### oepdev 1.0.0-alpha

Novel methods for Quantum Chemistry of Extended Molecular Aggregates

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## **Main Page**

#### oep-dev

Generalized One-Electron Potentials: Development Platform.

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#### Overview

Test various models of the intermolecular interaction that is based on the application of the **One-Electron Potentials** (**OEP's**) technique.

Currently, the interaction between two molecules described by the Hartree-Fock-Roothaan-Hall theory or the configuration interaction with singles theory is considered. In particular, the plugin tests the models of:

- 1. the Pauli exchange-repulsion interaction energy (Project II)
- 2. the Induction interaction energy (Project III)
- 3. the excitation energy transfer couplings (Project I)

against reference solutions (exact or other approximations).

Places to go:

- https://github.com/globulion/oepdev/blob/master/doc/git/doc\_oep\_design.md "OEP Design"
- https://github.com/globulion/oepdev/blob/master/doc/git/doc\_implemented\_models.md "Implemented Models"
- https://github.com/globulion/oepdev/blob/master/doc/git/doc\_programming\_etiquette.md "Programming Etiquette"
- Current Issues

#### References

[1]B. Błasiak, "One-Particle Density Matrix Polarization Susceptibility Tensors", \*Submitted\* \*\*2018\*\* XX, XXX

2 Main Page

### Introduction

Exploring biological phenomena at molecular scale is oftentimes indispensable to develop new drugs and intelligent materials.

Most of relevant system properties are affected by intermolecular interactions with nearby environment such as solvent or closely bound electronic chromophores. Studying such molecular aggregates requires rigorous and accurate quantum chemistry methods, the cost of which grows very fast with the number of electrons. Despite many methodologies have been devised to describe energetic and dynamical properties of **extended molecular systems** efficiently and accurately, there exist particularly difficult cases in which modelling is still challenging:

- · describing electronic transitions in solution or
- · when coupled with other electronic transition via resonance energy transfer,
- · performing molecular dynamics at very high level of theory including dynamic electron correlation,
- · vibrational frequency calculations of particular normal mode in condensed phases

and so on. The reason behind (sometimes prohibitively) high costs of fully *ab initio* calculations in the above areas is the complexity of mathematical models often based on wave functions rather then (conceptually more straightforward) electronic densities. On the other hand, it has been pointed out before that the one-electron density distributions are of particular importance in chemistry. It can be thus utilized as a means of developing a general model that re-expresses the physics of intermolecular interactions in terms of effective one-electron functions that are easier to handle in practice.

This Project will focus on finding a unified way to simplify various equations of Quantum Chemistry of extended molecular systems, i.e., molecular aggregates such as interacting chromophores and molecules solvated by water and other solvents. Indeed, one of the important difficulties encountered in Quantum Chemistry of large systems is the need of evaluation of special kind of numbers known as *electron repulsion integrals*, or in short, ERI's. In a typical calculation, the amount of ERI's can be as high as tens or even hundreds of millions (!) that unfortunately prevents from application of conventional methods when the number of particles in question is too large. In the Project, the complicated expressions involving ERI's shall be greatly simplified to reduce the computational costs as much as possible while introducing no or minor approximations to the original theories.

#### 2.1 Research Project Methodology

In this Project the new theoretical protocol based on the one-electron effective potentials (OEP's) is developed. The main principle is to rewrite arbitrary sum of functions f of electron repulsion integrals (ERI's) by defining OEP's according to the following general prescription:

$$\begin{split} &\sum_{f} f\left[\left(\phi_{i}^{A}\phi_{j}^{B}||\phi_{k}^{B}\phi_{l}^{B}\right)\right] = \left(\phi_{i}^{A}|v_{kl}^{B}|\phi_{j}^{A}\right) \rightarrow \text{ point charge or density fitting} \\ &\sum_{f} f\left[\left(\phi_{i}^{A}\phi_{j}^{B}||\phi_{k}^{B}\phi_{l}^{B}\right)\right] = \left(\phi_{i}^{A}|v_{kl}^{B}|\phi_{j}^{B}\right) \rightarrow \text{ density fitting,} \end{split}$$

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where A and B denote different molecules and  $\phi_i$  is the i-th molecular orbital or basis function. Here,  $v_{kl}^B$  denotes the List of One-Electron Potentals ab initio "OEP matrix element". The technique described above will be applied to simplify expressions for

- short-range excitation energy transfer couplings between chlorophyll subunits of reaction centres in photosynthesis
- · Pauli interaction repulsion energy
- · charge-transfer interaction energy
- electric field-induced charge density polarization of molecules.

The above developments might be used in fragment-based ab initio molecular dynamics protocols of new genera-

#### 2.2 Expected Impact on the Development of Science, Civilization and Society

The proposed OEP's are expected to significantly develop the fragment-based methods that are widely used in physical chemistry and modelling of biologically important systems. Owing to universality of OEP's, they could find applications in many branches of chemical science: non-empirical\* molecular dynamics, short-range resonance energy transfer in photosynthesis, electronic and vibrational solvatochromism, multidimensional spectroscopy and so on. In particular:

- the OEP-based models of Pauli repulsion energy and charge-transfer (CT) energy could be used to improve the computational performance of the second generation effective fragment potential method (EFP2). At present, the CT term is very time consuming and due to this reasons it is not used in most of applications of EFP2 to perform molecular dynamics simulations.
- the OEP-based model of EET couplings could significantly improve modelling of energy transfer in the light harvesting complexes. At present, short-range phenomena (Dexter mechanisms of EET) are very difficult to efficiently and quantitatively asses when performing statistical averaging and applying to large molecular aggregates. Such Dexter effects could be computed by using OEP's in much more efficient manner without loosing high accuracy of parent TDFI-TI method.
- the density matrix polarization (DMS) tensors could be used in new generation fragment-based *ab initio* molecular dynamics protocols that rigorously take into consideration electron correlation effects.

Therefore, it is strongly believed that the OEP's could have an indirect impact on the design of novel drugs and materials for industry.

#### 2.3 The OEPDev Code

To pursue the above challenges in the field of computational quantum chemistry of extended molecular aggregates, the OEPDev platform is developed. Accurate and efficient *ab initio* models based on OEP's are implemented in the OEPDev code, along with the state-of-the-art benchmark and competiting methods. Written entirely in C++, OEPDev is a plugin to Psi4 quantum chemistry package. Therefore, compilation and running the OEPDev code is straightforward and follows the API interface similar to the one used in Psi4 with just a few specific programing conventions. The detailed discussion about using the OEPDev code can be found in advanced usage section.

## **OEP Design.**

OEP (One-Electron Potential) is associated with certain quantum one-electron operator  $\hat{v}^A$  that defines the ability of molecule A to interact in a particular way with other molecules.

Technically, OEP can be understood as a **container object** (associated with the molecule in question) that stores the information about the above mentioned quantum operator. Here, it is assumed that similar OEP object is also defined for all other molecules in a molecular aggregate.

In case of interaction between molecules A and B, OEP object of molecule A interacts directly with wavefunction object of the molecule B. Defining a Solver class that handles such interaction Wavefunction class and OEP class the universal design of OEP-based approaches can be established and developed.

**Important:** OEP and Wavefunction classes should not be restricted to Hartree-Fock; in generall any correlated wavefunction and derived OEP's should be allowed to work with each other.

#### 3.1 OEP Classes

There are many types of OEP's, but the underlying principle is the same and independent of the type of intermolecular interaction. Therefore, the OEP's should be implemented by using a multi-level class design. In turn, this design depends on the way OEP's enter the mathematical expressions, i.e., on the types of matrix elements of the one-electron effective operator  $\hat{v}^A$ .

#### 3.1.1 Structure of possible OEP-based expressions and their unification

Structure of OEP-based mathematical expressions is listed below:

Туре	Matrix Element	Comment
Type 1	$(I \hat{v}^A J)$	$I \in A, J \in B$
Type 2	$(J \hat{v}^A \hat{L})$	$J,L\in B$

In the above table, I, J and K indices correspond to basis functions or molecular orbitals. Basis functions can be primary or auxiliary OEP-specialized density-fitting. Depending on the type of function and matrix element, there are many subtypes of resulting matrix elements that differ in their dimensionality. Examples are given below:

Matrix Element	DF-based form	ESP-based form
$\left(\mu \hat{v}^{A[\mu]} \sigma ight)$	$\sum_{\iota \in A} v_{\mu\iota}^A S_{\iota\sigma}$	$\sum_{lpha \in A} q_{lpha}^{A[\mu]} V_{\mu\sigma}^{(lpha)}$
$(i \hat{v}^{A[i]} j)$	$\sum_{i \in A} v_{ii}^A S_{1j}$	$\sum_{lpha \in A} q_{lpha}^{A[i]} V_{ij}^{(lpha)}$

6 OEP Design.



In the formulae above, the OEP-part (stored by OEP instances) and the Solver-part (to be computed by the Solver) are separated. It is apparent that all OEP-parts have the form of 2nd- or 3rd-rank tensors with different class of axes (molecular orbitals, primary/auxiliary basis, atomic space). Therefore, they can be uniquely defined by a unified *tensor object* (storing double precision numbers) and unified *dimension object* storing the information of the axes classes.

In Psi4, a perfect candidate for the above is psi4::Tensor class declared in psi4/libthce/thce.h. Except from the numeric content its instances also store the information of the dimensions in a form of a vector of psi4::Dimension instances.

Another possibility is to use psi::Matrix objects, instead of psi4::Tensor objects, possibly putting them into a std::vector container in case there is more than two axes.

### **List of One-Electron Potentals**

Here I provide the list of OEP's that have been already derived within the scope of the OEPDev project.

Note

Add here a table with all the OEP types along with their symbols used in the OEPDev code (e.g., Murrell.-etal-S1 etc).

#### 4.1 Electrostatic Energy OEP's

For electrostatic energy calculations, OEP is simply the electrostatic potential due to nuclei and electrons. 3D form:

$$v(\mathbf{r}) = \sum_{x} \frac{Z_{x}}{|\mathbf{r} - \mathbf{r}_{x}|} + \sum_{\mu\nu \in A} P_{\nu\mu} \int d\mathbf{r}' \frac{\phi_{\mu}^{*}(\mathbf{r}')\phi_{\nu}(\mathbf{r}')}{|\mathbf{r} - \mathbf{r}'|}$$

Matrix form:

$$v_{ik} = \sum_{x \in A} Z_x V_{ik}^{(x)} + \sum_{\mu \nu \in A} P_{\nu \mu} \left( \mu \nu | ik \right)$$

#### 4.2 Pauli Repulsion OEP's

The following potentials are derived for the evaluation of the Pauli repulsion energy based on Murrel's expressions.

#### 4.2.1 First-order contribution in overlap matrix expansion.

This contribution is simply the electrostatic potential coming from all nuclei and electron density except\* from electron density from molecular orbital i that interacts with the generalized overlap density between i of molecule A and j of molecule B.

3D forms:

$$v(\mathbf{r})_{S^{-1}}^{A[i]} = -\sum_{\mathbf{r} \in A} \frac{Z_{x}}{|\mathbf{r} - \mathbf{r}_{x}|} + \sum_{\mu, \nu \in A} \left\{ D_{\nu\mu} - C_{\mu i}^{*} C_{\nu i} \right\} \int d\mathbf{r}' \frac{\phi_{\mu}^{*}(\mathbf{r}') \phi_{\nu}(\mathbf{r}')}{|\mathbf{r} - \mathbf{r}'|}$$

Matrix forms:

$$v_{\xi_i}(S^{-1}) = \sum_{\kappa \in A} C_{i\kappa} \left\{ -\sum_{x \in A} V_{\kappa\xi}^{(x)} + \sum_{\mu\nu \in A} \left\{ D_{\nu\mu} - C_{\mu i}^* C_{\nu i} \right\} (\mu\nu | \xi \kappa) \right\}$$

4.2.2 Second-order contribution in overlap matrix expansion.

To be added here!

#### 4.3 Charge-Transfer Energy OEP's

To be added here!

#### 4.4 Excitonic Energy Transfer OEP's

The following potentials are derived for the evaluation of the short-range EET couplings based on Fujimoto's TDFI-TI method.

#### 4.4.1 ET contributions.

3D forms:

$$\begin{split} &v(\mathbf{r})_{1}^{A[\mu]} = -C_{\mu L}^{*} \sum_{x \in A} \frac{Z_{x}}{|\mathbf{r} - \mathbf{r}_{x}|} + \sum_{v_{K} \in A} \left\{ C_{\mu L}^{*} D_{v_{K}} - \frac{1}{2} C_{vL}^{*} D_{\mu_{K}} \right\} \int d\mathbf{r}' \frac{\phi_{v}^{*}(\mathbf{r}') \phi_{\kappa}(\mathbf{r}')}{|\mathbf{r} - \mathbf{r}'|} \\ &v(\mathbf{r})_{2}^{A[\mu]} = C_{\kappa H} \sum_{v_{K} \in A} \left\{ 2C_{vL}^{*} C_{\mu H}^{*} - C_{vH}^{*} C_{\mu L}^{*} \right\} \int d\mathbf{r}' \frac{\phi_{v}^{*}(\mathbf{r}') \phi_{\kappa}(\mathbf{r}')}{|\mathbf{r} - \mathbf{r}'|} \\ &v(\mathbf{r})_{3}^{A[\mu]} = v(\mathbf{r})_{1}^{A[\mu]} + v(\mathbf{r})_{1}^{A[\mu]} \end{split}$$

Matrix forms:

$$\begin{split} v_{\mu\xi}(1) &= -C_{\mu L}^* \sum_{\kappa \in A} V_{\mu\xi}^{\kappa} + \sum_{\nu\kappa \in A} \left\{ C_{\mu L}^* D_{\nu\kappa} - \frac{1}{2} C_{\nu L}^* D_{\mu\kappa} \right\} (\nu\kappa | \mu\xi) \\ v_{\mu\xi}(2) &= C_{\kappa H} \sum_{\nu\kappa \in A} \left\{ 2 C_{\nu L}^* C_{\mu H}^* - C_{\nu H}^* C_{\mu L}^* \right\} (\nu\kappa | \mu\xi) \\ v_{\mu\xi}(3) &= v_{\mu\xi}(1) + v_{\mu\xi}(2) \end{split}$$

#### 4.4.2 HT contributions.

Do be derived.

#### 4.4.3 CT contributions.

To be derived.

### 4.5 Full HF Interaction OEP's

The following potentials are derived for the evaluation of the full Hartree-Fock interaction energy based on the OEPDev equations.

п	iet	Ωf	On	e-F	lectr	nn	Pot	enta	ale
_	-131	OI.	VII	C-L	ICLI	UII	ГОІ	CIII	2113

## **Density-fitting Specialized for OEP's**

To get the ab-initio representation of a OEP, one can use a procedure similar to the typical density fitting or resolution of identity, both of which are nowadays widely used to compute electron-repulsion integrals (ERI's) more efficiently.

#### 5.1 Fitting in Complete Space

An arbitrary one-electron potential of molecule A acting on any state vector associated with molecule A can be expanded in an *auxiliary space* centered on A as

$$v|i) = \sum_{\xi \eta} v|\xi) [\mathbf{S}^{-1}]_{\xi \eta} (\eta|i)$$

under the necessary assumption that the auxiliary basis set is *complete*. In a special case when the basis set is orthogonal (e.g., molecular orbitals) the above relation simplifies to

$$v|i) = \sum_{\xi} v|\xi)(\xi|i)$$

It can be easily shown that the above general and exact expansion can be obtained by performing a density fitting in the complete space. We expand the LHS of the first equation on this page in a series of the auxiliary basis functions scaled by the undetermined expansion coefficients:

$$v|i) = \sum_{\xi} G_{i\xi}|\xi)$$

which we shall refer here as to the matrix form of the OEP operator. By constructing the least-squares objective function

$$Z[\{G_{\xi}^{(i)}\}] = \int d\mathbf{r}_1 \left[ v(\mathbf{r}_1)\phi_i(\mathbf{r}_1) - \sum_{\xi} G_{\xi}^{(i)}\phi_{\xi}(\mathbf{r}_1) \right]^2$$

and requiring that

$$rac{\partial Z[\{G_{m{\xi}}^{(i)}\}]}{\partial G_{u}^{(i)}}=0$$
 for all  $\mu$ 

we find the coefficients  $G_{\xi}^{(i)}$  to be

$$\mathbf{G}^{(i)} = \mathbf{v}^{(i)} \cdot \mathbf{S}^{-1}$$

where

$$v_{\eta}^{(i)} = (\eta | vi)$$
  
 $S_{\eta \xi} = (\eta | \xi)$ 

or explitictly

$$G_{i\xi} = \sum_{m{\eta}} [\mathbf{S}^{-1}]_{\xi\,m{\eta}}(m{\eta}|
u|i)$$

identical to what we obtained from application of the resolution of identity in space spanned by non-orthogonal complete set of basis vectors.

Since matrix elements of an OEP operator in auxiliary space can be computed in the same way as the matrix elements with any other basis function, one can formally write the following identity

$$(X|v|i) = \sum_{\xi \eta} S_{X\xi} [\mathbf{S}^{-1}]_{\xi \eta} (\eta |v|i)$$

where X is an arbitrary orbital. When the other orbital does not belong to molecule A but to the (changing) environment, it is straightforward to compute the resulting matrix element, which is simply given as

$$(j_{\in B}|v^A|i_{\in A}) = \sum_{\xi} S_{j\xi} G_{i\xi}$$

where *j* denotes the other (environmental) basis function.

