

Parameters

<i>name</i>	name of the functional ("HF" is now only available)
<i>options</i>	psi::Options object

Returns

psi::SharedSuperFunctional object with functional.

15.9.2.2 `std::shared_ptr< Molecule > oepdev::extract_monomer ( std::shared_ptr< const Molecule > molecule_dimer, int id )`

Extract molecule from dimer.

Parameters

<i>molecule_dimer</i>	psi::SharedMolecule object with dimer
<i>id</i>	index of a molecule (starts from 1)

Returns

psi::SharedMolecule object with indicated monomer

15.9.2.3 `std::shared_ptr< Wavefunction > oepdev::solve_scf ( std::shared_ptr< Molecule > molecule, std::shared_ptr< BasisSet > primary, std::shared_ptr< SuperFunctional > functional, Options & options, std::shared_ptr< PSIO > psio )`

Solve RHF-SCF equations for a given molecule in a given basis set.

Parameters

<i>molecule</i>	psi::SharedMolecule object with molecule
<i>primary</i>	shared primary basis set
<i>functional</i>	DFT functional
<i>options</i>	psi::Options object
<i>psio</i>	psi::PSIO object

Returns

psi::SharedWavefunction SCF wavefunction of the molecule

## 15.10 The OEPDev Testing Platform Library

Testing platform at C++ level of code. You should add more tests here when developing new functionalities, theories or models.

### Classes

- class `oepdev::test::Test`  
*Manages test routines.*

### 15.10.1 Detailed Description

Testing platform at C++ level of code. You should add more tests here when developing new functionalities, theories or models.



## Chapter 16

# Namespace Documentation

### 16.1 oepdev Namespace Reference

OEPDev module namespace.

#### Classes

- class [GenEffPar](#)  
*Generalized Effective Fragment Parameters. Container Class.*
- class [GenEffFrag](#)  
*Generalized Effective Fragment. Container Class.*
- class [GenEffParFactory](#)  
*Generalized Effective Fragment Factory. Abstract Base.*
- class [PolarGEFactory](#)  
*Polarization GEFP Factory.*
- class [MOScaledPolarGEFactory](#)  
*Polarization GEFP Factory with Least-Squares Scaling of MO Space.*
- class [FieldScaledPolarGEFactory](#)  
*Polarization GEFP Factory with Least-Squares Scaling of Cartesian Degrees of freedom.*
- class [TwoElectronInt](#)  
*General Two Electron Integral.*
- class [ERI\\_1\\_1](#)  
*2-centre ERI of the form  $\langle a|O(2)|b \rangle$  where  $O(2) = 1/r_{12}$ .*
- class [ERI\\_2\\_2](#)  
*4-centre ERI of the form  $\langle ab|O(2)|cd \rangle$  where  $O(2) = 1/r_{12}$ .*
- class [ERI\\_3\\_1](#)  
*4-centre ERI of the form  $\langle abc|O(2)|d \rangle$  where  $O(2) = 1/r_{12}$ .*
- struct [OEPTyp](#)  
*Container to handle the type of One-Electron Potentials.*
- class [OEPotential](#)  
*Generalized One-Electron Potential: Abstract base.*
- class [ElectrostaticEnergyOEPotential](#)  
*Generalized One-Electron Potential for Electrostatic Energy.*
- class [RepulsionEnergyOEPotential](#)  
*Generalized One-Electron Potential for Pauli Repulsion Energy.*
- class [ChargeTransferEnergyOEPotential](#)  
*Generalized One-Electron Potential for Charge-Transfer Interaction Energy.*

- class [EETCouplingOEPotential](#)  
*Generalized One-Electron Potential for EET coupling calculations.*
- class [TwoBodyAOInt](#)
- class [IntegralFactory](#)  
*Extended [IntegralFactory](#) for computing integrals.*
- class [PotentialInt](#)  
*Computes potential integrals.*
- class [CPHF](#)  
*CPHF solver class.*
- class [DIISManager](#)  
*DIIS manager.*
- class [ESPSolver](#)  
*Charges from Electrostatic Potential (ESP). A solver-type class.*
- class [ShellCombinationsIterator](#)  
*Iterator for Shell Combinations. Abstract Base.*
- class [AOIntegralsIterator](#)  
*Iterator for AO Integrals. Abstract Base.*
- class [AllAOShellCombinationsIterator\\_4](#)  
*Loop over all possible ERI shells in a shell quartet.*
- class [AllAOShellCombinationsIterator\\_2](#)  
*Loop over all possible ERI shells in a shell doublet.*
- class [AllAOIntegralsIterator\\_4](#)  
*Loop over all possible ERI within a particular shell quartet.*
- class [AllAOIntegralsIterator\\_2](#)  
*Loop over all possible ERI within a particular shell doublet.*
- class [OEPDevSolver](#)  
*Solver of properties of molecular aggregates. Abstract base.*
- class [ElectrostaticEnergySolver](#)  
*Compute the Coulombic interaction energy between unperturbed wavefunctions.*
- class [RepulsionEnergySolver](#)  
*Compute the Pauli-Repulsion interaction energy between unperturbed wavefunctions.*
- class [ChargeTransferEnergySolver](#)  
*Compute the Charge-Transfer interaction energy between unperturbed wavefunctions.*
- class [Points3DIterator](#)  
*Iterator over a collection of points in 3D space. Abstract base.*
- class [CubePoints3DIterator](#)  
*Iterator over a collection of points in 3D space. g09 Cube-like order.*
- class [RandomPoints3DIterator](#)  
*Iterator over a collection of points in 3D space. Random collection.*
- class [PointsCollection3D](#)  
*Collection of points in 3D space. Abstract base.*
- class [RandomPointsCollection3D](#)  
*Collection of random points in 3D space.*
- class [CubePointsCollection3D](#)  
*G09 cube-like ordered collection of points in 3D space.*
- class [ScalarField3D](#)  
*Scalar field in 3D space. Abstract base.*
- class [ElectrostaticPotential3D](#)  
*Electrostatic potential of a molecule.*
- class [OEPotential3D](#)  
*Class template for OEP scalar fields.*



- struct [ABCD](#)  
*Simple structure to hold the Fourier series expansion coefficients.*
- struct [Fourier9](#)  
*Simple structure to hold the Fourier series expansion coefficients for N=4.*
- class [UnitaryOptimizer](#)  
*Find the optimum unitary matrix of quadratic matrix equation.*
- class [UnitaryOptimizer\\_4\\_2](#)  
*Find the optimum unitary matrix for quartic-quadratic matrix equation with trace.*
- class [WavefunctionUnion](#)  
*Union of two Wavefunction objects.*

## Typedefs

- using **SharedWavefunction** = std::shared\_ptr< Wavefunction >
- using **SharedBasisSet** = std::shared\_ptr< BasisSet >
- using **SharedTensor** = std::shared\_ptr< Tensor >
- using **SharedMatrix** = std::shared\_ptr< Matrix >
- using **SharedVector** = std::shared\_ptr< Vector >
- using **SharedScalarField3D** = std::shared\_ptr< [ScalarField3D](#) >
- using **SharedIntegralFactory** = std::shared\_ptr< [IntegralFactory](#) >
- using **SharedTwoBodyAOInt** = std::shared\_ptr< [TwoBodyAOInt](#) >
- using [SharedShellsIterator](#) = std::shared\_ptr< [ShellCombinationsIterator](#) >  
*Iterator over shells as shared pointer.*
- using [SharedAOIntsIterator](#) = std::shared\_ptr< [AOIntegralsIterator](#) >  
*Iterator over AO integrals as shared pointer.*
- using **SharedWavefunctionUnion** = std::shared\_ptr< [WavefunctionUnion](#) >
- using **SharedOEPotential** = std::shared\_ptr< [OEPotential](#) >
- using **SharedMolecule** = std::shared\_ptr< Molecule >
- using **SharedSuperFunctional** = std::shared\_ptr< SuperFunctional >
- using **SharedMOSpace** = std::shared\_ptr< MOSpace >
- using **SharedMOSpaceVector** = std::vector< std::shared\_ptr< MOSpace >>
- using **SharedIntegralTransform** = std::shared\_ptr< IntegralTransform >
- using **SharedLocalizer** = std::shared\_ptr< Localizer >

## Functions

- **n\_max\_am\_** (2 \*max\_am\_+1)
- double **d\_N\_n1\_n2** (int N, int n1, int n2, double PA, double PB, double aP)  
*Compute McMurchie-Davidson-Hermite (MDH) coefficient for binomial expansion.*
- void **make\_mdh\_D2\_coeff\_explicit\_recursion** (int n1, int n2, double aP, double \*PA, double \*PB, double \*buffer)  
*Compute the McMurchie-Davidson-Hermite coefficients for binomial expansion by explicit recursion. This function makes the same changes to buffers as oepdev::make\_mdh\_D2\_coeff, but implements it through explicit recursion by calls to oepdev::d\_N\_n1\_n2. Therefore, it is slightly slower. Here for debugging purposes.*
- void **make\_mdh\_D1\_coeff** (int n1, double aPd, double \*buffer)  
*Compute the McMurchie-Davidson-Hermite coefficients for monomial expansion.*
- void **make\_mdh\_D2\_coeff** (int n1, int n2, double aPd, double \*PA, double \*PB, double \*buffer)  
*Compute the McMurchie-Davidson-Hermite coefficients for binomial expansion.*
- void **make\_mdh\_D3\_coeff** (int n1, int n2, int n3, double aPd, double \*PA, double \*PB, double \*PC, double \*buffer)  
*Compute the McMurchie-Davidson-Hermite coefficients for trinomial expansion.*

- void [make\\_mdh\\_R\\_coeff](#) (int N, int L, int M, double alpha, double a, double b, double c, double \*F, double \*buffer)

*Compute the McMurchie-Davidson R coefficients.*

- constexpr std::complex< double > **operator""\_i** (unsigned long long d)
- constexpr std::complex< double > **operator""\_i** (long double d)
- void [preamble](#) (void)

*Print preamble for module OEPDEV.*

- std::shared\_ptr< SuperFunctional > [create\\_superfunctional](#) (std::string name, Options &options)

*Set up DFT functional.*

- std::shared\_ptr< Molecule > [extract\\_monomer](#) (std::shared\_ptr< const Molecule > molecule\_dimer, int id)

*Extract molecule from dimer.*

- std::shared\_ptr< Wavefunction > [solve\\_scf](#) (std::shared\_ptr< Molecule > molecule, std::shared\_ptr< Basis-Set > primary, std::shared\_ptr< SuperFunctional > functional, Options &options, std::shared\_ptr< PSIO > psio)

*Solve RHF-SCF equations for a given molecule in a given basis set.*

- template<typename... Args>  
std::string [string\\_sprintf](#) (const char \*format, Args...args)

*Format string output. Example: std::string text = oepdev::string\_sprintf("Test %3d, %13.5f", 5, -10.5425);.*

### 16.1.1 Detailed Description

OEPDev module namespace. Contains:

## 16.2 psi Namespace Reference

Psi4 package namespace.

### Typedefs

- using **SharedVetor** = std::shared\_ptr< Vector >
- using **SharedBasisSet** = std::shared\_ptr< BasisSet >
- using **SharedMolecule** = std::shared\_ptr< Molecule >
- using **SharedMatrix** = std::shared\_ptr< Matrix >
- using **SharedWavefunction** = std::shared\_ptr< Wavefunction >

### Functions

- int [read\\_options](#) (std::string name, Options &options)  
*Options for the OEPDev plugin.*
- SharedWavefunction [oepdev](#) (SharedWavefunction ref\_wfn, Options &options)  
*Main routine of the OEPDev plugin.*

### 16.2.1 Detailed Description

Psi4 package namespace. Contains all Psi4 functionalities.

## 16.2.2 Function Documentation

### 16.2.2.1 SharedWavefunction psi::oepdev ( SharedWavefunction *ref\_wfn*, Options & *options* )

Main routine of the OEPDev plugin.

Created with intention to test various models of the interaction energy between two molecules, described by the Hartree-Fock-Roothaan-Hall theory or the configuration interaction with singles theory.

In particular, the plugin tests the models of:

1. the Pauli repulsion and CT interaction energy (Project II )
2. the Induction interaction energy (Project III)
3. the excitation energy transfer couplings (Project I )

against benchmarks (exact or reference solutions). The list of implemented models can be found in [Implemented Models](#) .

#### Parameters

<i>ref_wfn</i>	shared wavefunction of a dimer
<i>options</i>	psi::Options object

#### Returns

psi::SharedWavefunction (either *ref\_wfn* or wavefunction union)

### 16.2.2.2 int psi::read\_options ( std::string *name*, Options & *options* )

Options for the OEPDev plugin.

#### Parameters

<i>name</i>	name of driver function
<i>options</i>	psi::Options object

#### Returns

true



## Chapter 17

# Class Documentation

### 17.1 oepdev::ABCD Struct Reference

Simple structure to hold the Fourier series expansion coefficients.

```
#include <unitary_optimizer.h>
```

#### Public Attributes

- double **A**
- double **B**
- double **C**
- double **D**

#### 17.1.1 Detailed Description

Simple structure to hold the Fourier series expansion coefficients.

The documentation for this struct was generated from the following file:

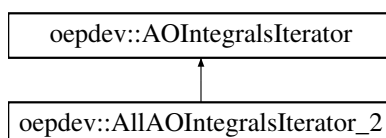
- oepdev/libutil/[unitary\\_optimizer.h](#)

### 17.2 oepdev::AllAOIntegralsIterator\_2 Class Reference

Loop over all possible ERI within a particular shell doublet.

```
#include <integrals_iter.h>
```

Inheritance diagram for oepdev::AllAOIntegralsIterator\_2:



#### Public Member Functions

- [AllAOIntegralsIterator\\_2](#) (const [ShellCombinationsIterator](#) \*shellIter)

- Construct by shell iterator (const object)*
  - [AllIAOIntegralsIterator\\_2](#) (std::shared\_ptr< [ShellCombinationsIterator](#) > shellIter)
- Construct by shell iterator (pointed by shared pointer)*
  - void [first](#) ()
- First iteration.*
  - void [next](#) ()
- Next iteration.*
  - int [i](#) () const
- Grab the current integral i index.*
  - int [j](#) () const
- Grab the current integral j index.*
  - int [index](#) () const

## Additional Inherited Members

### 17.2.1 Detailed Description

Loop over all possible ERI within a particular shell doublet.

Constructed by providing a const reference or shared pointer to an AllIAOShellCombinationsIterator object.

See Also

[AllIAOShellCombinationsIterator\\_2](#)

### 17.2.2 Constructor & Destructor Documentation

#### 17.2.2.1 AllIAOIntegralsIterator\_2::AllIAOIntegralsIterator\_2 ( const ShellCombinationsIterator \* shellIter )

Construct by shell iterator (const object)

Parameters

<i>shellIter</i>	- shell iterator object
------------------	-------------------------

#### 17.2.2.2 AllIAOIntegralsIterator\_2::AllIAOIntegralsIterator\_2 ( std::shared\_ptr< ShellCombinationsIterator > shellIter )

Construct by shell iterator (pointed by shared pointer)

Parameters

<i>shellIter</i>	- shell iterator object
------------------	-------------------------

### 17.2.3 Member Function Documentation

#### 17.2.3.1 int oepdev::AllIAOIntegralsIterator\_2::index ( void ) const [inline], [virtual]

Grab the current index of integral value stored in the buffer

Implements [oepdev::AOIntegralsIterator](#).

The documentation for this class was generated from the following files:

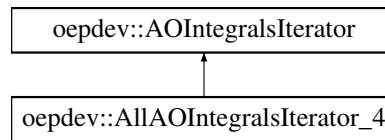
- oepdev/libutil/integrals\_iter.h
- oepdev/libutil/integrals\_iter.cc

## 17.3 oepdev::AllAOIntegralsIterator\_4 Class Reference

Loop over all possible ERI within a particular shell quartet.

```
#include <integrals_iter.h>
```

Inheritance diagram for oepdev::AllAOIntegralsIterator\_4:



### Public Member Functions

- [AllAOIntegralsIterator\\_4](#) (const [ShellCombinationsIterator](#) \*shellIter)  
*Construct by shell iterator (const object)*
- [AllAOIntegralsIterator\\_4](#) (std::shared\_ptr< [ShellCombinationsIterator](#) > shellIter)  
*Construct by shell iterator (pointed by shared pointer)*
- void [first](#) ()  
*First iteration.*
- void [next](#) ()  
*Next iteration.*
- int [i](#) () const  
*Grab the current integral i index.*
- int [j](#) () const  
*Grab the current integral j index.*
- int [k](#) () const  
*Grab the current integral k index.*
- int [l](#) () const  
*Grab the current integral l index.*
- int [index](#) () const

### Additional Inherited Members

#### 17.3.1 Detailed Description

Loop over all possible ERI within a particular shell quartet.

Constructed by providing a const reference or shared pointer to an AllAOShellCombinationsIterator object.

See Also

[AllAOShellCombinationsIterator\\_4](#)

#### 17.3.2 Constructor & Destructor Documentation

##### 17.3.2.1 AllAOIntegralsIterator\_4::AllAOIntegralsIterator\_4 ( const [ShellCombinationsIterator](#) \* shellIter )

Construct by shell iterator (const object)

## Parameters

<i>shellIter</i>	- shell iterator object
------------------	-------------------------

17.3.2.2 `AllAIOIntegralsIterator_4::AllAIOIntegralsIterator_4 ( std::shared_ptr< ShellCombinationsIterator > shellIter )`

Construct by shell iterator (pointed by shared pointer)

## Parameters

<i>shellIter</i>	- shell iterator object
------------------	-------------------------

## 17.3.3 Member Function Documentation

17.3.3.1 `int oepdev::AllAIOIntegralsIterator_4::index ( void ) const [inline], [virtual]`

Grab the current index of integral value stored in the buffer

Implements [oepdev::AIOIntegralsIterator](#).

The documentation for this class was generated from the following files:

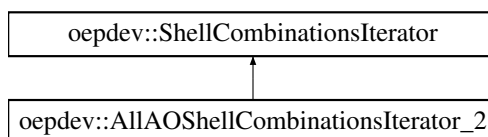
- [oepdev/libutil/integrals\\_iter.h](#)
- [oepdev/libutil/integrals\\_iter.cc](#)

17.4 `oepdev::AllAOShellCombinationsIterator_2` Class Reference

Loop over all possible ERI shells in a shell doublet.

```
#include <integrals_iter.h>
```

Inheritance diagram for `oepdev::AllAOShellCombinationsIterator_2`:



## Public Member Functions

- [AllAOShellCombinationsIterator\\_2](#) (SharedBasisSet [bs\\_1](#), SharedBasisSet [bs\\_2](#))  
*Iterate over shell doublets. Construct by providing basis sets for each axis. The basis sets must be defined for the same molecule.*
- [AllAOShellCombinationsIterator\\_2](#) (std::shared\_ptr< [IntegralFactory](#) > integrals)  
*Construct by providing integral factory.*
- [AllAOShellCombinationsIterator\\_2](#) (const [IntegralFactory](#) &integrals)
- [AllAOShellCombinationsIterator\\_2](#) (std::shared\_ptr< psi::IntegralFactory > integrals)  
*Construct by providing integral factory.*
- [AllAOShellCombinationsIterator\\_2](#) (const psi::IntegralFactory &integrals)
- void [first](#) ()  
*First iteration.*
- void [next](#) ()  
*Next iteration.*



- void `compute_shell` (std::shared\_ptr< oepdev::TwoBodyAOInt > tei) const  
*Compute ERI's for the current shell. The eris are stored in the buffer of the argument object.*
- void `compute_shell` (std::shared\_ptr< psi::TwoBodyAOInt > tei) const
- int `P` () const  
*Grab the current shell P index.*
- int `Q` () const  
*Grab the current shell Q index.*

## Additional Inherited Members

### 17.4.1 Detailed Description

Loop over all possible ERI shells in a shell doublet.

Constructed by providing [IntegralFactory](#) object or shared pointers to two basis set spaces.

### 17.4.2 Constructor & Destructor Documentation

#### 17.4.2.1 AllAOShellCombinationsIterator\_2::AllAOShellCombinationsIterator\_2 ( SharedBasisSet bs\_1, SharedBasisSet bs\_2 )

Iterate over shell doublets. Construct by providing basis sets for each axis. The basis sets must be defined for the same molecule.

Parameters

<code>bs_1</code>	- basis set of axis 1
<code>bs_2</code>	- basis set of axis 2

#### 17.4.2.2 oepdev::AllAOShellCombinationsIterator\_2::AllAOShellCombinationsIterator\_2 ( std::shared\_ptr< IntegralFactory > integrals )

Construct by providing integral factory.

Parameters

<code>integrals</code>	- OepDev integral factory object
------------------------	----------------------------------

#### 17.4.2.3 AllAOShellCombinationsIterator\_2::AllAOShellCombinationsIterator\_2 ( const IntegralFactory & integrals )

This is an overloaded member function, provided for convenience. It differs from the above function only in what argument(s) it accepts.

#### 17.4.2.4 AllAOShellCombinationsIterator\_2::AllAOShellCombinationsIterator\_2 ( std::shared\_ptr< psi::IntegralFactory > integrals )

Construct by providing integral factory.

Parameters

<code>integrals</code>	- Psi4 integral factory object
------------------------	--------------------------------

#### 17.4.2.5 AllAOShellCombinationsIterator\_2::AllAOShellCombinationsIterator\_2 ( const psi::IntegralFactory & integrals )

This is an overloaded member function, provided for convenience. It differs from the above function only in what argument(s) it accepts.

### 17.4.3 Member Function Documentation

#### 17.4.3.1 void AllAOShellCombinationsIterator\_2::compute\_shell ( std::shared\_ptr< oepdev::TwoBodyAOInt > tei ) const [virtual]

Compute ERI's for the current shell. The eris are stored in the buffer of the argument object.

##### Parameters

<i>tei</i>	- two electron AO integral
------------	----------------------------

Implements [oepdev::ShellCombinationsIterator](#).

The documentation for this class was generated from the following files:

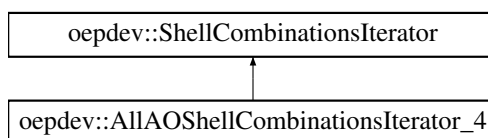
- [oepdev/libutil/integrals\\_iter.h](#)
- [oepdev/libutil/integrals\\_iter.cc](#)

## 17.5 oepdev::AllAOShellCombinationsIterator\_4 Class Reference

Loop over all possible ERI shells in a shell quartet.

```
#include <integrals_iter.h>
```

Inheritance diagram for oepdev::AllAOShellCombinationsIterator\_4:



### Public Member Functions

- [AllAOShellCombinationsIterator\\_4](#) (SharedBasisSet [bs\\_1](#), SharedBasisSet [bs\\_2](#), SharedBasisSet [bs\\_3](#), SharedBasisSet [bs\\_4](#))  
*Iterate over shell quartets. Construct by providing basis sets for each axis. The basis sets must be defined for the same molecule.*
- [AllAOShellCombinationsIterator\\_4](#) (std::shared\_ptr< [IntegralFactory](#) > integrals)  
*Construct by providing integral factory.*
- [AllAOShellCombinationsIterator\\_4](#) (const [IntegralFactory](#) &integrals)
- [AllAOShellCombinationsIterator\\_4](#) (std::shared\_ptr< psi::IntegralFactory > integrals)  
*Construct by providing integral factory.*
- [AllAOShellCombinationsIterator\\_4](#) (const psi::IntegralFactory &integrals)
- void [first](#) ()  
*Do the first iteration.*
- void [next](#) ()  
*Do the next iteration.*
- void [compute\\_shell](#) (std::shared\_ptr< oepdev::TwoBodyAOInt > tei) const
- void [compute\\_shell](#) (std::shared\_ptr< psi::TwoBodyAOInt > tei) const

- int **P** () const  
*Grab the current shell P index.*
- int **Q** () const  
*Grab the current shell Q index.*
- int **R** () const  
*Grab the current shell R index.*
- int **S** () const  
*Grab the current shell S index.*

## Additional Inherited Members

### 17.5.1 Detailed Description

Loop over all possible ERI shells in a shell quartet.

Constructed by providing [IntegralFactory](#) object or shared pointers to four basis set spaces.

### 17.5.2 Constructor & Destructor Documentation

**17.5.2.1** `AllAOShellCombinationsIterator_4::AllAOShellCombinationsIterator_4 ( SharedBasisSet bs_1, SharedBasisSet bs_2, SharedBasisSet bs_3, SharedBasisSet bs_4 )`

Iterate over shell quartets. Construct by providing basis sets for each axis. The basis sets must be defined for the same molecule.

Parameters

<i>bs_1</i>	- basis set of axis 1
<i>bs_2</i>	- basis set of axis 2
<i>bs_3</i>	- basis set of axis 3
<i>bs_4</i>	- basis set of axis 4

**17.5.2.2** `oepdev::AllAOShellCombinationsIterator_4::AllAOShellCombinationsIterator_4 ( std::shared_ptr< IntegralFactory > integrals )`

Construct by providing integral factory.

Parameters

<i>integrals</i>	- OepDev integral factory object
------------------	----------------------------------

**17.5.2.3** `AllAOShellCombinationsIterator_4::AllAOShellCombinationsIterator_4 ( const IntegralFactory & integrals )`

This is an overloaded member function, provided for convenience. It differs from the above function only in what argument(s) it accepts.

**17.5.2.4** `AllAOShellCombinationsIterator_4::AllAOShellCombinationsIterator_4 ( std::shared_ptr< psi::IntegralFactory > integrals )`

Construct by providing integral factory.

## Parameters

<i>integrals</i>	- OepDev integral factory object
------------------	----------------------------------

17.5.2.5 AllAOShellCombinationsIterator\_4::AllAOShellCombinationsIterator\_4 ( const psi::IntegralFactory & *integrals* )

This is an overloaded member function, provided for convenience. It differs from the above function only in what argument(s) it accepts.

## 17.5.3 Member Function Documentation

17.5.3.1 void AllAOShellCombinationsIterator\_4::compute\_shell ( std::shared\_ptr< oepdev::TwoBodyAOInt > *tei* ) const [virtual]

Compute integrals in a current shell. Works both for [oepdev::TwoBodyAOInt](#) and [psi::TwoBodyAOInt](#)

## Parameters

<i>tei</i>	- two body integral object
------------	----------------------------

Implements [oepdev::ShellCombinationsIterator](#).