In the above equation, the OEP-part (fragment parameters for molecule A only) and the Solver-part (subject to be computed by solver on the fly) are separated. This then forms a basis for fragment-based approach to solve Quantum Chemistry problems related to the extended molecular aggregates.

#### 5.2 Fitting in Incomplete Space

Density fitting scheme from previous section has practical disadvantage of a nearly-complete basis set being usually very large (spanned by large amount of basis set vectors). Any non-complete basis set won't work in the previous example. Since most of basis sets used in quantum chemistry do not form a complete set, it is beneficial to design a modified scheme in which it is possible to obtain the **effective** matrix elements of the OEP operator in a **incomplete** auxiliary space. This can be achieved by minimizing the following objective function

$$Z[\{G_{\xi}^{(i)}\}] = \iint d\mathbf{r}_1 d\mathbf{r}_2 \frac{\left[\nu(\mathbf{r}_1)\phi_i(\mathbf{r}_1) - \sum_{\xi} G_{\xi}^{(i)} \varphi_{\xi}(\mathbf{r}_1)\right] \left[\nu(\mathbf{r}_2)\phi_i(\mathbf{r}_2) - \sum_{\xi} G_{\eta}^{(i)} \varphi_{\eta}(\mathbf{r}_1)\right]}{|\mathbf{r}_1 - \mathbf{r}_2|}$$

Thus requesting that

$$rac{\partial Z[\{G_{oldsymbol{\xi}}^{(i)}\}]}{\partial G_{\mu}^{(i)}}=0 ext{ for all } \mu$$

we find the coefficients  $G_{\xi}^{(i)}$  to be

$$\mathbf{G}^{(i)} = \mathbf{b}^{(i)} \cdot \mathbf{A}^{-1}$$

where

$$b_{\eta}^{(i)} = (\eta || vi)$$
$$A_{\eta \xi} = (\eta || \xi)$$

The symbol || is to denote the operator  $r_{12}^{-1}$  and double integration over  $\mathbf{r}_1$  and  $\mathbf{r}_2$ . Thus, it is clear that in order to use this generalized density fitting scheme one must to compute two-centre electron repulsion integrals (implemented in oepdev::ERI\_1\_1) as well as four-centre asymmetric electron repulsion integrals of the type  $(\alpha\beta\gamma||\eta)$  (implemented in oepdev::ERI\_3\_1).

# **Implemented Models**

#### **6.1 Target Properties**

Detailed list of models which is to be implemented in the OEPDev project is given below:

Table 1. Models subject to be implemented and analyzed within oep-dev.

Pauli energy	Induction energy	EET Coupling
EFP2-Pauli	EFP2-Induced Dipoles	TrCAMM
Murrel et al.'s theory	Density Susceptibility	OEP-ET/HT
OEP-Murrel et al.'s		TDFI-TI
		FED
Exact (Stone's)	Exact (incl. CT)	Exact (ESD)

### 6.2 Target, Benchmark and Competing Models

The target models introduced in the Project shall be tested against the following benchmarks and compared with the following state-of-the-art models:

**Table 2.** Target models vs benchmarks and competitor models.

Target Model	Benchmarks	Competing Model
OEP-Murrel et al.'s	Murrel et al.'s	EFP2-Pauli
	Exact (Stone's)	
OEP-ET/HT + TrCAMM	Exact (ESD)	TDFI-TI
	FED	FED
	TDFI-TI	
Density Susceptibility	Exact (incl. CT)	EFP2-Induced Dipoles

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## Contributing to oep-dev

OepDev is a plugin to Psi4.

Therefore it should follow the programming etiquette of Psi4. Also, oep-dev has additional programming tips to make the code more versatile and easy in further development. Here, I emphasise on most important aspects regarding the **programming rules**.

#### 7.1 Main Plugin

Oep-dev has only *one* source file in the plugin base directory, i.e., main.cc. This is the main driver routine that handles the functionality of the whole OEP testing platform: specifies options for Psi4 input file and implements test routines based on the options. Include files directly related to main.cc are stored in the include directory, where only header files are present. Options are specified in include/oepdev\_options.h whereas macros and defines in include/oepdev\_files.h. Other sources are stored in MODULE/libNAME\* directories where NAME is the name of the library with sources and header files, whereas MODULE is the directory of the oep-dev module.

Things to remember:

- 1. **No other sources in base directory.** It is not permitted to place any new source or other files in the plugin base directory (i.e., where main.cc resides).
- 2. Sources in library directories. Any additional source code has to be placed in <code>oepdev/libNAME\*</code> directory (either existing one or a new one; in the latter case remember to add the new \*.cc files to <code>CMake-Lists.txt</code> in the plugin base directory.
- 3. **Miscellanea in special directories.** If you want to add additional documentation, put it in the doc directory. If you want to add graphics, put it in the images directory.

#### 7.2 Header files in libraries

Header files are handy in obtaining a quick glimpse of the functionality within certain library. Each library directory should contain at least one header file in oep-dev. However, header files can be problematic if not managed properly.

Things to remember:

1. **Header preprocessor variable**. Define the preprocessor variable specyfying the existence of include of the particular header file. The format of such is

```
#ifndef MODULE_LIBRARY_HEADER_h
#define MODULE_LIBRARY_HEADER_h
// rest of your code goes here
#endif // MODULE_LIBRARY_HEADER_h
```

Last line is the **end** of the header file. The preprocessor variables represents the directory tree <code>oepdev/-MODULE/LIBRARY/HEADER.h</code> structure (where <code>oepdev</code> is the base plugin directory). MODULE is the plugin module name (e.g. <code>oepdev</code>, the name of the module directory) <code>LIBRARY</code> is the name of the library (e.g. <code>libutil</code>, should be the same as library directory name) <code>HEADER</code> is the name of the header in library directory (e.g. <code>diis</code> for <code>diis.h</code> header file)

2. **Set module namespace**. To prevent naming clashes with other modules and with Psi4 it is important to operate in separate namespace (e.g. for a module).

```
namespace MODULE {
// your code goes here
} // EndNameSpace MODULE
```

For instance, all classes and functions in <code>oepdev</code> module are implemented within the namespace of the same label. Considering addition of other local namespaces within a module can also be useful in certain cases.

#### 7.3 Environmental variables

Defining the set of intrinsic environmental variables can help in code management and conditional compilation. The oep-dev environmental variables are defined in include/oepdev\_files.h file. Remember also about psi4 environmental variables defined in psi4/psifiles.h header. As a rule, the oep-dev environmental variable should have the following format:

```
OEPDEV_XXXX
```

where XXXX is the descriptive name of variable.

#### 7.4 Documenting the code

Code has to be documented (at best at a time it is being created). The place for documentation is always in header files. Additional documentation can be also placed in source files. Leaving a chunk of code for a production run without documentation is unacceptable.

Use Doxygen style for documentation all the time. Remember that it supports markdown which can make the documentation even more clear and easy to understand. Additionally you can create a nice .rst documentation file for Sphinx program. If you are coding equations, always include formulae in the documentation!

Things to remember:

- Descriptions of classes, structures, global functions, etc. Each programming object should have a description.
- 2. **Documentation for function arguments and return object**. Usage of functions and class methods should be explained by providing the description of all arguments (use \param and \return Doxygen keywords).
- 3. **One-line description of class member variables**. Any class member variable should be preceded by a one-liner documentation (starting from //).
- 4. Do not be afraid of long names in the code. Self-documenting code is a bless!

#### 7.5 Naming conventions

Naming is important because it helps to create more readable and clear self-documented code.

Some loose suggestions:

- 1. Do not be afraid of long names in the code, but avoid redundancy. Examples of good and bad names: good name: get\_density\_matrix; bad name: get\_matrix. Unless there is only one type of matrix a particular objects can store, matrix is not a good name for a getter method. good name: class Wavefunction, bad name: class WFN good name: int numberOfErrorVectors, bad name: int nvec, bad name: the\_number\_of\_error\_vectors good name: class EfPotential, probably bad name: class EffectiveFragmentPotential. The latter might be understood by some people as a class that inherits from EffectiveFragment class. If it is not the case, compromise between abbreviation and long description is OK.
- 2. Short names are OK in special situations. In cases meaning of a particular variable is obvious and it is frequently used in the code locally, it can be named shortly. Examples are: i when iterating no number of occupied orbitals, nv number of virtual orbitals, etc.
- 3. Clumped names for variables and dashed names for functions. Try to distinguish between variable name like sizeOfOEPTypeList and a method name get\_matrix() (neither size\_of\_OEP\_type\_-list, nor getMatrix()). This is little bit cosmetics, but helps in managing the code when it grows.
- 4. Class names start from capital letter. However, avoid only capital letters in class names, unless it is obvious. Avoid also dashes in class names (they are reserved for global functions and class methods). Examples: good name: DIISManager, bad name: DIIS. good name: EETCouplingSolver, bad name: EETSolver, very bad: EET.

#### 7.6 Use Object-Oriented Programming

Try to organise your creations in objects having special relationships and data structures. Encapsulation helps in producing self-maintaining code and is much easier to use. Use:

- · factory design for creating objects
- · container design for designing data structures
- · polymorphysm when dealing with various flavours of one particular feature in the data structure

*Note:* In Psi4, factories are frequently implemented as static methods of the base classes, for example psi::BasisSet::build static method. It can be followed when building object factories in oep-dev too.

Contri	huting	to o	ep-dev
COLL	Dutilly	IU U	cp-ucv

# **Advanced Usage**

This section is addressed for advanced users.

Make sure you have first read the introduction before proceeding.

- 8.1 OEPDev Code Structure
- 8.1.1 Main Plugin
- 8.1.2 Modules
- 8.1.3 Documentation
- 8.2 OEPDev Classes: Overview

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# Chapter 10

# **Module Index**

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# Chapter 11

# Namespace Index

# 11.1 Namespace List

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# Chapter 13

# **Class Index**

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# Chapter 14

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## 14.1 File List

Here is a list of all documented files with brief descriptions:

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include/oepdev_files.h
include/oepdev_options.h
include/doxygen/oepdev_manual.h
include/doxygen/oepdev_modules.h
include/doxygen/oepdev_namespaces.h
oepdev/lib3d/esp.h
oepdev/lib3d/ <b>space3d.h</b>
oepdev/libgefp/gefp.h
oepdev/libints/eri.h
oepdev/libints/recurr.h
oepdev/liboep/oep.h
oepdev/liboep/oep_gdf.h
oepdev/libpsi/integral.h
oepdev/libpsi/potential.h
oepdev/libtest/test.h
oepdev/libutil/cphf.h
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oepdev/libutil/scf_perturb.h
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oepdev/libutil/unitary_optimizer.h
oepdev/libutil/util.h
oepdev/libutil/wavefunction_union.h

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# **Chapter 15**

# **Module Documentation**

## 15.1 The Generalized One-Electron Potentials Library

Implements the goal of this project: The Generalized One-Electron Potentials (OEP's). You will find here OEP's for computation of Pauli repulsion energy, charge-transfer energy and others.

#### **Classes**

struct oepdev::OEPType

Container to handle the type of One-Electron Potentials.

· class oepdev::OEPotential

Generalized One-Electron Potential: Abstract base.

class oepdev::ElectrostaticEnergyOEPotential

Generalized One-Electron Potential for Electrostatic Energy.

class oepdev::RepulsionEnergyOEPotential

Generalized One-Electron Potential for Pauli Repulsion Energy.

• class oepdev::ChargeTransferEnergyOEPotential

Generalized One-Electron Potential for Charge-Transfer Interaction Energy.

class oepdev::EETCouplingOEPotential

Generalized One-Electron Potential for EET coupling calculations.

· class oepdev::GeneralizedDensityFit

Generalized Density Fitting Scheme. Abstract Base.

· class oepdev::SingleGeneralizedDensityFit

Generalized Density Fitting Scheme - Single Fit.

· class oepdev::DoubleGeneralizedDensityFit

Generalized Density Fitting Scheme - Double Fit.

#### 15.1.1 Detailed Description

Implements the goal of this project: The Generalized One-Electron Potentials (OEP's). You will find here OEP's for computation of Pauli repulsion energy, charge-transfer energy and others.

## 15.2 The OEPDev Solver Library

Implementations of various solvers for molecular properties as a functions of unperturbed monomeric wavefunctions. This is the place all target OEP-based models are implemented and compared with benchmark models.

#### Classes

· class oepdev::OEPDevSolver

Solver of properties of molecular aggregates. Abstract base.

· class oepdev::ElectrostaticEnergySolver

Compute the Coulombic interaction energy between unperturbed wavefunctions.

• class oepdev::RepulsionEnergySolver

Compute the Pauli-Repulsion interaction energy between unperturbed wavefunctions.

• class oepdev::ChargeTransferEnergySolver

Compute the Charge-Transfer interaction energy between unperturbed wavefunctions.

#### 15.2.1 Detailed Description

Implementations of various solvers for molecular properties as a functions of unperturbed monomeric wavefunctions. This is the place all target OEP-based models are implemented and compared with benchmark models.

### 15.3 The Generalized Effective Fragment Potentials Library

Implements the GEFP method, the far goal of the OEPDev project. Here you will find the containers for GEFP parameters, the density matrix susceptibility tensors and GEFP solvers.

#### Classes

· class oepdev::GenEffPar

Generalized Effective Fragment Parameters. Container Class.

class oepdev::GenEffFrag

Generalized Effective Fragment. Container Class.

· class oepdev::GenEffParFactory

Generalized Effective Fragment Factory. Abstract Base.

class oepdev::PolarGEFactory

Polarization GEFP Factory. Abstract Base.

class oepdev::AbInitioPolarGEFactory

Polarization GEFP Factory from First Principles. Hartree-Fock Approximation.

class oepdev::FFAbInitioPolarGEFactory

Polarization GEFP Factory from First Principles: Finite-Difference Model. Arbitrary level of theory.

· class oepdev::GeneralizedPolarGEFactory

Polarization GEFP Factory with Least-Squares Parameterization.

· class oepdev::UniformEFieldPolarGEFactory

Polarization GEFP Factory with Least-Squares Parameterization.

· class oepdev::NonUniformEFieldPolarGEFactory

Polarization GEFP Factory with Least-Squares Parameterization.

class oepdev::LinearUniformEFieldPolarGEFactory

Polarization GEFP Factory with Least-Squares Parameterization.

class oepdev::QuadraticUniformEFieldPolarGEFactory

Polarization GEFP Factory with Least-Squares Parameterization.

class oepdev::LinearNonUniformEFieldPolarGEFactory

 ${\it Polarization~GEFP~Factory~with~Least-Squares~Parameterization.}$ 

• class oepdev::QuadraticNonUniformEFieldPolarGEFactory

Polarization GEFP Factory with Least-Squares Parameterization.

• class oepdev::LinearGradientNonUniformEFieldPolarGEFactory

Polarization GEFP Factory with Least-Squares Parameterization.

class oepdev::QuadraticGradientNonUniformEFieldPolarGEFactory

Polarization GEFP Factory with Least-Squares Parameterization.

class oepdev::UnitaryTransformedMOPolarGEFactory

Polarization GEFP Factory with Least-Squares Scaling of MO Space.

### 15.3.1 Detailed Description

Implements the GEFP method, the far goal of the OEPDev project. Here you will find the containers for GEFP parameters, the density matrix susceptibility tensors and GEFP solvers.

## 15.4 The Integral Package Library

Implementations of various one- and two-body integrals via McMurchie-Davidson recurrence scheme.

#### Classes

· class oepdev::TwoElectronInt

General Two Electron Integral.

class oepdev::ERI\_1\_1

2-centre ERI of the form (a|O(2)|b) where O(2) = 1/r12.

• class oepdev::ERI 2 2

4-centre ERI of the form (ab |O(2)| cd) where O(2) = 1/r12.

class oepdev::ERI\_3\_1

4-centre ERI of the form (abc |O(2)|d) where O(2) = 1/r12.

- class oepdev::TwoBodyAOInt
- · class oepdev::IntegralFactory

Extended IntegralFactory for computing integrals.

· class oepdev::PotentialInt

Computes potential integrals.

#### **Macros**

#define D1\_INDEX(x, i, n) ((81\*(x))+(9\*(i))+(n))

Get the index of McMurchie-Davidson-Hermite D1 coefficient stored in the mdh\_buffer\_, that is attributed to the x Cartesian coordinate from angular momentum i of function 1, and the Hermite index n.

#define D2\_INDEX(x, i, j, n) ((1377\*(x))+(153\*(i))+(17\*(j))+(n))

Get the index of McMurchie-Davidson-Hermite D2 coefficient stored in the mdh\_buffer\_, that is attributed to the x Cartesian coordinate from angular momenta i, j of function 1 and 2, and the Hermite index n.

• #define D3\_INDEX(x, i, j, k, n) ((18225\*(x))+(2025\*(i))+(225\*(j))+(25\*(k))+(n))

Get the index of McMurchie-Davidson-Hermite D3 coefficient stored in the mdh\_buffer\_, that is attributed to the x Cartesian coordinate from angular momenta i, j and k of function 1, 2 and 3, and the Hermite index n.

• #define R\_INDEX(n, I, m, j) ((14739\*(n))+(867\*(l))+(51\*(m))+(j))

Get the index of McMurchie-Davidson R coefficient stored in the mdh\_buffer\_R\_ from angular momenta n, I and m and the Boys index j.

#### **Functions**

• double oepdev::d\_N\_n1\_n2 (int N, int n1, int n2, double PA, double PB, double aP)

Compute McMurchie-Davidson-Hermite (MDH) coefficient for binomial expansion.

• void oepdev::make\_mdh\_D1\_coeff (int n1, double aPd, double \*buffer)

Compute the McMurchie-Davidson-Hermite coefficients for monomial expansion.