The documentation for this class was generated from the following files:

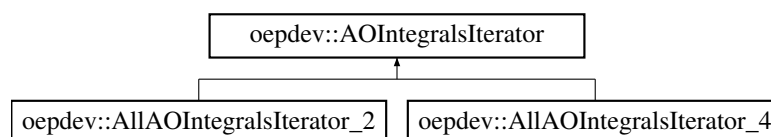
- [oepdev/libutil/integrals\\_iter.h](#)
- [oepdev/libutil/integrals\\_iter.cc](#)

## 17.6 oepdev::AOIntegralsIterator Class Reference

Iterator for AO Integrals. Abstract Base.

```
#include <integrals_iter.h>
```

Inheritance diagram for oepdev::AOIntegralsIterator:



## Public Member Functions

- [AOIntegralsIterator](#) ()  
*Base Constructor.*
- virtual [~AOIntegralsIterator](#) ()  
*Base Destructor.*
- virtual void [first](#) (void)=0  
*Do the first iteration.*
- virtual void [next](#) (void)=0  
*Do the next iteration.*
- virtual int [i](#) (void) const  
*Grab i-th index.*
- virtual int [j](#) (void) const

- Grab j-th index.*
- virtual int [k](#) (void) const
- Grab k-th index.*
- virtual int [l](#) (void) const
- Grab l-th index.*
- virtual int [index](#) (void) const =0
- Grab index in the integral buffer.*
- virtual bool [is\\_done](#) (void)
- Returns the status of an iterator.*

### Static Public Member Functions

- static std::shared\_ptr  
< [AOIntegralsIterator](#) > [build](#) (const [ShellCombinationsIterator](#) \*shellIter, std::string mode="ALL")
- static std::shared\_ptr  
< [AOIntegralsIterator](#) > [build](#) (std::shared\_ptr< [ShellCombinationsIterator](#) > shellIter, std::string mode="ALL")

### Protected Attributes

- bool [done](#)
- The status of an iterator.*

## 17.6.1 Detailed Description

Iterator for AO Integrals. Abstract Base.

## 17.6.2 Member Function Documentation

**17.6.2.1** `std::shared_ptr< AOIntegralsIterator > AOIntegralsIterator::build ( const ShellCombinationsIterator *  
shellIter, std::string mode = "ALL" ) [static]`

Build AO integrals iterator from current state of iterator over shells

Parameters

<a href="#">shellIter</a>	- iterator over shells - either "ALL" or "UNIQUE" (iterate over all or unique integrals)
---------------------------	--

Returns

iterator over AO integrals

**17.6.2.2** `std::shared_ptr< AOIntegralsIterator > AOIntegralsIterator::build ( std::shared_ptr<  
ShellCombinationsIterator > shellIter, std::string mode = "ALL" ) [static]`

This is an overloaded member function, provided for convenience. It differs from the above function only in what argument(s) it accepts.

The documentation for this class was generated from the following files:

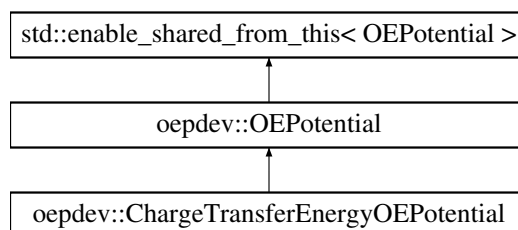
- oepdev/libutil/[integrals\\_iter.h](#)
- oepdev/libutil/[integrals\\_iter.cc](#)

## 17.7 oepdev::ChargeTransferEnergyOEPotential Class Reference

Generalized One-Electron Potential for Charge-Transfer Interaction Energy.

```
#include <oep.h>
```

Inheritance diagram for oepdev::ChargeTransferEnergyOEPotential:



### Public Member Functions

- **ChargeTransferEnergyOEPotential** (SharedWavefunction [wfn](#), SharedBasisSet auxiliary, Options &options)
- **ChargeTransferEnergyOEPotential** (SharedWavefunction [wfn](#), Options &options)
- virtual void [compute](#) (const std::string &oepType) override  
*Compute matrix forms of all OEP's within a specified OEP type.*
- virtual void [compute\\_3D](#) (const std::string &oepType, const double &x, const double &y, const double &z, double &v) override  
*Compute value of potential in point x, y, z and save at v.*
- virtual void **print\_header** () const override

### Additional Inherited Members

#### 17.7.1 Detailed Description

Generalized One-Electron Potential for Charge-Transfer Interaction Energy.

Contains the following OEP types:

- `Otto-Ladik.V1` - DF-based term
- `Otto-Ladik.V2` - ESP-based term
- `Otto-Ladik.V3` - ESP-based term

The documentation for this class was generated from the following files:

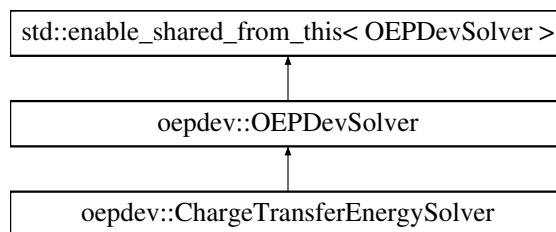
- oepdev/liboep/[oep.h](#)
- oepdev/liboep/oep.cc

## 17.8 oepdev::ChargeTransferEnergySolver Class Reference

Compute the Charge-Transfer interaction energy between unperturbed wavefunctions.

```
#include <solver.h>
```

Inheritance diagram for oepdev::ChargeTransferEnergySolver:



## Public Member Functions

- **ChargeTransferEnergySolver** (SharedWavefunctionUnion wfn\_union)
- virtual double [compute\\_oeplibased](#) (const std::string &method="DEFAULT")  
*Compute property by using OEP's.*
- virtual double [compute\\_benchmark](#) (const std::string &method="DEFAULT")  
*Compute property by using benchmark method.*

## Additional Inherited Members

### 17.8.1 Detailed Description

Compute the Charge-Transfer interaction energy between unperturbed wavefunctions.

The implemented methods are shown below

Keyword	Method Description
<b>Benchmark Methods</b>	
OTTO_LADIK	*Default*. CT energy at HF level from Otto and Ladik (1975).
EFP2	CT energy at HF level from EFP2 model.
<b>OEP-Based Methods</b>	
OTTO_LADIK	*Default*. OEP-based Otto-Ladik expressions.

Table 17.1: Methods available in the Solver

In order to construct this solver, **always** use the [OEPDevSolver::build](#) static factory method.

Below the detailed description of the implemented equations is given for each of the above provided methods. In the formulae across, it is assumed that the orbitals are real. The Coulomb notation for electron repulsion integrals (ERI's) is adopted; i.e,

$$(ac|bd) = \iint d\mathbf{r}_1 d\mathbf{r}_2 \phi_a(\mathbf{r}_1) \phi_c(\mathbf{r}_1) \frac{1}{r_{12}} \phi_b(\mathbf{r}_2) \phi_d(\mathbf{r}_2)$$

Greek subscripts denote basis set orbitals whereas Italic subscripts denote the occupied molecular orbitals.

The CT energy between molecules *A* and *B* is given by

$$E^{\text{CT}} = E^{A^+B^-} + E^{A^-B^+}$$

## Benchmark Methods

CT energy at HF level by Otto and Ladik (1975).

For a closed-shell system, CT energy equation of Otto and Ladik becomes

$$E^{A+B^-} \approx 2 \sum_{i \in A}^{\text{Occ}_A} \sum_{n \in B}^{\text{Vir}_B} \frac{V_{in}^2}{\epsilon_i - \epsilon_n}$$

where

$$V_{in} = V_{in}^B + 2 \sum_{j \in B}^{\text{Occ}_B} (in|jj) - \sum_{k \in A}^{\text{Occ}_A} S_{kn} \left\{ V_{ik}^B + 2 \sum_{j \in B}^{\text{Occ}_B} (ik|jj) \right\} \\ - \sum_{j \in B}^{\text{Occ}_B} \left[ S_{ij} \left\{ V_{nj}^A + 2 \sum_{k \in A}^{\text{Occ}_A} (1 - \delta_{ik})(nj|kk) \right\} - (nj|ij) \right] + \sum_{k \in A}^{\text{Occ}_A} \sum_{j \in B}^{\text{Occ}_B} S_{kj} (1 - \delta_{ik})(ik|nj)$$

and analogously the twin term.

CT energy at HF level by EFP2.

In EFP2 method, CT energy is given as

$$E^{A+B^-} \approx 2 \sum_{i \in A}^{\text{Occ}_A} \sum_{n \in B}^{\text{Vir}_B} \frac{V_{in}^2}{F_{ii} - T_{nn}}$$

where

$$V_{in}^2 = \frac{V_{in}^B - \sum_{m \in A}^{\text{All}_A} V_{im} S_{mn}^B}{1 - \sum_{m \in A}^{\text{All}_A} S_{mn}^2} \left\{ V_{in}^B - \sum_{m \in A}^{\text{All}_A} V_{im}^B S_{mn} + \sum_{j \in B}^{\text{Occ}_B} S_{ij} \left( T_{nj} - \sum_{m \in A}^{\text{All}_A} S_{nm} T_{mj} \right) \right\}$$

and analogously the twin term.

## OEP-Based Methods

OEP-Based Otto-Ladik's theory

After introducing OEP's, the original Otto-Ladik's theory is reformulated *without* approximation as

$$E^{A+B^-} \approx 2 \sum_{i \in A}^{\text{Occ}_A} \sum_{n \in B}^{\text{Vir}_B} \frac{\left( V_{in}^{\text{DF}} + V_{in}^{\text{ESP},A} + V_{in}^{\text{ESP},B} \right)^2}{\epsilon_i - \epsilon_n}$$

where

$$V_{in}^{\text{DF}} = \sum_{\eta \in B}^{\text{Aux}_B} S_{i\eta} G_{\eta n}^B \\ V_{in}^{\text{ESP},A} = \sum_{k \in A}^{\text{Occ}_A} \sum_{j \in B}^{\text{Occ}_B} S_{kj} \sum_{x \in A} V_{nj}^{(x)} q_{ik}^{(x)} \\ V_{in}^{\text{ESP},B} = - \sum_{k \in A}^{\text{Occ}_A} S_{kn} V_{ik}^B$$

The OEP matrix for density fitted part is given by

$$G_{\eta n}^B = \sum_{\eta' \in B}^{\text{Aux}_B} [S^{-1}]_{\eta\eta'} \left\{ V_{\eta'n}^B + \sum_{j \in B}^{\text{Occ}_B} [2(\eta'n|jj) - (\eta'j|nj)] \right\}$$



The OEP ESP-A charges are fit to reproduce the OEP potential

$$v_{ik}^A(\mathbf{r}) \equiv (1 - \delta_{ik}) \int \frac{\phi_i(\mathbf{r}')\phi_k(\mathbf{r}')}{|\mathbf{r} - \mathbf{r}'|} d\mathbf{r}' - \delta_{ik} \left( \sum_{x \in A} \frac{-Z_x}{|\mathbf{r} - \mathbf{r}_x|} + 2 \sum_{k \in A}^{\text{Occ}_A} \int \frac{\phi_k(\mathbf{r}')\phi_k(\mathbf{r}')}{|\mathbf{r} - \mathbf{r}'|} d\mathbf{r}' - 2 \int \frac{\phi_i(\mathbf{r}')\phi_i(\mathbf{r}')}{|\mathbf{r} - \mathbf{r}'|} d\mathbf{r}' \right)$$

so that

$$v_{ik}^A(\mathbf{r}) \cong \sum_{x \in A} \frac{q_{ik}^{(x)}}{|\mathbf{r} - \mathbf{r}_x|}$$

The OEP ESP-B charges are fit to reproduce the electrostatic potential of molecule *B* (they are standard ESP charges).

## 17.8.2 Member Function Documentation

**17.8.2.1** `double ChargeTransferEnergySolver::compute_benchmark ( const std::string & method = "DEFAULT" )`  
[virtual]

Compute property by using benchmark method.

Each solver object has one `DEFAULT` benchmark method

Parameters

<i>method</i>	- benchmark method
---------------	--------------------

Implements [oepdev::OEPDevSolver](#).

**17.8.2.2** `double ChargeTransferEnergySolver::compute_oep_based ( const std::string & method = "DEFAULT" )`  
[virtual]

Compute property by using OEP's.

Each solver object has one `DEFAULT` OEP-based method.

Parameters

<i>method</i>	- flavour of OEP model
---------------	------------------------

Implements [oepdev::OEPDevSolver](#).

The documentation for this class was generated from the following files:

- [oepdev/libutil/solver.h](#)
- [oepdev/libutil/solver.cc](#)

## 17.9 oepdev::CPHF Class Reference

[CPHF](#) solver class.

```
#include <cphf.h>
```

### Public Member Functions

- [CPHF](#) (SharedWavefunction ref\_wfn, Options &[options](#))  
*Constructor.*
- [~CPHF](#) ()  
*Destructor.*
- void [compute](#) (void)

- run the calculations*
- void `print` (void) const  
*print to output file*
- int `nocc` (void) const  
*get the number of occupied orbitals*
- std::shared\_ptr< Wavefunction > `wfn` (void) const  
*grab the wavefunction*
- Options & `options` (void) const  
*grab the Psi4 options*
- std::shared\_ptr< Matrix > `polarizability` (void) const  
*retrieve the molecular (total) polarizability*
- std::shared\_ptr< Matrix > `polarizability` (int i) const  
*retrieve the i-th orbital-associated polarizability*
- std::shared\_ptr< Matrix > `polarizability` (int i, int j) const  
*retrieve the charge-transfer polarizability associated with orbitals i and j*
- std::shared\_ptr< Matrix > `X` (int x) const  
*retrieve the X operator O-V perturbation matrix in AO basis for x-th component*
- std::shared\_ptr< Vector > `lmo_centroid` (int i) const  
*retrieve the i-th orbital (LMO) centroid*
- std::shared\_ptr< Localizer > `localizer` (void) const  
*retrieve the orbital localizer*

## Protected Attributes

- std::shared\_ptr  
  < psi::Wavefunction > `_wfn`  
  *Wavefunction object.*
- std::shared\_ptr< Localizer > `_localizer`  
  *Orbital localizer.*
- const int `_no`  
  *Number of occupied orbitals.*
- const int `_nv`  
  *Number of virtual orbitals.*
- const int `_nn`  
  *Number of basis functions.*
- long int `_memory`  
  *Memory.*
- int `_maxiter`  
  *Maximum number of iterations.*
- double `_conv`  
  *CPHF convergence threshold.*
- bool `_with_diis`  
  *whether use DIIS or not*
- const int `_diis_dim`  
  *Size of subspace.*
- std::shared\_ptr< BasisSet > `_primary`  
  *Primary Basis Set.*
- std::shared\_ptr< Matrix > `_cocc`  
  *Occupied orbitals.*
- std::shared\_ptr< Matrix > `_cvir`

- Virtual orbitals.*
- `std::shared_ptr< Vector > _eps_occ`
- Occupied orbital energies.*
- `std::shared_ptr< Vector > _eps_vir`
- Virtual orbital energies.*
- `std::vector< std::shared_ptr< oepdev::DIISManager > > _diis`  
*the DIIS managers for each perturbation operator x, y and z*
- Options & `_options`
- Options.*
- `std::shared_ptr< Matrix > _molecularPolarizability`  
*Total (molecular) polarizability tensor.*
- `std::vector< std::shared_ptr< Vector > > _orbitalCentroids`  
*LMO centroids.*
- `std::vector< std::shared_ptr< Matrix > > _orbitalPolarizabilities`  
*orbital-associated polarizability tensors*
- `std::vector< std::vector< std::shared_ptr< Matrix > > > _orbitalChargeTransferPolarizabilities`  
*orbital-orbital charge-transfer polarizability tensors*
- `std::vector< std::shared_ptr< Matrix > > _X_OV_ao_matrices`  
*Perturbation X Operator O->V matrices in AO basis.*

### 17.9.1 Detailed Description

**CPHF** solver class.

Solves **CPHF** equations (now only for RHF wavefunction). Computes molecular and polarizabilities associated with the localized molecular orbitals (LMO).

#### Note

Useful options:

- `CPHF_CONVER` - convergence of **CPHF**. Default: `1e-8 (au)`
- `CPHF_CONVER` - maximum number of iterations. Default: `50`
- `CPHF_DIIS` - wheather use DIIS or not. Default: `True`
- `CPHF_DIIS_DIM` - dimension of iterative subspace. Default: `3`
- `CPHF_LOCALIZER` - set orbital localization method. Available: `BOYS` and `PIPEK_MEZEY`. Default: `BOYS`

### 17.9.2 Constructor & Destructor Documentation

#### 17.9.2.1 `oepdev::CPHF::CPHF ( SharedWavefunction ref_wfn, Options & options )`

Constructor.

Parameters

---

<i>ref_wfn</i>	reference HF wavefunction
<i>options</i>	set of Psi4 options

The documentation for this class was generated from the following files:

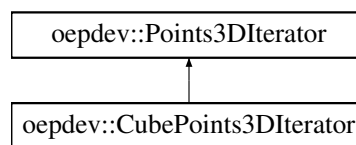
- oepdev/libutil/cphf.h
- oepdev/libutil/cphf.cc

## 17.10 oepdev::CubePoints3DIterator Class Reference

Iterator over a collection of points in 3D space. g09 Cube-like order.

```
#include <space3d.h>
```

Inheritance diagram for oepdev::CubePoints3DIterator:



### Public Member Functions

- **CubePoints3DIterator** (const int &nx, const int &ny, const int &nz, const double &dx, const double &dy, const double &dz, const double &ox, const double &oy, const double &oz)
- virtual void [first](#) ()  
*Initialize first iteration.*
- virtual void [next](#) ()  
*Step to next iteration.*

### Protected Attributes

- const int **nx\_**
- const int **ny\_**
- const int **nz\_**
- const double **dx\_**
- const double **dy\_**
- const double **dz\_**
- const double **ox\_**
- const double **oy\_**
- const double **oz\_**
- int **ii\_**
- int **jj\_**
- int **kk\_**

### Additional Inherited Members

#### 17.10.1 Detailed Description

Iterator over a collection of points in 3D space. g09 Cube-like order.

**Note:** Always create instances by using static factory method from [Points3DIterator](#). Do not use constructor of this class.

The documentation for this class was generated from the following files:

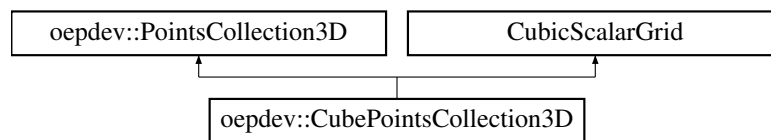
- oepdev/libutil/space3d.h
- oepdev/libutil/space3d.cc

## 17.11 oepdev::CubePointsCollection3D Class Reference

G09 cube-like ordered collection of points in 3D space.

```
#include <space3d.h>
```

Inheritance diagram for oepdev::CubePointsCollection3D:



### Public Member Functions

- **CubePointsCollection3D** ([Collection](#) collectionType, const int &nx, const int &ny, const int &nz, const double &px, const double &py, const double &pz, psi::SharedBasisSet bs, psi::Options &options)
- virtual void [print](#) () const  
*Print the information to Psi4 output file.*
- virtual void **write\_cube\_file** (psi::SharedMatrix v, const std::string &name)

### Additional Inherited Members

#### 17.11.1 Detailed Description

G09 cube-like ordered collection of points in 3D space.

**Note:** Do not use constructors of this class explicitly. Instead, use static factory methods of the superclass to create instances.

The documentation for this class was generated from the following files:

- oepdev/libutil/space3d.h
- oepdev/libutil/space3d.cc

## 17.12 oepdev::DIISManager Class Reference

DIIS manager.

```
#include <diis.h>
```

### Public Member Functions

- [DIISManager](#) (int dim, int na, int nb)
- [~DIISManager](#) ()

*Destructor.*

- void [put](#) (const std::shared\_ptr< const Matrix > &error, const std::shared\_ptr< const Matrix > &vector)
- void [compute](#) (void)
- void [update](#) (std::shared\_ptr< Matrix > &other)

### 17.12.1 Detailed Description

DIIS manager.

Instance can interact directly with the process of solving vector quantities in iterative manner. One needs to pass the dimensions of solution vector as well as the DIIS subspace size. The iterative procedure requires providing the current vector and also an estimate of the error vector. The updated DIIS vector can be copied to an old vector through the Instance.

### 17.12.2 Constructor & Destructor Documentation

#### 17.12.2.1 oepdev::DIISManager::DIISManager ( int *dim*, int *na*, int *nb* )

Constructor.

Parameters

<i>dim</i>	Size of DIIS subspace
<i>na</i>	Number of solution rows
<i>nb</i>	Number of solution columns

### 17.12.3 Member Function Documentation

#### 17.12.3.1 void oepdev::DIISManager::compute ( void )

Perform DIIS interpolation.

#### 17.12.3.2 void oepdev::DIISManager::put ( const std::shared\_ptr< const Matrix > & *error*, const std::shared\_ptr< const Matrix > & *vector* )

Put the current solution to the DIIS manager.

Parameters

<i>error</i>	Shared matrix with current solution error
<i>vector</i>	Shared matrix with current solution vector

#### 17.12.3.3 void oepdev::DIISManager::update ( std::shared\_ptr< Matrix > & *other* )

Update solution vector. Pass the Shared pointer to current solution. Then it will be overridden by the updated DIIS solution.

The documentation for this class was generated from the following files:

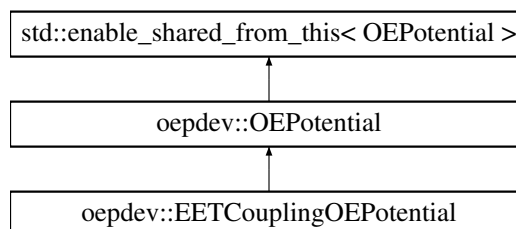
- oepdev/libutil/[diis.h](#)
- oepdev/libutil/diis.cc

## 17.13 oepdev::EETCouplingOEPotential Class Reference

Generalized One-Electron Potential for EET coupling calculations.

```
#include <oep.h>
```

Inheritance diagram for oepdev::EETCouplingOEPotential:



### Public Member Functions

- **EETCouplingOEPotential** (SharedWavefunction [wfn](#), SharedBasisSet auxiliary, Options &options)
- **EETCouplingOEPotential** (SharedWavefunction [wfn](#), Options &options)
- virtual void [compute](#) (const std::string &oepType) override  
*Compute matrix forms of all OEP's within a specified OEP type.*
- virtual void [compute\\_3D](#) (const std::string &oepType, const double &x, const double &y, const double &z, double &v) override  
*Compute value of potential in point x, y, z and save at v.*
- virtual void **print\_header** () const override

### Additional Inherited Members

#### 17.13.1 Detailed Description

Generalized One-Electron Potential for EET coupling calculations.

Contains the following OEP types:

- Fujimoto.ET1
- Fujimoto.ET2
- Fujimoto.HT1
- Fujimoto.HT1
- Fujimoto.HT2
- Fujimoto.CT1
- Fujimoto.CT2

The documentation for this class was generated from the following files:

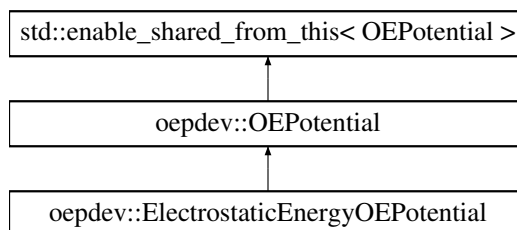
- oepdev/liboep/[oep.h](#)
- oepdev/liboep/oep.cc

## 17.14 oepdev::ElectrostaticEnergyOEPotential Class Reference

Generalized One-Electron Potential for Electrostatic Energy.

```
#include <oep.h>
```

Inheritance diagram for oepdev::ElectrostaticEnergyOEPotential:



### Public Member Functions

- [ElectrostaticEnergyOEPotential](#) (SharedWavefunction [wfn](#), Options &options)  
*Only ESP-based potential is worth implementing.*
- virtual void [compute](#) (const std::string &oepType) override  
*Compute matrix forms of all OEP's within a specified OEP type.*
- virtual void [compute\\_3D](#) (const std::string &oepType, const double &x, const double &y, const double &z, double &v) override  
*Compute value of potential in point x, y, z and save at v.*
- virtual void **print\_header** () const override

### Additional Inherited Members

#### 17.14.1 Detailed Description

Generalized One-Electron Potential for Electrostatic Energy.

Contains the following OEP types:

- $V$

The documentation for this class was generated from the following files:

- oepdev/liboep/[oep.h](#)
- oepdev/liboep/oep.cc

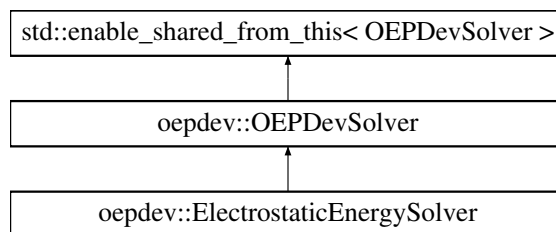
## 17.15 oepdev::ElectrostaticEnergySolver Class Reference

Compute the Coulombic interaction energy between unperturbed wavefunctions.

```
#include <solver.h>
```

Inheritance diagram for oepdev::ElectrostaticEnergySolver:





## Public Member Functions

- **ElectrostaticEnergySolver** (SharedWavefunctionUnion wfn\_union)
- virtual double [compute\\_oep\\_based](#) (const std::string &method="DEFAULT")  
*Compute property by using OEP's.*
- virtual double [compute\\_benchmark](#) (const std::string &method="DEFAULT")  
*Compute property by using benchmark method.*

## Additional Inherited Members

### 17.15.1 Detailed Description

Compute the Coulombic interaction energy between unperturbed wavefunctions.

The implemented methods are shown in below

Keyword	Method Description
<b>Benchmark Methods</b>	
AO_EXPANDED	*Default*. Exact Coulombic energy from atomic orbital expansions.
MO_EXPANDED	Exact Coulombic energy from molecular orbital expansions
<b>OEP-Based Methods</b>	
ESP_SYMMETRIZED	*Default*. Coulombic energy from ESP charges interacting with nuclei and electronic density. Symmetrized with respect to monomers.

Table 17.2: Methods available in the Solver

Below the detailed description of the above methods is given.

## Benchmark Methods

Exact Coulombic energy from atomic orbital expansions.

The Coulombic interaction energy is given by

$$E^{\text{Coul}} = E^{\text{Nuc-Nuc}} + E^{\text{Nuc-El}} + E^{\text{El-El}}$$

where the nuclear-nuclear repulsion energy is

$$E^{\text{Nuc-Nuc}} = \sum_{x \in A} \sum_{y \in B} \frac{Z_x Z_y}{|\mathbf{r}_x - \mathbf{r}_y|}$$

the nuclear-electronic attraction energy is

$$E^{\text{Nuc-EI}} = \sum_{x \in A} \sum_{\lambda \sigma \in B} Z_x V_{\lambda \sigma}^{(x)} (D_{\lambda \sigma}^{(\alpha)} + D_{\lambda \sigma}^{(\beta)}) + \sum_{y \in B} \sum_{\mu \nu \in A} Z_y V_{\mu \nu}^{(y)} (D_{\mu \nu}^{(\alpha)} + D_{\mu \nu}^{(\beta)})$$

and the electron-electron repulsion energy is

$$E^{\text{EI-EI}} = \sum_{\mu \nu \in A} \sum_{\lambda \sigma \in B} \{D_{\mu \nu}^{(\alpha)} + D_{\mu \nu}^{(\beta)}\} \{D_{\lambda \sigma}^{(\alpha)} + D_{\lambda \sigma}^{(\beta)}\} (\mu \nu | \lambda \sigma)$$

In the above equations,

$$V_{\lambda \sigma}^{(x)} \equiv \int \frac{\phi_{\lambda}^*(\mathbf{r}) \phi_{\sigma}(\mathbf{r})}{|\mathbf{r} - \mathbf{r}_x|} d\mathbf{r}$$

**Exact Coulombic energy from molecular orbital expansion.**

This approach is fully equivalent to the atomic orbital expansion shown above. For the closed shell case, the Coulombic interaction energy is given by

$$E^{\text{Coul}} = E^{\text{Nuc-Nuc}} + E^{\text{Nuc-EI}} + E^{\text{EI-EI}}$$

where the nuclear-nuclear repulsion energy is

$$E^{\text{Nuc-Nuc}} = \sum_{x \in A} \sum_{y \in B} \frac{Z_x Z_y}{|\mathbf{r}_x - \mathbf{r}_y|}$$

the nuclear-electronic attraction energy is

$$E^{\text{Nuc-EI}} = 2 \sum_{i \in A} \sum_{y \in B} V_{ii}^{(y)} + 2 \sum_{j \in B} \sum_{x \in A} V_{jj}^{(x)}$$

and the electron-electron repulsion energy is

$$E^{\text{EI-EI}} = 4 \sum_{i \in A} \sum_{j \in B} (ii | jj)$$

## OEP-Based Methods

**Coulombic energy from ESP charges interacting with nuclei and electronic density.**

In this approach, nuclear and electronic density of either species is approximated by ESP charges. In order to achieve symmetric expression, the interaction is computed twice (ESP of A interacting with density matrix and nuclear charges of B and vice versa) and then divided by 2. Thus,

$$E^{\text{Coul}} \approx \frac{1}{2} \left[ \sum_{x \in A} \sum_{y \in B} \frac{Z_x q_y}{|\mathbf{r}_x - \mathbf{r}_y|} + \sum_{y \in B} \sum_{\mu \nu \in A} q_y V_{\mu \nu}^{(y)} (D_{\mu \nu}^{(\alpha)} + D_{\mu \nu}^{(\beta)}) + \sum_{y \in B} \sum_{x \in A} \frac{q_x Z_y}{|\mathbf{r}_x - \mathbf{r}_y|} + \sum_{x \in A} \sum_{\lambda \sigma \in B} Z_x V_{\lambda \sigma}^{(x)} (D_{\lambda \sigma}^{(\alpha)} + D_{\lambda \sigma}^{(\beta)}) \right]$$

If the basis set is large and the number of ESP centres  $q_{x(y)}$  is sufficient, the sum of first two contributions equals the sum of the latter two contributions.

*Notes:*

- This solver also computes and prints the ESP-ESP point charge interaction energy,

$$E^{\text{Coul,ESP}} \approx \sum_{x \in A} \sum_{y \in B} \frac{q_x q_y}{|\mathbf{r}_x - \mathbf{r}_y|}$$

for reference purposes.

- In order to construct this solver, **always** use the `OEPDevSolver::build` static factory method.

### 17.15.2 Member Function Documentation

17.15.2.1 `double ElectrostaticEnergySolver::compute_benchmark ( const std::string & method = "DEFAULT" )`  
`[virtual]`

Compute property by using benchmark method.

Each solver object has one `DEFAULT` benchmark method

Parameters

<i>method</i>	- benchmark method
---------------	--------------------

Implements [oepdev::OEPDevSolver](#).

17.15.2.2 `double ElectrostaticEnergySolver::compute_oep_based ( const std::string & method = "DEFAULT" )`  
`[virtual]`

Compute property by using OEP's.

Each solver object has one `DEFAULT` OEP-based method.

Parameters

<i>method</i>	- flavour of OEP model
---------------	------------------------

Implements [oepdev::OEPDevSolver](#).

The documentation for this class was generated from the following files:

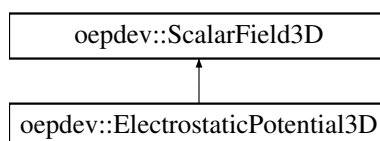
- [oepdev/libutil/solver.h](#)
- [oepdev/libutil/solver.cc](#)

## 17.16 oepdev::ElectrostaticPotential3D Class Reference

Electrostatic potential of a molecule.

```
#include <space3d.h>
```

Inheritance diagram for `oepdev::ElectrostaticPotential3D`:



### Public Member Functions

- **ElectrostaticPotential3D** (const int &np, const double &padding, psi::SharedWavefunction [wfn](#), psi::Options &options)
- **ElectrostaticPotential3D** (const int &nx, const int &ny, const int &nz, const double &px, const double &py, const double &pz, psi::SharedWavefunction [wfn](#), psi::Options &options)
- virtual double [compute\\_xyz](#) (const double &x, const double &y, const double &z)  
*Compute a value of scalar field at point (x, y, z)*
- virtual void [print](#) () const  
*Print information of the object to Psi4 output.*

## Additional Inherited Members

### 17.16.1 Detailed Description

Electrostatic potential of a molecule.

Computes the electrostatic potential of a molecule directly from the wavefunction. The electrostatic potential  $v(\mathbf{r})$  at point  $\mathbf{r}$  is computed from the following formula:

$$v(\mathbf{r}) = v_{\text{nuc}}(\mathbf{r}) + v_{\text{el}}(\mathbf{r})$$

where the nuclear and electronic contributions are defined accordingly as

$$v_{\text{nuc}}(\mathbf{r}) = \sum_x \frac{Z_x}{|\mathbf{r} - \mathbf{r}_x|}$$

$$v_{\text{el}}(\mathbf{r}) = \sum_{\mu\nu} \left\{ D_{\mu\nu}^{(\alpha)} + D_{\mu\nu}^{(\beta)} \right\} V_{\nu\mu}(\mathbf{r})$$

In the above equations,  $Z_x$  denotes the charge of  $x$ th nucleus,  $D_{\mu\nu}^{(\omega)}$  is the one-particle (relaxed) density matrix element in AO basis associated with the  $\omega$  electron spin, and  $V_{\mu\nu}(\mathbf{r})$  is the potential one-electron integral defined by

$$V_{\nu\mu}(\mathbf{r}) \equiv \int d\mathbf{r}' \phi_{\nu}^*(\mathbf{r}') \frac{1}{|\mathbf{r} - \mathbf{r}'|} \phi_{\mu}(\mathbf{r}')$$

The documentation for this class was generated from the following files:

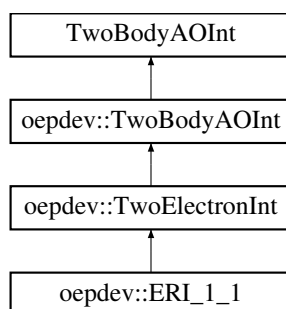
- oepdev/libutil/space3d.h
- oepdev/libutil/space3d.cc

## 17.17 oepdev::ERI\_1\_1 Class Reference

2-centre ERI of the form  $(a|O(2)|b)$  where  $O(2) = 1/r_{12}$ .

```
#include <eri.h>
```

Inheritance diagram for oepdev::ERI\_1\_1:



## Public Member Functions

- [ERI\\_1\\_1](#) (const [IntegralFactory](#) \*integral, int deriv=0, bool use\_shell\_pairs=false)  
*Constructor. Use [oepdev::IntegralFactory](#) to generate this object.*
- [~ERI\\_1\\_1](#) ()  
*Destructor.*

## Protected Member Functions

- `size_t compute_doublet` (int, int)  
*Compute ERI's between 2 shells.*

## Protected Attributes

- `double * mdh_buffer_1_`  
*Buffer for McMurchie-Davidson-Hermite coefficients for monomial expansion (shell 1)*
- `double * mdh_buffer_2_`  
*Buffer for McMurchie-Davidson-Hermite coefficients for monomial expansion (shell 2)*

### 17.17.1 Detailed Description

2-centre ERI of the form  $(a|O(2)|b)$  where  $O(2) = 1/r12$ .

ERI's are computed for a shell doublet  $(P|Q)$  and stored in the `target_full_` buffer, accessible through `buffer()` method:

$$\begin{aligned} &\text{For each } (n_1, l_1, m_1) \in P : \\ &\quad \text{For each } (n_2, l_2, m_2) \in Q : \\ &\quad \text{ERI} = (A|B)[\{\alpha\}, \mathbf{n}, \mathbf{l}, \mathbf{m}] \end{aligned}$$

For detailed description of the McMurchie-Davidson scheme, refer to [The Integral Package Library](#).

### 17.17.2 Implementation

A set of ERI's in a shell is decontracted as

$$(A|B)[\{\alpha\}, \mathbf{n}, \mathbf{l}, \mathbf{m}] = \sum_{ij} c_i(\alpha_1) c_j(\alpha_2) (i|j)[\{\alpha\}, \mathbf{n}, \mathbf{l}, \mathbf{m}]$$

where the primitive ERI is given by

$$(i|j)[\{\alpha\}, \mathbf{n}, \mathbf{l}, \mathbf{m}] = \sum_{N_1=0}^{n_1} \sum_{L_1=0}^{l_1} \sum_{M_1=0}^{m_1} \sum_{N_2=0}^{n_2} \sum_{L_2=0}^{l_2} \sum_{M_2=0}^{m_2} d_{N_1}^{n_1} d_{L_1}^{l_1} d_{M_1}^{m_1} d_{N_2}^{n_2} d_{L_2}^{l_2} d_{M_2}^{m_2} [N_1 L_1 M_1 | N_2 L_2 M_2]$$

The documentation for this class was generated from the following files:

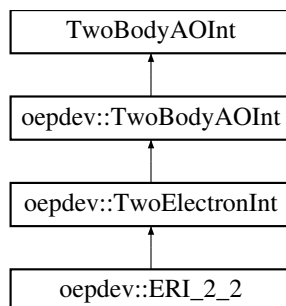
- `oepdev/libints/eri.h`
- `oepdev/libints/eri.cc`

## 17.18 oepdev::ERI\_2\_2 Class Reference

4-centre ERI of the form  $(ab|O(2)|cd)$  where  $O(2) = 1/r12$ .

```
#include <eri.h>
```

Inheritance diagram for `oepdev::ERI_2_2`:



## Public Member Functions

- [ERI\\_2\\_2](#) (const [IntegralFactory](#) \*integral, int deriv=0, bool use\_shell\_pairs=false)  
*Constructor. Use [oepdev::IntegralFactory](#) to generate this object.*
- [~ERI\\_2\\_2](#) ()  
*Destructor.*

## Protected Member Functions

- `size_t compute\_quartet (int, int, int, int)`  
*Compute ERI's between 4 shells.*

## Protected Attributes

- `double * mdh\_buffer\_12\_`  
*Buffer for McMurchie-Davidson-Hermite coefficients for binomial expansion (shells 1 and 2)*
- `double * mdh\_buffer\_34\_`  
*Buffer for McMurchie-Davidson-Hermite coefficients for binomial expansion (shells 3 and 4)*

### 17.18.1 Detailed Description

4-centre ERI of the form  $(ab|O(2)|cd)$  where  $O(2) = 1/r_{12}$ .

ERI's are computed for a shell quartet (PQ|RS) and stored in the `target_full_` buffer, accessible through `buffer()` method:

For each  $(n_1, l_1, m_1) \in P$  :  
 For each  $(n_2, l_2, m_2) \in Q$  :  
 For each  $(n_3, l_3, m_3) \in R$  :  
 For each  $(n_4, l_4, m_4) \in S$  :  
 $ERI = (AB|CD)[\{\alpha\}, \mathbf{n}, \mathbf{l}, \mathbf{m}]$

For detailed description of the McMurchie-Davidson scheme, refer to [The Integral Package Library](#).

### 17.18.2 Implementation

A set of ERI's in a shell is decontracted as

$$(AB|CD)[\{\alpha\}, \mathbf{n}, \mathbf{l}, \mathbf{m}] = \sum_{ijkl} c_i(\alpha_1) c_j(\alpha_2) c_k(\alpha_3) c_l(\alpha_4) (ij|kl)[\{\alpha\}, \mathbf{n}, \mathbf{l}, \mathbf{m}]$$

where the primitive ERI is given by

$$(ij|kl)[\{\alpha\}, \mathbf{n}, \mathbf{l}, \mathbf{m}] = E_{ij}(\alpha_1, \alpha_2) E_{kl}(\alpha_3, \alpha_4) \\ \times \sum_{N_1=0}^{n_1+n_2} \sum_{L_1=0}^{l_1+l_2} \sum_{M_1=0}^{m_1+m_2} \sum_{N_2=0}^{n_3+n_4} \sum_{L_2=0}^{l_3+l_4} \sum_{M_2=0}^{m_3+m_4} d_{N_1}^{n_1 n_2} d_{L_1}^{l_1 l_2} d_{M_1}^{m_1 m_2} d_{N_2}^{n_3 n_4} d_{L_2}^{l_3 l_4} d_{M_2}^{m_3 m_4} [N_1 L_1 M_1 | N_2 L_2 M_2]$$

In the above equation, the multiplicative constants are given as

$$E_{ij}(\alpha_1, \alpha_2) = \exp \left[ -\frac{\alpha_1 \alpha_2}{\alpha_1 + \alpha_2} |\mathbf{A} - \mathbf{B}|^2 \right] \\ E_{kl}(\alpha_3, \alpha_4) = \exp \left[ -\frac{\alpha_3 \alpha_4}{\alpha_3 + \alpha_4} |\mathbf{C} - \mathbf{D}|^2 \right]$$

The documentation for this class was generated from the following files:

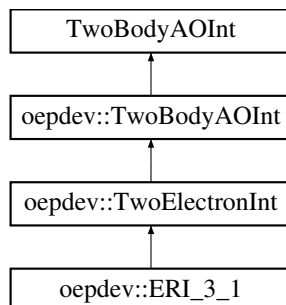
- oepdev/libints/eri.h
- oepdev/libints/eri.cc

## 17.19 oepdev::ERI\_3\_1 Class Reference

4-centre ERI of the form (abc|O(2)|d) where O(2) = 1/r<sup>12</sup>.

```
#include <eri.h>
```

Inheritance diagram for oepdev::ERI\_3\_1:



### Public Member Functions

- [ERI\\_3\\_1](#) (const [IntegralFactory](#) \*integral, int deriv=0, bool use\_shell\_pairs=false)  
*Constructor. Use [oepdev::IntegralFactory](#) to generate this object.*
- [~ERI\\_3\\_1](#) ()  
*Destructor.*

### Protected Member Functions

- [size\\_t compute\\_quartet](#) (int, int, int, int)  
*Compute ERI's between 4 shells.*

## Protected Attributes

- double \* `mdh_buffer_123_`  
*Buffer for McMurchie-Davidson-Hermite coefficients for trinomial expansion (shells 1, 2 and 3)*
- double \* `mdh_buffer_4_`  
*Buffer for McMurchie-Davidson-Hermite coefficients for monomial expansion (shell 4)*

### 17.19.1 Detailed Description

4-centre ERI of the form  $(abc|O(2)|d)$  where  $O(2) = 1/r12$ .

ERI's are computed for a shell quartet  $(PQR|S)$  and stored in the `target_full_` buffer, accessible through `buffer()` method:

For each  $(n_1, l_1, m_1) \in P$  :  
 For each  $(n_2, l_2, m_2) \in Q$  :  
 For each  $(n_3, l_3, m_3) \in R$  :  
 For each  $(n_4, l_4, m_4) \in S$  :  
 ERI =  $(ABC|D)[\{\alpha\}, \mathbf{n}, \mathbf{l}, \mathbf{m}]$

For detailed description of the McMurchie-Davidson scheme, refer to [The Integral Package Library](#).

### 17.19.2 Implementation

A set of ERI's in a shell is decontracted as

$$(ABC|D)[\{\alpha\}, \mathbf{n}, \mathbf{l}, \mathbf{m}] = \sum_{ijkl} c_i(\alpha_1) c_j(\alpha_2) c_k(\alpha_3) c_l(\alpha_4) (ijk|l)[\{\alpha\}, \mathbf{n}, \mathbf{l}, \mathbf{m}]$$

where the primitive ERI is given by

$$(ijk|l)[\{\alpha\}, \mathbf{n}, \mathbf{l}, \mathbf{m}] = E_{ijk}(\alpha_1, \alpha_2, \alpha_3) \times \sum_{N_1=0}^{n_1+n_2+n_3} \sum_{L_1=0}^{l_1+l_2+l_3} \sum_{M_1=0}^{m_1+m_2+m_3} \sum_{N_2=0}^{n_4} \sum_{L_2=0}^{l_4} \sum_{M_2=0}^{m_4} d_{N_1}^{n_1 n_2 n_3} d_{L_1}^{l_1 l_2 l_3} d_{M_1}^{m_1 m_2 m_3} d_{N_2}^{n_4} d_{L_2}^{l_4} d_{M_2}^{m_4} [N_1 L_1 M_1 | N_2 L_2 M_2]$$

In the above equation, the multiplicative constants are given as

$$E_{ijk}(\alpha_1, \alpha_2, \alpha_3) = \exp \left[ -\frac{\alpha_1 \alpha_2}{\alpha_1 + \alpha_2} |\mathbf{A} - \mathbf{B}|^2 \right] \exp \left[ -\frac{(\alpha_1 + \alpha_2) \alpha_3}{\alpha_1 + \alpha_2 + \alpha_3} |\mathbf{P} - \mathbf{C}|^2 \right]$$

The documentation for this class was generated from the following files:

- [oepdev/libints/eri.h](#)
- [oepdev/libints/eri.cc](#)

## 17.20 oepdev::ESPSolver Class Reference

Charges from Electrostatic Potential (ESP). A solver-type class.

```
#include <esp.h>
```



## Public Member Functions

- [ESPSolver](#) (SharedScalarField3D field)  
*Construct from scalar field.*
- [ESPSolver](#) (SharedScalarField3D field, psi::SharedMatrix [centres](#))  
*Construct from scalar field.*
- virtual [~ESPSolver](#) ()  
*Destructor.*
- virtual psi::SharedVector [charges](#) () const  
*Get the (fit) charges.*
- virtual psi::SharedMatrix [centres](#) () const  
*Get the charge distribution centres.*
- virtual void [compute](#) ()  
*Perform fitting of effective charges.*

## Protected Attributes

- const int [nCentres\\_](#)  
*Number of fit centres.*
- SharedScalarField3D [field\\_](#)  
*Scalar field.*
- psi::SharedVector [charges\\_](#)  
*Charges to be fit.*
- psi::SharedMatrix [centres\\_](#)  
*Centres, at which fit charges will reside.*

### 17.20.1 Detailed Description

Charges from Electrostatic Potential (ESP). A solver-type class.

Solves the least-squares problem to fit the generalized charges  $q_m$ , that reproduce the reference generalized potential  $v^{\text{ref}}(\mathbf{r})$  supplied by the [ScalarField3D](#) object:

$$\int d\mathbf{r}' \left[ v^{\text{ref}}(\mathbf{r}') - \sum_m \frac{q_m}{|\mathbf{r}' - \mathbf{r}_m|} \right]^2 \rightarrow \text{minimize}$$

The charges are subject to the following constraint:

$$\sum_m q_m = 0$$

**Method description.**

$M$  generalized charges is found by solving the matrix equation

$$\begin{pmatrix} \mathbf{A} & 0 \\ 0 & 1 \end{pmatrix}^{-1} \cdot \begin{pmatrix} \mathbf{b} \\ 0 \end{pmatrix} = \begin{pmatrix} \mathbf{q} \\ \lambda \end{pmatrix}$$

where the  $\mathbf{A}$  matrix of dimension  $M \times M$  and  $\mathbf{b}$  vector of length  $M$  are given as

$$A_{mn} = \sum_i \frac{1}{r_{im} r_{in}}$$

$$b_m = \sum_i \frac{v^{\text{ref}}(\mathbf{r}_m)}{r_{im}}$$

In the above equation, summations run over all sample points, at which reference potential is known.

## 17.20.2 Constructor & Destructor Documentation

### 17.20.2.1 oepdev::ESPSolver::ESPSolver ( SharedScalarField3D *field* )

Construct from scalar field.

Assume that the centres are on atoms associated with the scalar field.

Parameters

<i>field</i>	- oepdev scalar field object
--------------	------------------------------

### 17.20.2.2 oepdev::ESPSolver::ESPSolver ( SharedScalarField3D *field*, psi::SharedMatrix *centres* )

Construct from scalar field.

Solve ESP equations for a custom set of charge distribution centres.

Parameters

<i>field</i>	- oepdev scalar field object
<i>centres</i>	- matrix with coordinates of charge distribution centres

The documentation for this class was generated from the following files:

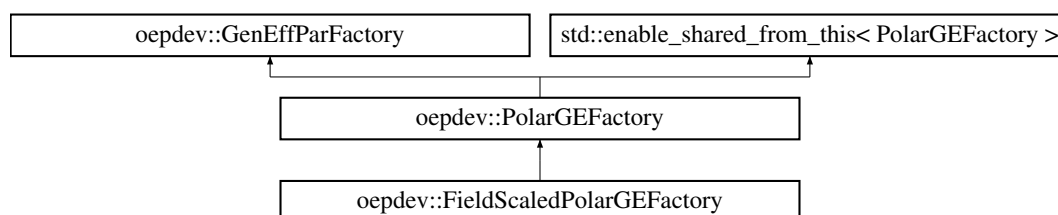
- oepdev/libutil/[esp.h](#)
- oepdev/libutil/[esp.cc](#)

## 17.21 oepdev::FieldScaledPolarGEFactory Class Reference

Polarization GEFP Factory with Least-Squares Scaling of Cartesian Degrees of freedom.

```
#include <gefp.h>
```

Inheritance diagram for oepdev::FieldScaledPolarGEFactory:



### Public Member Functions

- [FieldScaledPolarGEFactory](#) (std::shared\_ptr< [CPHF](#) > cphf, psi::Options &opt)  
Construct from [CPHF](#) object and Psi4 options.
- [FieldScaledPolarGEFactory](#) (std::shared\_ptr< [CPHF](#) > cphf)  
Construct from [CPHF](#) object only (options will be read from [CPHF](#) object)
- virtual [~FieldScaledPolarGEFactory](#) ()  
Destruct.
- std::shared\_ptr< [GenEffPar](#) > [compute](#) (void)  
Perform Least-Squares Fit.

## Additional Inherited Members

### 17.21.1 Detailed Description

Polarization GEFP Factory with Least-Squares Scaling of Cartesian Degrees of freedom.

The documentation for this class was generated from the following files:

- oepdev/libgefp/[gefp.h](#)
- oepdev/libgefp/gefp.cc

## 17.22 oepdev::Fourier9 Struct Reference

Simple structure to hold the Fourier series expansion coefficients for  $N=4$ .

```
#include <unitary_optimizer.h>
```

### Public Attributes

- double **a0**
- double **a1**
- double **a2**
- double **a3**
- double **a4**
- double **b1**
- double **b2**
- double **b3**
- double **b4**

### 17.22.1 Detailed Description

Simple structure to hold the Fourier series expansion coefficients for  $N=4$ .

The documentation for this struct was generated from the following file:

- oepdev/libutil/[unitary\\_optimizer.h](#)

## 17.23 oepdev::GenEffFrag Class Reference

Generalized Effective Fragment. Container Class.

```
#include <gefp.h>
```

### Public Member Functions

- [GenEffFrag](#) ()  
*Initialize with default name of GEFP (Default)*
- [GenEffFrag](#) (std::string name)  
*Initialize with custom name of GEFP.*
- [~GenEffFrag](#) ()  
*Destruct.*
- void [rotate](#) (std::shared\_ptr< psi::Matrix > R)

- Rotate.*
- void [translate](#) (std::shared\_ptr< psi::Vector > T)
- Translate.*
- void [superimpose](#) (std::shared\_ptr< psi::Matrix > targetXYZ, std::vector< int > supList)
- Superimpose.*
- void [set\\_gefp\\_polarization](#) (const std::shared\_ptr< [GenEffPar](#) > &par)
- Set the Density Matrix Susceptibility Tensors.*
- void [set\\_dmat\\_susceptibility](#) (const std::vector< std::vector< std::shared\_ptr< psi::Matrix >>> &susc)
- std::vector< std::shared\_ptr< psi::Matrix > > [susceptibility](#) (int i) const
- Grab the density matrix susceptibility tensor for the i-th LMO.*
- std::shared\_ptr< psi::Matrix > [susceptibility](#) (int i, int x) const
- Grab the density matrix susceptibility tensor x-th component for the i-th LMO.*

## Public Attributes

- std::map< std::string, std::shared\_ptr< [GenEffPar](#) > > [parameters](#)
- Dictionary of All GEF Parameters.*

## Protected Attributes

- std::string [name\\_](#)
- Name of GEFP.*
- std::shared\_ptr< [GenEffPar](#) > [densityMatrixSusceptibilityGEF\\_](#)
- Density Matrix Susceptibility Tensor.*
- std::shared\_ptr< [GenEffPar](#) > [electrostaticEnergyGEF\\_](#)
- Electrostatic Energy Effective One-Electron Potential.*
- std::shared\_ptr< [GenEffPar](#) > [repulsionEnergyGEF\\_](#)
- Exchange-Repulsion Effective One-Electron Potential.*
- std::shared\_ptr< [GenEffPar](#) > [chargeTransferEnergyGEF\\_](#)
- Charge-Transfer Effective One-Electron Potential.*
- std::shared\_ptr< [GenEffPar](#) > [EETCouplingConstantGEF\\_](#)
- EET Coupling Effective One-Electron Potential.*

### 17.23.1 Detailed Description

Generalized Effective Fragment. Container Class.

Describes the GEFP fragment that is in principle designed to work at correlated levels of theory.

The documentation for this class was generated from the following files:

- oepdev/libgefp/[gefp.h](#)
- oepdev/libgefp/[gefp.cc](#)

## 17.24 oepdev::GenEffPar Class Reference

Generalized Effective Fragment Parameters. Container Class.

```
#include <gefp.h>
```

## Public Member Functions

- [GenEffPar](#) (std::string name)  
*Create with name of this parameter type.*
- [~GenEffPar](#) ()  
*Destruct.*
- void [set\\_susceptibility](#) (const std::vector< std::vector< std::shared\_ptr< psi::Matrix >>> &susc)  
*Set The Density Matrix Susceptibility Tensors.*
- std::vector< std::shared\_ptr< psi::Matrix >> [susceptibility](#) (int i) const  
*Grab the density matrix susceptibility tensor for the i-th LMO.*
- std::shared\_ptr< psi::Matrix > [susceptibility](#) (int i, int x) const  
*Grab the density matrix susceptibility tensor x-th component for the i-th LMO.*

## Protected Attributes

- std::string [name\\_](#)  
*The Name of Parameter Type.*
- std::vector< std::vector< std::shared\_ptr< psi::Matrix >>> [densityMatrixSusceptibility\\_](#)  
*The Density Matrix Susceptibility Tensors.*

### 17.24.1 Detailed Description

Generalized Effective Fragment Parameters. Container Class.