 $\bullet \ \ void\ oepdev:: make\_mdh\_D2\_coeff\ (int\ n1,\ int\ n2,\ double\ aPd,\ double\ *PA,\ double\ *PB,\ double\ *buffer)$ 

Compute the McMurchie-Davidson-Hermite coefficients for binomial expansion.

void oepdev::make\_mdh\_D3\_coeff (int n1, int n2, int n3, double aPd, double \*PA, double \*PB, double \*PC, double \*buffer)

Compute the McMurchie-Davidson-Hermite coefficients for trinomial expansion.

• void oepdev::make\_mdh\_D2\_coeff\_explicit\_recursion (int n1, int n2, double aP, double \*PA, double \*PB, double \*buffer)

Compute the McMurchie-Davidson-Hermite coefficients for binomial expansion by explicit recursion. This function makes the same changes to buffers as oepdev::make\_mdh\_D2\_coeff, but implements it through explicit recursion by calls to oepdev::d\_N\_n1\_n2. Therefore, it is slightly slower. Here for debugging purposes.

void oepdev::make\_mdh\_R\_coeff (int N, int L, int M, double alpha, double a, double b, double c, double \*F, double \*buffer)

Compute the McMurchie-Davidson R coefficients.

#### 15.4.1 Detailed Description

Implementations of various one- and two-body integrals via McMurchie-Davidson recurrence scheme. Here, we define the primitive Gaussian type functions (GTO's)

$$\phi_{i}(\mathbf{r}) \equiv x_{A}^{n_{1}} y_{A}^{l_{1}} z_{A}^{m_{1}} e^{-\alpha_{1} r_{A}^{2}}$$

$$\phi_{j}(\mathbf{r}) \equiv x_{B}^{n_{2}} y_{B}^{l_{2}} z_{B}^{m_{2}} e^{-\alpha_{2} r_{B}^{2}}$$

$$\phi_{k}(\mathbf{r}) \equiv x_{C}^{n_{3}} y_{C}^{l_{3}} z_{C}^{m_{3}} e^{-\alpha_{3} r_{C}^{2}}$$

in which  $\mathbf{r}_A \equiv \mathbf{r} - \mathbf{A}$  and so on.  $\mathbf{A}$  is the centre of the GTO,  $\alpha_1$  its exponent, whereas  $n_1, l_1, m_1$  the Cartesian angular momenta, with the total angular momentum  $\theta_1 = n_1 + l_1 + m_1$ .

In OEPDev implementations, the following definition shall be in use:

$$\mathbf{P} \equiv \frac{\alpha_1 \mathbf{A} + \alpha_2 \mathbf{B}}{\alpha_1 + \alpha_2}$$

$$\mathbf{Q} \equiv \frac{\alpha_3 \mathbf{C} + \alpha_4 \mathbf{D}}{\alpha_3 + \alpha_4}$$

$$\mathbf{R} \equiv \frac{\alpha_1 \mathbf{A} + \alpha_2 \mathbf{B} + \alpha_3 \mathbf{C}}{\alpha_1 + \alpha_2 + \alpha_3}$$

$$\alpha_P \equiv \alpha_1 + \alpha_2$$

$$\alpha_Q \equiv \alpha_3 + \alpha_4$$

$$\alpha_R \equiv \alpha_1 + \alpha_2 + \alpha_3$$

The unnormalized products of primitive GTO's are denoted here as

$$[ij] \equiv \phi_i(\mathbf{r})\phi_j(\mathbf{r})$$
$$[ijk] \equiv \phi_i(\mathbf{r})\phi_j(\mathbf{r})\phi_k(\mathbf{r})$$

#### 15.4.2 Hermite Operators

It is convenient to define

$$\Lambda_j(x_P;\alpha_P) \equiv \left(\frac{\partial}{\partial P_x}\right)^j = \alpha_P^{j/2} H_j(\sqrt{\alpha_P} x_P)$$

where  $H_j(x)$  is the Hermite polynomial of order j evaluated at x. Introduction of the above Hermite operator can be used by invoking the recurrence relationship due to Hermite polynomial properties:

$$x_A \Lambda_j(x_P; \alpha_P) = j\Lambda_{j-1} + |\mathbf{P} - \mathbf{A}|_x \Lambda_j + \frac{1}{2\alpha_P} \Lambda_{j+1}$$

This can be directly used to derive very useful McMurchie-Davidson-Hermite coefficients as expansion coefficients of the polynomial expansions.

### 15.4.2.1 Polynomial Expansions as Hermite Series

By using the previous relation, it is possible to express the following expansions in Hermite series:

$$x_A^{n_1} = \sum_{N=0}^{n_1} d_N^{n_1} \Lambda_N(x_A; \alpha_A)$$

$$x_A^{n_1} x_B^{n_2} = \sum_{N=0}^{n_1+n_2} d_N^{n_1 n_2} \Lambda_N(x_P; \alpha_P)$$

$$x_A^{n_1} x_B^{n_2} x_C^{n_3} = \sum_{N=0}^{n_1+n_2+n_3} d_N^{n_1 n_2 n_3} \Lambda_N(x_R; \alpha_R)$$

The recurrence relationships can be easily found and they read

$$d_N^{n_1+1} = \frac{1}{2\alpha_A} d_{N-1}^{n_1} + (N+1) d_{N+1}^{n_1}$$

as well as

$$d_N^{n_1+1,n_2} = \frac{1}{2\alpha_P} d_{N-1}^{n_1n_2} + |\mathbf{P} - \mathbf{A}|_x d_N^{n_1n_2} + (N+1) d_{N+1}^{n_1n_2}$$
  
$$d_N^{n_1,n_2+1} = \frac{1}{2\alpha_P} d_{N-1}^{n_1n_2} + |\mathbf{P} - \mathbf{B}|_x d_N^{n_1n_2} + (N+1) d_{N+1}^{n_1n_2}$$

and

$$\begin{split} d_N^{n_1+1,n_2,n_3} &= \frac{1}{2\alpha_R} d_{N-1}^{n_1n_2n_3} + |\mathbf{R} - \mathbf{A}|_x d_N^{n_1n_2n_3} + (N+1) d_{N+1}^{n_1n_2n_3} \\ d_N^{n_1,n_2+1,n_3} &= \frac{1}{2\alpha_R} d_{N-1}^{n_1n_2n_3} + |\mathbf{R} - \mathbf{B}|_x d_N^{n_1n_2n_3} + (N+1) d_{N+1}^{n_1n_2n_3} \\ d_N^{n_1,n_2,n_3+1} &= \frac{1}{2\alpha_R} d_{N-1}^{n_1n_2n_3} + |\mathbf{R} - \mathbf{C}|_x d_N^{n_1n_2n_3} + (N+1) d_{N+1}^{n_1n_2n_3} \end{split}$$

respectively. The first elements are given by

$$d_0^0 = 1$$
$$d_0^{00} = 1$$
$$d_0^{000} = 1$$

By using the above formalisms, it is strightforward to express the doublet of primitive GTO's as

$$[ij] = E_{ij} \sum_{N=0}^{n_1+n_2} \sum_{l=0}^{l_1+l_2} \sum_{M=0}^{m_1+m_2} d_N^{n_1n_2} d_L^{l_1l_2} d_M^{m_1m_2} \Lambda_N(x_P) \Lambda_L(y_P) \Lambda_M(z_P) e^{-\alpha_P r_P^2}$$

Analogously, the triplet of primitive GTO's is given by

$$[ijk] = E_{ijk} \sum_{N=0}^{n_1 + n_2 + n_3} \sum_{l=0}^{l_1 + l_2 + l + 3} \sum_{M=0}^{m_1 + m_2 + m_3} d_N^{n_1 n_2 n_3} d_L^{l_1 l_2 l_3} d_M^{m_1 m_2 m_3} \Lambda_N(x_R) \Lambda_L(y_R) \Lambda_M(z_R) e^{-\alpha_R r_R^2}$$

The multiplicative constants are given by

$$E_{ij}(\alpha_1, \alpha_2) = \exp\left[-\frac{\alpha_1 \alpha_2}{\alpha_1 + \alpha_2} |\mathbf{A} - \mathbf{B}|^2\right]$$

$$E_{ijk}(\alpha_1, \alpha_2, \alpha_3) = \exp\left[-\frac{\alpha_1 \alpha_2}{\alpha_1 + \alpha_2} |\mathbf{A} - \mathbf{B}|^2\right] \exp\left[-\frac{(\alpha_1 + \alpha_2) \alpha_3}{\alpha_1 + \alpha_2 + \alpha_3} |\mathbf{P} - \mathbf{C}|^2\right]$$

#### 15.4.3 One-Body Integrals over Hermite Functions

The fundamental Hermite integrals that appear during computations of any kind of one-body integrals over GTO's are as follows

$$[NLM|\Theta(1)] \equiv \int d\mathbf{r}_1 \Theta(\mathbf{r}_1) \Lambda_N(x_{1P}; \alpha_P) \Lambda_L(y_{1P}; \alpha_P) \Lambda_M(z_{1P}; \alpha_P) e^{-\alpha_P r_{1P}^2}$$

It immediately follows that the overlap, dipole, quadrupole and potential integrals are given as

$$[NLM|1] = \delta_{N0}\delta_{L0}\delta_{M0} \left(\frac{\pi}{\alpha_P}\right)^{3/2}$$

$$[NLM|x_C] = [\delta_{N1} + |\mathbf{PC}|_x \delta_{N0}] \delta_{L0}\delta_{M0} \left(\frac{\pi}{\alpha_P}\right)^{3/2}$$

$$[NLM|x_C^2] = \left[2\delta_{N2} + 2|\mathbf{PC}|_x \delta_{N1} + \left(|\mathbf{PC}|_x^2 + \frac{1}{2\alpha_P}\right)\delta_{N0}\right] \delta_{L0}\delta_{M0} \left(\frac{\pi}{\alpha_P}\right)^{3/2}$$

$$[NLM|x_C y_C] = (\delta_{N1} + |\mathbf{PC}|_x \delta_{N0}) \left(\delta_{L1} + |\mathbf{PC}|_y \delta_{L0}\right) \delta_{M0} \left(\frac{\pi}{\alpha_P}\right)^{3/2}$$

$$[NLM|r_C^{-1}] = \frac{2\pi}{\alpha_P} R_{NLM}$$

The coefficients  $R_{NLM}$  are discussed in separate section below.

#### 15.4.4 Two-Body Integrals over Hermite Functions

The fundamental Hermite integrals that appear during computations of any kind of two-electron integrals over GTO's are as follows

$$[N_{1}L_{2}M_{2}|N_{2}L_{2}M_{2}] \equiv \iint d\mathbf{r}_{1}d\mathbf{r}_{2}\Lambda_{N_{1}}(x_{1P};\alpha_{P})\Lambda_{L_{1}}(y_{1P};\alpha_{P})\Lambda_{M_{1}}(z_{1P};\alpha_{P})\Lambda_{N_{2}}(x_{2Q};\alpha_{Q})\Lambda_{L_{2}}(y_{2Q};\alpha_{Q})\Lambda_{M_{2}}(z_{2Q};\alpha_{Q})e^{-\alpha_{P}r_{1P}^{2}-\alpha_{Q}r_{2Q}^{2}}$$

The above formula dramatically reduces to the following

$$[N_1L_2M_2|N_2L_2M_2] = \lambda(-)^{N_2+L_2+M_2}R_{N_1+N_2,L_1+L_2,M_1+M_2}$$

with

$$\lambda \equiv \frac{2\pi^{5/2}}{\alpha_P \alpha_O \sqrt{\alpha_P + \alpha_O}}$$

To compute the  $R_{N1+N2,L1+L2,M1+M2}$  coefficients, the parameter T is given by

$$T = \frac{\alpha_P \alpha_Q}{\alpha_P + \alpha_O} |\mathbf{P} - \mathbf{Q}|^2$$

#### 15.4.5 The R(N,L,M) Coefficients

The R coefficients are defined as

$$R_{NLM} \equiv \left(\frac{\partial}{\partial a}\right)^N \left(\frac{\partial}{\partial b}\right)^L \left(\frac{\partial}{\partial c}\right)^M \int_0^1 e^{-Tu^2} du$$

with

$$T \equiv \alpha \left( a^2 + b^2 + c^2 \right)$$

By extending the above definition to more general

$$R_{NLMj} \equiv \left(-\sqrt{\alpha}\right)^{N+L+M} (-2\alpha)^{j} \int_{0}^{1} u^{N+L+M+2j} H_{N}(au\sqrt{\alpha}) H_{L}(bu\sqrt{\alpha}) H_{M}(cu\sqrt{\alpha}) e^{-Tu^{2}} du$$

one can see that

$$R_{000j} = (-2\alpha)^j F_j(T)$$

The Boys function is here given by

$$F_j(T) \equiv \int_0^1 u^{2j} e^{-Tu^2} du$$

and its efficient implementation can be discussed elsewhere. In Psi4,  $psi::Taylor_Fjt$  class is used for this purpose.

Now, it is possible to show that the following recursion relationships are true:

$$R_{0,0,M+1,j} = cR_{0,0,M,j+1} + MR_{0,0,M-1,j+1}$$
  
 $R_{0,L+1,M,j} = bR_{0,L,M,j+1} + LR_{0,L-1,M,j+1}$   
 $R_{N+1,L,M,j} = aR_{N,L,M,j+1} + NR_{N-1,L,M,j+1}$ 

This scheme is implemented in OEPDev.

#### 15.4.6 Function Documentation

15.4.6.1 double oepdev::d\_N\_n1\_n2 ( int N, int n1, int n2, double PA, double PB, double aP)

Compute McMurchie-Davidson-Hermite (MDH) coefficient for binomial expansion.

#### **Parameters**

N	- increment in the summation of MDH series
n1	- angular momentum of first function
n2	- angular momentum of second function
PA	- cartesian component of P-A distance
PB	- cartesian component of P-B distance
aP	- free parameter of MDH expansion

#### Returns

the McMurchie-Davidson-Hermite coefficient

15.4.6.2 void oepdev::make\_mdh\_D1\_coeff ( int n1, double aPd, double \* buffer )

Compute the McMurchie-Davidson-Hermite coefficients for monomial expansion.

#### **Parameters**

n1	- angular momentum of first function
aPd	- parameter equal to 0.500/Pa where Pa is exponent
buffer	- the McMurchie-Davidson-Hermite 3-dimensional array (raveled to vector):
	<ul> <li>axis 0: dimension 3 (x, y or z Cartesian component)</li> <li>axis 1: dimension n1+1 (0 to n1)</li> <li>axis 2: dimension n1+1 (0 to n1)</li> </ul>

#### See Also

### D1\_INDEX

15.4.6.3 void oepdev::make\_mdh\_D2\_coeff ( int n1, int n2, double aPd, double \* PA, double \* PB, double \* buffer )

Compute the McMurchie-Davidson-Hermite coefficients for binomial expansion.

#### **Parameters**

n1	- angular momentum of first function
n2	- angular momentum of second function
aPd	- parameter equal to 0.500/Pa where Pa is exponent
PA	- cartesian components of P-A distance
PB	- cartesian components of P-B distance
buffer	- the McMurchie-Davidson-Hermite 4-dimensional array (raveled to vector):
	<ul> <li>axis 0: dimension 3 (x, y or z Cartesian component)</li> <li>axis 1: dimension n1+1 (0 to n1)</li> <li>axis 2: dimension n2+1 (0 to n2)</li> </ul>
	axis 3: dimension n1+n2+1 (0 to n1+n2)

#### See Also

D2\_INDEX

15.4.6.4 void oepdev::make\_mdh\_D2\_coeff\_explicit\_recursion ( int n1, int n2, double aP, double \* PA, double \* PB, double \* buffer )

Compute the McMurchie-Davidson-Hermite coefficients for binomial expansion by explicit recursion. This function makes the same changes to buffers as oepdev::make\_mdh\_D2\_coeff, but implements it through explicit recursion by calls to oepdev::d\_N\_n1\_n2. Therefore, it is slightly slower. Here for debugging purposes.

#### **Parameters**

n1	- angular momentum of first function
n2	- angular momentum of second function
aPd	- parameter equal to 0.500/Pa where Pa is exponent
PA	- cartesian components of P-A distance
PB	- cartesian components of P-B distance
buffer	- the McMurchie-Davidson-Hermite 4-dimensional array (raveled to vector):
	axis 0: dimension 3 (x, y or z Cartesian component)
	axis 1: dimension n1+1 (0 to n1)
	axis 2: dimension n2+1 (0 to n2)
	• axis 3: dimension n1+n2+1 (0 to n1+n2)

#### See Also

D2\_INDEX

15.4.6.5 void oepdev::make\_mdh\_D3\_coeff ( int *n1*, int *n2*, int *n3*, double *aPd*, double \* *PA*, double \* *PB*, double \* *PC*, double \* *buffer* )

Compute the McMurchie-Davidson-Hermite coefficients for trinomial expansion.

#### **Parameters**

n1	- angular momentum of first function
n2	- angular momentum of second function
n3	- angular momentum of third function
aPd	- parameter equal to 0.500/Pa where Pa is exponent
PA	- cartesian components of P-A distance
PB	- cartesian components of P-B distance
PC	- cartesian components of P-C distance
buffer	- the McMurchie-Davidson-Hermite 5-dimensional array (raveled to vector):
	axis 0: dimension 3 (x, y or z Cartesian component)
	axis 1: dimension n1+1 (0 to n1)
	axis 2: dimension n2+1 (0 to n2)
	axis 3: dimension n3+1 (0 to n3)
	• axis 4: dimension n1+n2+n3+1 (0 to n1+n2+n3)

#### See Also

D3\_INDEX

15.4.6.6 void oepdev::make\_mdh\_R\_coeff ( int N, int L, int M, double a, double a, double b, double c, double \* F, double \* buffer )

Compute the McMurchie-Davidson R coefficients.