The documentation for this class was generated from the following file:

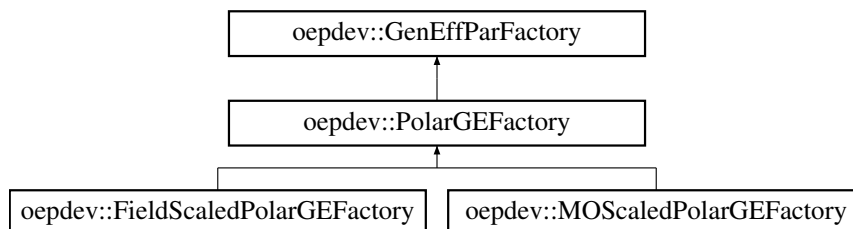
- [oepdev/libgefp/gefp.h](#)

## 17.25 oepdev::GenEffParFactory Class Reference

Generalized Effective Fragment Factory. Abstract Base.

```
#include <gefp.h>
```

Inheritance diagram for oepdev::GenEffParFactory:



## Public Member Functions

- [GenEffParFactory](#) (std::shared\_ptr< psi::Wavefunction > [wfn](#), psi::Options &opt)  
*Construct from wavefunction and Psi4 options.*
- virtual [~GenEffParFactory](#) ()  
*Destruct.*

- virtual std::shared\_ptr  
< [GenEffPar](#) > [compute](#) (void)=0  
*Compute the fragment parameters.*
- virtual std::shared\_ptr  
< psi::Wavefunction > [wfn](#) (void) const  
*Grab wavefunction.*
- virtual psi::Options & [options](#) (void) const  
*Grab options.*

### Protected Member Functions

- virtual double [random\\_double](#) ()  
*Draw random number.*
- virtual std::shared\_ptr  
< psi::Vector > [draw\\_random\\_point](#) ()
- virtual bool [is\\_in\\_vdWsphere](#) (double x, double y, double z) const

### Protected Attributes

- std::shared\_ptr  
< psi::Wavefunction > [wfn\\_](#)  
*Wavefunction.*
- psi::Options & [options\\_](#)  
*Psi4 Options.*
- std::default\_random\_engine [randomNumberGenerator\\_](#)  
*Random number generators.*
- std::uniform\_real\_distribution  
< double > [randomDistribution\\_](#)
- std::shared\_ptr< psi::Matrix > [excludeSpheres\\_](#)
- std::map< std::string, double > [vdwRadius\\_](#)
- double [cx\\_](#)
- double [cy\\_](#)
- double [cz\\_](#)
- double [radius\\_](#)

### 17.25.1 Detailed Description

Generalized Effective Fragment Factory. Abstract Base.

Describes the GEFP fragment that is in principle designed to work at correlated levels of theory.

The documentation for this class was generated from the following files:

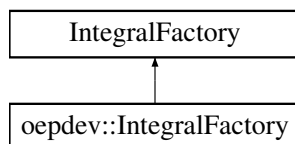
- oepdev/libgefp/[gefp.h](#)
- oepdev/libgefp/gefp.cc

## 17.26 oepdev::IntegralFactory Class Reference

Extended [IntegralFactory](#) for computing integrals.

```
#include <integral.h>
```

Inheritance diagram for oepdev::IntegralFactory:



## Public Member Functions

- [IntegralFactory](#) (std::shared\_ptr< psi::BasisSet > bs1, std::shared\_ptr< psi::BasisSet > bs2, std::shared\_ptr< psi::BasisSet > bs3, std::shared\_ptr< psi::BasisSet > bs4)  
*Initialize integral factory given a BasisSet for each center. Becomes (bs1 bs2 | bs3 bs4).*
- [IntegralFactory](#) (std::shared\_ptr< psi::BasisSet > bs1, std::shared\_ptr< psi::BasisSet > bs2)  
*Initialize integral factory given a BasisSet for two centres. Becomes (bs1 bs2 | bs1 bs2).*
- [IntegralFactory](#) (std::shared\_ptr< psi::BasisSet > bs1)  
*Initialize integral factory given a BasisSet for two centres. Becomes (bs1 bs1 | bs1 bs1).*
- virtual [~IntegralFactory](#) ()  
*Destructor.*
- virtual [oepdev::TwoBodyAOInt](#) \* [eri\\_1\\_1](#) (int deriv=0, bool use\_shell\_pairs=false)  
*Returns an [ERI\\_1\\_1](#) integral object.*
- virtual [oepdev::TwoBodyAOInt](#) \* [eri\\_2\\_1](#) (int deriv=0, bool use\_shell\_pairs=false)  
*Returns an [ERI\\_2\\_1](#) integral object.*
- virtual [oepdev::TwoBodyAOInt](#) \* [eri\\_2\\_2](#) (int deriv=0, bool use\_shell\_pairs=false)  
*Returns an [ERI\\_2\\_2](#) integral object.*
- virtual [oepdev::TwoBodyAOInt](#) \* [eri\\_3\\_1](#) (int deriv=0, bool use\_shell\_pairs=false)  
*Returns an [ERI\\_3\\_1](#) integral object.*

### 17.26.1 Detailed Description

Extended [IntegralFactory](#) for computing integrals.

In addition to integrals available in Psi4, [oepdev::IntegralFactory](#) enables to compute also:

- OEI's:
  - none at that moment
- ERI's:
  - integrals of type (a|b) - [oepdev::ERI\\_1\\_1](#)
  - integrals of type (ab|c) - [oepdev::ERI\\_2\\_1](#)
  - integrals of type (abc|d) - [oepdev::ERI\\_3\\_1](#)
  - integrals of type (ab|cd) - [oepdev::ERI\\_2\\_2](#) (also in Psi4 as `psi::ERI`)

The documentation for this class was generated from the following files:

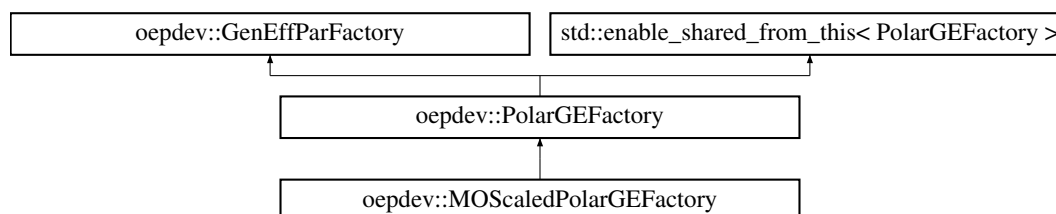
- [oepdev/libpsi/integral.h](#)
- [oepdev/libpsi/integral.cc](#)

## 17.27 oepdev::MOScaledPolarGEFactory Class Reference

Polarization GEFP Factory with Least-Squares Scaling of MO Space.

```
#include <gefp.h>
```

Inheritance diagram for oepdev::MOScaledPolarGEFactory:



### Public Member Functions

- [MOScaledPolarGEFactory](#) (std::shared\_ptr< [CPHF](#) > cphf, psi::Options &opt)  
*Construct from [CPHF](#) object and Psi4 options.*
- [MOScaledPolarGEFactory](#) (std::shared\_ptr< [CPHF](#) > cphf)  
*Construct from [CPHF](#) object only (options will be read from [CPHF](#) object)*
- virtual [~MOScaledPolarGEFactory](#) ()  
*Destruct.*
- std::shared\_ptr< [GenEffPar](#) > [compute](#) (void)  
*Peform Least-Squares Fit.*

### Additional Inherited Members

#### 17.27.1 Detailed Description

Polarization GEFP Factory with Least-Squares Scaling of MO Space.

The documentation for this class was generated from the following files:

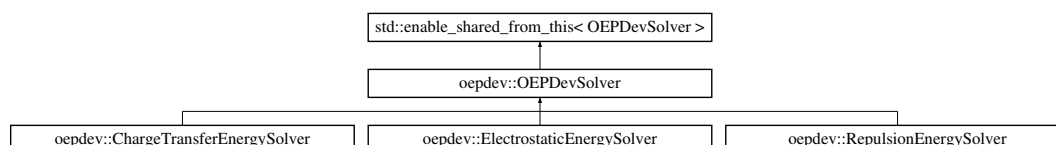
- oepdev/libgefp/[gefp.h](#)
- oepdev/libgefp/[gefp.cc](#)

## 17.28 oepdev::OEPDevSolver Class Reference

Solver of properties of molecular aggregates. Abstract base.

```
#include <solver.h>
```

Inheritance diagram for oepdev::OEPDevSolver:





## Public Member Functions

- [OEPDevSolver](#) (SharedWavefunctionUnion wfn\_union)  
*Take wavefunction union and initialize the Solver.*
- virtual [~OEPDevSolver](#) ()  
*Destructor.*
- virtual double [compute\\_oep\\_based](#) (const std::string &method="DEFAULT")=0  
*Compute property by using OEP's.*
- virtual double [compute\\_benchmark](#) (const std::string &method="DEFAULT")=0  
*Compute property by using benchmark method.*

## Static Public Member Functions

- static std::shared\_ptr  
< [OEPDevSolver](#) > [build](#) (const std::string &target, SharedWavefunctionUnion wfn\_union)  
*Build a solver of a particular property for given molecular cluster.*

## Protected Attributes

- SharedWavefunctionUnion [wfn\\_union\\_](#)  
*Wavefunction union.*
- std::vector< std::string > [methods\\_oepBased\\_](#)  
*Names of all OEP-based methods implemented for a solver.*
- std::vector< std::string > [methods\\_benchmark\\_](#)  
*Names of all benchmark methods implemented for a solver.*

### 17.28.1 Detailed Description

Solver of properties of molecular aggregates. Abstract base.

Uses only a wavefunction union object to initialize. Available solvers:

- ELECTROSTATIC ENERGY
- REPULSION ENERGY
- CHARGE TRANSFER ENERGY

### 17.28.2 Constructor & Destructor Documentation

#### 17.28.2.1 OEPDevSolver::OEPDevSolver ( SharedWavefunctionUnion wfn\_union )

Take wavefunction union and initialize the Solver.

Parameters

<i>wfn_union</i>	- wavefunction union of isolated molecular wavefunctions
------------------	--

### 17.28.3 Member Function Documentation

#### 17.28.3.1 std::shared\_ptr< OEPDevSolver > OEPDevSolver::build ( const std::string & target, SharedWavefunctionUnion wfn\_union ) [static]

Build a solver of a particular property for given molecular cluster.

## Parameters

<i>target</i>	- target property
<i>wfn_union</i>	- wavefunction union of isolated molecular wavefunctions

Implemented target properties:

- `ELECTROSTATIC_ENERGY` - Coulombic interaction energy between unperturbed wavefunctions.
- `REPULSION_ENERGY` - Pauli repulsion interaction energy between unperturbed wavefunctions.

## See Also

[ElectrostaticEnergySolver](#)

**17.28.3.2** `double OEPDevSolver::compute_benchmark ( const std::string & method = "DEFAULT" )` [pure virtual]

Compute property by using benchmark method.

Each solver object has one `DEFAULT` benchmark method

## Parameters

<i>method</i>	- benchmark method
---------------	--------------------

Implemented in [oepdev::ChargeTransferEnergySolver](#), [oepdev::RepulsionEnergySolver](#), and [oepdev::ElectrostaticEnergySolver](#).

**17.28.3.3** `double OEPDevSolver::compute_oep_based ( const std::string & method = "DEFAULT" )` [pure virtual]

Compute property by using OEP's.

Each solver object has one `DEFAULT` OEP-based method.

## Parameters

<i>method</i>	- flavour of OEP model
---------------	------------------------

Implemented in [oepdev::ChargeTransferEnergySolver](#), [oepdev::RepulsionEnergySolver](#), and [oepdev::ElectrostaticEnergySolver](#).

The documentation for this class was generated from the following files:

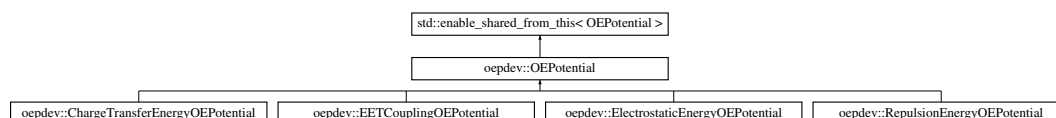
- [oepdev/libutil/solver.h](#)
- [oepdev/libutil/solver.cc](#)

## 17.29 oepdev::OEPotential Class Reference

Generalized One-Electron Potential: Abstract base.

```
#include <oep.h>
```

Inheritance diagram for `oepdev::OEPotential`:



## Public Member Functions

- **OEPotential** (SharedWavefunction [wfn](#), Options &options)  
*Fully ESP-based OEP object.*
- **OEPotential** (SharedWavefunction [wfn](#), SharedBasisSet auxiliary, Options &options)  
*General OEP object.*
- virtual **~OEPotential** ()  
*Destructor.*
- virtual void **compute** (void)  
*Compute matrix forms of all OEP's within all OEP types.*
- virtual void **compute** (const std::string &oepType)=0  
*Compute matrix forms of all OEP's within a specified OEP type.*
- virtual void **compute\_3D** (const std::string &oepType, const double &x, const double &y, const double &z, double &v)=0  
*Compute value of potential in point x, y, z and save at v.*
- virtual void **write\_cube** (const std::string &oepType, const std::string &fileName)  
*Write potential to a cube file.*
- virtual void **rotate** (const Matrix &rotmat)  
*Rotate.*
- virtual void **translate** (const Vector &trans)  
*Translate.*
- virtual void **superimpose** (const Matrix &refGeometry, const std::vector< int > &supList, const std::vector< int > &reordList)  
*Superimpose.*
- std::string **name** () const  
*Retrieve name of this OEP.*
- **OEPType** **oep** (const std::string &oepType) const  
*Retrieve the potentials.*
- SharedMatrix **matrix** (const std::string &oepType) const  
*Retrieve the potentials in a matrix form.*
- SharedWavefunction **wfn** () const  
*Retrieve wavefunction object.*
- void **set\_name** (const std::string &name)
- virtual void **print\_header** () const =0

## Static Public Member Functions

- static std::shared\_ptr  
< **OEPotential** > **build** (const std::string &category, SharedWavefunction [wfn](#), Options &options)  
*Build fully ESP-based OEP object.*
- static std::shared\_ptr  
< **OEPotential** > **build** (const std::string &category, SharedWavefunction [wfn](#), SharedBasisSet auxiliary, Options &options)  
*Build general OEP object.*

## Protected Attributes

- Options [options\\_](#)  
*Psi4 options.*
- SharedWavefunction [wfn\\_](#)  
*Wavefunction.*

- SharedBasisSet [primary\\_](#)  
*Primary Basis set.*
- SharedBasisSet [auxiliary\\_](#)  
*Auxiliary Basis set.*
- std::string [name\\_](#)  
*Name of this OEP.*
- std::map< std::string, [OEType](#) > [oepTypes\\_](#)  
*Types of OEP's within the scope of this object.*
- std::shared\_ptr  
< psi::IntegralFactory > [intsFactory\\_](#)  
*Integral factory.*
- std::shared\_ptr< psi::Matrix > [potMat\\_](#)  
*Matrix of potential one-electron integrals.*
- std::shared\_ptr  
< psi::OneBodyAOInt > [OEInt\\_](#)  
*One-electron integral shared pointer.*
- std::shared\_ptr< [PotentialInt](#) > [potInt\\_](#)  
*One-electron potential shared pointer.*

### 17.29.1 Detailed Description

Generalized One-Electron Potential: Abstract base.

Manages OEP's in matrix and 3D forms. Available OEP categories:

- ELECTROSTATIC ENERGY
- REPULSION ENERGY
- CHARGE TRANSFER ENERGY
- EET COUPLING CONSTANT

### 17.29.2 Constructor & Destructor Documentation

#### 17.29.2.1 OEPotential::OEPotential ( SharedWavefunction *wfn*, Options & *options* )

Fully ESP-based OEP object.

Parameters

<i>wfn</i>	- wavefunction
<i>options</i>	- Psi4 options

#### 17.29.2.2 OEPotential::OEPotential ( SharedWavefunction *wfn*, SharedBasisSet *auxiliary*, Options & *options* )

General OEP object.

Parameters

<i>wfn</i>	- wavefunction
------------	----------------

<i>auxiliary</i>	- basis set for density fitting of OEP's
<i>options</i>	- Psi4 options

### 17.29.3 Member Function Documentation

17.29.3.1 `std::shared_ptr< OEPotential > OEPotential::build ( const std::string & category, SharedWavefunction wfn, Options & options ) [static]`

Build fully ESP-based OEP object.

Parameters

<i>type</i>	- OEP category
<i>wfn</i>	- wavefunction
<i>options</i>	- Psi4 options

17.29.3.2 `std::shared_ptr< OEPotential > OEPotential::build ( const std::string & category, SharedWavefunction wfn, SharedBasisSet auxiliary, Options & options ) [static]`

Build general OEP object.

Parameters

<i>type</i>	- OEP category
<i>wfn</i>	- wavefunction
<i>auxiliary</i>	- basis set for density fitting of OEP's
<i>options</i>	- Psi4 options

The documentation for this class was generated from the following files:

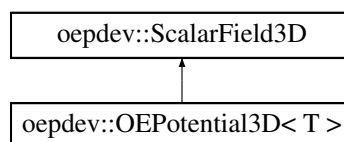
- oepdev/liboep/oep.h
- oepdev/liboep/oep.cc

## 17.30 oepdev::OEPotential3D< T > Class Template Reference

Class template for OEP scalar fields.

```
#include <space3d.h>
```

Inheritance diagram for oepdev::OEPotential3D< T >:



### Public Member Functions

- [OEPotential3D](#) (const int &np, const double &padding, std::shared\_ptr< T > oep, const std::string &oepType)  
*Construct random spherical collection of scalar field of type T.*
- [OEPotential3D](#) (const int &nx, const int &ny, const int &nz, const double &px, const double &py, const double &pz, std::shared\_ptr< T > oep, const std::string &oepType, psi::Options &options)  
*Construct ordered 3D collection of scalar field of type T.*

- virtual `~OEPotential3D()`  
*Destructor.*
- virtual double `compute_xyz` (const double &x, const double &y, const double &z)  
*Compute a value of scalar field at point (x, y, z)*
- virtual void `print()` const  
*Print information of the object to Psi4 output.*

## Protected Attributes

- `std::shared_ptr< T > oep_`  
*Shared pointer to the instance of class T*
- `std::string oepType_`  
*Descriptor of the scalar field type stored in instance of T*

## Additional Inherited Members

### 17.30.1 Detailed Description

`template<class T>class oepdev::OEPotential3D< T >`

Class template for OEP scalar fields.

Used for special type of classes T that contain following public member functions:

```
class T : public std::enable_shared_from_this<T> {
public:
    void compute_3D(const std::string& descriptor,
                  const double& x, const double& y, const double& z,
                  double& v);

    shared_ptr<psi::Wavefunction> wfn() const {return wfn_;}
};
```

with the `descriptor` of a certain scalar field type, `x`, `y`, `z` the points in 3D space in which the scalar field has to be computed and stored at `v`. Instances of `T` should store shared pointer to wavefunction object. List of classes `T` that are compatible with this class template and are currently implemented in `oepdev` is given below:

- `oepdev::OEPotential` abstract base (do not use derived classes as `T`)

Template parameters:

Template Parameters

<code>T</code>	the compatible class (e.g. <code>oepdev::OEPotential</code> )
----------------	---

The documentation for this class was generated from the following file:

- `oepdev/libutil/space3d.h`

## 17.31 oepdev::OEType Struct Reference

Container to handle the type of One-Electron Potentials.

```
#include <oep.h>
```

## Public Attributes

- std::string [name](#)  
*Name of this type of OEP.*
- bool [is\\_density\\_fitted](#)  
*Is this OEP DF-based?*
- int [n](#)  
*Number of OEP's within a type.*
- SharedMatrix [matrix](#)  
*All OEP's of this type gathered in a matrix form.*

### 17.31.1 Detailed Description

Container to handle the type of One-Electron Potentials.

The documentation for this struct was generated from the following file:

- [oepdev/liboep/oep.h](#)

## 17.32 oepdev::Points3DIterator::Point Struct Reference

## Public Attributes

- double **x**
- double **y**
- double **z**
- int **index**

The documentation for this struct was generated from the following file:

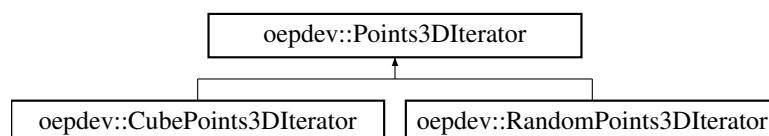
- [oepdev/libutil/space3d.h](#)

## 17.33 oepdev::Points3DIterator Class Reference

Iterator over a collection of points in 3D space. Abstract base.

```
#include <space3d.h>
```

Inheritance diagram for oepdev::Points3DIterator:



## Classes

- struct [Point](#)

## Public Member Functions

- [Points3DIterator](#) (const int &np)  
*Plain constructor. Initializes the abstract features.*
- virtual [~Points3DIterator](#) ()  
*Destructor.*
- virtual bool [is\\_done](#) ()  
*Check if iteration is finished.*
- virtual void [first](#) ()=0  
*Initialize first iteration.*
- virtual void [next](#) ()=0  
*Step to next iteration.*
  
- virtual double [x](#) () const
- virtual double [y](#) () const
- virtual double [z](#) () const
- virtual int [index](#) () const

## Static Public Member Functions

- static shared\_ptr  
< [Points3DIterator](#) > [build](#) (const int &nx, const int &ny, const int &nz, const double &dx, const double &dy, const double &dz, const double &ox, const double &oy, const double &oz)  
*Build G09 Cube collection iterator.*
- static shared\_ptr  
< [Points3DIterator](#) > [build](#) (const int &np, const double &radius, const double &cx, const double &cy, const double &cz)  
*Build random collection iterator.*
- static shared\_ptr  
< [Points3DIterator](#) > [build](#) (const int &np, const double &pad, psi::SharedMolecule mol)  
*Build random collection iterator.*

## Protected Attributes

- const int [np\\_](#)  
*Number of points.*
- bool [done\\_](#)  
*Status of the iterator.*
- int [index\\_](#)  
*Current index.*
  
- [Point](#) [current\\_](#)

### 17.33.1 Detailed Description

Iterator over a collection of points in 3D space. Abstract base.

Points3DIterators are constructed either as iterators over:

- a random collections or
- an ordered (g09 cube-like) collections. **Note:** Always create instances by using static factory methods.



### 17.33.2 Constructor & Destructor Documentation

#### 17.33.2.1 oepdev::Points3Dlterator::Points3Dlterator ( const int & *np* )

Plain constructor. Initializes the abstract features.

## Parameters

<i>np</i>	- number of points this iterator is constructed for
-----------	---

## 17.33.3 Member Function Documentation

17.33.3.1 `std::shared_ptr< Points3DIterator > oepdev::Points3DIterator::build ( const int & nx, const int & ny, const int & nz, const double & dx, const double & dy, const double & dz, const double & ox, const double & oy, const double & oz ) [static]`

Build G09 Cube collection iterator.

The points are generated according to Gaussian cube file format.

## Parameters

<i>nx</i>	- number of points along x direction
<i>ny</i>	- number of points along y direction
<i>nz</i>	- number of points along z direction
<i>dx</i>	- spacing distance along x direction
<i>dy</i>	- spacing distance along y direction
<i>dz</i>	- spacing distance along y direction
<i>ox</i>	- coordinate x of cube origin
<i>oy</i>	- coordinate y of cube origin
<i>oz</i>	- coordinate z of cube origin

17.33.3.2 `std::shared_ptr< Points3DIterator > oepdev::Points3DIterator::build ( const int & np, const double & radius, const double & cx, const double & cy, const double & cz ) [static]`

Build random collection iterator.

The points are drawn according to uniform distrinution in 3D space.

## Parameters

<i>np</i>	- number of points to draw
<i>radius</i>	- sphere radius inside which points are to be drawn
<i>cx</i>	- coordinate x of sphere's centre
<i>cy</i>	- coordinate y of sphere's centre
<i>cz</i>	- coordinate z of sphere's centre

17.33.3.3 `shared_ptr< Points3DIterator > oepdev::Points3DIterator::build ( const int & np, const double & pad, psi::SharedMolecule mol ) [static]`

Build random collection iterator.

The points are drawn according to uniform distrinution in 3D space enclosing a molecule given. All drawn points lie outside the van der Waals volume.

## Parameters

<i>np</i>	- number of points to draw
<i>pad</i>	- radius padding of a minimal sphere enclosing the molecule
<i>mol</i>	- Psi4 molecule object

The documentation for this class was generated from the following files:

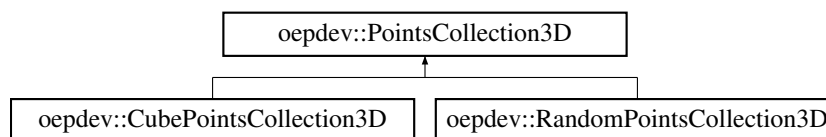
- oepdev/libutil/space3d.h
- oepdev/libutil/space3d.cc

## 17.34 oepdev::PointsCollection3D Class Reference

Collection of points in 3D space. Abstract base.

```
#include <space3d.h>
```

Inheritance diagram for oepdev::PointsCollection3D:



### Public Types

- enum [Collection](#) { **Random**, **Cube** }

*Public descriptor of collection type.*

### Public Member Functions

- [PointsCollection3D](#) ([Collection](#) collectionType, int &np)  
*Initialize abstract features.*
- **PointsCollection3D** ([Collection](#) collectionType, const int &np)
- virtual [~PointsCollection3D](#) ()  
*Destructor.*
- virtual int [npoints](#) () const  
*Get the number of points.*
- virtual shared\_ptr  
< [Points3DIterator](#) > [points\\_iterator](#) () const  
*Get the iterator over this collection of points.*
- virtual [Collection](#) [get\\_type](#) () const  
*Get the collection type.*
- virtual void [print](#) () const =0  
*Print the information to Psi4 output file.*

### Static Public Member Functions

- static shared\_ptr  
< [PointsCollection3D](#) > [build](#) (const int &[npoints](#), const double &radius, const double &cx=0.0, const double &cy=0.0, const double &cz=0.0)  
*Build random collection of points.*
- static shared\_ptr  
< [PointsCollection3D](#) > [build](#) (const int &[npoints](#), const double &padding, psi::SharedMolecule mol)  
*Build random collection of points.*
- static shared\_ptr  
< [PointsCollection3D](#) > [build](#) (const int &nx, const int &ny, const int &nz, const double &px, const double &py, const double &pz, psi::SharedBasisSet bs, psi::Options &options)  
*Build G09 Cube collection of points.*

## Protected Attributes

- const int `np_`  
*Number of points.*
- Collection `collectionType_`  
*Collection type.*
- shared\_ptr< `Points3DIterator` > `pointsIterator_`  
*iterator over points collection*

### 17.34.1 Detailed Description

Collection of points in 3D space. Abstract base.