#### **Parameters**

N	- increment in the summation of MDH series along x direction
L	- increment in the summation of MDH series along <i>y</i> direction
М	- increment in the summation of MDH series along z direction
alpha	- alpha parameter of R coefficient
а	- x component of PQ vector of R coefficient
b	- y component of PQ vector of R coefficient
С	- z component of PQ vector of R coefficient
F	- array of Boys function values for given alpha and PQ
buffer	- the McMurchie-Davidson 4-dimensional array (raveled to vector):
	• axis 0: dimension N+1
	axis 1: dimension L+1
	axis 2: dimension M+1
	axis 3: dimension N+L+M+1 (j-th element)

### 15.5 The Integral Helper Library

You will find here various iterators to go through shells while computing ERI, or iterators over ERI itself.

#### Classes

· class oepdev::ShellCombinationsIterator

Iterator for Shell Combinations. Abstract Base.

· class oepdev::AOIntegralsIterator

Iterator for AO Integrals. Abstract Base.

class oepdev::AllAOShellCombinationsIterator\_4

Loop over all possible ERI shells in a shell quartet.

class oepdev::AllAOShellCombinationsIterator\_2

Loop over all possible ERI shells in a shell doublet.

· class oepdev::AllAOIntegralsIterator\_4

Loop over all possible ERI within a particular shell quartet.

• class oepdev::AllAOIntegralsIterator\_2

Loop over all possible ERI within a particular shell doublet.

#### **Typedefs**

- using oepdev::SharedShellsIterator = std::shared\_ptr< ShellCombinationsIterator >
   Iterator over shells as shared pointer.
- using oepdev::SharedAOIntsIterator = std::shared\_ptr< AOIntegralsIterator >
   Iterator over AO integrals as shared pointer.

### 15.5.1 Detailed Description

You will find here various iterators to go through shells while computing ERI, or iterators over ERI itself.

### 15.6 The Three-Dimensional Scalar Fields Library

Handles all sorts of scalar distributions in 3D Euclidean space, such as potentials defined at particular collection of points. In this Module, you will also find handling both random and ordered points collections in a form of a G09 cube, as well as handling G09 Cube files.

#### Classes

· class oepdev::Points3DIterator

Iterator over a collection of points in 3D space. Abstract base.

class oepdev::CubePoints3DIterator

Iterator over a collection of points in 3D space. g09 Cube-like order.

· class oepdev::RandomPoints3DIterator

Iterator over a collection of points in 3D space. Random collection.

· class oepdev::PointsCollection3D

Collection of points in 3D space. Abstract base.

class oepdev::RandomPointsCollection3D

Collection of random points in 3D space.

· class oepdev::CubePointsCollection3D

G09 cube-like ordered collection of points in 3D space.

• class oepdev::ScalarField3D

Scalar field in 3D space. Abstract base.

class oepdev::ElectrostaticPotential3D

Electrostatic potential of a molecule.

class oepdev::OEPotential3D< T >

Class template for OEP scalar fields.

#### **Functions**

oepdev::OEPotential3D
 T >::OEPotential3D (const int &np, const double &padding, std::shared\_ptr< T > oep, const std::string &oepType)

Construct random spherical collection of scalar field of type T.

oepdev::OEPotential3D< T >::OEPotential3D (const int &nx, const int &ny, const int &nz, const double &px, const double &pz, std::shared\_ptr< T > oep, const std::string &oepType, psi::Options &options)

Construct ordered 3D collection of scalar field of type T.

virtual oepdev::OEPotential3D
 T >::~OEPotential3D ()

Destructor.

virtual void oepdev::OEPotential3D< T >::print () const

Print information of the object to Psi4 output.

virtual double oepdev::OEPotential3D< T >::compute\_xyz (const double &x, const double &y, const double &z)

Compute a value of scalar field at point (x, y, z)

#### 15.6.1 Detailed Description

Handles all sorts of scalar distributions in 3D Euclidean space, such as potentials defined at particular collection of points. In this Module, you will also find handling both random and ordered points collections in a form of a G09 cube, as well as handling G09 Cube files.

#### 15.6.2 Function Documentation

15.6.2.1 template < class T > oepdev::OEPotential3D< T >::OEPotential3D ( const int & np, const double & padding, std::shared\_ptr< T > oep, const std::string & oepType )

Construct random spherical collection of scalar field of type T.

The points are drawn according to uniform distrinution in 3D space.

#### **Parameters**

np	- number of points to draw
padding	- spherical padding distance (au)
оер	- OEP object of type T
оерТуре	- type of OEP

15.6.2.2 template < class T > oepdev::OEPotential3D < T >::OEPotential3D ( const int & nx, const int & ny, const int & ny, const int & nz, const double & px, const double & px, std::shared\_ptr < T > oep, const std::string & oepType, psi::Options & options )

Construct ordered 3D collection of scalar field of type T.

The points are generated according to Gaussian cube file format.

#### **Parameters**

nx	- number of points along x direction
ny	- number of points along y direction
nz	- number of points along z direction
px	- padding distance along x direction
ру	- padding distance along y direction
pz	- padding distance along z direction
оер	- OEP object of type T
оерТуре	- type of OEP
options	- Psi4 options object

## 15.7 The Multipole Fitting Library

Implements methods to fit the generalized multipole moments of a generalized density distribution based on the input generalized potential scalar field. Among others, you will find here the electrostatic potential (ESP) fitting method.

#### Classes

· class oepdev::ESPSolver

Charges from Electrostatic Potential (ESP). A solver-type class.

### **Typedefs**

using oepdev::SharedScalarField3D = std::shared\_ptr< ScalarField3D >

#### 15.7.1 Detailed Description

Implements methods to fit the generalized multipole moments of a generalized density distribution based on the input generalized potential scalar field. Among others, you will find here the electrostatic potential (ESP) fitting method.

# 15.8 The Density Functional Theory Library

Implements the OEPDev ab initio DFT methods.

Implements the OEPDev ab initio DFT methods.

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#### 15.9 The OEPDev Utilities

Contains utility functions such as printing OEPDev preambule to the output file, class for wavefunction union etc.

#### Classes

· class oepdev::CPHF

CPHF solver class.

· class oepdev::DIISManager

DIIS manager.

· struct oepdev::PerturbCharges

Structure to hold perturbing charges.

· class oepdev::RHFPerturbed

RHF theory under electrostatic perturbation.

struct oepdev::ABCD

Simple structure to hold the Fourier series expansion coefficients.

struct oepdev::Fourier9

Simple structure to hold the Fourier series expansion coefficients for N=4.

class oepdev::UnitaryOptimizer

Find the optimim unitary matrix of quadratic matrix equation.

class oepdev::UnitaryOptimizer\_4\_2

Find the optimim unitary matrix for quartic-quadratic matrix equation with trace.

class oepdev::WavefunctionUnion

Union of two Wavefunction objects.

#### **Macros**

• #define OEPDEV\_USE\_PSI4\_DIIS\_MANAGER 0

Use DIIS from Psi4 (1) or OEPDev (0)?

• #define OEPDEV\_MAX\_AM 8

L\_max.

• #define OEPDEV\_N\_MAX\_AM 17

2L\_max+1

• #define OEPDEV\_CRIT\_ERI 1e-9

ERI criterion for E12, E34, E123 and lambda\*EXY coefficients.

• #define OEPDEV SIZE BUFFER R 250563

Size of R buffer (OEPDEV\_N\_MAX\_AM\*OEPDEV\_N\_MAX\_AM\*OEPDEV\_N\_MAX\_AM\*3)

#define OEPDEV\_SIZE\_BUFFER\_D2 3264

 $\textit{Size of D2 buffer } (3*(OEPDEV\_MAX\_AM+1)*(OEPDEV\_MAX\_AM+1)*OEPDEV\_N\_MAX\_AM) \\$ 

#### **Functions**

void oepdev::preambule (void)

Print preambule for module OEPDEV.

• template<typename... Args>

std::string oepdev::string\_sprintf (const char \*format, Args...args)

Format string output. Example: std::string text = oepdev::string\_sprinff("Test %3d, %13.5f", 5, -10.5425);.

• std::shared\_ptr< SuperFunctional > oepdev::create\_superfunctional (std::string name, Options & options)

Set up DFT functional.

std::shared\_ptr< Molecule > oepdev::extract\_monomer (std::shared\_ptr< const Molecule > molecule\_dimer, int id)

Extract molecule from dimer.

std::shared\_ptr< Wavefunction > oepdev::solve\_scf (std::shared\_ptr< Molecule > molecule, std::shared\_ptr< BasisSet > primary, std::shared\_ptr< SuperFunctional > functional, Options &options, std::shared\_ptr< PSIO > psio)

Solve RHF-SCF equations for a given molecule in a given basis set.

double oepdev::average\_moment (std::shared\_ptr< psi::Vector > moment)

Compute the scalar magnitude of multipole moment.

#### 15.9.1 Detailed Description

Contains utility functions such as printing OEPDev preambule to the output file, class for wavefunction union etc.

#### 15.9.2 Function Documentation

15.9.2.1 double oepdev::average\_moment ( std::shared\_ptr< psi::Vector > moment )

Compute the scalar magnitude of multipole moment.

#### **Parameters**

moment	- multipole moment vector with unique matrix elements. Now supported only for dipole and	1
	quadrupole.	

#### Returns

- the average multipole moment value.

The magnitudes of multipole moments are defined here as follows:

· The dipole moment magnitude is just a norm

$$|\mu| \equiv \sqrt{\mu_x^2 + \mu_y^2 + \mu_z^2}$$

· The quadrupole moment magnitude refers to the traceless moment in Buckingham convention

$$|\Theta| \equiv \sqrt{\Theta_{zz}^2 + \frac{1}{3} \left(\Theta_{xx} - \Theta_{yy}\right)^2 + \frac{4}{3} \left(\Theta_{xy}^2 + \Theta_{xz}^2 + \Theta_{yz}^2\right)}$$

In the above equation, the quadrupole moment elements refer to its traceless form.

15.9.2.2 std::shared\_ptr< SuperFunctional > oepdev::create\_superfunctional ( std::string name, Options & options )

Set up DFT functional.

Now it accepts only pure HF functional.

#### Parameters

name	name of the functional ("HF" is now only available)
options	psi::Options object

#### Returns

psi::SharedSuperFunctional object with functional.

#### **Examples:**

example scf perturb.cc.

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15.9.2.3 std::shared\_ptr< Molecule > oepdev::extract\_monomer ( std::shared\_ptr< const Molecule > molecule\_dimer, int id )

Extract molecule from dimer.

#### **Parameters**

molecule_dimer	psi::SharedMolecule object with dimer
id	index of a molecule (starts from 1)

#### Returns

psi::SharedMolecule object with indicated monomer

15.9.2.4 std::shared\_ptr< Wavefunction > oepdev::solve\_scf ( std::shared\_ptr< Molecule > molecule, std::shared\_ptr< BasisSet > primary, std::shared\_ptr< SuperFunctional > functional, Options & options, std::shared\_ptr< PSIO > psio )

Solve RHF-SCF equations for a given molecule in a given basis set.

#### **Parameters**

molecule	psi::SharedMolecule object with molecule
primary	shared primary basis set
functional	DFT functional
options	psi::Options object
psio	psi::PSIO object

#### Returns

psi::SharedWavefunction SCF wavefunction of the molecule

## 15.10 The OEPDev Testing Platform Library

Testing platform at C++ level of code. You should add more tests here when developing new functionalities, theories or models.

#### Classes

• class oepdev::test::Test

Manages test routines.

### 15.10.1 Detailed Description

Testing platform at C++ level of code. You should add more tests here when developing new functionalities, theories or models.

# **Chapter 16**

# **Namespace Documentation**

## 16.1 oepdev Namespace Reference

OEPDev module namespace.

#### Classes

· class ESPSolver

Charges from Electrostatic Potential (ESP). A solver-type class.

· class Points3DIterator

Iterator over a collection of points in 3D space. Abstract base.

class CubePoints3DIterator

Iterator over a collection of points in 3D space. g09 Cube-like order.

• class RandomPoints3DIterator

Iterator over a collection of points in 3D space. Random collection.

class PointsCollection3D

Collection of points in 3D space. Abstract base.

class RandomPointsCollection3D

Collection of random points in 3D space.

class CubePointsCollection3D

G09 cube-like ordered collection of points in 3D space.

class ScalarField3D

Scalar field in 3D space. Abstract base.

· class ElectrostaticPotential3D

Electrostatic potential of a molecule.

class OEPotential3D

Class template for OEP scalar fields.

· class GenEffPar

Generalized Effective Fragment Parameters. Container Class.

· class GenEffFrag

Generalized Effective Fragment. Container Class.

class GenEffParFactory

Generalized Effective Fragment Factory. Abstract Base.

class PolarGEFactory

Polarization GEFP Factory. Abstract Base.

· class AbInitioPolarGEFactory

Polarization GEFP Factory from First Principles. Hartree-Fock Approximation.

· class FFAbInitioPolarGEFactory

Polarization GEFP Factory from First Principles: Finite-Difference Model. Arbitrary level of theory.

class GeneralizedPolarGEFactory

Polarization GEFP Factory with Least-Squares Parameterization.

class UniformEFieldPolarGEFactory

Polarization GEFP Factory with Least-Squares Parameterization.

· class NonUniformEFieldPolarGEFactory

Polarization GEFP Factory with Least-Squares Parameterization.

class LinearUniformEFieldPolarGEFactory

Polarization GEFP Factory with Least-Squares Parameterization.

class QuadraticUniformEFieldPolarGEFactory

Polarization GEFP Factory with Least-Squares Parameterization.

class LinearNonUniformEFieldPolarGEFactory

Polarization GEFP Factory with Least-Squares Parameterization.

class QuadraticNonUniformEFieldPolarGEFactory

Polarization GEFP Factory with Least-Squares Parameterization.

class LinearGradientNonUniformEFieldPolarGEFactory

Polarization GEFP Factory with Least-Squares Parameterization.

· class QuadraticGradientNonUniformEFieldPolarGEFactory

Polarization GEFP Factory with Least-Squares Parameterization.

class UnitaryTransformedMOPolarGEFactory

Polarization GEFP Factory with Least-Squares Scaling of MO Space.

class TwoElectronInt

General Two Electron Integral.

• class ERI\_1\_1

2-centre ERI of the form (a|O(2)|b) where O(2) = 1/r12.

class ERI\_2\_2

4-centre ERI of the form (ab|O(2)|cd) where O(2) = 1/r12.

• class ERI\_3\_1

4-centre ERI of the form (abc|O(2)|d) where O(2) = 1/r12.

struct OEPType

Container to handle the type of One-Electron Potentials.

· class OEPotential

Generalized One-Electron Potential: Abstract base.

class ElectrostaticEnergyOEPotential

Generalized One-Electron Potential for Electrostatic Energy.

class RepulsionEnergyOEPotential

Generalized One-Electron Potential for Pauli Repulsion Energy.

class ChargeTransferEnergyOEPotential

Generalized One-Electron Potential for Charge-Transfer Interaction Energy.

class EETCouplingOEPotential

Generalized One-Electron Potential for EET coupling calculations.

· class GeneralizedDensityFit

Generalized Density Fitting Scheme. Abstract Base.

class SingleGeneralizedDensityFit

Generalized Density Fitting Scheme - Single Fit.

· class DoubleGeneralizedDensityFit

Generalized Density Fitting Scheme - Double Fit.

- class TwoBodyAOInt
- class IntegralFactory

Extended IntegralFactory for computing integrals.

class PotentialInt

Computes potential integrals.

class CPHF

CPHF solver class.

· class DIISManager

DIIS manager.

· class ShellCombinationsIterator

Iterator for Shell Combinations. Abstract Base.

· class AOIntegralsIterator

Iterator for AO Integrals. Abstract Base.

· class AllAOShellCombinationsIterator 4

Loop over all possible ERI shells in a shell quartet.

class AllAOShellCombinationsIterator\_2

Loop over all possible ERI shells in a shell doublet.

class AllAOIntegralsIterator\_4

Loop over all possible ERI within a particular shell quartet.

class AllAOIntegralsIterator\_2

Loop over all possible ERI within a particular shell doublet.

struct PerturbCharges

Structure to hold perturbing charges.

· class RHFPerturbed

RHF theory under electrostatic perturbation.

class OEPDevSolver

Solver of properties of molecular aggregates. Abstract base.

· class ElectrostaticEnergySolver

Compute the Coulombic interaction energy between unperturbed wavefunctions.

class RepulsionEnergySolver

Compute the Pauli-Repulsion interaction energy between unperturbed wavefunctions.

class ChargeTransferEnergySolver

Compute the Charge-Transfer interaction energy between unperturbed wavefunctions.

struct ABCD

Simple structure to hold the Fourier series expansion coefficients.

struct Fourier9

Simple structure to hold the Fourier series expansion coefficients for N=4.

· class UnitaryOptimizer

Find the optimim unitary matrix of quadratic matrix equation.

class UnitaryOptimizer\_4\_2

Find the optimim unitary matrix for quartic-quadratic matrix equation with trace.

class WavefunctionUnion

Union of two Wavefunction objects.

#### **Typedefs**

- using SharedScalarField3D = std::shared\_ptr< ScalarField3D >
- using SharedWavefunction = std::shared ptr< Wavefunction >
- using SharedBasisSet = std::shared\_ptr< BasisSet >
- using SharedTensor = std::shared\_ptr< Tensor >
- using SharedMatrix = std::shared\_ptr< Matrix >
- using SharedVector = std::shared\_ptr< Vector >
- using SharedIntegralFactory = std::shared\_ptr< IntegralFactory >
- using SharedTwoBodyAOInt = std::shared\_ptr< TwoBodyAOInt >

- using SharedShellsIterator = std::shared\_ptr< ShellCombinationsIterator >
   Iterator over shells as shared pointer.
- using SharedAOIntsIterator = std::shared\_ptr< AOIntegralsIterator >

Iterator over AO integrals as shared pointer.

- using SharedWavefunctionUnion = std::shared\_ptr< WavefunctionUnion >
- using SharedOEPotential = std::shared ptr< OEPotential >
- using SharedMolecule = std::shared ptr< Molecule >
- using SharedSuperFunctional = std::shared\_ptr< SuperFunctional >
- using SharedMOSpace = std::shared\_ptr< MOSpace >
- using **SharedMOSpaceVector** = std::vector< std::shared ptr< MOSpace >>
- using SharedIntegralTransform = std::shared ptr< IntegralTransform >
- using SharedLocalizer = std::shared\_ptr< Localizer >

#### **Functions**

- n\_max\_am\_ (2 \*max\_am\_+1)
- double d\_N\_n1\_n2 (int N, int n1, int n2, double PA, double PB, double aP)

Compute McMurchie-Davidson-Hermite (MDH) coefficient for binomial expansion.

void make\_mdh\_D2\_coeff\_explicit\_recursion (int n1, int n2, double aP, double \*PA, double \*PB, double \*buffer)

Compute the McMurchie-Davidson-Hermite coefficients for binomial expansion by explicit recursion. This function makes the same changes to buffers as oepdev::make\_mdh\_D2\_coeff, but implements it through explicit recursion by calls to oepdev::d\_N\_n1\_n2. Therefore, it is slightly slower. Here for debugging purposes.

• void make\_mdh\_D1\_coeff (int n1, double aPd, double \*buffer)

Compute the McMurchie-Davidson-Hermite coefficients for monomial expansion.

• void make\_mdh\_D2\_coeff (int n1, int n2, double aPd, double \*PA, double \*PB, double \*buffer)

Compute the McMurchie-Davidson-Hermite coefficients for binomial expansion.

 void make\_mdh\_D3\_coeff (int n1, int n2, int n3, double aPd, double \*PA, double \*PB, double \*PC, double \*buffer)

Compute the McMurchie-Davidson-Hermite coefficients for trinomial expansion.

• void make\_mdh\_R\_coeff (int N, int L, int M, double alpha, double a, double b, double c, double \*F, double \*buffer)

Compute the McMurchie-Davidson R coefficients.

- constexpr std::complex< double > operator""\_i (unsigned long long d)
- constexpr std::complex< double > operator'''\_i (long double d)
- void preambule (void)

Print preambule for module OEPDEV.

• std::shared ptr< SuperFunctional > create superfunctional (std::string name, Options & options)

Set up DFT functional.

- std::shared\_ptr< Molecule > extract\_monomer (std::shared\_ptr< const Molecule > molecule\_dimer, int id)
   Extract molecule from dimer.
- std::shared\_ptr< Wavefunction > solve\_scf (std::shared\_ptr< Molecule > molecule, std::shared\_ptr< Basis-Set > primary, std::shared\_ptr< SuperFunctional > functional, Options &options, std::shared\_ptr< PSIO > psio)

Solve RHF-SCF equations for a given molecule in a given basis set.

double average\_moment (std::shared\_ptr< psi::Vector > moment)

Compute the scalar magnitude of multipole moment.

template<typename... Args>

std::string string\_sprintf (const char \*format, Args...args)

Format string output. Example: std::string text = oepdev::string\_sprinff("Test %3d, %13.5f", 5, -10.5425);.

# 16.1.1 Detailed Description

OEPDev module namespace. Contains all the functionalities for the development of the Generalized One-Electroc Potentials (OEP's).

# 16.2 psi Namespace Reference

Psi4 package namespace.

# **Typedefs**

- using SharedVetor = std::shared\_ptr< Vector >
- using SharedBasisSet = std::shared\_ptr< BasisSet >
- using SharedMolecule = std::shared\_ptr< Molecule >
- using SharedMatrix = std::shared\_ptr< Matrix >
- using SharedWavefunction = std::shared\_ptr< Wavefunction >

# **Functions**

- int read\_options (std::string name, Options &options)
  - Options for the OEPDev plugin.
- SharedWavefunction oepdev (SharedWavefunction ref\_wfn, Options & options)

Main routine of the OEPDev plugin.

# 16.2.1 Detailed Description

Psi4 package namespace. Contains all Psi4 functionalities.

# 16.2.2 Function Documentation

16.2.2.1 SharedWavefunction psi::oepdev ( SharedWavefunction ref\_wfn, Options & options )

Main routine of the OEPDev plugin.

Created with intention to test various models of the interaction energy between two molecules, described by the Hartree-Fock-Roothaan-Hall theory or the configuration interaction with singles theory.

In particular, the plugin tests the models of:

- 1. the Pauli repulsion and CT interaction energy (Project II)
- 2. the Induction interaction energy (Project III)
- 3. the excitation energy transfer couplings (Project I)

against benchmarks (exact or reference solutions). The list of implemented models can be found in Implemented Models .

**Parameters** 

ref_wfn	wfn shared wavefunction of a dimer	
options psi::Options object		

# Returns

psi::SharedWavefunction (either ref\_wfn or wavefunction union)

16.2.2.2 int psi::read\_options ( std::string name, Options & options )

Options for the OEPDev plugin.

# **Parameters**

name	name of driver function
options psi::Options object	

# Returns

true

# **Chapter 17**

# **Class Documentation**

# 17.1 oepdev::ABCD Struct Reference

Simple structure to hold the Fourier series expansion coefficients.

#include <unitary\_optimizer.h>

# **Public Attributes**

- · double A
- double B
- double C
- double **D**

# 17.1.1 Detailed Description

Simple structure to hold the Fourier series expansion coefficients.

The documentation for this struct was generated from the following file:

• oepdev/libutil/unitary\_optimizer.h

# 17.2 oepdev::AblnitioPolarGEFactory Class Reference

Polarization GEFP Factory from First Principles. Hartree-Fock Approximation.

```
#include <gefp.h>
```

Inheritance diagram for oepdev::AbInitioPolarGEFactory:



# **Public Member Functions**

- AbInitioPolarGEFactory (std::shared ptr< psi::Wavefunction > wfn, psi::Options &opt)
- · virtual std::shared\_ptr

< GenEffPar > compute (void)

Compute the density matrix susceptibility tensors.

# **Additional Inherited Members**

# 17.2.1 Detailed Description

Polarization GEFP Factory from First Principles. Hartree-Fock Approximation.

Implements creation of the density matrix susceptibility tensors for which X=1. Guarantees the idempotency of the density matrix up to first-order in LCAO-MO variation. The density matrix susceptibility tensor is represented by:

$$\delta D_{\alpha\beta} = \sum_{i} \mathbf{B}_{\alpha\beta}^{(i;1)} \cdot \mathbf{F}(\mathbf{r}_i)$$

where  $\mathbf{B}_{\alpha\beta}^{(i;1)}$  is the density matrix dipole polarizability defined for the distributed LMO site at  $\mathbf{r}_i$ . Its explicit form is given by

$$\mathbf{B}_{\alpha\beta}^{(i;1)} = C_{\alpha i}^{(0)} \mathbf{b}_{\beta}^{(i;1)} C_{\beta i}^{(0)} \mathbf{b}_{\alpha}^{(i;1)} - \sum_{\gamma} \left( D_{\alpha \gamma}^{(0)} C_{\beta i}^{(0)} + D_{\beta \gamma}^{(0)} C_{\alpha i}^{(0)} \right) \mathbf{b}_{\gamma}^{(i;1)}$$

where the susceptibility of the LCAO-MO coefficient is given by

$$b_{\alpha;w}^{(i;1)} = \frac{1}{4} \sum_{u}^{x,y,z} [\alpha_i]_{uw} \left[ [\mathbf{L}_i]_{\text{Left}}^{-1} \right]_{u;\alpha}$$

for w = x, y, z. The auxiliary tensor  $\mathbb{L}$  is defined as

$$\mathbb{L} = \mathbf{C}^{(0)\mathrm{T}} \cdot \mathbb{M} \cdot \left( \mathbf{1} - \mathbf{D}^{(0)} \right)$$

where  $\mathbb{M}$  is the dipole integral vector of matrices in AO representation. The left inverse of the i-th element is defined as

$$[\mathbf{L}_i]_{\text{Left}}^{-1} \equiv \left[\mathbf{L}_i^{\text{T}} \cdot \mathbf{L}_i\right]^{-1} \cdot \mathbf{L}_i^{\text{T}}$$

Note that  $L_i \equiv [\mathbb{L}]_i$  is a  $n \times 3$  matrix, whereas its left inverse is a  $3 \times n$  matrix with n being the size of the AO basis set.

The documentation for this class was generated from the following files:

- · oepdev/libgefp/gefp.h
- · oepdev/libgefp/gefp\_polar\_abinitio.cc

# 17.3 oepdev::AllAOIntegralsIterator\_2 Class Reference

Loop over all possible ERI within a particular shell doublet.

#include <integrals\_iter.h>

Inheritance diagram for oepdev::AllAOIntegralsIterator 2:

oepdev::AOIntegralsIterator
oepdev::AllAOIntegralsIterator\_2

# **Public Member Functions**

AllAOIntegralsIterator\_2 (const ShellCombinationsIterator \*shellIter)

Construct by shell iterator (const object)

AllAOIntegralsIterator\_2 (std::shared\_ptr< ShellCombinationsIterator > shellIter)

Construct by shell iterator (pointed by shared pointer)

• void first ()

First iteration.

• void next ()

Next iteration.

· int i () const

Grab the current integral i index.

int j () const

Grab the current integral j index.

• int index () const

#### **Additional Inherited Members**

# 17.3.1 Detailed Description

Loop over all possible ERI within a particular shell doublet.

Constructed by providing a const reference or shared pointer to an AllAOShellCombinationsIterator object.

See Also

AllAOShellCombinationsIterator\_2

# 17.3.2 Constructor & Destructor Documentation

17.3.2.1 AllAOIntegralsIterator\_2::AllAOIntegralsIterator\_2 ( const ShellCombinationsIterator \* shellIter )

Construct by shell iterator (const object)

**Parameters** 

shellIter - shell iterator object

 $17.3.2.2 \quad All AO Integrals Iterator\_2 :: All AO Integrals Iterator\_2 \ ( \ std:: shared\_ptr < Shell Combinations Iterator > shell Iterator\_2 \ ( \ std:: shared\_ptr < Shell Combinations Iterator\_2 \ ( \ std:: shared\_ptr < Shell Combinations Iterator\_2 \ ( \ std:: shared\_ptr < Shell Combinations Iterator\_2 \ ( \ std:: shared\_ptr < Shell Combinations Iterator\_2 \ ( \ std:: shared\_ptr < Shell Combinations Iterator\_2 \ ( \ std:: shared\_ptr < Shell Combinations Iterator\_2 \ ( \ std:: shared\_ptr < Shell Combinations Iterator\_2 \ ( \ std:: shared\_ptr < Shell Combinations Iterator\_2 \ ( \ std:: shared\_ptr < Shell Combinations Iterator\_2 \ ( \ std:: shared\_ptr < Shell Combinations Iterator\_2 \ ( \ std:: shared\_ptr < Shell Combinations Iterator\_2 \ ( \ std:: shared\_ptr < Shell Combinations Iterator\_2 \ ( \ std:: shared\_ptr < Shell Combinations Iterator\_2 \ ( \ std:: shared\_ptr < Shell Combinations Iterator\_2 \ ( \ std:: shared\_ptr < Shell Combinations Iterator\_2 \ ( \ std:: shared\_ptr < Shell Combinations Iterator\_2 \ ( \ std:: shared\_ptr < Shell Combinations Iterator\_2 \ ( \ std:: shared\_ptr < Shell Combinations Iterator\_2 \ ( \ std:: shared\_ptr < Shell Combinations Iterator\_2 \ ( \ std:: shared\_ptr < Shell Combinations Iterator\_2 \ ( \ std:: shared\_ptr < Shell Combinations Iterator\_2 \ ( \ std:: shared\_ptr < Shell Combinations Iterator\_2 \ ( \ std:: shared\_ptr < Shell Combinations Iterator\_2 \ ( \ std:: shared\_ptr < Shell Combinations Iterator\_2 \ ( \ std:: shared\_ptr < Shell Combinations Iterator\_2 \ ( \ std:: shared\_ptr < Shell Combinations Iterator\_2 \ ( \ std:: shared\_ptr < Shell Combinations Iterator\_2 \ ( \ std:: shared\_ptr < Shell Combinations Iterator\_2 \ ( \ std:: shared\_ptr < Shell Combinations Iterator\_2 \ ( \ std:: shared\_ptr < Shell Combinations Iterator\_2 \ ( \ std:: shared\_ptr < Shell Combinations Iterator\_2 \ ( \ std:: shared\_ptr < Shell Combinations Iterator\_2 \ ( \ std:: shared\_ptr < Shell Combinations Iterator\_2 \ ( \ std:: shared\_ptr < Shell Combinations Iterator\_2 \ ( \ std:: shared\_ptr < Shell C$ 

Construct by shell iterator (pointed by shared pointer)

**Parameters** 

shellIter - shell iterator object

# 17.3.3 Member Function Documentation

17.3.3.1 int oepdev::AllAOIntegralsIterator\_2::index(void) const [inline], [virtual]

Grab the current index of integral value stored in the buffer

Implements oepdev::AOIntegralsIterator.

The documentation for this class was generated from the following files:

- · oepdev/libutil/integrals\_iter.h
- · oepdev/libutil/integrals\_iter.cc

# 17.4 oepdev::AllAOIntegralsIterator\_4 Class Reference

Loop over all possible ERI within a particular shell quartet.

```
#include <integrals_iter.h>
```

Inheritance diagram for oepdev::AllAOIntegralsIterator 4:



#### **Public Member Functions**

AllAOIntegralsIterator\_4 (const ShellCombinationsIterator \*shellIter)

Construct by shell iterator (const object)

AllAOIntegralsIterator\_4 (std::shared\_ptr< ShellCombinationsIterator > shellIter)

Construct by shell iterator (pointed by shared pointer)

void first ()

First iteration.

· void next ()

Next iteration.

· int i () const

Grab the current integral i index.

• int j () const

Grab the current integral j index.

· int k () const

Grab the current integral k index.

• int I () const

Grab the current integral I index.

• int index () const

# **Additional Inherited Members**

# 17.4.1 Detailed Description

Loop over all possible ERI within a particular shell quartet.

Constructed by providing a const reference or shared pointer to an AllAOShellCombinationsIterator object.

See Also

AllAOShellCombinationsIterator\_4

# 17.4.2 Constructor & Destructor Documentation

17.4.2.1 AllAOIntegralsIterator 4::AllAOIntegralsIterator 4 ( const ShellCombinationsIterator \* shellIter )

Construct by shell iterator (const object)

#### **Parameters**

```
shellIter - shell iterator object
```

# 17.4.2.2 AllAOIntegralsIterator\_4::AllAOIntegralsIterator\_4( std::shared\_ptr< ShellCombinationsIterator > shellIter )

Construct by shell iterator (pointed by shared pointer)

**Parameters** 

```
shellIter - shell iterator object
```

# 17.4.3 Member Function Documentation

```
17.4.3.1 int oepdev::AllAOIntegralsIterator_4::index ( void ) const [inline], [virtual]
```

Grab the current index of integral value stored in the buffer

Implements oepdev::AOIntegralsIterator.

The documentation for this class was generated from the following files:

- · oepdev/libutil/integrals\_iter.h
- · oepdev/libutil/integrals\_iter.cc

# 17.5 oepdev::AllAOShellCombinationsIterator\_2 Class Reference

Loop over all possible ERI shells in a shell doublet.

```
#include <integrals_iter.h>
```

Inheritance diagram for oepdev::AllAOShellCombinationsIterator\_2:



# **Public Member Functions**

AllAOShellCombinationsIterator\_2 (SharedBasisSet bs\_1, SharedBasisSet bs\_2)

Iterate over shell doublets. Construct by providing basis sets for each axis. The basis sets must be defined for the same molecule.

AllAOShellCombinationsIterator 2 (std::shared ptr< IntegralFactory > integrals)

Construct by providing integral factory.

- AllAOShellCombinationsIterator\_2 (const IntegralFactory &integrals)
- AllAOShellCombinationsIterator\_2 (std::shared\_ptr< psi::IntegralFactory > integrals)

Construct by providing integral factory.

- AllAOShellCombinationsIterator\_2 (const psi::IntegralFactory &integrals)
- void first ()

First iteration.

• void next ()

Next iteration.

void compute\_shell (std::shared\_ptr< oepdev::TwoBodyAOInt > tei) const

Compute ERI's for the current shell. The eris are stored in the buffer of the argument object.

- void compute\_shell (std::shared\_ptr< psi::TwoBodyAOInt > tei) const
- int P () const

Grab the current shell P index.

• int Q () const

Grab the current shell Q index.

# **Additional Inherited Members**

# 17.5.1 Detailed Description

Loop over all possible ERI shells in a shell doublet.