Create random or ordered (g09 cube-like) collections of points in 3D space.

**Note:** Always create instances by using static factory methods.

### 17.34.2 Constructor & Destructor Documentation

17.34.2.1 `oepdev::PointsCollection3D::PointsCollection3D ( Collection collectionType, int & np )`

Initialize abstract features.

Parameters

<i>np</i>	- number of points to be created
-----------	----------------------------------

### 17.34.3 Member Function Documentation

17.34.3.1 `std::shared_ptr< PointsCollection3D > oepdev::PointsCollection3D::build ( const int & npoints, const double & radius, const double & cx = 0.0, const double & cy = 0.0, const double & cz = 0.0 ) [static]`

Build random collection of points.

Points uniformly span a sphere.

Parameters

<i>npoints</i>	- number of points to draw
<i>radius</i>	- sphere radius inside which points are to be drawn
<i>cx</i>	- coordinate x of sphere's centre
<i>cy</i>	- coordinate y of sphere's centre
<i>cz</i>	- coordinate z of sphere's centre

17.34.3.2 `std::shared_ptr< PointsCollection3D > oepdev::PointsCollection3D::build ( const int & npoints, const double & padding, psi::SharedMolecule mol ) [static]`

Build random collection of points.

Points uniformly span space inside a sphere enclosing a molecule. excluding the van der Waals volume.

Parameters

<i>np</i>	- number of points to draw
-----------	----------------------------

<i>padding</i>	- radius padding of a minimal sphere enclosing the molecule
<i>mol</i>	- Psi4 molecule object

17.34.3.3 `std::shared_ptr< PointsCollection3D > oepdev::PointsCollection3D::build ( const int & nx, const int & ny, const int & nz, const double & px, const double & py, const double & pz, psi::SharedBasisSet bs, psi::Options & options )`  
`[static]`

Build G09 Cube collection of points.

The points span a parallelepiped according to Gaussian cube file format.

Parameters

<i>nx</i>	- number of points along x direction
<i>ny</i>	- number of points along y direction
<i>nz</i>	- number of points along z direction
<i>px</i>	- padding distance along x direction
<i>py</i>	- padding distance along y direction
<i>pz</i>	- padding distance along z direction
<i>bs</i>	- Psi4 basis set object
<i>options</i>	- Psi4 options object

The documentation for this class was generated from the following files:

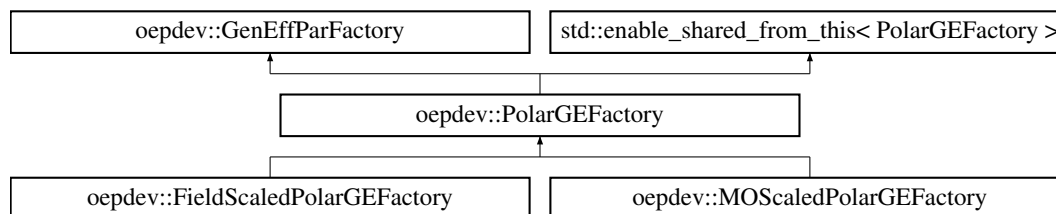
- oepdev/libutil/space3d.h
- oepdev/libutil/space3d.cc

## 17.35 oepdev::PolarGEFactory Class Reference

Polarization GEFP Factory.

```
#include <gefp.h>
```

Inheritance diagram for oepdev::PolarGEFactory:



### Public Member Functions

- [PolarGEFactory](#) (`std::shared_ptr< CPHF > cphf, psi::Options &opt`)  
Construct from [CPHF](#) object and Psi4 options.
- [PolarGEFactory](#) (`std::shared_ptr< CPHF > cphf`)  
Construct from [CPHF](#) object only (options will be read from [CPHF](#) object)
- virtual `~PolarGEFactory ()`  
Destruct.
- virtual `std::shared_ptr< GenEffPar > compute (void)`  
Compute the density matrix susceptibility tensors.

## Protected Member Functions

- `std::shared_ptr< psi::Vector > draw_field ()`  
*Randomly draw electric field value.*
- `std::shared_ptr< psi::Matrix > perturbed_dmat (const std::shared_ptr< psi::Vector > &field)`  
*Solve SCF equations to find perturbed one-particle density matrix due to uniform electric field.*
- `std::shared_ptr< psi::Matrix > perturbed_dmat (const std::shared_ptr< psi::Vector > &pos, const double &charge)`  
*Solve SCF equations to find perturbed one-particle density matrix due to point charge.*

## Protected Attributes

- `std::shared_ptr< CPHF > cphfSolver_`  
*The CPHF object.*

### 17.35.1 Detailed Description

Polarization GEFP Factory.

Implements creation of the density matrix susceptibility tensors.

The documentation for this class was generated from the following files:

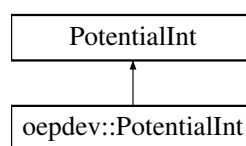
- `oepdev/libgefp/gefp.h`
- `oepdev/libgefp/gefp.cc`

## 17.36 oepdev::PotentialInt Class Reference

Computes potential integrals.

```
#include <potential.h>
```

Inheritance diagram for `oepdev::PotentialInt`:



## Public Member Functions

- `PotentialInt (std::vector< psi::SphericalTransform > &st, std::shared_ptr< psi::BasisSet > bs1, std::shared_ptr< psi::BasisSet > bs2, int deriv=0)`  
*Constructor. Initialize identically like in psi::Potentillnt.*
- `PotentialInt (std::vector< psi::SphericalTransform > &st, std::shared_ptr< psi::BasisSet > bs1, std::shared_ptr< psi::BasisSet > bs2, std::shared_ptr< psi::Matrix > Qxyz, int deriv=0)`  
*Constructor. Takes an arbitrary collection of charges.*
- `PotentialInt (std::vector< psi::SphericalTransform > &, std::shared_ptr< psi::BasisSet >, std::shared_ptr< psi::BasisSet >, const double &x, const double &y, const double &z, const double &q=1.0, int deriv=0)`  
*Constructor. Computes potential for one point x, y, z for a test particle of charge q.*
- `void set_charge_field (const double &x, const double &y, const double &z, const double &q=1.0)`  
*Mutator. Set the charge field to be a x, y, z point of charge q.*

### 17.36.1 Detailed Description

Computes potential integrals.

### 17.36.2 Constructor & Destructor Documentation

**17.36.2.1** `oepdev::PotentialInt::PotentialInt ( std::vector< psi::SphericalTransform > & st, std::shared_ptr< psi::BasisSet > bs1, std::shared_ptr< psi::BasisSet > bs2, int deriv = 0 )`

Constructor. Initialize identically like in psi::PotentillInt.

Parameters

<i>st</i>	- Spherical transform object
<i>bs1</i>	- basis set for first space
<i>bs2</i>	- basis set for second space
<i>deriv</i>	- derivative level

**17.36.2.2** `oepdev::PotentialInt::PotentialInt ( std::vector< psi::SphericalTransform > & st, std::shared_ptr< psi::BasisSet > bs1, std::shared_ptr< psi::BasisSet > bs2, std::shared_ptr< psi::Matrix > Qxyz, int deriv = 0 )`

Constructor. Takes an arbitrary collection of charges.

Parameters

<i>st</i>	- Spherical transform object
<i>bs1</i>	- basis set for first space
<i>bs2</i>	- basis set for second space
<i>Qxyz</i>	- matrix with charges and their positions
<i>deriv</i>	- derivative level

**17.36.2.3** `oepdev::PotentialInt::PotentialInt ( std::vector< psi::SphericalTransform > & st, std::shared_ptr< psi::BasisSet > bs1, std::shared_ptr< psi::BasisSet > bs2, const double & x, const double & y, const double & z, const double & q = 1.0, int deriv = 0 )`

Constructor. Computes potential for one point x, y, z for a test particle of charge q.

Parameters

<i>st</i>	- Spherical transform object
<i>bs1</i>	- basis set for first space
<i>bs2</i>	- basis set for second space
<i>x</i>	- x coordinate of q
<i>y</i>	- y coordinate of q
<i>z</i>	- z coordinate of q
<i>q</i>	- value of the probe charge
<i>deriv</i>	- derivative level

### 17.36.3 Member Function Documentation

**17.36.3.1** `void oepdev::PotentialInt::set_charge_field ( const double & x, const double & y, const double & z, const double & q = 1.0 )`

Mutator. Set the charge field to be a x, y, z point of charge q.

## Parameters

$x$	- x coordinate of $q$
$y$	- y coordinate of $q$
$z$	- z coordinate of $q$
$q$	- value of the probe charge

The documentation for this class was generated from the following files:

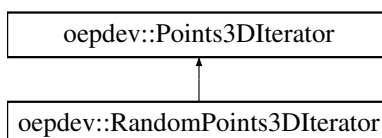
- oepdev/libpsi/[potential.h](#)
- oepdev/libpsi/potential.cc

## 17.37 oepdev::RandomPoints3DIterator Class Reference

Iterator over a collection of points in 3D space. Random collection.

```
#include <space3d.h>
```

Inheritance diagram for oepdev::RandomPoints3DIterator:



### Public Member Functions

- **RandomPoints3DIterator** (const int &np, const double &radius, const double &cx, const double &cy, const double &cz)
- **RandomPoints3DIterator** (const int &np, const double &pad, psi::SharedMolecule mol)
- virtual void [first](#) ()  
*Initialize first iteration.*
- virtual void [next](#) ()  
*Step to next iteration.*

### Protected Member Functions

- virtual double **random\_double** ()
- virtual void **draw\_random\_point** ()
- virtual bool **is\_in\_vdWsphere** (double x, double y, double z) const

### Protected Attributes

- double **cx\_**
- double **cy\_**
- double **cz\_**
- double **radius\_**
- double **r\_**
- double **phi\_**
- double **theta\_**
- double **x\_**
- double **y\_**



- double **z\_**
- psi::SharedMatrix **excludeSpheres\_**
- std::map< std::string, double > **vdwRadius\_**
- std::default\_random\_engine **randomNumberGenerator\_**
- std::uniform\_real\_distribution< double > **randomDistribution\_**

## Additional Inherited Members

### 17.37.1 Detailed Description

Iterator over a collection of points in 3D space. Random collection.

**Note:** Always create instances by using static factory method from [Points3DIterator](#). Do not use constructors of this class.

The documentation for this class was generated from the following files:

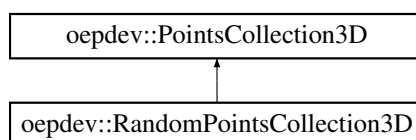
- oepdev/libutil/space3d.h
- oepdev/libutil/space3d.cc

## 17.38 oepdev::RandomPointsCollection3D Class Reference

Collection of random points in 3D space.

```
#include <space3d.h>
```

Inheritance diagram for oepdev::RandomPointsCollection3D:



## Public Member Functions

- **RandomPointsCollection3D** ([Collection](#) collectionType, const int &npoints, const double &radius, const double &cx, const double &cy, const double &cz)
- **RandomPointsCollection3D** ([Collection](#) collectionType, const int &npoints, const double &padding, psi::SharedMolecule mol)
- virtual void [print](#) () const  
*Print the information to Psi4 output file.*

## Additional Inherited Members

### 17.38.1 Detailed Description

Collection of random points in 3D space.

**Note:** Do not use constructors of this class explicitly. Instead, use static factory methods of the superclass to create instances.

The documentation for this class was generated from the following files:

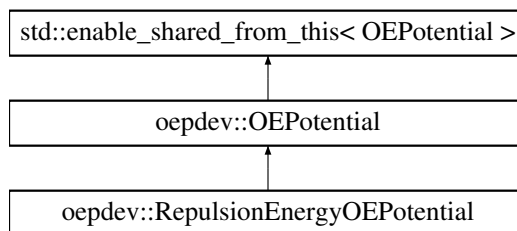
- oepdev/libutil/space3d.h
- oepdev/libutil/space3d.cc

## 17.39 oepdev::RepulsionEnergyOEPotential Class Reference

Generalized One-Electron Potential for Pauli Repulsion Energy.

```
#include <oep.h>
```

Inheritance diagram for oepdev::RepulsionEnergyOEPotential:



### Public Member Functions

- **RepulsionEnergyOEPotential** (SharedWavefunction [wfn](#), SharedBasisSet auxiliary, Options &options)
- **RepulsionEnergyOEPotential** (SharedWavefunction [wfn](#), Options &options)
- virtual void [compute](#) (const std::string &oepType) override  
*Compute matrix forms of all OEP's within a specified OEP type.*
- virtual void [compute\\_3D](#) (const std::string &oepType, const double &x, const double &y, const double &z, double &v) override  
*Compute value of potential in point x, y, z and save at v.*
- virtual void **print\_header** () const override

### Additional Inherited Members

#### 17.39.1 Detailed Description

Generalized One-Electron Potential for Pauli Repulsion Energy.

Contains the following OEP types:

- Murrell-etal.S1
- Otto-Ladik.S2

The documentation for this class was generated from the following files:

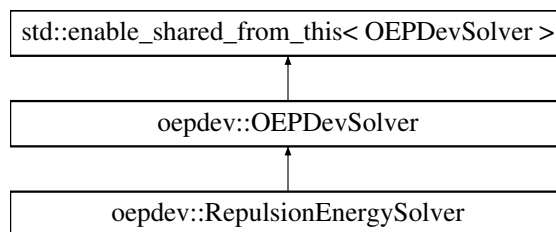
- oepdev/liboep/[oep.h](#)
- oepdev/liboep/oep.cc

## 17.40 oepdev::RepulsionEnergySolver Class Reference

Compute the Pauli-Repulsion interaction energy between unperturbed wavefunctions.

```
#include <solver.h>
```

Inheritance diagram for oepdev::RepulsionEnergySolver:



## Public Member Functions

- **RepulsionEnergySolver** (SharedWavefunctionUnion wfn\_union)
- virtual double [compute\\_oep\\_based](#) (const std::string &method="DEFAULT")  
*Compute property by using OEP's.*
- virtual double [compute\\_benchmark](#) (const std::string &method="DEFAULT")  
*Compute property by using benchmark method.*

## Additional Inherited Members

### 17.40.1 Detailed Description

Compute the Pauli-Repulsion interaction energy between unperturbed wavefunctions.

The implemented methods are shown below *Note*:

Keyword	Method Description
<b>Benchmark Methods</b>	
HAYES_STONE	*Default*. Pauli Repulsion energy at HF level from Hayes and Stone (1984).
DENSITY_BASED	Pauli Repulsion energy at HF level from Mandado and Hermida-Ramon (2012).
MURRELL_ETAL	Approximate Pauli Repulsion energy at HF level from Murrell et al (1967).
OTTO_LADIK	Approximate Pauli Repulsion energy at HF level from Otto and Ladik (1975).
EFP2	Approximate Pauli Repulsion energy at HF level from EFP2 model.
<b>OEP-Based Methods</b>	
MURRELL_ETAL_MIX	*Default*. OEP-Murrell et al's: S1 term via DF-OEP, S2 term via ESP-OEP.
MURRELL_ETAL_ESP	OEP-Murrell et al's: S1 and S2 via ESP-OEP

Table 17.3: Methods available in the Solver

- This solver also computes and prints the exchange energy at HF level (formulae are given below) for reference purposes.
- In order to construct this solver, **always** use the [OEPDevSolver::build](#) static factory method.

Below the detailed description of the implemented equations is given for each of the above provided methods. In the formulae across, it is assumed that the orbitals are real. The Coulomb notation for electron repulsion integrals

(ERI's) is adopted; i.e,

$$(ac|bd) = \iint d\mathbf{r}_1 d\mathbf{r}_2 \phi_a(\mathbf{r}_1) \phi_c(\mathbf{r}_1) \frac{1}{r_{12}} \phi_b(\mathbf{r}_2) \phi_d(\mathbf{r}_2)$$

Greek subscripts denote basis set orbitals whereas Italic subscripts denote the occupied molecular orbitals.

## Benchmark Methods

### Pauli Repulsion energy at HF level by Hayes and Stone (1984).

For a closed-shell system, equation of Hayes and Stone (1984) becomes

$$E^{\text{Rep}} = 2 \sum_{kl} (V_{kl}^A + V_{kl}^B + T_{kl}) [S^{-1}]_{lk} - \delta_{lk}] + \sum_{klmn} (kl|mn) \{ 2[S^{-1}]_{kl}[S^{-1}]_{mn} - [S^{-1}]_{kn}[S^{-1}]_{lm} - 2\delta_{kl}\delta_{mn} + \delta_{kn}\delta_{lm} \}$$

where  $\mathbf{S}$  is the overlap matrix between the doubly-occupied orbitals. The exact, pure exchange energy is for a closed shell case given as

$$E^{\text{Ex,pure}} = -2 \sum_{a \in A} \sum_{b \in B} (ab|ba)$$

Similarity transformation of molecular orbitals does not affect the resulting energies. The overall exchange-repulsion interaction energy is then (always net repulsive)

$$E^{\text{Ex-Rep}} = E^{\text{Ex,pure}} + E^{\text{Rep}}$$

### Repulsion energy of Mandado and Hermida-Ramon (2011)

At the Hartree-Fock level, the exchange-repulsion energy from the density-based scheme of Mandado and Hermida-Ramon (2011) is fully equivalent to the method by Hayes and Stone (1984). However, density-based method enables to compute exchange-repulsion energy at any level of theory. It is derived based on the Pauli deformation density matrix,

$$\Delta \mathbf{D}^{\text{Pauli}} \equiv \mathbf{D}^{oo} - \mathbf{D}$$

where  $\mathbf{D}^{oo}$  and  $\mathbf{D}$  are the density matrix formed from mutually orthogonal sets of molecular orbitals within the entire aggregate (formed by symmetric orthogonalization of MO's) and the density matrix of the unperturbed system (that can be understood as a Hadamard sum  $\mathbf{D} \equiv \mathbf{D}^A \oplus \mathbf{D}^B$ ).

At HF level, the Pauli deformation density matrix is given by

$$\Delta \mathbf{D}^{\text{Pauli}} = \mathbf{C} [\mathbf{S}^{-1} - \mathbf{1}] \mathbf{C}^\dagger$$

whereas the density matrix constructed from mutually orthogonal orbitals is

$$\mathbf{D}^{oo} = \mathbf{C} \mathbf{S}^{-1} \mathbf{C}^\dagger$$

In the above equations,  $\mathbf{S}$  is the overlap matrix between doubly occupied molecular orbitals of the entire aggregate.

Here, the expressions for the exchange-repulsion energy at any level of theory are shown for the case of open-shell system. The net repulsive energy is given as

$$E^{\text{Ex-Rep}} = E^{\text{Rep},1} + E^{\text{Rep},2} + E^{\text{Ex}}$$

where the one- and two-electron part of the repulsion energy is

$$E^{\text{Rep},1} = E^{\text{Rep,Kin}} + E^{\text{Rep,Nuc}}$$

$$E^{\text{Rep},2} = E^{\text{Rep,el-}\Delta} + E^{\text{Rep},\Delta-\Delta}$$

The kinetic and nuclear contributions are

$$E^{\text{Rep,Kin}} = 2 \sum_{\alpha\beta \in A,B} \Delta D_{\alpha\beta}^{\text{Pauli}} T_{\alpha\beta}$$

$$E^{\text{Rep,Nuc}} = 2 \sum_{\alpha\beta \in A,B} \Delta D_{\alpha\beta}^{\text{Pauli}} \sum_{z \in A,B} V_{\alpha\beta}^{(z)}$$

whereas the electron-deformation and deformation-deformation interaction contributions are

$$E^{\text{Rep,el-}\Delta} = 4 \sum_{\alpha\beta\gamma\delta \in A,B} \Delta D_{\alpha\beta}^{\text{Pauli}} D_{\gamma\delta}(\alpha\beta|\gamma\delta)$$

$$E^{\text{Rep},\Delta-\Delta} = 2 \sum_{\alpha\beta\gamma\delta \in A,B} \Delta D_{\alpha\beta}^{\text{Pauli}} \Delta D_{\gamma\delta}^{\text{Pauli}}(\alpha\beta|\gamma\delta)$$

The associated exchange energy is given by

$$E^{\text{Ex}} = - \sum_{\alpha\beta\gamma\delta \in A,B} \left[ D_{\alpha\delta}^{\text{oo}} D_{\beta\gamma}^{\text{oo}} - D_{\alpha\delta}^A D_{\beta\gamma}^A - D_{\alpha\delta}^B D_{\beta\gamma}^B \right] (\alpha\beta|\gamma\delta)$$

It is important to emphasise that, although, at HF level, the particular 'repulsive' and 'exchange' energies computed by using either Hayes and Stone or Mandado and Hermida-Ramon methods are not equal to each other, they sum up to exactly the same exchange-repulsion energy,  $E^{\text{Ex-Rep}}$ . Therefore, these methods at HF level are fully equivalent but the nature of partitioning of repulsive and exchange parts is different. It is also noted that the orbital localization does *not* affect the resulting energies, as opposed to the few approximate methods described below (Otto-Ladik and EFP2 methods).

#### Approximate Pauli Repulsion energy at HF level from Murrell et al.

By expanding the overlap matrix in a Taylor series one can show that the Pauli repulsion energy is approximately given as

$$E^{\text{Rep}} = E^{\text{Rep}}(\mathcal{O}(S)) + E^{\text{Rep}}(\mathcal{O}(S^2))$$

where the first-order term is

$$E^{\text{Rep}}(\mathcal{O}(S)) = -2 \sum_{a \in A} \sum_{b \in B} S_{ab} \left\{ V_{ab}^A + \sum_{c \in A} [2(ab|cc) - (ac|bc)] + V_{ab}^B + \sum_{d \in B} [2(ab|dd) - (ad|bd)] \right\}$$

whereas the second-order term is

$$E^{\text{Rep}}(\mathcal{O}(S^2)) = 2 \sum_{a \in A} \sum_{b \in B} S_{ab} \left\{ \sum_{c \in A} S_{bc} \left[ V_{ac}^B + 2 \sum_{d \in B} (ac|dd) \right] + \sum_{d \in B} S_{ad} \left[ V_{bd}^A + 2 \sum_{x \in A} (bd|cc) \right] - \sum_{c \in A} \sum_{d \in B} S_{cd} (ac|bd) \right\}$$

Thus derived repulsion energy is invariant with respect to transformation of molecular orbitals, similarly as Hayes--Stone's method and density-based method. By using OEP technique, the above theory can be exactly re-cast *without* any further approximations.

#### Approximate Pauli Repulsion energy at HF level from Otto and Ladik (1975).

The Pauli repulsion energy is approximately given as

$$E^{\text{Rep}} = E^{\text{Rep}}(\mathcal{O}(S)) + E^{\text{Rep}}(\mathcal{O}(S^2))$$

where the first-order term is

$$E^{\text{Rep}}(\mathcal{O}(S)) = -2 \sum_{a \in A} \sum_{b \in B} S_{ab} \left\{ V_{ab}^A + 2 \sum_{c \in A} (ab|cc) - (ab|aa) + V_{ab}^B + 2 \sum_{d \in B} (ab|dd) - (ab|bb) \right\}$$

whereas the second-order term is

$$E^{\text{Rep}}(\mathcal{O}(S^2)) = 2 \sum_{a \in A} \sum_{b \in B} S_{ab}^2 \left\{ V_{aa}^B + V_{bb}^A + 2 \sum_{c \in A} (cc|bb) + 2 \sum_{d \in B} (aa|dd) - (aa|bb) \right\}$$

Thus derived repulsion energy is *not* invariant with respect to transformation of molecular orbitals, in contrast to Hayes-Stone's method and density-based method. It was shown that good results are obtained when using localized molecular orbitals, whereas using canonical molecular orbitals brings poor results. By using OEP technique, the above theory can be exactly re-cast *without* any further approximations.

Approximate Pauli Repulsion energy at HF level from Jensen and Gordon (1996).

The Pauli repulsion energy used within the EFP2 approach is approximately given as

$$E^{\text{Rep}} = E^{\text{Rep}}(\mathcal{O}(S)) + E^{\text{Rep}}(\mathcal{O}(S^2))$$

where the first-order term is

$$E^{\text{Rep}}(\mathcal{O}(S)) = -2 \sum_{a \in A} \sum_{b \in B} S_{ab} \left\{ \sum_{c \in A} F_{ac}^A S_{cb} + \sum_{d \in B} F_{bd}^B S_{da} - 2T_{ab} \right\}$$

whereas the second-order term is

$$E^{\text{Rep}}(\mathcal{O}(S^2)) = 2 \sum_{a \in A} \sum_{b \in B} S_{ab}^2 \left\{ \sum_{x \in A} \frac{-Z_x}{R_{xb}} + \sum_{y \in B} \frac{-Z_y}{R_{ya}} + \sum_{c \in A} \frac{2}{R_{bc}} + \sum_{d \in B} \frac{2}{R_{ad}} - \frac{1}{R_{ab}} \right\}$$

Thus derived repulsion energy is *not* invariant with respect to transformation of molecular orbitals, in contrast to Hayes-Stone's method and density-based method. It was shown that good results are obtained when using localized molecular orbitals, whereas using canonical molecular orbitals brings poor results.

In EFP2, exchange energy is approximated by spherical Gaussian approximation (SGO). The result of this is the following formula for the exchange energy:

$$E^{\text{Ex}} \approx -4 \sum_{a \in A} \sum_{b \in B} \sqrt{\frac{-2 \ln |S_{ab}|}{\pi}} \frac{S_{ab}^2}{R_{ab}}$$

In all the above formulas,  $R_{ij}$  are distances between position vectors of  $i$ th and  $j$ th point. The LMO centroids are defined by

$$\mathbf{r}_a = (a | \mathbf{r} | a)$$

where  $a$  denotes the occupied molecular orbital.

## OEP-Based Methods

The Murrell et al's theory of Pauli repulsion for S-1 term and the Otto-Ladik's theory for S-2 term is here re-cast by introducing OEP's. The S-1 term is expressed via DF-OEP, whereas the S-2 term via ESP-OEP.

### S-1 term (Murrell et al.)

The OEP reduction without any approximations leads to the following formula

$$E^{\text{Rep}}(\mathcal{O}(S^1)) = -2 \sum_{a \in A} \sum_{b \in B} S_{ab} \left\{ \sum_{\xi \in A} S_{b\xi} G_{\xi a}^A + \sum_{\eta \in B} S_{a\eta} G_{\eta b}^B \right\}$$

where the OEP matrices are given as

$$G_{\xi a}^A = \sum_{\xi' \in A} [\mathbf{S}^{-1}]_{\xi \xi'} \sum_{\alpha \in A} \left\{ C_{\alpha a} V_{\alpha \xi'}^A + \sum_{\mu \nu \in A} [2C_{\alpha a} D_{\mu \nu} - C_{\nu a} D_{\alpha \mu}] (\alpha \xi' | \mu \nu) \right\}$$

and analogously for molecule  $B$ . Here, the nuclear attraction integrals are denoted by  $V_{\alpha \xi'}^A$ .