Constructed by providing IntegralFactory object or shared pointers to two basis set spaces.

#### 17.5.2 Constructor & Destructor Documentation

17.5.2.1 AllAOShellCombinationsIterator\_2::AllAOShellCombinationsIterator\_2 ( SharedBasisSet bs\_1, SharedBasisSet bs\_2 )

Iterate over shell doublets. Construct by providing basis sets for each axis. The basis sets must be defined for the same molecule.

#### **Parameters**

bs_1	- basis set of axis 1
bs_2	- basis set of axis 2

17.5.2.2 oepdev::AllAOShellCombinationsIterator\_2::AllAOShellCombinationsIterator\_2 ( std::shared\_ptr< IntegralFactory > integrals )

Construct by providing integral factory.

# **Parameters**

integrals	- OepDev integral factory object

17.5.2.3 AllAOShellCombinationsIterator\_2::AllAOShellCombinationsIterator\_2 ( const IntegralFactory & integrals )

This is an overloaded member function, provided for convenience. It differs from the above function only in what argument(s) it accepts.

17.5.2.4 AllAOShellCombinationsIterator\_2::AllAOShellCombinationsIterator\_2 ( std::shared\_ptr< psi::IntegralFactory > integrals )

Construct by providing integral factory.

# **Parameters**

integrals	- Psi4 integral factory object

17.5.2.5 AllAOShellCombinationsIterator\_2::AllAOShellCombinationsIterator\_2 ( const psi::IntegralFactory & integrals )

This is an overloaded member function, provided for convenience. It differs from the above function only in what argument(s) it accepts.

# 17.5.3 Member Function Documentation

17.5.3.1 void AllAOShellCombinationsIterator\_2::compute\_shell ( std::shared\_ptr< oepdev::TwoBodyAOInt > tei ) const [virtual]

Compute ERI's for the current shell. The eris are stored in the buffer of the argument object.

#### **Parameters**

```
tei - two electron AO integral
```

Implements oepdev::ShellCombinationsIterator.

The documentation for this class was generated from the following files:

- · oepdev/libutil/integrals iter.h
- · oepdev/libutil/integrals iter.cc

# 17.6 oepdev::AllAOShellCombinationsIterator\_4 Class Reference

Loop over all possible ERI shells in a shell quartet.

```
#include <integrals_iter.h>
```

Inheritance diagram for oepdev::AllAOShellCombinationsIterator\_4:



# **Public Member Functions**

AllAOShellCombinationsIterator\_4 (SharedBasisSet bs\_1, SharedBasisSet bs\_2, SharedBasisSet bs\_3, SharedBasisSet bs\_4)

Iterate over shell quartets. Construct by providing basis sets for each axis. The basis sets must be defined for the same molecule.

- AllAOShellCombinationsIterator\_4 (std::shared\_ptr< IntegralFactory > integrals)
  - Construct by providing integral factory.
- AllAOShellCombinationsIterator\_4 (const IntegralFactory &integrals)
- AllAOShellCombinationsIterator\_4 (std::shared\_ptr< psi::IntegralFactory > integrals)

Construct by providing integral factory.

- AllAOShellCombinationsIterator\_4 (const psi::IntegralFactory &integrals)
- void first ()

Do the first iteration.

• void next ()

Do the next iteration.

- void compute shell (std::shared ptr< oepdev::TwoBodyAOInt > tei) const
- void compute\_shell (std::shared\_ptr< psi::TwoBodyAOInt > tei) const

• int P () const

Grab the current shell P index.

• int Q () const

Grab the current shell Q index.

• int R () const

Grab the current shell R index.

• int S () const

Grab the current shell S index.

#### **Additional Inherited Members**

# 17.6.1 Detailed Description

Loop over all possible ERI shells in a shell quartet.

Constructed by providing IntegralFactory object or shared pointers to four basis set spaces.

### 17.6.2 Constructor & Destructor Documentation

17.6.2.1 AllAOShellCombinationslterator\_4::AllAOShellCombinationslterator\_4 ( SharedBasisSet bs\_1, SharedBasisSet bs\_2, SharedBasisSet bs\_3, SharedBasisSet bs\_4 )

Iterate over shell quartets. Construct by providing basis sets for each axis. The basis sets must be defined for the same molecule.

# **Parameters**

bs_1	- basis set of axis 1
bs_2	- basis set of axis 2
bs_3	- basis set of axis 3
bs_4	- basis set of axis 4

17.6.2.2 oepdev::AllAOShellCombinationsIterator\_4::AllAOShellCombinationsIterator\_4 ( std::shared\_ptr< IntegralFactory > integrals )

Construct by providing integral factory.

# **Parameters**

integrals	- OepDev integral factory object

17.6.2.3 AllAOShellCombinationsIterator\_4::AllAOShellCombinationsIterator\_4 ( const IntegralFactory & integrals )

This is an overloaded member function, provided for convenience. It differs from the above function only in what argument(s) it accepts.

17.6.2.4 AllAOShellCombinationsIterator\_4::AllAOShellCombinationsIterator\_4 ( std::shared\_ptr< psi::IntegralFactory > integrals )

Construct by providing integral factory.

#### **Parameters**

integrals	- OepDev integral factory object

17.6.2.5 AllAOShellCombinationsIterator\_4::AllAOShellCombinationsIterator\_4 ( const psi::IntegralFactory & integrals )

This is an overloaded member function, provided for convenience. It differs from the above function only in what argument(s) it accepts.

# 17.6.3 Member Function Documentation

17.6.3.1 void AllAOShellCombinationsIterator\_4::compute\_shell ( std::shared\_ptr< oepdev::TwoBodyAOInt > tei ) const [virtual]

 $Compute\ integrals\ in\ a\ current\ shell.\ Works\ both\ for\ oepdev:: TwoBodyAOInt\ and\ psi:: TwoBodyAOInt\ and\ psi:$ 

#### **Parameters**

```
tei - two body integral object
```

Implements oepdev::ShellCombinationsIterator.

The documentation for this class was generated from the following files:

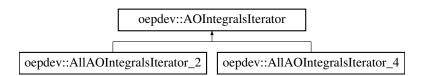
- · oepdev/libutil/integrals\_iter.h
- · oepdev/libutil/integrals\_iter.cc

# 17.7 oepdev::AOIntegralsIterator Class Reference

Iterator for AO Integrals. Abstract Base.

#include <integrals\_iter.h>

Inheritance diagram for oepdev::AOIntegralsIterator:



# **Public Member Functions**

· AOIntegralsIterator ()

Base Constructor.

virtual ∼AOIntegralsIterator ()

Base Destructor.

virtual void first (void)=0

Do the first iteration.

virtual void next (void)=0

Do the next iteration.

· virtual int i (void) const

Grab i-th index.

virtual int j (void) const

Grab j-th index.

virtual int k (void) const

Grab k-th index.

virtual int I (void) const

Grab I-th index.

• virtual int index (void) const =0

Grab index in the integral buffer.

virtual bool is\_done (void)

Returns the status of an iterator.

# **Static Public Member Functions**

```
    static std::shared_ptr
    AOIntegralsIterator > build (const ShellCombinationsIterator *shellIter, std::string mode="ALL")
```

static std::shared\_ptr
 AOIntegralsIterator > build (std::shared\_ptr< ShellCombinationsIterator > shellIter, std::string mode="A-LL")

# **Protected Attributes**

• bool done

The status of an iterator.

# 17.7.1 Detailed Description

Iterator for AO Integrals. Abstract Base.

# 17.7.2 Member Function Documentation

```
17.7.2.1 std::shared_ptr< AOIntegralsIterator > AOIntegralsIterator::build ( const ShellCombinationsIterator * shellIter, std::string mode = "ALL" ) [static]
```

Build AO integrals iterator from current state of iterator over shells

**Parameters** 

```
shellIter - iterator over shells - either "ALL" or "UNIQUE" (iterate over all or unique integrals)
```

# Returns

iterator over AO integrals

```
17.7.2.2 std::shared_ptr< AOIntegralsIterator > AOIntegralsIterator::build ( std::shared_ptr< ShellCombinationsIterator > shellIter, std::string mode = "ALL" ) [static]
```

This is an overloaded member function, provided for convenience. It differs from the above function only in what argument(s) it accepts.

The documentation for this class was generated from the following files:

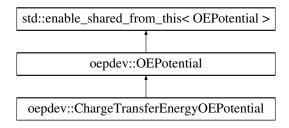
- · oepdev/libutil/integrals\_iter.h
- · oepdev/libutil/integrals\_iter.cc

# 17.8 oepdev::ChargeTransferEnergyOEPotential Class Reference

Generalized One-Electron Potential for Charge-Transfer Interaction Energy.

#include <oep.h>

Inheritance diagram for oepdev::ChargeTransferEnergyOEPotential:



# **Public Member Functions**

- ChargeTransferEnergyOEPotential (SharedWavefunction wfn, SharedBasisSet auxiliary, SharedBasisSet intermediate, Options & options)
- ChargeTransferEnergyOEPotential (SharedWavefunction wfn, Options & options)
- virtual void compute (const std::string &oepType) override

Compute matrix forms of all OEP's within a specified OEP type.

virtual void compute\_3D (const std::string &oepType, const double &x, const double &y, const double &z, double &v) override

Compute value of potential in point x, y, z and save at v.

• virtual void print header () const override

### **Additional Inherited Members**

# 17.8.1 Detailed Description

Generalized One-Electron Potential for Charge-Transfer Interaction Energy.

Contains the following OEP types:

- Otto-Ladik.V1 DF-based term
- Otto-Ladik. V2 ESP-based term
- Otto-Ladik.V3 ESP-based term

The documentation for this class was generated from the following files:

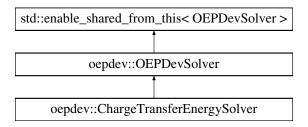
- · oepdev/liboep/oep.h
- oepdev/liboep/oep.cc

# 17.9 oepdev::ChargeTransferEnergySolver Class Reference

Compute the Charge-Transfer interaction energy between unperturbed wavefunctions.

#include <solver.h>

 $Inheritance\ diagram\ for\ oepdev:: Charge Transfer Energy Solver:$ 



# **Public Member Functions**

- ChargeTransferEnergySolver (SharedWavefunctionUnion wfn\_union)
- virtual double compute\_oep\_based (const std::string &method="DEFAULT")
   Compute property by using OEP's.
- virtual double compute\_benchmark (const std::string &method="DEFAULT")
   Compute property by using benchmark method.

# **Additional Inherited Members**

# 17.9.1 Detailed Description

Compute the Charge-Transfer interaction energy between unperturbed wavefunctions.

The implemented methods are shown below

Keyword	Method Description
	Benchmark Methods
OTTO_LADIK	*Default*. CT energy at HF level from Otto and Ladik (1975).
EFP2	CT energy at HF level from EFP2 model.
OEP-Based Methods	
OTTO_LADIK	*Default*. OEP-based Otto-Ladik expressions.

Table 17.1: Methods available in the Solver

In order to construct this solver, always use the <code>OEPDevSolver::build</code> static factory method.

Below the detailed description of the implemented equations is given for each of the above provided methods. In the formulae across, it is assumed that the orbitals are real. The Coulomb notation for electron repulsion integrals (ERI's) is adopted; i.e,

$$(ac|bd) = \iint d\mathbf{r}_1 d\mathbf{r}_2 \phi_a(\mathbf{r}_1) \phi_c(\mathbf{r}_1) \frac{1}{r_{12}} \phi_b(\mathbf{r}_2) \phi_d(\mathbf{r}_2)$$

Greek subscripts denote basis set orbitals whereas Italic subscripts denote the occupied molecular orbitals.

The CT energy between molecules A and B is given by

$$E^{\text{CT}} = E^{\text{A}^{+}\text{B}^{-}} + E^{\text{A}^{-}\text{B}^{+}}$$

# **Benchmark Methods**

CT energy at HF level by Otto and Ladik (1975).

For a closed-shell system, CT energy equation of Otto and Ladik becomes

$$E^{\mathrm{A^+B^-}} \approx 2 \sum_{i \in A}^{\mathrm{Occ_A}} \sum_{n \in B}^{\mathrm{Vir_B}} \frac{V_{in}^2}{\varepsilon_i - \varepsilon_n}$$

where

$$\begin{aligned} V_{in} &= V_{in}^{B} + 2\sum_{j \in B}^{\text{Occ}_{B}} (in|jj) - \sum_{k \in A}^{\text{Occ}_{A}} S_{kn} \left\{ V_{ik}^{B} + 2\sum_{j \in B}^{\text{Occ}_{B}} (ik|jj) \right\} \\ &- \sum_{j \in B}^{\text{Occ}_{B}} \left[ S_{ij} \left\{ V_{nj}^{A} + 2\sum_{k \in A}^{\text{Occ}_{A}} (1 - \delta_{ik})(nj|kk) \right\} - (nj|ij) \right] + \sum_{k \in A}^{\text{Occ}_{A}} \sum_{j \in B}^{\text{Occ}_{B}} S_{kj} (1 - \delta_{ik})(ik|nj) \end{aligned}$$

and analogously the twin term.

CT energy at HF level by EFP2.

In EFP2 method, CT energy is given as

$$E^{\mathrm{A^+B^-}} \approx 2 \sum_{i \in A}^{\mathrm{Occ_A}} \sum_{n \in B}^{\mathrm{Vir_B}} \frac{V_{in}^2}{F_{ii} - T_{nn}}$$

where

$$V_{in}^{2} = \frac{V_{in}^{B} - \sum_{m \in A}^{\text{All}_{A}} V_{im} S_{mn}^{B}}{1 - \sum_{m \in A}^{\text{All}_{A}} S_{mn}^{2}} \left\{ V_{in}^{B} - \sum_{m \in A}^{\text{All}_{A}} V_{im}^{B} S_{mn} + \sum_{j \in B}^{\text{Occ}_{B}} S_{ij} \left( T_{nj} - \sum_{m \in A}^{\text{All}_{A}} S_{nm} T_{mj} \right) \right\}$$

and analogously the twin term.

# **OEP-Based Methods**

**OEP-Based Otto-Ladik's theory** 

After introducing OEP's, the original Otto-Ladik's theory is reformulated without approximation as

$$E^{\mathrm{A^{+}B^{-}}} \approx 2 \sum_{i \in A}^{\mathrm{Occ_{A}}} \sum_{n \in B}^{\mathrm{Vir_{B}}} \frac{\left(V_{in}^{\mathrm{DF}} + V_{in}^{\mathrm{ESP,A}} + V_{in}^{\mathrm{ESP,B}}\right)^{2}}{\varepsilon_{i} - \varepsilon_{n}}$$

where

$$V_{in}^{ ext{DF}} = \sum_{\eta \in B}^{ ext{Aux}_{ ext{B}}} S_{i\eta} G_{\eta n}^{B}$$
 $V_{in}^{ ext{ESP,A}} = \sum_{k \in A}^{ ext{Occ}_{ ext{A}}} \sum_{j \in B}^{ ext{Occ}_{ ext{B}}} S_{kj} \sum_{x \in A} V_{nj}^{(x)} q_{ik}^{(x)}$ 
 $V_{in}^{ ext{ESP,B}} = -\sum_{k \in A}^{ ext{Occ}_{ ext{A}}} S_{kn} V_{ik}^{B}$ 

The OEP matrix for density fitted part is given by

$$G^{B}_{\boldsymbol{\eta}\boldsymbol{n}} = \sum_{\boldsymbol{\eta}' \in B}^{\mathrm{Aux_B}} [\mathbf{S}^{-1}]_{\boldsymbol{\eta}\boldsymbol{\eta}'} \left\{ V^{B}_{\boldsymbol{\eta}'\boldsymbol{n}} + \sum_{j \in B}^{\mathrm{Occ_B}} \left[ 2(\boldsymbol{\eta}'\boldsymbol{n}|jj) - (\boldsymbol{\eta}'j|nj) \right] \right\}$$

The OEP ESP-A charges are fit to reproduce the OEP potential

$$v_{ik}^{A}(\mathbf{r}) \equiv (1 - \delta_{ik}) \int \frac{\phi_i(\mathbf{r}')\phi_k(\mathbf{r}')}{|\mathbf{r} - \mathbf{r}'|} d\mathbf{r}' - \delta_{ik} \left( \sum_{x \in A} \frac{-Z_x}{|\mathbf{r} - \mathbf{r}_x|} + 2 \sum_{k \in A}^{\mathrm{Occ}_A} \int \frac{\phi_k(\mathbf{r}')\phi_k(\mathbf{r}')}{|\mathbf{r} - \mathbf{r}'|} d\mathbf{r}' - 2 \int \frac{\phi_i(\mathbf{r}')\phi_i(\mathbf{r}')}{|\mathbf{r} - \mathbf{r}'|} d\mathbf{r}' \right) d\mathbf{r}' \right) d\mathbf{r}' + \delta_{ik} \left( \sum_{x \in A} \frac{-Z_x}{|\mathbf{r} - \mathbf{r}_x|} + 2 \sum_{k \in A}^{\mathrm{Occ}_A} \int \frac{\phi_k(\mathbf{r}')\phi_k(\mathbf{r}')}{|\mathbf{r} - \mathbf{r}'|} d\mathbf{r}' - 2 \int \frac{\phi_i(\mathbf{r}')\phi_i(\mathbf{r}')}{|\mathbf{r} - \mathbf{r}'|} d\mathbf{r}' \right) d\mathbf{r}' \right) d\mathbf{r}' + \delta_{ik} \left( \sum_{x \in A} \frac{-Z_x}{|\mathbf{r} - \mathbf{r}_x|} + 2 \sum_{k \in A}^{\mathrm{Occ}_A} \int \frac{\phi_k(\mathbf{r}')\phi_k(\mathbf{r}')}{|\mathbf{r} - \mathbf{r}'|} d\mathbf{r}' - 2 \int \frac{\phi_i(\mathbf{r}')\phi_i(\mathbf{r}')}{|\mathbf{r} - \mathbf{r}'|} d\mathbf{r}' \right) d\mathbf{r}' d\mathbf{r}' \right) d\mathbf{r}' + \delta_{ik} \left( \sum_{x \in A} \frac{-Z_x}{|\mathbf{r} - \mathbf{r}_x|} + 2 \sum_{k \in A}^{\mathrm{Occ}_A} \int \frac{\phi_k(\mathbf{r}')\phi_k(\mathbf{r}')}{|\mathbf{r} - \mathbf{r}'|} d\mathbf{r}' \right) d\mathbf{r}' d\mathbf{r$$

so that

$$v_{ik}^A(\mathbf{r}) \cong \sum_{x \in A} \frac{q_{ik}^{(x)}}{|\mathbf{r} - \mathbf{r}_x|}$$

The OEP ESP-B charges are fit to reproduce the electrostatic potential of molecule *B* (they are standard ESP charges).

# 17.9.2 Member Function Documentation

17.9.2.1 double ChargeTransferEnergySolver::compute\_benchmark ( const std::string & method = "DEFAULT" )
[virtual]

Compute property by using benchmark method.

Each solver object has one DEFAULT benchmark method

**Parameters** 

method - benchmark method

Implements oepdev::OEPDevSolver.

17.9.2.2 double ChargeTransferEnergySolver::compute\_oep\_based ( const std::string & method = "DEFAULT" )
[virtual]

Compute property by using OEP's.

Each solver object has one DEFAULT OEP-based method.

**Parameters** 

method - flavour of OEP model

Implements oepdev::OEPDevSolver.

The documentation for this class was generated from the following files:

- oepdev/libutil/solver.h
- · oepdev/libutil/solver.cc

# 17.10 oepdev::CPHF Class Reference

**CPHF** solver class.

#include <cphf.h>

#### **Public Member Functions**

- CPHF (SharedWavefunction ref\_wfn, Options &options)
  - Constructor.
- ∼CPHF ()

Desctructor.

• void compute (void)

```
run the calculations

    void print (void) const

      print to output file
• int nocc (void) const
      get the number of occupied orbitals

    std::shared_ptr< Wavefunction > wfn (void) const

      grab the wavefunction
• Options & options (void) const
      grab the Psi4 options
```

std::shared ptr< Matrix > polarizability (void) const

retrieve the molecular (total) polarizability

std::shared\_ptr< Matrix > polarizability (int i) const

retrieve the i-th orbital-associated polarizability

std::shared\_ptr< Matrix > polarizability (int i, int j) const

retrieve the charge-transfer polarizability associated with orbitals i and j

std::shared\_ptr< Matrix > X (int x) const

retrieve the X operator O-V perturbation matrix in AO basis for x-th component

std::shared\_ptr< Vector > Imo\_centroid (int i) const

retrieve the i-th orbital (LMO) centroid

std::shared\_ptr< Localizer > localizer (void) const

retrieve the orbital localizer

# **Protected Attributes**

```
· std::shared ptr
  < psi::Wavefunction > _wfn
      Wavefunction object.

    std::shared_ptr< Localizer > _localizer

     Orbital localizer.
· const int _no
     Number of occupied orbitals.
```

Number of virtual orbitals.

· const int \_nn

· const int \_nv

Number of basis functions.

long int \_memory

Memory.

· int \_maxiter

Maximum number of iterations.

double <u>conv</u>

CPHF convergence threshold.

· bool \_with\_diis

whether use DIIS or not

· const int \_diis\_dim

Size of subspace.

std::shared\_ptr< BasisSet > \_primary

Primary Basis Set.

std::shared\_ptr< Matrix > \_cocc

Occupied orbitals.

std::shared\_ptr< Matrix > \_cvir

Virtual orbitals.

std::shared\_ptr< Vector > \_eps\_occ

Occupied orbital energies.

• std::shared ptr< Vector > eps vir

Virtual orbital energies.

• std::vector< std::shared\_ptr

< oepdev::DIISManager > > \_diis

the DIIS managers for each perturbation operator x, y and z

• Options & \_options

Options.

std::shared\_ptr< Matrix > \_molecularPolarizability

Total (molecular) polarizability tensor.

- std::vector< std::shared\_ptr</li>
  - < Vector >> \_orbitalCentroids

LMO centroids.

- std::vector< std::shared ptr
  - < Matrix >> \_orbitalPolarizabilities

orbital-associated polarizability tensors

- std::vector< std::vector</li>
  - < std::shared\_ptr< Matrix >> > \_orbitalChargeTransferPolarizabilities

orbital-orbital charge-transfer polarizability tensors

- std::vector< std::shared ptr</li>
  - < Matrix >> \_X\_OV\_ao\_matrices

Perturbation X Operator O-> V matrices in AO basis.

# 17.10.1 Detailed Description

**CPHF** solver class.

Solves CPHF equations (now only for RHF wavefunction). Computes molecular and polarizabilities associated with the localized molecular orbitals (LMO).

Note

# Useful options:

- CPHF\_CONVER convergence of CPHF. Default: 1e-8 (au)
- CPHF\_CONVER maximum number of iterations. Default: 50
- CPHF\_DIIS wheather use DIIS or not. Default: true
- CPHF\_DIIS\_DIM dimension of iterative subspace. Default: 3
- $\bullet$  CPHF\_LOCALIZE localize the molecular orbitals? Default:  ${\tt true}$
- CPHF\_LOCALIZER set orbital localization method. Available: BOYS and PIPEK\_MEZEY. Default: BOYS

# 17.10.2 Constructor & Destructor Documentation

17.10.2.1 oepdev::CPHF::CPHF ( SharedWavefunction ref\_wfn, Options & options )

Constructor.

#### **Parameters**

ref_wfn	reference HF wavefunction	
options set of Psi4 options		

The documentation for this class was generated from the following files:

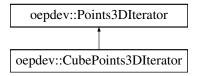
- · oepdev/libutil/cphf.h
- · oepdev/libutil/cphf.cc

# 17.11 oepdev::CubePoints3DIterator Class Reference

Iterator over a collection of points in 3D space. g09 Cube-like order.

#include <space3d.h>

Inheritance diagram for oepdev::CubePoints3DIterator:



# **Public Member Functions**

- CubePoints3Dlterator (const int &nx, const int &ny, const int &nz, const double &dx, const double &dy, const double &dx, const double &dx, const double &ox)
- · virtual void first ()

Initialize first iteration.

• virtual void next ()

Step to next iteration.

# **Protected Attributes**

- const int nx\_
- const int ny\_
- const int nz
- const double dx\_
- const double dy\_
- const double dz
- const double **ox**\_
- const double **oy\_**
- · const double oz\_
- int ii\_
- int **jj\_**
- int kk\_

# **Additional Inherited Members**

# 17.11.1 Detailed Description

Iterator over a collection of points in 3D space. g09 Cube-like order.

**Note:** Always create instances by using static factory method from Points3Dlterator. Do not use constructor of this class

The documentation for this class was generated from the following files:

- oepdev/lib3d/space3d.h
- · oepdev/lib3d/space3d.cc

# 17.12 oepdev::CubePointsCollection3D Class Reference

G09 cube-like ordered collection of points in 3D space.

```
#include <space3d.h>
```

Inheritance diagram for oepdev::CubePointsCollection3D:



#### **Public Member Functions**

- CubePointsCollection3D (Collection collectionType, const int &nx, const int &ny, const int &nz, const double &px, const double &px, const double &px, psi::SharedBasisSet bs, psi::Options &options)
- · virtual void print () const

Print the information to Psi4 output file.

virtual void write\_cube\_file (psi::SharedMatrix v, const std::string &name)

#### **Additional Inherited Members**

# 17.12.1 Detailed Description

G09 cube-like ordered collection of points in 3D space.

**Note:** Do not use constructors of this class explicitly. Instead, use static factory methods of the superclass to create instances.

The documentation for this class was generated from the following files:

- · oepdev/lib3d/space3d.h
- · oepdev/lib3d/space3d.cc

# 17.13 oepdev::DIISManager Class Reference

# DIIS manager.

#include <diis.h>

# **Public Member Functions**

- DIISManager (int dim, int na, int nb)
- ∼DIISManager ()

#### Destructor.

- void put (const std::shared\_ptr< const Matrix > &error, const std::shared\_ptr< const Matrix > &vector)
- void compute (void)
- void update (std::shared\_ptr< Matrix > &other)

# 17.13.1 Detailed Description

# DIIS manager.

Instance can interact directly with the process of solving vector quantities in iterative manner. One needs to pass the dimensions of solution vector as well as the DIIS subspace size. The iterative procedure requires providing the current vector and also an estimate of the error vector. The updated DIIS vector can be copied to an old vector through the Instance.

#### 17.13.2 Constructor & Destructor Documentation

17.13.2.1 oepdev::DIISManager::DIISManager ( int dim, int na, int nb )

#### Constructor.

#### **Parameters**

dim	Size of DIIS subspace	
na	Number of solution rows	
nb	Number of solution columns	

### 17.13.3 Member Function Documentation

17.13.3.1 void oepdev::DIISManager::compute ( void )

Perform DIIS interpolation.

17.13.3.2 void oepdev::DIISManager::put ( const std::shared\_ptr< const Matrix > & error, const std::shared\_ptr< const Matrix > & vector )

Put the current solution to the DIIS manager.

#### **Parameters**

error	Shared matrix with current solution error
vector	Shared matrix with current solution vector

17.13.3.3 void oepdev::DIISManager::update ( std::shared\_ptr< Matrix > & other )

Update solution vector. Pass the Shared pointer to current solution. Then it will be overriden by the updated DIIS solution.

The documentation for this class was generated from the following files:

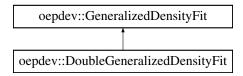
- · oepdev/libutil/diis.h
- · oepdev/libutil/diis.cc

# 17.14 oepdev::DoubleGeneralizedDensityFit Class Reference

Generalized Density Fitting Scheme - Double Fit.

#include <oep\_gdf.h>

Inheritance diagram for oepdev::DoubleGeneralizedDensityFit:



# **Public Member Functions**

- DoubleGeneralizedDensityFit (std::shared\_ptr< psi::BasisSet > bs\_auxiliary, std::shared\_ptr< psi::BasisSet > bs\_intermediate, std::shared\_ptr< psi::Matrix > v\_vector)
- std::shared\_ptr< psi::Matrix > compute (void)
   Perform the generalized density fit.

Additional Inherited Members

# 17.14.1 Detailed Description

Generalized Density Fitting Scheme - Double Fit.

The density fitting map projects the OEP onto an arbitrary (not necessarily complete) auxiliary basis set space through application of the self energy minimization technique. The resulting three-electron repulsion integrals are computed by utilizing the resolution of identity in an intermediate, nearly-complete basis set space, hence performing an internal density fitting in nearly complete basis. Refer to density fitting specialized for OEP's for more details.

# 17.14.2 Determination of the OEP matrix

Coefficients G are computed by using the following relation

$$\mathbf{G} = \mathbf{A}^{-1} \cdot \mathbf{R} \cdot \mathbf{H}$$

where the intermediate projection matrix is given by

$$\mathbf{H} = \mathbf{S}^{-1} \cdot \mathbf{V}$$

In the above equations,

$$egin{aligned} A_{\xi\xi'} &= \left(\xi || \xi' 
ight) \ R_{\xiarepsilon} &= \left(\xi || arepsilon 
ight) \ S_{arepsilonarepsilon'} &= \left(arepsilon || arepsilon' 
ight) \ V^{arepsilon i} &= \left(arepsilon || \hat{v}i 
ight) \end{aligned}$$

The following labeling convention is used here:

- *i* denotes the arbitrary state vector
- $\xi$  denotes the auxiliary basis set element
- arepsilon denotes the intermediate (nearly complete) basis set element

In the above, denotes the single integration over electron coordinate, i.e.,

$$(a|b) \equiv \int d\mathbf{r} \phi_a^*(\mathbf{r}) \phi_b(\mathbf{r})$$

whereas || acts as shown below:

$$(a||b) \equiv \iint d\mathbf{r}' d\mathbf{r}'' \frac{\phi_a^*(\mathbf{r}')\phi_b(\mathbf{r}'')}{|\mathbf{r}' - \mathbf{r}''|}$$

The spatial form of the potential operator  $\hat{v}$  can be expressed by

$$v(\mathbf{r}) \equiv \int d\mathbf{r}' \frac{\rho(\mathbf{r}')}{|\mathbf{r}' - \mathbf{r}|}$$

with  $\rho(\mathbf{r})$  being the effective one-electron density associated with  $\hat{v}$ .

### 17.14.2.1 Theory behind the double GDF scheme

In order to perform the generalized density fitting in an incomplete auxiliary basis set, one must apply the following formula:

$$G = A^{-1} \cdot B$$

where one encounters the need of evaluation of the following three-electron integrals

$$B_{\xi i} = (\xi || \hat{v}i) \equiv \iiint d\mathbf{r}' d\mathbf{r}'' d\mathbf{r}''' \phi_{\xi}^*(\mathbf{r}') \frac{1}{|\mathbf{r}' - \mathbf{r}''|} \rho(\mathbf{r}''') \frac{1}{|\mathbf{r}''' - \mathbf{r}''|} \phi_i(\mathbf{r}'')$$

Computation of all the necessery integrals of this kind is very costly and impractical for larger molecules. However, one can use the same trick that is a kernel of the OEP technique introduced in the OEPDev project, i.e., introduce the effective potential in order to get rid of one integration. This can be done by performing the generalized density fitting in the nearly complete intermediate basis

$$\hat{v}|i)\cong\sum_{\mathcal{E}}H_{\mathcal{E}i}|\mathcal{E})$$

Note that this is done just for the sake of factorizing the triple integral and computing the OEP matrix for the incomplete auxiliary basis. Therefore, the intermediate basis set is used just for a while during density fitting and is no longer necessary later on. By inserting the above identity to the triple integral one can transform it into a sum of the two-electron integrals that are much easier to evaluate. This leads to equations given in the beginning of this section.

# 17.14.3 Member Function Documentation

17.14.3.1 std::shared\_ptr< psi::Matrix > DoubleGeneralizedDensityFit::compute ( void ) [virtual]

Perform the generalized density fit.

Returns

The OEP coefficients  $G_{\xi_i}$ 

Implements oepdev::GeneralizedDensityFit.

The documentation for this class was generated from the following files:

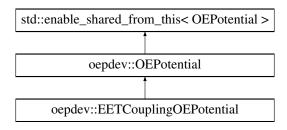
- oepdev/liboep/oep\_gdf.h
- · oepdev/liboep/oep\_gdf.cc

# 17.15 oepdev::EETCouplingOEPotential Class Reference

Generalized One-Electron Potential for EET coupling calculations.

#include <oep.h>

Inheritance diagram for oepdev::EETCouplingOEPotential:



# **Public Member Functions**

- **EETCouplingOEPotential** (SharedWavefunction wfn, SharedBasisSet auxiliary, SharedBasisSet intermediate, Options & options)
- EETCouplingOEPotential (SharedWavefunction wfn, Options & options)
- virtual void compute (const std::string &oepType) override

Compute matrix forms of all OEP's within a specified OEP type.

virtual void compute\_3D (const std::string &oepType, const double &x, const double &y, const double &z, double &v) override

Compute value of potential in point x, y, z and save at v.

• virtual void **print\_header** () const override

# **Additional Inherited Members**

# 17.15.1 Detailed Description

Generalized One-Electron Potential for EET coupling calculations.

Contains the following OEP types:

- Fujimoto.ET1
- Fujimoto.ET2
- Fujimoto.HT1
- Fujimoto.HT1
- Fujimoto.HT2
- Fujimoto.CT1
- Fujimoto.CT2

The documentation for this class was generated from the following files:

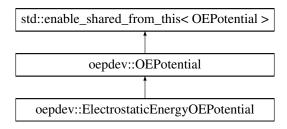
- oepdev/liboep/oep.h
- · oepdev/liboep/oep.cc

# 17.16 oepdev::ElectrostaticEnergyOEPotential Class Reference

Generalized One-Electron Potential for Electrostatic Energy.

#include <oep.h>

Inheritance diagram for oepdev::ElectrostaticEnergyOEPotential:



# **Public Member Functions**

• ElectrostaticEnergyOEPotential (SharedWavefunction wfn, Options & options)

Only ESP-based potential is worth implementing.

• virtual void compute (const std::string &oepType) override

Compute matrix forms of all OEP's within a specified OEP type.

virtual void compute\_3D (const std::string &oepType, const double &x, const double &y, const double &z, double &v) override

Compute value of potential in point x, y, z and save at v.

virtual void print\_header () const override

# **Additional Inherited Members**

# 17.16.1 Detailed Description

Generalized One-Electron Potential for Electrostatic Energy.

Contains the following OEP types:

V

The documentation for this class was generated from the following files:

- oepdev/liboep/oep.h
- oepdev/liboep/oep.cc

# 17.17 oepdev::ElectrostaticEnergySolver Class Reference

Compute the Coulombic interaction energy between unperturbed wavefunctions.