### S-2 term (Otto-Ladik)

After the OEP reduction, this contribution under Otto-Ladik approximation has the following form:

$$E^{\text{Rep}}(\mathcal{O}(S^2)) = 2 \sum_{a \in A} \sum_{b \in B} S_{ab}^2 \left\{ \sum_{x \in A} q_{xa} V_{bb}^{(x)} + \sum_{y \in B} q_{yb} V_{aa}^{(y)} \right\}$$

where the ESP charges associated with each occupied molecular orbital reproduce the *effective potential* of molecule in question, i.e.,

$$\sum_{x \in A} \frac{q_{xa}}{|\mathbf{r} - \mathbf{r}_x|} \cong v_a^A(\mathbf{r})$$

where the potential is given by

$$v_a^A(\mathbf{r}) = \sum_{x \in A} \frac{-Z_x}{|\mathbf{r} - \mathbf{r}_x|} + 2 \sum_{c \in A} \int \frac{\phi_c(\mathbf{r}') \phi_c(\mathbf{r}')}{|\mathbf{r} - \mathbf{r}'|} d\mathbf{r}' - \frac{1}{2} \int \frac{\phi_a(\mathbf{r}') \phi_a(\mathbf{r}')}{|\mathbf{r} - \mathbf{r}'|} d\mathbf{r}'$$

## 17.40.2 Member Function Documentation

**17.40.2.1** `double RepulsionEnergySolver::compute_benchmark ( const std::string & method = "DEFAULT" )`  
[virtual]

Compute property by using benchmark method.

Each solver object has one `DEFAULT` benchmark method

Parameters

<i>method</i>	- benchmark method
---------------	--------------------

Implements [oepdev::OEPDevSolver](#).

**17.40.2.2** `double RepulsionEnergySolver::compute_oep_based ( const std::string & method = "DEFAULT" )`  
[virtual]

Compute property by using OEP's.

Each solver object has one `DEFAULT` OEP-based method.

Parameters

<i>method</i>	- flavour of OEP model
---------------	------------------------

Implements [oepdev::OEPDevSolver](#).

The documentation for this class was generated from the following files:

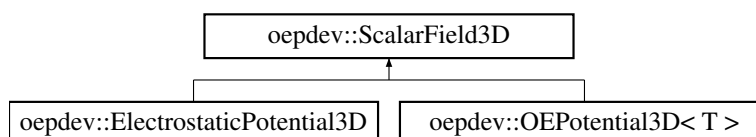
- [oepdev/libutil/solver.h](#)
- [oepdev/libutil/solver.cc](#)

## 17.41 oepdev::ScalarField3D Class Reference

Scalar field in 3D space. Abstract base.

```
#include <space3d.h>
```

Inheritance diagram for `oepdev::ScalarField3D`:



### Public Member Functions

- [ScalarField3D](#) (const int &np, const double &pad, psi::SharedWavefunction [wfn](#), psi::Options &options)

- Construct potential on random grid by providing wavefunction.*

  - [ScalarField3D](#) (const int &nx, const int &ny, const int &nz, const double &px, const double &py, const double &pz, std::shared\_ptr< psi::Wavefunction > [wfn](#), psi::Options &options)

*Construct potential on cube grid by providing wavefunction.*

  - virtual [~ScalarField3D](#) ()

*Destructor.*

  - virtual int [npoints](#) () const

*Get the number of points at which the scalar field is defined.*

  - virtual std::shared\_ptr< [PointsCollection3D](#) > [points\\_collection](#) () const

*Get the collection of points.*

  - virtual std::shared\_ptr< psi::Matrix > [data](#) () const

*Get the data matrix in a form { [x, y, z, f(x, y, z)] }.*

  - virtual std::shared\_ptr< psi::Wavefunction > [wfn](#) () const

*Get the wavefunction.*

  - virtual bool [is\\_computed](#) () const

*Get the information if data is already computed or not.*

  - virtual void [compute](#) ()

*Compute the scalar field in each point from the point collection.*

  - virtual double [compute\\_xyz](#) (const double &x, const double &y, const double &z)=0

*Compute a value of scalar field at point (x, y, z)*

  - virtual void [write\\_cube\\_file](#) (const std::string &name)

*Write the cube file (only for Cube collections, otherwise does nothing)*

  - virtual void [print](#) () const =0

*Print information of the object to Psi4 output.*

## Static Public Member Functions

- static shared\_ptr< [ScalarField3D](#) > [build](#) (const std::string &type, const int &np, const double &pad, psi::SharedWavefunction [wfn](#), psi::Options &options)
- Build scalar field of random points.*
- static shared\_ptr< [ScalarField3D](#) > [build](#) (const std::string &type, const int &nx, const int &ny, const int &nz, const double &px, const double &py, const double &pz, psi::SharedWavefunction [wfn](#), psi::Options &options)
- Build scalar field of points on a g09-cube grid.*

## Protected Attributes

- std::shared\_ptr< [PointsCollection3D](#) > [pointsCollection\\_](#)
- Collection of points at which the scalar field is to be computed.*
- std::shared\_ptr< psi::Matrix > [data\\_](#)
- The data matrix in a form { [x, y, z, f(x, y, z)] }.*
- std::shared\_ptr< psi::Wavefunction > [wfn\\_](#)
- Wavefunction.*
- psi::Matrix [geom\\_](#)
- Geometry of a molecule.*
- std::shared\_ptr< psi::IntegralFactory > [fact\\_](#)



- Integral factory.*
- `std::shared_ptr< psi::Matrix > pot_`  
*Matrix of potential one-electron integrals.*
- `std::shared_ptr< psi::OneBodyAoint > oneInt_`  
*One-electron integral shared pointer.*
- `std::shared_ptr< PotentialInt > potInt_`  
*One-electron potential shared pointer.*
- `std::shared_ptr< psi::BasisSet > primary_`  
*Basis set.*
- `int nbf_`  
*Number of basis functions.*
- `bool isComputed_`  
*Has data already computed?*

### 17.41.1 Detailed Description

Scalar field in 3D space. Abstract base.

Create scalar field defined at points distributed randomly or as an ordered g09 cube-like collection. Currently implemented scalar fields are:

- Electrostatic potential - computes electrostatic potential (requires wavefunction)
- Template of generic classes - compute custom scalar fields (requires generic object that is able to compute the field in 3D space)

**Note:** Always create instances by using static factory methods `build`. The following types of scalar field are currently implemented:

- `ELECTROSTATIC POTENTIAL`

### 17.41.2 Member Function Documentation

17.41.2.1 `std::shared_ptr< ScalarField3D > oepdev::ScalarField3D::build ( const std::string & type, const int & np, const double & pad, psi::SharedWavefunction wfn, psi::Options & options ) [static]`

Build scalar field of random points.

Parameters

<i>type</i>	- type of scalar field
<i>np</i>	- number of points
<i>pad</i>	- radius padding of a minimal sphere enclosing the molecule
<i>wfn</i>	- Psi4 Wavefunction containing the molecule
<i>options</i>	- Psi4 options

17.41.2.2 `std::shared_ptr< ScalarField3D > oepdev::ScalarField3D::build ( const std::string & type, const int & nx, const int & ny, const int & nz, const double & px, const double & py, const double & pz, psi::SharedWavefunction wfn, psi::Options & options ) [static]`

Build scalar field of points on a g09-cube grid.

## Parameters

<i>type</i>	- type of scalar field
<i>nx</i>	- number of points along x direction
<i>ny</i>	- number of points along y direction
<i>nz</i>	- number of points along z direction
<i>px</i>	- padding distance along x direction
<i>py</i>	- padding distance along y direction
<i>pz</i>	- padding distance along z direction
<i>wfn</i>	- Psi4 Wavefunction containing the molecule
<i>options</i>	- Psi4 options

The documentation for this class was generated from the following files:

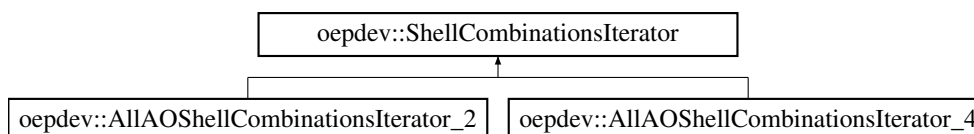
- oepdev/libutil/space3d.h
- oepdev/libutil/space3d.cc

## 17.42 oepdev::ShellCombinationsIterator Class Reference

Iterator for Shell Combinations. Abstract Base.

```
#include <integrals_iter.h>
```

Inheritance diagram for oepdev::ShellCombinationsIterator:



### Public Member Functions

- [ShellCombinationsIterator](#) (int [nshell](#))  
*Constructor.*
- virtual [~ShellCombinationsIterator](#) ()  
*Destructor.*
- virtual void [first](#) (void)=0  
*First iteration.*
- virtual void [next](#) (void)=0  
*Next iteration.*
- virtual std::shared\_ptr  
< psi::BasisSet > [bs\\_1](#) (void) const  
*Grab the basis set of axis 1.*
- virtual std::shared\_ptr  
< psi::BasisSet > [bs\\_2](#) (void) const  
*Grab the basis set of axis 2.*
- virtual std::shared\_ptr  
< psi::BasisSet > [bs\\_3](#) (void) const  
*Grab the basis set of axis 3.*
- virtual std::shared\_ptr  
< psi::BasisSet > [bs\\_4](#) (void) const  
*Grab the basis set of axis 4.*
- virtual int [P](#) (void) const

- Grab the current shell P index.*
- virtual int [Q](#) (void) const
- Grab the current shell Q index.*
- virtual int [R](#) (void) const
- Grab the current shell R index.*
- virtual int [S](#) (void) const
- Grab the current shell S index.*
- virtual bool [is\\_done](#) (void)
- Return status of an iterator.*
- virtual const int [nshell](#) (void) const
- Return number of shells this iterator is for.*
- virtual std::shared\_ptr  
< [AOIntegralIterator](#) > [ao\\_iterator](#) (std::string mode="ALL") const
- virtual void [compute\\_shell](#) (std::shared\_ptr< [oepdev::TwoBodyAOInt](#) > tei) const =0
- virtual void [compute\\_shell](#) (std::shared\_ptr< [psi::TwoBodyAOInt](#) > tei) const =0

### Static Public Member Functions

- static std::shared\_ptr  
< [ShellCombinationsIterator](#) > [build](#) (const [IntegralFactory](#) &ints, std::string mode="ALL", int [nshell](#)=4)  
*Build shell iterator from [oepdev::IntegralFactory](#).*
- static std::shared\_ptr  
< [ShellCombinationsIterator](#) > [build](#) (std::shared\_ptr< [IntegralFactory](#) > ints, std::string mode="ALL", int [nshell](#)=4)  
*This is an overloaded member function, provided for convenience. It differs from the above function only in what argument(s) it accepts.*
- static std::shared\_ptr  
< [ShellCombinationsIterator](#) > [build](#) (const [psi::IntegralFactory](#) &ints, std::string mode="ALL", int [nshell](#)=4)  
*Build shell iterator from [psi::IntegralFactory](#).*
- static std::shared\_ptr  
< [ShellCombinationsIterator](#) > [build](#) (std::shared\_ptr< [psi::IntegralFactory](#) > ints, std::string mode="ALL", int [nshell](#)=4)  
*This is an overloaded member function, provided for convenience. It differs from the above function only in what argument(s) it accepts.*

### Protected Attributes

- SharedBasisSet [bs\\_1\\_](#)  
*Basis set of axis 1.*
- SharedBasisSet [bs\\_2\\_](#)  
*Basis set of axis 2.*
- SharedBasisSet [bs\\_3\\_](#)  
*Basis set of axis 3.*
- SharedBasisSet [bs\\_4\\_](#)  
*Basis set of axis 4.*
- const int [nshell\\_](#)  
*Number of shells this iterator is for.*
- bool [done](#)  
*Status of an iterator.*

### 17.42.1 Detailed Description

Iterator for Shell Combinations. Abstract Base.

Date

2018/03/01 17:22:00

### 17.42.2 Constructor & Destructor Documentation

#### 17.42.2.1 ShellCombinationsIterator::ShellCombinationsIterator ( int *nshell* )

Constructor.

Parameters

<i>nshell</i>	- number of shells this iterator is for
---------------	---

### 17.42.3 Member Function Documentation

#### 17.42.3.1 std::shared\_ptr< AOIntegralsIterator > ShellCombinationsIterator::ao\_iterator ( std::string *mode* = "ALL" ) const [virtual]

Make an AO integral iterator based on current shell

Parameters

<i>mode</i>	- either "ALL" or "UNIQUE" (iterate over all or unique integrals)
-------------	---

Returns

iterator over AO integrals

#### 17.42.3.2 std::shared\_ptr< ShellCombinationsIterator > ShellCombinationsIterator::build ( const IntegralFactory & *ints*, std::string *mode* = "ALL", int *nshell* = 4 ) [static]

Build shell iterator from [oepdev::IntegralFactory](#).

Parameters

<i>ints</i>	- integral factory
<i>mode</i>	- mode of iteration (either ALL or UNIQUE)
<i>nshell</i>	- number of shells to iterate through

Returns

shell iterator

Examples:

[example\\_integrals\\_iter.cc](#).

#### 17.42.3.3 std::shared\_ptr< ShellCombinationsIterator > ShellCombinationsIterator::build ( const psi::IntegralFactory & *ints*, std::string *mode* = "ALL", int *nshell* = 4 ) [static]

Build shell iterator from [psi::IntegralFactory](#).

## Parameters

<i>ints</i>	- integral factory
<i>mode</i>	- mode of iteration (either ALL or UNIQUE)
<i>nshell</i>	- number of shells to iterate through

## Returns

shell iterator

17.42.3.4 `void ShellCombinationsIterator::compute_shell ( std::shared_ptr< oepdev::TwoBodyAOInt > tei ) const`  
`[pure virtual]`

Compute integrals in a current shell. Works both for [oepdev::TwoBodyAOInt](#) and [psi::TwoBodyAOInt](#)

## Parameters

<i>tei</i>	- two body integral object
------------	----------------------------

Implemented in [oepdev::AllAOShellCombinationsIterator\\_2](#), and [oepdev::AllAOShellCombinationsIterator\\_4](#).

The documentation for this class was generated from the following files:

- [oepdev/libutil/integrals\\_iter.h](#)
- [oepdev/libutil/integrals\\_iter.cc](#)

## 17.43 oepdev::test::Test Class Reference

Manages test routines.

```
#include <test.h>
```

### Public Member Functions

- [Test](#) (std::shared\_ptr< psi::Wavefunction > wfn, psi::Options &options)  
*Construct the tester.*
- [~Test](#) ()  
*Destructor.*
- double [run](#) (void)  
*Peform the test.*

### Protected Member Functions

- double [test\\_basic](#) (void)  
*Test the basic functionalities of OEPDev.*
- double [test\\_cphf](#) (void)  
*Test the CPHF method.*
- double [test\\_dmatPol](#) (void)  
*Test the density matrix susceptibility.*
- double [test\\_eri\\_1\\_1](#) (void)  
*Test the oepdev::ERI\_1\_1 class against psi::ERI.*
- double [test\\_eri\\_2\\_2](#) (void)  
*Test the oepdev::ERI\_2\_2 class against psi::ERI.*

- double [test\\_eri\\_3\\_1](#) (void)  
*Test the `oepdev::ERI_3_1` class against `psi::ERI`.*
- double [test\\_unitaryOptimizer](#) (void)  
*Test the `oepdev::UnitaryOptimizer` class.*
- double [test\\_unitaryOptimizer\\_4\\_2](#) (void)  
*Test the `oepdev::UnitaryOptimizer_4_2` class.*

### Protected Attributes

- `std::shared_ptr`  
    < `psi::Wavefunction` > [wfn\\_](#)  
    *Wavefunction object.*
- `psi::Options` & [options\\_](#)  
    *Psi4 Options.*

### 17.43.1 Detailed Description

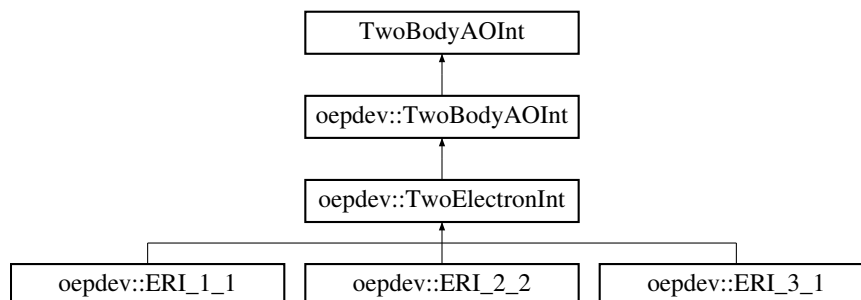
Manages test routines.

The documentation for this class was generated from the following files:

- `oepdev/libtest/test.h`
- `oepdev/libtest/test.cc`

## 17.44 `oepdev::TwoBodyAOInt` Class Reference

Inheritance diagram for `oepdev::TwoBodyAOInt`:



### Public Member Functions

- virtual void [compute](#) (`std::shared_ptr`< `psi::Matrix` > &result, int ibs1=0, int ibs2=2)  
    *Compute two-body two-centre integral and put it into matrix.*
- virtual void [compute](#) (`psi::Matrix` &result, int ibs1=0, int ibs2=2)
- virtual `size_t` [compute\\_shell](#) (int, int, int, int)=0
- virtual `size_t` [compute\\_shell](#) (int, int, int)=0
- virtual `size_t` [compute\\_shell](#) (int, int)=0
- virtual `size_t` [compute\\_shell\\_deriv1](#) (int, int, int, int)=0
- virtual `size_t` [compute\\_shell\\_deriv2](#) (int, int, int, int)=0
- virtual `size_t` [compute\\_shell\\_deriv1](#) (int, int, int)=0
- virtual `size_t` [compute\\_shell\\_deriv2](#) (int, int, int)=0
- virtual `size_t` [compute\\_shell\\_deriv1](#) (int, int)=0
- virtual `size_t` [compute\\_shell\\_deriv2](#) (int, int)=0

## Protected Member Functions

- **TwoBodyAOInt** (const [IntegralFactory](#) \*intsfactory, int deriv=0)
- **TwoBodyAOInt** (const [TwoBodyAOInt](#) &rhs)

### 17.44.1 Member Function Documentation

17.44.1.1 void oepdev::TwoBodyAOInt::compute ( std::shared\_ptr< psi::Matrix > &result, int ibs1 = 0, int ibs2 = 2 )  
[virtual]

Compute two-body two-centre integral and put it into matrix.

#### Parameters

<i>result</i>	- matrix where to store (i  j) two-body integrals
<i>ibs1</i>	- first basis set axis
<i>ibs2</i>	- second basis set axis

17.44.1.2 void oepdev::TwoBodyAOInt::compute ( psi::Matrix &result, int ibs1 = 0, int ibs2 = 2 ) [virtual]

This is an overloaded member function, provided for convenience. It differs from the above function only in what argument(s) it accepts.

The documentation for this class was generated from the following files:

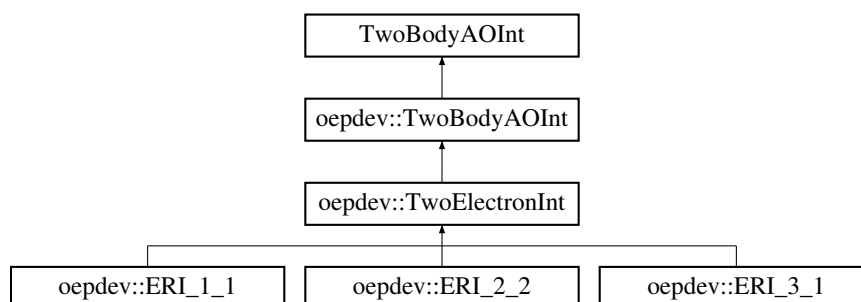
- oepdev/libpsi/[integral.h](#)
- oepdev/libpsi/integral.cc

## 17.45 oepdev::TwoElectronInt Class Reference

General Two Electron Integral.

```
#include <eri.h>
```

Inheritance diagram for oepdev::TwoElectronInt:



## Public Member Functions

- **TwoElectronInt** (const [IntegralFactory](#) \*integral, int deriv, bool use\_shell\_pairs)
- virtual size\_t **compute\_shell** (int, int)  
*Compute ERI's between 2 shells. Result is stored in buffer.*
- virtual size\_t **compute\_shell** (int, int, int)  
*Compute ERI's between 3 shells. Result is stored in buffer.*

- virtual size\_t [compute\\_shell](#) (int, int, int, int)  
*Compute ERI's between 4 shells. Result is stored in buffer.*
- virtual size\_t [compute\\_shell](#) (const psi::AOShellCombinationsIterator &)
- virtual size\_t [compute\\_shell\\_deriv1](#) (int, int)  
*Compute first derivatives of ERI's between 2 shells.*
- virtual size\_t [compute\\_shell\\_deriv2](#) (int, int)  
*Compute second derivatives of ERI's between 2 shells.*
- virtual size\_t [compute\\_shell\\_deriv1](#) (int, int, int)  
*Compute first derivatives of ERI's between 3 shells.*
- virtual size\_t [compute\\_shell\\_deriv2](#) (int, int, int)  
*Compute second derivatives of ERI's between 3 shells.*
- virtual size\_t [compute\\_shell\\_deriv1](#) (int, int, int, int)  
*Compute first derivatives of ERI's between 4 shells.*
- virtual size\_t [compute\\_shell\\_deriv2](#) (int, int, int, int)  
*Compute second derivatives of ERI's between 4 shells.*

### Protected Member Functions

- int [get\\_cart\\_am](#) (int am, int n, int x)  
*Get the angular momentum per Cartesian component.*
- double [get\\_R](#) (int N, int L, int M)  
*Get the (N,L,M)th McMurchie-Davidson coefficient.*
- virtual size\_t [compute\\_doublet](#) (int, int)  
*Computes the ERI's between three shells.*
- virtual size\_t [compute\\_triplet](#) (int, int, int)  
*Computes the ERI's between three shells.*
- virtual size\_t [compute\\_quartet](#) (int, int, int, int)  
*Computes the ERI's between four shells.*

### Protected Attributes

- const int [max\\_am\\_](#)  
*Maximum angular momentum.*
- const int [n\\_max\\_am\\_](#)  
*Maximum number of angular momentum functions.*
- psi::Fjt \* [fjt\\_](#)  
*Computes the fundamental: Boys function value at T for degree v.*
- bool [use\\_shell\\_pairs\\_](#)  
*Should we use shell pair information?*
- const double [cartMap\\_](#) [60]  
*Map of Cartesian components per each am.*
- const double [df\\_](#) [8]  
*Double factorial array.*
- double \* [mdh\\_buffer\\_R\\_](#)  
*Buffer for the McMurchie-Davidson-Hermite R coefficients.*



### 17.45.1 Detailed Description

General Two Electron Integral.

Implements the McMurchie-Davidson recursive scheme for all integral types. The integral can be defined for any number of Gaussian centres, thus it is not limited to 2-by-2 four-centre ERI. Currently implemented subtypes are:

- [oepdev::ERI\\_1\\_1](#) - 2-centre electron-repulsion integral (i|j)
- [oepdev::ERI\\_2\\_2](#) - 4-centre electron-repulsion integral (ij|kl)
- [oepdev::ERI\\_3\\_1](#) - 4-centre electron-repulsion integral (ijk|l)

See Also

[The Integral Package Library](#)

### 17.45.2 Member Function Documentation

17.45.2.1 `size_t oepdev::TwoElectronInt::compute_shell ( const psi::AOShellCombinationsIterator & shellIter )`  
[virtual]

Compute ERIs between 4 shells. Result is stored in buffer. Only for use with [ERI\\_2\\_2](#) and the same basis sets, otherwise shell pairs won't be compatible.

The documentation for this class was generated from the following files:

- [oepdev/libints/eri.h](#)
- [oepdev/libints/eri.cc](#)

## 17.46 oepdev::UnitaryOptimizer Class Reference

Find the optimum unitary matrix of quadratic matrix equation.

```
#include <unitary_optimizer.h>
```

### Public Member Functions

- [UnitaryOptimizer](#) (double \*R, double \*P, int n, double conv=1.0e-6, int maxiter=100, bool verbose=true)  
*Create from R and P matrices and optimization options.*
- [UnitaryOptimizer](#) (std::shared\_ptr< psi::Matrix > R, std::shared\_ptr< psi::Vector > P, double conv=1.0e-6, int maxiter=100, bool verbose=true)  
*Create from R and P matrices and optimization options.*
- [~UnitaryOptimizer](#) ()  
*Clear memory.*
- bool [maximize](#) ()  
*Run the minimization.*
- bool [minimize](#) ()  
*Run the maximization.*
- std::shared\_ptr< psi::Matrix > [X](#) ()  
*Get the unitary matrix (solution)*
- double \* [get\\_X](#) () const  
*Get the unitary matrix (pointer to solution)*
- double [Z](#) ()  
*Get the actual value of Z function.*
- bool [success](#) () const  
*Get the status of the optimization.*

## Protected Member Functions

- [UnitaryOptimizer](#) (int n, double conv, int maxiter, bool verbose)  
*Initialize the basic memory.*
- void [common\\_init\\_](#) ()  
*Prepare the optimizer.*
- void [run\\_](#) (const std::string &opt)  
*Run the optimization (intermediate interface)*
- void [optimize\\_](#) (const std::string &opt)  
*Run the optimization (inner interface)*
- void [refresh\\_](#) ()  
*Restore the initial state of the optimizer.*
- void [update\\_conv\\_](#) ()  
*Update the convergence.*
- void [update\\_iter\\_](#) ()  
*Update the iterates.*
- void [update\\_Z\\_](#) ()  
*Update Z value.*
- void [update\\_RP\\_](#) ()  
*Uptade R and P matrices.*
- void [update\\_X\\_](#) ()  
*Update the solution matrix X.*
- double [eval\\_Z\\_](#) (double \*X, double \*R, double \*P)  
*Evaluate the objective Z function.*
- double [eval\\_Z\\_](#) ()
- double [eval\\_dZ\\_](#) (double g, double \*R, double \*P, int i, int j)  
*Evaluate the change in Z.*
- double [eval\\_Z\\_trial\\_](#) (int i, int j, double gamma)  
*Evaluate the trial Z value.*
- void [form\\_X0\\_](#) ()  
*Create identity matrix.*
- void [form\\_X\\_](#) (int i, int j, double gamma)  
*Form unitary matrix X (store in buffer Xnew\_)*
- void [form\\_next\\_X\\_](#) (const std::string &opt)  
*Form the next unitary matrix X.*
- [ABCD](#) [get\\_ABCD\\_](#) (int i, int j)  
*Retrieve [ABCD](#) parameters for root search.*
- void [find\\_roots\\_boyd\\_](#) (const [ABCD](#) &abcd)  
*Solve for all roots of equation  $A*\sin(g) + B*\cos(g) + C*\sin(2*g) + D*\cos(2*g) = 0$  -> implements Boyd's method.*
- double [find\\_root\\_halley\\_](#) (double x0, const [ABCD](#) &abcd)  
*Solve for root of equation  $A*\sin(g) + B*\cos(g) + C*\sin(2*g) + D*\cos(2*g) = 0$  -> implements Halley's method.*
- double [find\\_gamma\\_](#) (const [ABCD](#) &abcd, int i, int j, const std::string &opt)  
*Compute gamma from roots of base equations.*
- bool [lt\\_](#) (double a, double b)  
*less-than function*
- bool [gt\\_](#) (double a, double b)  
*greater-than function*
- double [func\\_0\\_](#) (double g, const [ABCD](#) &abcd)  
*Function  $f(\text{gamma}) = d(dZ)/d\text{gamma}$ .*
- double [func\\_1\\_](#) (double g, const [ABCD](#) &abcd)  
*Gradient of  $f(\text{gamma})$*

- double [func\\_2\\_](#) (double g, const [ABCD](#) &abcd)  
*Hessian of f(gamma) - used only for Halley method (not implemented since Boyd method is more suitable here)*
- `std::shared_ptr< psi::Matrix >` [psi\\_X\\_](#) ()  
*Form the Psi4 matrix with the transformation matrix.*

## Protected Attributes

- const int [n\\_](#)  
*Dimension of the problem.*
- const double [conv\\_](#)  
*Convergence.*
- const int [maxiter\\_](#)  
*Maximum number of iterations.*
- const bool [verbose\\_](#)  
*Verbose mode.*
- double \* [R\\_](#)  
*R matrix.*
- double \* [P\\_](#)  
*P vector.*
- double \* [R0\\_](#)  
*Reference R matrix.*
- double \* [P0\\_](#)  
*Reference P vector.*
- double \* [X\\_](#)  
*X Matrix (accumulated solution)*
- double \* [W\\_](#)  
*Work place.*
- double \* [Xold\\_](#)  
*Temporary X matrix.*
- double \* [Xnew\\_](#)  
*Temporary X matrix.*
- int [niter\\_](#)  
*Current number of iterations.*
- double [S\\_](#) [4]  
*Current solutions.*
- double [Zinit\\_](#)  
*Initial Z value.*
- double [Zold\\_](#)  
*Old Z value.*
- double [Znew\\_](#)  
*New Z value.*
- double [conv\\_current\\_](#)  
*Current convergence.*
- bool [success\\_](#)  
*Status of optimization.*

### 17.46.1 Detailed Description

Find the optimum unitary matrix of quadratic matrix equation.

The objective function of the orthogonal matrix  $\mathbf{X}$

$$Z(\mathbf{X}) \equiv \sum_{ijkl} X_{ij} X_{kl} R_{jl} - \sum_{ij} X_{ij} P_j$$

is optimized by using the Jacobi iteration algorithm. In the above equation,  $\mathbf{R}$  is a square, general real matrix of size  $N \times N$  whereas  $\mathbf{P}$  is a real vector of length  $N$ .

**Algorithm.**

Optimization of  $\mathbf{X}$  is factorized into a sequence of 2-dimensional rotations with one real parameter  $\gamma$ :

$$\mathbf{X}^{\text{New}} = \mathbf{U}(\gamma) \cdot \mathbf{X}^{\text{Old}}$$

where

$$\mathbf{U}(\gamma) \equiv \begin{pmatrix} \ddots & & & & \\ & \cos(\gamma) & \cdots & \sin(\gamma) & \\ & \vdots & \ddots & \vdots & \\ & -\sin(\gamma) & \cdots & \cos(\gamma) & \\ & & & & \ddots \end{pmatrix}$$

is the Jacobi transformation matrix constructed for the  $I$ th and  $J$ th element from the entire  $N$ -dimensional set. For the sake of algorithmic simplicity, every iteration after  $\mathbf{U}(\gamma)$  has been formed,  $\mathbf{X}^{\text{Old}}$  is for a while assumed to be an identity matrix and the  $\mathbf{R}$  matrix and  $\mathbf{P}$  vector are transformed according to the following formulae

$$\begin{aligned} \mathbf{R} &\rightarrow \mathbf{U}\mathbf{R}\mathbf{U}^T \\ \mathbf{P} &\rightarrow \mathbf{U}\mathbf{P} \end{aligned}$$

The full transformation matrix is accumulated in the memory buffer until convergence.

In each iteration, the optimum angle  $\gamma$  is found as follows: First, the roots of the finite Fourier series

$$A \sin(\gamma) + B \cos(\gamma) + C \sin(2\gamma) + D \cos(2\gamma) = 0$$

are found. In the above equations, the expansion coefficients are given as

$$\begin{aligned} A &= P_I + P_J - \sum_{k \neq I, J} (R_{Ik} + R_{Jk} + R_{kI} + R_{kJ}) \\ B &= P_I - P_J - \sum_{k \neq I, J} (R_{Ik} - R_{Jk} + R_{kI} - R_{kJ}) \\ C &= -2(R_{IJ} + R_{JI}) \\ D &= -2(R_{II} - R_{JJ}) \end{aligned}$$

and  $I, J$  are the chosen indices in the Jacobi iteration subspace. The roots are evaluated by applying the Boyd's method[1], in which they are given as

$$\gamma_n = \Re[-i \ln(\lambda_n)]$$

where  $\lambda_n$  is an eigenvalue of the following 4 by 4 complex matrix:

$$\begin{pmatrix} 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \\ -\frac{D+iC}{D-iC} & -\frac{B+iC}{D-iC} & 0 & -\frac{B-iC}{D-iC} \end{pmatrix}$$

Once the four roots of the Fourier series equation are found, one solution out of four is chosen which satisfies the global optimum condition, i.e., the largest increase/decrease in the objective function given by

$$\delta Z = A(1 - \cos(\gamma)) + B \sin(\gamma) + C \sin^2(\gamma) + \frac{D}{2} \sin(2\gamma)$$

The discrimination between the minima/maxima is performed based on the evaluation of the Hessian of  $Z$  with respect to  $\gamma$ ,

$$\frac{\partial^2 Z}{\partial \gamma^2} = A \cos(\gamma) - B \sin(\gamma) + 2C \cos(2\gamma) - 2D \sin(2\gamma)$$

All the  $N(N-1)/2$  unique pairs of molecular orbitals are checked and the optimal set of  $\gamma, I, J$  is chosen to construct  $\mathbf{X}^{\text{New}}$ .

#### References:

[1] Boyd, J.P.; J. Eng. Math. (2006) 56, pp. 203-219

## 17.46.2 Constructor & Destructor Documentation

**17.46.2.1** `oepdev::UnitaryOptimizer::UnitaryOptimizer ( double *  $R$ , double *  $P$ , int  $n$ , double  $conv = 1.0e-6$ , int  $maxiter = 100$ , bool  $verbose = true$  )`

Create from  $R$  and  $P$  matrices and optimization options.

#### Parameters

$R$	- $\mathbf{R}$ matrix
$P$	- $\mathbf{P}$ vector
$n$	- dimensionality of the problem ( $N$ )
$conv$	- convergence in the $Z$ function
$maxiter$	- maximum number of iterations
$verbose$	- whether print information of iteration process or not Sets up the optimizer.

**17.46.2.2** `oepdev::UnitaryOptimizer::UnitaryOptimizer ( std::shared_ptr< psi::Matrix >  $R$ , std::shared_ptr< psi::Vector >  $P$ , double  $conv = 1.0e-6$ , int  $maxiter = 100$ , bool  $verbose = true$  )`

Create from  $R$  and  $P$  matrices and optimization options.

#### Parameters

$R$	- $\mathbf{R}$ matrix
$P$	- $\mathbf{P}$ vector
$conv$	- convergence in the $Z$ function
$maxiter$	- maximum number of iterations
$verbose$	- whether print information of iteration process or not Sets up the optimizer.

**17.46.2.3** `oepdev::UnitaryOptimizer::UnitaryOptimizer ( int  $n$ , double  $conv$ , int  $maxiter$ , bool  $verbose$  )` [protected]

Initialize the basic memory.

#### Parameters

$n$	- dimensionality of the problem ( $N$ )
$conv$	- convergence in the $Z$ function
$maxiter$	- maximum number of iterations
$verbose$	- whether print information of iteration process or not Sets up the optimizer.

The documentation for this class was generated from the following files:

- oepdev/libutil/unitary\_optimizer.h
- oepdev/libutil/unitary\_optimizer.cc

## 17.47 oepdev::UnitaryOptimizer\_4\_2 Class Reference

Find the optimim unitary matrix for quartic-quadratic matrix equation with trace.

```
#include <unitary_optimizer.h>
```

### Public Member Functions

- [UnitaryOptimizer\\_4\\_2](#) (double \*R, double \*P, int n, double conv=1.0e-6, int maxiter=100, bool verbose=true)  
*Create from R and P matrices and optimization options.*
- [~UnitaryOptimizer\\_4\\_2](#) ()  
*Clear memory.*
- bool [maximize](#) ()  
*Run the minimization.*
- bool [minimize](#) ()  
*Run the maximization.*
- std::shared\_ptr< psi::Matrix > [X](#) ()  
*Get the unitary matrix (solution)*
- double \* [get\\_X](#) () const  
*Get the unitary matrix (pointer to solution)*
- double [Z](#) ()  
*Get the actual value of Z function.*
- bool [success](#) () const  
*Get the status of the optimization.*

### Protected Member Functions

- [UnitaryOptimizer\\_4\\_2](#) (int n, double conv, int maxiter, bool verbose)  
*Initialize the basic memory.*
- void [common\\_init](#) ()  
*Prepare the optimizer.*
- void [run](#) (const std::string &opt)  
*Run the optimization (intermediate interface)*
- void [optimize](#) (const std::string &opt)  
*Run the optimization (inner interface)*
- void [refresh](#) ()  
*Restore the initial state of the optimizer.*
- void [update\\_conv](#) ()  
*Update the convergence.*
- void [update\\_iter](#) ()  
*Update the iterates.*
- void [update\\_Z](#) ()  
*Update Z value.*
- void [update\\_RP](#) ()  
*Uptade R and P matrices.*
- void [update\\_X](#) ()  
*Update the solution matrix X.*
- double [eval\\_Z](#) (double \*X, double \*R, double \*P)  
*Evaluate the objective Z function.*
- double [eval\\_Z](#) ()
- double [eval\\_dZ](#) (double g, double \*R, double \*P, int I, int J)

- Evaluate the change in Z.*
  - double [eval\\_Z\\_trial\\_](#) (int I, int J, double gamma)
- Evaluate the trial Z value.*
  - void [form\\_X0\\_](#) ()
- Create identity matrix.*
  - void [form\\_X\\_](#) (int I, int J, double gamma)
- Form unitary matrix X (store in buffer Xnew\_)*
  - void [form\\_next\\_X\\_](#) (const std::string &opt)
- Form the next unitary matrix X.*
  - [Fourier9](#) [get\\_fourier\\_](#) (int I, int J)
- Retrieve ABCD parameters for root search.*
  - void [find\\_roots\\_boyd\\_](#) (const [Fourier9](#) &abcd)
- Solve for all roots of equation  $A*\sin(g) + B*\cos(g) + C*\sin(2*g) + D*\cos(2*g) = 0$  -> implements Boyd's method.*
  - double [find\\_root\\_halley\\_](#) (double x0, const [Fourier9](#) &abcd)
- Solve for root of equation  $A*\sin(g) + B*\cos(g) + C*\sin(2*g) + D*\cos(2*g) = 0$  -> implements Halley's method.*
  - double [find\\_gamma\\_](#) (const [Fourier9](#) &abcd, int i, int j, const std::string &opt)
- Compute gamma from roots of base equations.*
  - bool [lt\\_](#) (double a, double b)
- less-than function*
  - bool [gt\\_](#) (double a, double b)
- greater-than function*
  - std::shared\_ptr< [psi::Matrix](#) > [psi\\_X\\_](#) ()
- Form the Psi4 matrix with the transformation matrix.*

## Protected Attributes

- const int [n\\_](#)
  - Dimension of the problem.*
- const double [conv\\_](#)
  - Convergence.*
- const int [maxiter\\_](#)
  - Maximum number of iterations.*
- const bool [verbose\\_](#)
  - Verbose mode.*
- double \* [R\\_](#)
  - R tensor.*
- double \* [P\\_](#)
  - P tensor.*
- double \* [R0\\_](#)
  - Reference R tensor.*
- double \* [P0\\_](#)
  - Reference P tensor.*
- double \* [X\\_](#)
  - X Matrix (accumulated solution)*
- double \* [W\\_](#)
  - Work place.*
- double \* [Xold\\_](#)
  - Temporary X matrix.*
- double \* [Xnew\\_](#)
  - Temporary X matrix.*

- int `niter_`  
Current number of iterations.
- double `S_` [8]  
Current solutions.
- double `Zinit_`  
Initial Z value.
- double `Zold_`  
Old Z value.
- double `Znew_`  
New Z value.
- double `conv_current_`  
Current convergence.
- bool `success_`  
Status of optimization.

### 17.47.1 Detailed Description

Find the optimum unitary matrix for quartic-quadratic matrix equation with trace.

The objective function of the orthogonal matrix  $\mathbf{X}$

$$Z(\mathbf{X}) \equiv \sum_{ijklmn} X_{ki} X_{lj} X_{mi} X_{nj} R_{ijklmn} + \sum_{ijk} X_{ji} X_{ki} P_{ijk}$$

is optimized by using the Jacobi iteration algorithm. In the above equation,  $\mathbf{R}$  is a general real sixth-rank tensor of size  $N^6$  whereas  $\mathbf{P}$  is a general real third-rank tensor of size  $N^3$ .

**Algorithm.**

Optimization of  $\mathbf{X}$  is factorized into a sequence of 2-dimensional rotations with one real parameter  $\gamma$ :

$$\mathbf{X}^{\text{New}} = \mathbf{X}^{\text{Old}} \cdot \mathbf{U}(\gamma)$$

where

$$\mathbf{U}(\gamma) \equiv \begin{pmatrix} \ddots & & & & \\ & \cos(\gamma) & \cdots & \sin(\gamma) & \\ & \vdots & \ddots & \vdots & \\ & -\sin(\gamma) & \cdots & \cos(\gamma) & \\ & & & & \ddots \end{pmatrix}$$

is the Jacobi transformation matrix constructed for the  $I$ th and  $J$ th element from the entire  $N$ -dimensional set. For the sake of algorithmic simplicity, every iteration after  $\mathbf{U}(\gamma)$  has been formed,  $\mathbf{X}^{\text{Old}}$  is for a while assumed to be an identity matrix and the  $\mathbf{R}$  as well as  $\mathbf{P}$  tensors are transformed according to the following formulae

$$R_{ijklmn} \rightarrow \sum_{k'l'm'n'} R_{ijk'l'm'n'} X_{k'k} X_{l'l} X_{m'm} X_{n'n}$$

$$P_{ijk} \rightarrow \sum_{j'k'} P_{ij'k'} X_{j'j} X_{k'k}$$

The full transformation matrix is accumulated in the memory buffer until convergence.

In each iteration, the optimum angle  $\gamma$  is found as follows: First, the roots of the finite Fourier series

$$a_0 + \sum_{p=1}^4 \{a_p \cos(px) + b_p \sin(px)\} = 0$$



are found. In the above equations, the expansion coefficients are calculated analytically as a function of  $I, J$  - the chosen indices in the Jacobi iteration subspace. The roots are evaluated by applying the Boyd's method[1], in which they are given as

$$\gamma_n = \Re[-i \ln(\lambda_n)]$$

where  $\lambda_n$  is an eigenvalue of the following 8 by 8 complex matrix:

$$\begin{pmatrix} 0 & 1 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 1 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 1 & 0 \\ -\frac{a_4+ib_4}{a_4-ib_4} & -\frac{a_3+ib_3}{a_4-ib_4} & -\frac{a_2+ib_2}{a_4-ib_4} & -\frac{a_1+ib_1}{a_4-ib_4} & -\frac{2a_0}{a_4-ib_4} & -\frac{a_1-ib_1}{a_4-ib_4} & -\frac{a_2-ib_2}{a_4-ib_4} & -\frac{a_3-ib_3}{a_4-ib_4} \end{pmatrix}$$

Once the eight roots of the Fourier series equation are found, one solution out of eight is chosen which satisfies the global optimum condition, i.e., the largest increase/decrease in the objective function given by

$$\delta Z = Z(\mathbf{U}(\gamma)) - Z(\mathbf{1})$$

The Hessian is not computed. All the  $N(N-1)/2$  unique pairs of molecular orbitals are checked and the optimal set of  $\gamma, I, J$  is chosen to construct  $\mathbf{X}^{\text{New}}$ .

#### References:

[1] Boyd, J.P.; J. Eng. Math. (2006) 56, pp. 203-219

### 17.47.2 Constructor & Destructor Documentation

**17.47.2.1** `oepdev::UnitaryOptimizer_4_2::UnitaryOptimizer_4_2 ( double * R, double * P, int n, double conv = 1.0e-6, int maxiter = 100, bool verbose = true )`

Create from R and P matrices and optimization options.

#### Parameters

<i>R</i>	- <b>R</b> tensor (flattened row-wise)
<i>P</i>	- <b>P</b> tensor (flattened row-wise)
<i>n</i>	- dimensionality of the problem ( <i>N</i> )
<i>conv</i>	- convergence in the <i>Z</i> function
<i>maxiter</i>	- maximum number of iterations
<i>verbose</i>	- whether print information of iteration process or not Sets up the optimizer.

**17.47.2.2** `oepdev::UnitaryOptimizer_4_2::UnitaryOptimizer_4_2 ( int n, double conv, int maxiter, bool verbose )`  
[protected]

Initialize the basic memory.

#### Parameters

<i>n</i>	- dimensionality of the problem ( <i>N</i> )
<i>conv</i>	- convergence in the <i>Z</i> function
<i>maxiter</i>	- maximum number of iterations

<code>verbose</code>	- whether print information of iteration process or not Sets up the optimizer.
----------------------	--

The documentation for this class was generated from the following files:

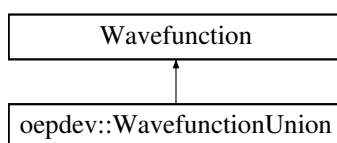
- oepdev/libutil/[unitary\\_optimizer.h](#)
- oepdev/libutil/[unitary\\_optimizer.cc](#)

## 17.48 oepdev::WavefunctionUnion Class Reference

Union of two Wavefunction objects.

```
#include <wavefunction_union.h>
```

Inheritance diagram for oepdev::WavefunctionUnion:



### Public Member Functions

- [WavefunctionUnion](#) (SharedWavefunction ref\_wfn, Options &options)  
*Constructor.*
- virtual [~WavefunctionUnion](#) ()  
*Destructor.*
- virtual double [compute\\_energy](#) ()  
*Compute Energy (now blank)*
- virtual double [nuclear\\_repulsion\\_interaction\\_energy](#) ()  
*Compute Nuclear Repulsion Energy between unions.*
- void [localize\\_orbitals](#) ()  
*Localize Molecular Orbitals.*
- void [transform\\_integrals](#) ()  
*Transform Integrals (2- and 4-index transformations)*
- int [l\\_nmo](#) (int n) const  
*Get number of molecular orbitals of the \*n\*th fragment.*
- int [l\\_nso](#) (int n) const  
*Get number of symmetry orbitals of the \*n\*th fragment.*
- int [l\\_ndocc](#) (int n) const  
*Get number of doubly occupied orbitals of the \*n\*th fragment.*
- int [l\\_nvir](#) (int n) const  
*Get number of virtual orbitals of the \*n\*th fragment.*
- int [l\\_nalpha](#) (int n) const  
*Get the number of the alpha electrons of the \*n\*th fragment.*
- int [l\\_nbeta](#) (int n) const  
*Get the number of the beta electrons of the \*n\*th fragment.*
- int [l\\_nbf](#) (int n) const  
*Get number of basis functions of the \*n\*th fragment.*
- int [l\\_noffs\\_ao](#) (int n) const  
*Get the basis set offset of the \*n\*th fragment.*
- double [l\\_energy](#) (int n) const

- Get the reference energy of the \*n\*th fragment.*
- SharedMolecule [l\\_molecule](#) (int n) const
  - Get the molecule object of the \*n\*th fragment.*
- SharedBasisSet [l\\_primary](#) (int n) const
  - Get the primary basis set object of the \*n\*th fragment.*
- SharedBasisSet [l\\_auxiliary](#) (int n) const
  - Get the auxiliary basis set object of the \*n\*th fragment.*
- SharedWavefunction [l\\_wfn](#) (int n) const
  - Get the wavefunction object of the \*n\*th fragment.*
- SharedMOSpace [l\\_mospace](#) (int n, const std::string &label) const
  - Get the MO space named label (either OCC or VIR) of the \*n\*th fragment.*
- SharedLocalizer [l\\_localizer](#) (int n) const
  - Get the orbital localizer object of the \*n\*th fragment.*
- SharedIntegralTransform [integrals](#) (void) const
  - Get the integral transform object of the entire union.*
- bool [has\\_localized\\_orbitals](#) (void) const
  - If union got its molecular orbital localized or not.*
- SharedBasisSet [primary](#) (void) const
  - Get the primary basis set for the entire union.*
- SharedMOSpace [mospace](#) (const std::string &label) const
  - Get the MO space named label (either OCC or VIR)*
- SharedMatrix [Ca\\_subset](#) (const std::string &basis="SO", const std::string &subset="ALL")
- SharedMatrix [Cb\\_subset](#) (const std::string &basis="SO", const std::string &subset="ALL")
- SharedMatrix [C\\_subset\\_helper](#) (SharedMatrix C, const Dimension &noccpi, SharedVector epsilon, const std::string &basis, const std::string &subset)
  - Helpers for Ca\_ and Cb\_ matrix transformers.*
- SharedVector [epsilon\\_subset\\_helper](#) (SharedVector epsilon, const Dimension &noccpi, const std::string &basis, const std::string &subset)
  - Helper for epsilon transformer.*
- void [print\\_header](#) (void)
  - Print information about this wavefunction union.*
- void [print\\_mo\\_integrals](#) (void)
  - Print the MO integrals.*

## Protected Attributes

- int [nIsolatedMolecules\\_](#)
  - Number of isolated molecules.*
- SharedWavefunction [dimer\\_wavefunction\\_](#)
  - The wavefunction for a dimer (electrons relaxed in the field of monomers)*
- SharedIntegralTransform [integrals\\_](#)
  - Integral transform object (2- and 4-index transformations)*
- bool [hasLocalizedOrbitals\\_](#)
  - whether orbitals of the union were localized (or not)*
- std::map< const std::string, SharedMOSpace > [mospacesUnion\\_](#)
  - Dictionary of MO spaces for the entire union (OCC and VIR)*
- std::vector< SharedMolecule > [l\\_molecule\\_](#)
  - List of molecules.*
- std::vector< SharedBasisSet > [l\\_primary\\_](#)
  - List of primary basis functions per molecule.*

- `std::vector< SharedBasisSet > l_auxiliary_`  
*List of auxiliary basis functions per molecule.*
- `std::vector< SharedWavefunction > l_wfn_`  
*List of original isolated wavefunctions (electrons unrelaxed)*
- `std::vector< std::string > l_name_`  
*List of names of isolated wavefunctions.*
- `std::vector< int > l_nbf_`  
*List of basis function numbers per molecule.*
- `std::vector< int > l_nmo_`  
*List of numbers of molecular orbitals (MO's) per molecule.*
- `std::vector< int > l_nso_`  
*List of numbers of SO's per molecule.*
- `std::vector< int > l_ndocc_`  
*List of numbers of doubly occupied orbitals per molecule.*
- `std::vector< int > l_nvir_`  
*List of numbers of virtual orbitals per molecule.*
- `std::vector< int > l_noffs_ao_`  
*List of basis set offsets per molecule.*
- `std::vector< double > l_energy_`  
*List of energies of isolated wavefunctions.*
- `std::vector< double > l_efzc_`  
*List of frozen-core energies per isolated wavefunction.*
- `std::vector< bool > l_density_fitted_`  
*List of information per wfn whether it was obtained using DF or not.*
- `std::vector< int > l_nalpha_`  
*List of numbers of alpha electrons per isolated wavefunction.*
- `std::vector< int > l_nbeta_`  
*List of numbers of beta electrons per isolated wavefunction.*
- `std::vector< int > l_nfrzc_`  
*List of numbers of frozen-core orbitals per isolated molecule.*
- `std::vector< SharedLocalizer > l_localizer_`  
*List of orbital localizers.*
- `std::vector< std::map< const std::string, SharedMOSpace > > l_mospace_`  
*List of dictionaries of MO spaces.*

### 17.48.1 Detailed Description

Union of two Wavefunction objects.

The [WavefunctionUnion](#) is the union of two unperturbed Wavefunctions.

#### Notes:

1. Works only for C1 symmetry! Therefore `this->nirrep() = 1`.
2. Does not set `reference_wavefunction_`
3. Sets `oeprop_` for the union of uncoupled molecules
4. Performs Hadamard sums on `H_`, `Fa_`, `Da_`, `Ca_` and `S_` based on uncoupled wavefunctions.
5. Since it is based on shallow copy of the original Wavefunction, it **changes** contents of this wavefunction. Reallocate and copy if you want to keep the original wavefunction.

**Warnings:**

1. Gradients, Hessians and frequencies are not touched, hence they are **wrong**!
2. Lagrangian (if present) is not touched, hence its **wrong**!
3. Ca/Cb and epsilon subsets were reimplemented from psi::Wavefunction to remove sorting of orbitals. However, the corresponding member functions are not virtual in psi::Wavefunction. This could bring problems when upcasting.

The following variables are *shallow* copies of variables inside the Wavefunction object, that is created for the *whole* molecule cluster:

- `basissets_` (DF/RI/F12/etc basis sets)
- `basisset_` (ORBITAL basis set)
- `sobasisset_` (Primary basis set for SO integrals)
- `AO2SO_` (AO2SO conversion matrix (AO in rows, SO in cols))
- `molecule_` (Molecule that this wavefunction is run on)
- `options_` (Options object)
- `psio_` (PSI file access variables)
- `integral_` (Integral factory)
- `factory_` (Matrix factory for creating standard sized matrices)
- `memory_` (How much memory you have access to)
- `nalpha_, nbeta_` (Total alpha and beta electrons)
- `nfrzc_` (Total frozen core orbitals)
- `doccpi_` (Number of doubly occupied per irrep)
- `soccpi_` (Number of singly occupied per irrep)
- `frzcpi_` (Number of frozen core per irrep)
- `frzvpi_` (Number of frozen virtuals per irrep)
- `nalphapi_` (Number of alpha electrons per irrep)
- `nbetapi_` (Number of beta electrons per irrep)
- `nsopi_` (Number of so per irrep)
- `nmopi_` (Number of mo per irrep)
- `nso_` (Total number of SOs)
- `nmo_` (Total number of MOs)
- `nirrep_` (Number of irreps; must be equal to 1 due to symmetry reasons)
- `same_a_b_dens_` and `same_a_b_orbs_` The rest is altered so that the Wavefunction parameters reflect a cluster of non-interacting (uncoupled, isolated, unrelaxed) molecular electron densities.

**17.48.2 Constructor & Destructor Documentation****17.48.2.1 oepdev::WavefunctionUnion::WavefunctionUnion ( SharedWavefunction *ref\_wfn*, Options & *options* )**

Constructor.

Provide wavefunction with molecule containing at least 2 fragments.

## Parameters

<i>ref_wfn</i>	- reference wavefunction
<i>options</i>	- Psi4 options

### 17.48.3 Member Function Documentation

**17.48.3.1** SharedMatrix oepdev::WavefunctionUnion::Ca\_subset ( const std::string & *basis* = "SO", const std::string & *subset* = "ALL" )

Return a subset of the Ca matrix in a desired basis

## Parameters

<i>basis</i>	the symmetry basis to use AO, SO
<i>subset</i>	the subset of orbitals to return ALL, ACTIVE, FROZEN, OCC, VIR, FROZEN_OCC, ACTIVE_OCC, ACTIVE_VIR, FROZEN_VIR

## Returns

the matrix in Pitzer order in the desired basis

**17.48.3.2** SharedMatrix oepdev::WavefunctionUnion::Cb\_subset ( const std::string & *basis* = "SO", const std::string & *subset* = "ALL" )

Return a subset of the Cb matrix in a desired basis

## Parameters

<i>basis</i>	the symmetry basis to use AO, SO
<i>subset</i>	the subset of orbitals to return ALL, ACTIVE, FROZEN, OCC, VIR, FROZEN_OCC, ACTIVE_OCC, ACTIVE_VIR, FROZEN_VIR

## Returns

the matrix in Pitzer order in the desired basis

The documentation for this class was generated from the following files:

- oepdev/libutil/[wavefunction\\_union.h](#)
- oepdev/libutil/wavefunction\_union.cc

# Chapter 18

## File Documentation

### 18.1 include/oepdev\_files.h File Reference

#### Macros

- #define `OEPDEV_USE_PSI4_DIIS_MANAGER` 0

*Use DIIS from Psi4 (1) or OEPDev (0)?*

- #define `OEPDEV_MAX_AM` 8

*L<sub>max</sub>.*

- #define `OEPDEV_N_MAX_AM` 17

*2L<sub>max</sub>+1*

- #define `OEPDEV_CRIT_ERI` 1e-9

*ERI criterion for E12, E34, E123 and lambda\*EXY coefficients.*

- #define `OEPDEV_SIZE_BUFFER_R` 250563

*Size of R buffer (OEPDEV\_N\_MAX\_AM\*OEPDEV\_N\_MAX\_AM\*OEPDEV\_N\_MAX\_AM\*OEPDEV\_N\_MAX\_AM\*3)*

- #define `OEPDEV_SIZE_BUFFER_D2` 3264

*Size of D2 buffer (3\*(OEPDEV\_MAX\_AM+1)\*(OEPDEV\_MAX\_AM+1)\*OEPDEV\_N\_MAX\_AM)*

## 18.2 main.cc File Reference

```
#include <cstdlib>
#include <cstdio>
#include <string>
#include "psi4/psi4-dec.h"
#include "psi4/psifiles.h"
#include "psi4/libdpd/dpd.h"
#include "include/oepdev_files.h"
#include "psi4/libparallel/parallel.h"
#include "psi4/liboptions/liboptions.h"
#include "psi4/libpsio/psio.h"
#include "psi4/libpsio/psio.hpp"
#include "psi4/libmints/molecule.h"
#include "psi4/libmints/wavefunction.h"
#include "psi4/libmints/basisset.h"
#include "psi4/libfunctional/superfunctional.h"
#include "oepdev/libutil/util.h"
#include "oepdev/libutil/cphf.h"
#include "oepdev/libutil/wavefunction_union.h"
#include "oepdev/libutil/integrals_iter.h"
#include "oepdev/libutil/space3d.h"
#include "oepdev/libutil/esp.h"
#include "oepdev/libutil/solver.h"
#include "oepdev/liboep/oep.h"
#include "oepdev/libpsi/potential.h"
#include "psi4/libtrans/mospace.h"
#include "psi4/libtrans/integraltransform.h"
#include "oepdev/libints/eri.h"
#include "oepdev/libpsi/integral.h"
#include "oepdev/libtest/test.h"
```

### Namespaces

- [psi](#)

*Psi4 package namespace.*

### Typedefs

- using **SharedMolecule** = std::shared\_ptr< Molecule >
- using **SharedSuperFunctional** = std::shared\_ptr< SuperFunctional >
- using **SharedWavefunction** = std::shared\_ptr< Wavefunction >
- using **SharedVector** = std::shared\_ptr< Vector >
- using **SharedMatrix** = std::shared\_ptr< Matrix >
- using **SharedBasisSet** = std::shared\_ptr< BasisSet >
- using **SharedUnion** = std::shared\_ptr< [oepdev::WavefunctionUnion](#) >
- using **SharedPSIO** = std::shared\_ptr< PSIO >
- using **SharedCPHF** = std::shared\_ptr< [oepdev::CPHF](#) >
- using **SharedMOSpace** = std::shared\_ptr< MOSpace >
- using **SharedIntegralTransform** = std::shared\_ptr< IntegralTransform >
- using **SharedIntegralFactory** = std::shared\_ptr< IntegralFactory >
- using **SharedTwoBodyAOInt** = std::shared\_ptr< TwoBodyAOInt >
- using **SharedMOSpaceVector** = std::vector< std::shared\_ptr< MOSpace >>
- using **intVector** = std::vector< int >



- using **SharedLocalizer** = std::shared\_ptr< Localizer >
- using **SharedOEPotential** = std::shared\_ptr< oepdev::OEPotential >
- using **SharedField3D** = std::shared\_ptr< oepdev::ScalarField3D >

## Functions

- int **psi::read\_options** (std::string name, Options &options)  
*Options for the OEPDev plugin.*
- SharedWavefunction **psi::oepdev** (SharedWavefunction ref\_wfn, Options &options)  
*Main routine of the OEPDev plugin.*

## 18.3 oepdev/libgefp/gefp.h File Reference

```
#include <vector>
#include <string>
#include <random>
#include <cmath>
#include "psi4/libmints/wavefunction.h"
#include "psi4/libmints/matrix.h"
#include "psi4/libmints/vector3.h"
#include "../liboep/oep.h"
#include "../libutil/cphf.h"
```

## Classes

- class **oepdev::GenEffPar**  
*Generalized Effective Fragment Parameters. Container Class.*
- class **oepdev::GenEffFrag**  
*Generalized Effective Fragment. Container Class.*
- class **oepdev::GenEffParFactory**  
*Generalized Effective Fragment Factory. Abstract Base.*
- class **oepdev::PolarGEFactory**  
*Polarization GEFP Factory.*
- class **oepdev::MOScaledPolarGEFactory**  
*Polarization GEFP Factory with Least-Squares Scaling of MO Space.*
- class **oepdev::FieldScaledPolarGEFactory**  
*Polarization GEFP Factory with Least-Squares Scaling of Cartesian Degrees of freedom.*

## Namespaces

- **oepdev**  
*OEPDev module namespace.*

## 18.4 oepdev/libints/eri.h File Reference

```
#include "psi4/libpsi4util/exception.h"
#include "psi4/libmints/integral.h"
#include "psi4/libmints/basisset.h"
#include "psi4/libmints/fjt.h"
#include "../libpsi/integral.h"
#include "recurr.h"
```

### Classes

- class [oepdev::TwoElectronInt](#)  
*General Two Electron Integral.*
- class [oepdev::ERI\\_1\\_1](#)  
*2-centre ERI of the form  $\langle a|O(2)|b\rangle$  where  $O(2) = 1/r^{12}$ .*
- class [oepdev::ERI\\_2\\_2](#)  
*4-centre ERI of the form  $\langle ab|O(2)|cd\rangle$  where  $O(2) = 1/r^{12}$ .*
- class [oepdev::ERI\\_3\\_1](#)  
*4-centre ERI of the form  $\langle abc|O(2)|d\rangle$  where  $O(2) = 1/r^{12}$ .*

### Namespaces

- [oepdev](#)  
*OEPEDev module namespace.*

## 18.5 oepdev/libints/recurr.h File Reference

### Namespaces

- [oepdev](#)  
*OEPEDev module namespace.*

### Macros

- `#define D1\_INDEX(x, i, n) ((81*(x))+(9*(i))+(n))`  
*Get the index of McMurchie-Davidson-Hermite D1 coefficient stored in the `mdh_buffer_`, that is attributed to the x Cartesian coordinate from angular momentum i of function 1, and the Hermite index n.*
- `#define D2\_INDEX(x, i, j, n) ((1377*(x))+(153*(i))+(17*(j))+(n))`  
*Get the index of McMurchie-Davidson-Hermite D2 coefficient stored in the `mdh_buffer_`, that is attributed to the x Cartesian coordinate from angular momenta i, j of function 1 and 2, and the Hermite index n.*
- `#define D3\_INDEX(x, i, j, k, n) ((18225*(x))+(2025*(i))+(225*(j))+(25*(k))+(n))`  
*Get the index of McMurchie-Davidson-Hermite D3 coefficient stored in the `mdh_buffer_`, that is attributed to the x Cartesian coordinate from angular momenta i, j and k of function 1, 2 and 3, and the Hermite index n.*
- `#define R\_INDEX(n, l, m, j) ((14739*(n))+(867*(l))+(51*(m))+(j))`  
*Get the index of McMurchie-Davidson R coefficient stored in the `mdh_buffer_R_` from angular momenta n, l and m and the Boys index j.*

## Functions

- double [oepdev::d\\_N\\_n1\\_n2](#) (int N, int n1, int n2, double PA, double PB, double aP)  
*Compute McMurchie-Davidson-Hermite (MDH) coefficient for binomial expansion.*
- void [oepdev::make\\_mdh\\_D1\\_coeff](#) (int n1, double aPd, double \*buffer)  
*Compute the McMurchie-Davidson-Hermite coefficients for monomial expansion.*
- void [oepdev::make\\_mdh\\_D2\\_coeff](#) (int n1, int n2, double aPd, double \*PA, double \*PB, double \*buffer)  
*Compute the McMurchie-Davidson-Hermite coefficients for binomial expansion.*
- void [oepdev::make\\_mdh\\_D3\\_coeff](#) (int n1, int n2, int n3, double aPd, double \*PA, double \*PB, double \*PC, double \*buffer)  
*Compute the McMurchie-Davidson-Hermite coefficients for trinomial expansion.*
- void [oepdev::make\\_mdh\\_D2\\_coeff\\_explicit\\_recursion](#) (int n1, int n2, double aP, double \*PA, double \*PB, double \*buffer)  
*Compute the McMurchie-Davidson-Hermite coefficients for binomial expansion by explicit recursion. This function makes the same changes to buffers as [oepdev::make\\_mdh\\_D2\\_coeff](#), but implements it through explicit recursion by calls to [oepdev::d\\_N\\_n1\\_n2](#). Therefore, it is slightly slower. Here for debugging purposes.*
- void [oepdev::make\\_mdh\\_R\\_coeff](#) (int N, int L, int M, double alpha, double a, double b, double c, double \*F, double \*buffer)  
*Compute the McMurchie-Davidson R coefficients.*

## 18.6 oepdev/liboep/oep.h File Reference

```
#include <stdio>
#include <string>
#include <vector>
#include <map>
#include "psi4/libparallel/parallel.h"
#include "psi4/liboptions/liboptions.h"
#include "psi4/libmints/wavefunction.h"
#include "psi4/libmints/basisset.h"
#include "psi4/libmints/matrix.h"
#include "psi4/libmints/vector.h"
#include "psi4/libthce/thce.h"
#include "psi4/libcubeprop/csg.h"
#include "../libutil/space3d.h"
```

## Classes

- struct [oepdev::OEType](#)  
*Container to handle the type of One-Electron Potentials.*
- class [oepdev::OEPotential](#)  
*Generalized One-Electron Potential: Abstract base.*
- class [oepdev::ElectrostaticEnergyOEPotential](#)  
*Generalized One-Electron Potential for Electrostatic Energy.*
- class [oepdev::RepulsionEnergyOEPotential](#)  
*Generalized One-Electron Potential for Pauli Repulsion Energy.*
- class [oepdev::ChargeTransferEnergyOEPotential](#)  
*Generalized One-Electron Potential for Charge-Transfer Interaction Energy.*
- class [oepdev::EETCouplingOEPotential](#)  
*Generalized One-Electron Potential for EET coupling calculations.*

## Namespaces

- [oepdev](#)

*OEPDev module namespace.*

## Typedefs

- using **oepdev::SharedWavefunction** = std::shared\_ptr< Wavefunction >
- using **oepdev::SharedBasisSet** = std::shared\_ptr< BasisSet >
- using **oepdev::SharedTensor** = std::shared\_ptr< Tensor >
- using **oepdev::SharedMatrix** = std::shared\_ptr< Matrix >
- using **oepdev::SharedVector** = std::shared\_ptr< Vector >

## 18.7 oepdev/libpsi/integral.h File Reference

```
#include "psi4/libmints/integral.h"
#include "psi4/libmints/basisset.h"
#include "psi4/libmints/matrix.h"
```

## Classes

- class [oepdev::TwoBodyAOInt](#)
- class [oepdev::IntegralFactory](#)

*Extended [IntegralFactory](#) for computing integrals.*

## Namespaces

- [oepdev](#)

*OEPDev module namespace.*

## 18.8 oepdev/libpsi/potential.h File Reference

```
#include <vector>
#include "psi4/psi4-dec.h"
#include "psi4/libparallel/parallel.h"
#include "psi4/liboptions/liboptions.h"
#include "psi4/libpsio/psio.h"
#include "psi4/libmints/typedefs.h"
#include "psi4/libmints/onebody.h"
#include "psi4/libmints/potential.h"
#include "psi4/libmints/sointegral_onebody.h"
#include "psi4/libmints/osrecur.h"
```

## Classes

- class [oepdev::PotentialInt](#)

*Computes potential integrals.*

## Namespaces

- [oepdev](#)  
*OEPCDev module namespace.*

## 18.9 oepdev/libtest/test.h File Reference

```
#include <vector>
#include "psi4/psi4-dec.h"
#include "psi4/libparallel/parallel.h"
#include "psi4/liboptions/liboptions.h"
#include "psi4/libpsio/psio.h"
#include "psi4/libmints/integral.h"
#include "psi4/libmints/wavefunction.h"
#include "psi4/libmints/basisset.h"
#include "psi4/libqt/qt.h"
#include "../libpsi/integral.h"
#include "../libutil/integrals_iter.h"
```

## Classes

- class [oepdev::test::Test](#)  
*Manages test routines.*

## Namespaces

- [oepdev](#)  
*OEPCDev module namespace.*

## 18.10 oepdev/libutil/diis.h File Reference

```
#include <cstdio>
#include <string>
#include <vector>
#include "psi4/libparallel/parallel.h"
#include "psi4/libciomr/libciomr.h"
#include "psi4/libmints/vector.h"
#include "psi4/libmints/matrix.h"
#include "psi4/libqt/qt.h"
```

## Classes

- class [oepdev::DIISManager](#)  
*DIIS manager.*

## Namespaces

- [oepdev](#)  
*OEPCDev module namespace.*

## 18.11 oepdev/libutil/esp.h File Reference

```
#include "psi4/libmints/vector.h"
#include "space3d.h"
```

### Classes

- class [oepdev::ESPSolver](#)  
*Charges from Electrostatic Potential (ESP). A solver-type class.*

### Namespaces

- [psi](#)  
*Psi4 package namespace.*
- [oepdev](#)  
*OEPPDev module namespace.*

### Typedefs

- using [psi::SharedVector](#) = std::shared\_ptr< Vector >
- using [oepdev::SharedScalarField3D](#) = std::shared\_ptr< ScalarField3D >

## 18.12 oepdev/libutil/integrals\_iter.h File Reference

```
#include <cstdio>
#include "psi4/libparallel/parallel.h"
#include "psi4/libmints/basisset.h"
#include "psi4/libmints/integral.h"
#include "../libpsi/integral.h"
```

### Classes

- class [oepdev::ShellCombinationsIterator](#)  
*Iterator for Shell Combinations. Abstract Base.*
- class [oepdev::AOIntegralsIterator](#)  
*Iterator for AO Integrals. Abstract Base.*
- class [oepdev::AllAOShellCombinationsIterator\\_4](#)  
*Loop over all possible ERI shells in a shell quartet.*
- class [oepdev::AllAOShellCombinationsIterator\\_2](#)  
*Loop over all possible ERI shells in a shell doublet.*
- class [oepdev::AllAOIntegralsIterator\\_4](#)  
*Loop over all possible ERI within a particular shell quartet.*
- class [oepdev::AllAOIntegralsIterator\\_2](#)  
*Loop over all possible ERI within a particular shell doublet.*

## Namespaces

- [oepdev](#)  
*OEPEv module namespace.*

## Typedefs

- using **oepdev::SharedIntegralFactory** = std::shared\_ptr< IntegralFactory >
- using **oepdev::SharedTwoBodyAOInt** = std::shared\_ptr< TwoBodyAOInt >
- using [oepdev::SharedShellsIterator](#) = std::shared\_ptr< ShellCombinationsIterator >  
*Iterator over shells as shared pointer.*
- using [oepdev::SharedAOIntsIterator](#) = std::shared\_ptr< AOIntegralsIterator >  
*Iterator over AO integrals as shared pointer.*

## 18.13 oepdev/libutil/solver.h File Reference

```
#include <cstdio>
#include <string>
#include <map>
#include "psi4/psi4-dec.h"
#include "psi4/libparallel/parallel.h"
#include "psi4/liboptions/liboptions.h"
#include "psi4/libpsio/psio.h"
#include "psi4/libmints/potential.h"
#include "psi4/libmints/integral.h"
#include "wavefunction_union.h"
#include "integrals_iter.h"
#include "../libpsi/integral.h"
#include "../liboep/oep.h"
```

## Classes

- class [oepdev::OEPEvSolver](#)  
*Solver of properties of molecular aggregates. Abstract base.*
- class [oepdev::ElectrostaticEnergySolver](#)  
*Compute the Coulombic interaction energy between unperturbed wavefunctions.*
- class [oepdev::RepulsionEnergySolver](#)  
*Compute the Pauli-Repulsion interaction energy between unperturbed wavefunctions.*
- class [oepdev::ChargeTransferEnergySolver](#)  
*Compute the Charge-Transfer interaction energy between unperturbed wavefunctions.*

## Namespaces

- [oepdev](#)  
*OEPEv module namespace.*

## Typedefs

- using **oepdev::SharedWavefunctionUnion** = std::shared\_ptr< WavefunctionUnion >
- using **oepdev::SharedOEPotential** = std::shared\_ptr< OEPotential >

## 18.14 oepdev/libutil/unitary\_optimizer.h File Reference

```
#include <string>
#include <complex>
#include "psi4/libmints/vector.h"
#include "psi4/libmints/matrix.h"
```

### Classes

- struct [oepdev::ABCD](#)  
*Simple structure to hold the Fourier series expansion coefficients.*
- struct [oepdev::Fourier9](#)  
*Simple structure to hold the Fourier series expansion coefficients for N=4.*
- class [oepdev::UnitaryOptimizer](#)  
*Find the optimim unitary matrix of quadratic matrix equation.*
- class [oepdev::UnitaryOptimizer\\_4\\_2](#)  
*Find the optimim unitary matrix for quartic-quadratic matrix equation with trace.*

### Namespaces

- [oepdev](#)  
*OEPEv module namespace.*

### Macros

- `#define IDX(i, j, n) ((n)*(i)+(j))`
- `#define IDX3(i, j, k) (n2_*(i)+n_*(j)+(k))`
- `#define IDX6(i, j, k, l, m, n) (n5_*(i)+n4_*(j)+n3_*(k)+n2_*(l)+n_*(m)+(n))`

### Functions

- `constexpr std::complex< double > oepdev::operator""_i (unsigned long long d)`
- `constexpr std::complex< double > oepdev::operator""_i (long double d)`



## 18.15 oepdev/libutil/util.h File Reference

```
#include <cstdio>
#include <string>
#include <map>
#include "psi4/psi4-dec.h"
#include "psi4/libparallel/parallel.h"
#include "psi4/liboptions/liboptions.h"
#include "psi4/libpsio/psio.h"
#include "psi4/libciomr/libciomr.h"
#include "psi4/libpsio/psio.hpp"
#include "psi4/libiwl/iwl.h"
#include "psi4/libqt/qt.h"
#include "psi4/libmints/molecule.h"
#include "psi4/libmints/writer.h"
#include "psi4/libmints/writer_file_prefix.h"
#include "psi4/libmints/wavefunction.h"
#include "psi4/libmints/basisset.h"
#include "psi4/libmints/vector.h"
#include "psi4/libmints/matrix.h"
#include "psi4/libmints/oeprop.h"
#include "psi4/libmints/local.h"
#include "psi4/libfunctional/superfunctional.h"
#include "psi4/libtrans/mospace.h"
#include "psi4/libtrans/integraltransform.h"
#include "psi4/libscf_solver/rhf.h"
#include "psi4/libdpd/dpd.h"
```

### Namespaces

- [oepdev](#)

*OEPEDev module namespace.*

### Typedefs

- using **oepdev::SharedMolecule** = std::shared\_ptr< Molecule >
- using **oepdev::SharedSuperFunctional** = std::shared\_ptr< SuperFunctional >
- using **oepdev::SharedMOSpace** = std::shared\_ptr< MOSpace >
- using **oepdev::SharedMOSpaceVector** = std::vector< std::shared\_ptr< MOSpace >>
- using **oepdev::SharedIntegralTransform** = std::shared\_ptr< IntegralTransform >
- using **oepdev::SharedLocalizer** = std::shared\_ptr< Localizer >

### Functions

- void [oepdev::preamble](#) (void)  
*Print preamble for module OEPEDEV.*
- template<typename... Args>  
std::string [oepdev::string\\_sprintf](#) (const char \*format, Args...args)  
*Format string output. Example: std::string text = oepdev::string\_sprintf("Test %3d, %13.5f", 5, -10.5425);.*
- std::shared\_ptr< SuperFunctional > [oepdev::create\\_superfunctional](#) (std::string name, Options &options)  
*Set up DFT functional.*
- std::shared\_ptr< Molecule > [oepdev::extract\\_monomer](#) (std::shared\_ptr< const Molecule > molecule\_  
dimer, int id)

*Extract molecule from dimer.*

- `std::shared_ptr< Wavefunction > oepdev::solve_scf` (`std::shared_ptr< Molecule > molecule`, `std::shared_ptr< BasisSet > primary`, `std::shared_ptr< SuperFunctional > functional`, `Options &options`, `std::shared_ptr< PSIO > psio`)

*Solve RHF-SCF equations for a given molecule in a given basis set.*

## 18.16 oepdev/libutil/wavefunction\_union.h File Reference

```
#include <cstdio>
#include <string>
#include <map>
#include "psi4/psi4-dec.h"
#include "psi4/libparallel/parallel.h"
#include "psi4/liboptions/liboptions.h"
#include "psi4/libpsio/psio.h"
#include "psi4/libciomr/libciomr.h"
#include "psi4/libpsio/psio.hpp"
#include "psi4/libqt/qt.h"
#include "psi4/libmints/molecule.h"
#include "psi4/libmints/writer.h"
#include "psi4/libmints/writer_file_prefix.h"
#include "psi4/libmints/wavefunction.h"
#include "psi4/libmints/basisset.h"
#include "psi4/libmints/vector.h"
#include "psi4/libmints/matrix.h"
#include "psi4/libmints/oeprop.h"
#include "psi4/libmints/local.h"
#include "psi4/libfunctional/superfunctional.h"
#include "psi4/libtrans/mospace.h"
#include "psi4/libtrans/integraltransform.h"
#include "psi4/libscf_solver/rhf.h"
#include "psi4/libdpd/dpd.h"
```

### Classes

- class `oepdev::WavefunctionUnion`  
*Union of two Wavefunction objects.*

### Namespaces

- `oepdev`  
*OEPEv module namespace.*

## Chapter 19

# Example Documentation

### 19.1 example\_cphf.cc

Shows how to use the `oeplib::CPHF` solver to compute molecular and LMO-distributed polarizabilities at RHF level of theory.

```
void example_cphf(std::shared_ptr<psi::Wavefunction> wfn, psi::Options& opt){  
    // build the solver  
    std::shared_ptr<oeplib::CPHF> solver = std::make_shared<oeplib::CPHF>(wfn, opt);  
  
    // run the solver to converge CPHF equations  
    solver->compute();  
  
    // print the LMO-distributed polarizabilities  
    for (int i=0; i<solver->nocc(); i++) {  
        solver->polarizability(i)->print();  
    }  
  
    // print the molecular polarizability  
    solver->polarizability()->print();  
  
    // grab 4th LMO-distributed polarizability and its associated LMO centroid  
    psi::SharedMatrix pol_4 = solver->polarizability(3);  
    psi::SharedVector rmo_4 = solver->lmo_centroid(3);  
};
```

### 19.2 example\_integrals\_iter.cc

Iterations over electron repulsion integrals in AO basis. This is an example of how to use

- the `oeplib::ShellCombinationsIterator` class
- the `oeplib::AOIntegralsIterator` class.

```
void iterate(std::shared_ptr<oeplib::IntegralFactory> ints)  
{  
    // Prepare for direct calculation of ERI's (shell by shell)  
    std::shared_ptr<psi::TwoBodyAOInt> tei(ints->eri());  
  
    // Grab the buffer where the integrals for a current shell will be placed  
    const double* buffer = tei->buffer();  
  
    // Create iterator to go through all shell quartet combinations  
    oeplib::SharedShellsIterator shellIter =  
        oeplib::ShellCombinationsIterator::build(ints, "ALL", 4);  
  
    // Iterate over shells, and then over all integrals in each shell quartet  
    for (shellIter->first(); shellIter->is_done() == false; shellIter->next())  
    {  
        // Compute all integrals between shells in the current quartet  
        shellIter->compute_shell(tei);  
    }  
}
```

```
// Create iterator to go through all integrals within a shell quartet
oepdev::SharedAOIntsIterator intsIter = shellIter->ao_iterator("ALL");

for (intsIter->first(); intsIter->is_done() == false; intsIter->next())
{
    // Grab current (ij|kl) indices here
    int i = intsIter->i();
    int j = intsIter->j();
    int k = intsIter->k();
    int l = intsIter->l();

    // Grab the (ij|kl) integral
    double integral = buffer[intsIter->index()];
}
}
```

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