#include <solver.h>

Inheritance diagram for oepdev::ElectrostaticEnergySolver:



# **Public Member Functions**

- ElectrostaticEnergySolver (SharedWavefunctionUnion wfn\_union)
- virtual double compute\_oep\_based (const std::string &method="DEFAULT")
   Compute property by using OEP's.
- virtual double compute\_benchmark (const std::string &method="DEFAULT")
   Compute property by using benchmark method.

# **Additional Inherited Members**

# 17.17.1 Detailed Description

Compute the Coulombic interaction energy between unperturbed wavefunctions.

The implemented methods are shown in below

Keyword	Method Description
	Benchmark Methods
AO_EXPANDED	*Default*. Exact Coulombic energy from atomic
	orbital expansions.
MO_EXPANDED	Exact Coulombic energy from molecular orbital
	expansions
	OEP-Based Methods
ESP_SYMMETRIZED	*Default*. Coulombic energy from ESP charges
	interacting with nuclei and electronic density.
	Symmetrized with respect to monomers.

Table 17.2: Methods available in the Solver

Below the detailed description of the above methods is given.

# **Benchmark Methods**

Exact Coulombic energy from atomic orbital expansions.

The Coulombic interaction energy is given by

$$E^{\text{Coul}} = E^{\text{Nuc-Nuc}} + E^{\text{Nuc-El}} + E^{\text{El-El}}$$

where the nuclear-nuclear repulsion energy is

$$E^{\text{Nuc-Nuc}} = \sum_{x \in A} \sum_{y \in B} \frac{Z_x Z_y}{|\mathbf{r}_x - \mathbf{r}_y|}$$

the nuclear-electronic attraction energy is

$$E^{\text{Nuc-El}} = \sum_{x \in A} \sum_{\lambda \sigma \in B} Z_x V_{\lambda \sigma}^{(x)} \left( D_{\lambda \sigma}^{(\alpha)} + D_{\lambda \sigma}^{(\beta)} \right) + \sum_{y \in B} \sum_{\mu \nu \in A} Z_y V_{\mu \nu}^{(y)} \left( D_{\mu \nu}^{(\alpha)} + D_{\mu \nu}^{(\beta)} \right)$$

and the electron-electron repulsion energy is

$$E^{\mathrm{El-El}} = \sum_{\mu\nu\in A} \sum_{\lambda\sigma\in B} \left\{ D_{\mu\nu}^{(\alpha)} + D_{\mu\nu}^{(\beta)} \right\} \left\{ D_{\lambda\sigma}^{(\alpha)} + D_{\lambda\sigma}^{(\beta)} \right\} (\mu\nu|\lambda\sigma)$$

In the above equations,

$$V_{\lambda\sigma}^{(x)} \equiv \int \frac{\varphi_{\lambda}^{*}(\mathbf{r})\varphi_{\sigma}(\mathbf{r})}{|\mathbf{r} - \mathbf{r}_{x}|} d\mathbf{r}$$

Exact Coulombic energy from molecular orbital expansion.

This approach is fully equivalent to the atomic orbital expansion shown above. For the closed shell case, the Coulombic interaction energy is given by

$$E^{\text{Coul}} = E^{\text{Nuc-Nuc}} + E^{\text{Nuc-El}} + E^{\text{El-El}}$$

where the nuclear-nuclear repulsion energy is

$$E^{\text{Nuc-Nuc}} = \sum_{x \in A} \sum_{y \in B} \frac{Z_x Z_y}{|\mathbf{r}_x - \mathbf{r}_y|}$$

the nuclear-electronic attraction energy is

$$E^{\text{Nuc-El}} = 2\sum_{i \in A} \sum_{y \in B} V_{ii}^{(y)} + 2\sum_{j \in B} \sum_{x \in A} V_{jj}^{(x)}$$

and the electron-electron repulsion energy is

$$E^{\text{El-El}} = 4\sum_{i \in A} \sum_{j \in B} (ii|jj)$$

# **OEP-Based Methods**

Coulombic energy from ESP charges interacting with nuclei and electronic density.

In this approach, nuclear and electronic density of either species is approximated by ESP charges. In order to achieve symmetric expression, the interaction is computed twice (ESP of A interacting with density matrix and nuclear charges of B and vice versa) and then divided by 2. Thus,

$$E^{\text{Coul}} \approx \frac{1}{2} \left[ \sum_{x \in A} \sum_{y \in B} \frac{Z_x q_y}{|\mathbf{r}_x - \mathbf{r}_y|} + \sum_{y \in B} \sum_{\mu \nu \in A} q_y V_{\mu\nu}^{(y)} \left( D_{\mu\nu}^{(\alpha)} + D_{\mu\nu}^{(\beta)} \right) + \sum_{y \in B} \sum_{x \in A} \frac{q_x Z_y}{|\mathbf{r}_x - \mathbf{r}_y|} + \sum_{x \in A} \sum_{\lambda \sigma \in B} q_x V_{\lambda\sigma}^{(x)} \left( D_{\lambda\sigma}^{(\alpha)} + D_{\lambda\sigma}^{(\beta)} \right) \right]$$

If the basis set is large and the number of ESP centres  $q_{x(y)}$  is sufficient, the sum of first two contributions equals the sum of the latter two contributions.

Notes:

· This solver also computes and prints the ESP-ESP point charge interaction energy,

$$E^{\text{Coul,ESP}} \approx \sum_{x \in A} \sum_{y \in B} \frac{q_x q_y}{|\mathbf{r}_x - \mathbf{r}_y|}$$

for reference purposes.

• In order to construct this solver, always use the OEPDevSolver::build static factory method.

# 17.17.2 Member Function Documentation

17.17.2.1 double ElectrostaticEnergySolver::compute\_benchmark ( const std::string & method = "DEFAULT" )
[virtual]

Compute property by using benchmark method.

Each solver object has one DEFAULT benchmark method

**Parameters** 

```
method - benchmark method
```

Implements oepdev::OEPDevSolver.

```
17.17.2.2 double ElectrostaticEnergySolver::compute_oep_based ( const std::string & method = "DEFAULT" )
[virtual]
```

Compute property by using OEP's.

Each solver object has one DEFAULT OEP-based method.

**Parameters** 

```
method - flavour of OEP model
```

Implements oepdev::OEPDevSolver.

The documentation for this class was generated from the following files:

- oepdev/libutil/solver.h
- · oepdev/libutil/solver.cc

# 17.18 oepdev::ElectrostaticPotential3D Class Reference

Electrostatic potential of a molecule.

```
#include <space3d.h>
```

Inheritance diagram for oepdev::ElectrostaticPotential3D:



### **Public Member Functions**

- ElectrostaticPotential3D (const int &np, const double &padding, psi::SharedWavefunction wfn, psi::Options &options)
- ElectrostaticPotential3D (const int &nx, const int &ny, const int &nz, const double &px, const double &px, const double &px, psi::SharedWavefunction wfn, psi::Options &options)
- virtual double compute xyz (const double &x, const double &y, const double &z)

Compute a value of scalar field at point (x, y, z)

• virtual void print () const

Print information of the object to Psi4 output.

# **Additional Inherited Members**

# 17.18.1 Detailed Description

Electrostatic potential of a molecule.

Computes the electrostatic potential of a molecule directly from the wavefunction. The electrostatic potential  $v(\mathbf{r})$  at point  $\mathbf{r}$  is computed from the following formula:

$$v(\mathbf{r}) = v_{\text{nuc}}(\mathbf{r}) + v_{\text{el}}(\mathbf{r})$$

where the nuclear and electronic contributions are defined accordingly as

$$v_{\text{nuc}}(\mathbf{r}) = \sum_{x} \frac{Z_{x}}{|\mathbf{r} - \mathbf{r}_{x}|}$$
$$v_{\text{el}}(\mathbf{r}) = \sum_{\mu\nu} \left\{ D_{\mu\nu}^{(\alpha)} + D_{\mu\nu}^{(\beta)} \right\} V_{\nu\mu}(\mathbf{r})$$

In the above equations,  $Z_x$  denotes the charge of xth nucleus,  $D_{\mu\nu}^{(\omega)}$  is the one-particle (relaxed) density matrix element in AO basis associated with the  $\omega$  electron spin, and  $V_{\mu\nu}(\mathbf{r})$  is the potential one-electron integral defined by

$$V_{
u\mu}(\mathbf{r}) \equiv \int d\mathbf{r}' \boldsymbol{\varphi}_{
u}^*(\mathbf{r}') rac{1}{|\mathbf{r} - \mathbf{r}'|} \boldsymbol{\varphi}_{\mu}(\mathbf{r}')$$

The documentation for this class was generated from the following files:

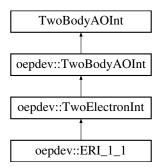
- · oepdev/lib3d/space3d.h
- · oepdev/lib3d/space3d.cc

# 17.19 oepdev::ERI\_1\_1 Class Reference

2-centre ERI of the form (a|O(2)|b) where O(2) = 1/r12.

#include <eri.h>

Inheritance diagram for oepdev::ERI\_1\_1:



# **Public Member Functions**

- ERI\_1\_1 (const IntegralFactory \*integral, int deriv=0, bool use\_shell\_pairs=false)
  - Constructor. Use oepdev::IntegralFactory to generate this object.
- ∼ERI 1 1 ()

Destructor.

# **Protected Member Functions**

• size\_t compute\_doublet (int, int)

Compute ERI's between 2 shells.

# **Protected Attributes**

• double \* mdh\_buffer\_1\_

Buffer for McMurchie-Davidson-Hermite coefficents for monomial expansion (shell 1)

double \* mdh\_buffer\_2\_

Buffer for McMurchie-Davidson-Hermite coefficents for monomial expansion (shell 2)

# 17.19.1 Detailed Description

2-centre ERI of the form (a|O(2)|b) where O(2) = 1/r12.

ERI's are computed for a shell doublet (P|Q) and stored in the target\_full\_ buffer, accessible through buffer() method:

For each 
$$(n_1,l_1,m_1)\in P$$
:  
For each  $(n_2,l_2,m_2)\in Q$ :  
 $\mathrm{ERI}=(A|B)[\{lpha\},\mathbf{n},\mathbf{l},\mathbf{m}]$ 

For detailed description of the McMurchie-Davidson scheme, refer to The Integral Package Library.

# 17.19.2 Implementation

A set of ERI's in a shell is decontracted as

$$(A|B)[\{\boldsymbol{\alpha}\},\mathbf{n},\mathbf{l},\mathbf{m}] = \sum_{ij} c_i(\boldsymbol{\alpha}_1) c_j(\boldsymbol{\alpha}_2)(i|j)[\{\boldsymbol{\alpha}\},\mathbf{n},\mathbf{l},\mathbf{m}]$$

where the primitive ERI is given by

$$(i|j)[\{\alpha\},\mathbf{n},\mathbf{l},\mathbf{m}] \qquad \qquad = \qquad \sum_{N_1=0}^{n_1} \sum_{L_1=0}^{l_1} \sum_{M_1=0}^{m_1} \sum_{N_2=0}^{n_2} \sum_{L_2=0}^{l_2} \sum_{M_2=0}^{m_2} d_{N_1}^{n_1} d_{L_1}^{l_1} d_{M_1}^{m_1} d_{N_2}^{n_2} d_{L_2}^{l_2} d_{M_2}^{m_2} [N_1 L_1 M_1 | N_2 L_2 M_2]$$

The documentation for this class was generated from the following files:

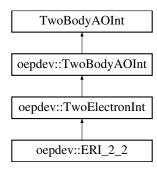
- · oepdev/libints/eri.h
- · oepdev/libints/eri.cc

# 17.20 oepdev::ERI\_2\_2 Class Reference

4-centre ERI of the form (ab|O(2)|cd) where O(2) = 1/r12.

#include <eri.h>

Inheritance diagram for oepdev::ERI\_2\_2:



# **Public Member Functions**

- ERI\_2\_2 (const IntegralFactory \*integral, int deriv=0, bool use\_shell\_pairs=false)

  Constructor. Use oepdev::IntegralFactory to generate this object.
- ~ERI\_2\_2 ()
   Destructor.

# **Protected Member Functions**

size\_t compute\_quartet (int, int, int, int)
 Compute ERI's between 4 shells.

# **Protected Attributes**

- double \* mdh\_buffer\_12\_
  - Buffer for McMurchie-Davidson-Hermite coefficents for binomial expansion (shells 1 and 2)
- double \* mdh\_buffer\_34\_

Buffer for McMurchie-Davidson-Hermite coefficents for binomial expansion (shells 3 and 4)

# 17.20.1 Detailed Description

4-centre ERI of the form (ab|O(2)|cd) where O(2) = 1/r12.

ERI's are computed for a shell quartet (PQ|RS) and stored in the  $target_full_buffer$ , accessible through buffer () method:

For each 
$$(n_1,l_1,m_1)\in P$$
:  
For each  $(n_2,l_2,m_2)\in Q$ :  
For each  $(n_3,l_3,m_3)\in R$ :  
For each  $(n_4,l_4,m_4)\in S$ :  
 $\mathrm{ERI}=(AB|CD)[\{\alpha\},\mathbf{n},\mathbf{l},\mathbf{m}]$ 

For detailed description of the McMurchie-Davidson scheme, refer to The Integral Package Library.

# 17.20.2 Implementation

A set of ERI's in a shell is decontracted as

$$(AB|CD)[\{\alpha\},\mathbf{n},\mathbf{l},\mathbf{m}] = \sum_{ijkl} c_i(\alpha_1)c_j(\alpha_2)c_k(\alpha_3)c_l(\alpha_4)(ij|kl)[\{\alpha\},\mathbf{n},\mathbf{l},\mathbf{m}]$$

where the primitive ERI is given by

$$(ij|kl)[\{\alpha\},\mathbf{n},\mathbf{l},\mathbf{m}] = E_{ij}(\alpha_1,\alpha_2)E_{kl}(\alpha_3,\alpha_4)$$

$$\times \sum_{N_1=0}^{n_1+n_2} \sum_{L_1=0}^{l_1+l_2} \sum_{M_2=0}^{m_1+m_2} \sum_{L_2=0}^{n_3+n_4} \sum_{L_2=0}^{l_3+l_4} \sum_{M_2=0}^{m_3+n_4} d_{N_1}^{n_1n_2} d_{N_1}^{l_1l_2} d_{M_1}^{m_1m_2} d_{N_2}^{n_3n_4} d_{L_2}^{l_3l_4} d_{M_2}^{m_3m_4} [N_1L_1M_1|N_2L_2M_2]$$

In the above equation, the multiplicative constants are given as

$$E_{ij}(\alpha_1, \alpha_2) = \exp\left[-\frac{\alpha_1 \alpha_2}{\alpha_1 + \alpha_2} |\mathbf{A} - \mathbf{B}|^2\right]$$
$$E_{kl}(\alpha_3, \alpha_4) = \exp\left[-\frac{\alpha_3 \alpha_4}{\alpha_3 + \alpha_4} |\mathbf{C} - \mathbf{D}|^2\right]$$

The documentation for this class was generated from the following files:

- · oepdev/libints/eri.h
- · oepdev/libints/eri.cc

# 17.21 oepdev::ERI\_3\_1 Class Reference

4-centre ERI of the form (abc|O(2)|d) where O(2) = 1/r12.

#include <eri.h>

Inheritance diagram for oepdev::ERI\_3\_1:



#### **Public Member Functions**

• ERI\_3\_1 (const IntegralFactory \*integral, int deriv=0, bool use\_shell\_pairs=false)

Constructor. Use oepdev::IntegralFactory to generate this object.

• ∼ERI 3 1 ()

Destructor.

# **Protected Member Functions**

size\_t compute\_quartet (int, int, int, int)

Compute ERI's between 4 shells.

# **Protected Attributes**

double \* mdh\_buffer\_123\_

Buffer for McMurchie-Davidson-Hermite coefficents for trinomial expansion (shells 1, 2 and 3)

double \* mdh\_buffer\_4\_

Buffer for McMurchie-Davidson-Hermite coefficents for monomial expansion (shell 4)

# 17.21.1 Detailed Description

4-centre ERI of the form (abc|O(2)|d) where O(2) = 1/r12.

ERI's are computed for a shell quartet (PQR|S) and stored in the target\_full\_ buffer, accessible through buffer() method:

For each 
$$(n_1,l_1,m_1)\in P$$
:  
For each  $(n_2,l_2,m_2)\in Q$ :  
For each  $(n_3,l_3,m_3)\in R$ :  
For each  $(n_4,l_4,m_4)\in S$ :  
 $\mathrm{ERI}=(ABC|D)[\{\alpha\},\mathbf{n},\mathbf{l},\mathbf{m}]$ 

For detailed description of the McMurchie-Davidson scheme, refer to The Integral Package Library.

# 17.21.2 Implementation

A set of ERI's in a shell is decontracted as

$$(ABC|D)[\{\alpha\}, \mathbf{n}, \mathbf{l}, \mathbf{m}] = \sum_{ijkl} c_i(\alpha_1)c_j(\alpha_2)c_k(\alpha_3)c_l(\alpha_4)(ijk|l)[\{\alpha\}, \mathbf{n}, \mathbf{l}, \mathbf{m}]$$

where the primitive ERI is given by

$$(ijk|l)[\{\alpha\},\mathbf{n},\mathbf{l},\mathbf{m}] = E_{ijk}(\alpha_1,\alpha_2,\alpha_3) \\ \times \sum_{N_1=0}^{n_1+n_2+n_3} \sum_{L_1=0}^{l_1+l_2+l_3} \sum_{M_1=0}^{m_1+m_2+m_3} \sum_{N_2=0}^{n_4} \sum_{L_2=0}^{m_4} \sum_{M_2=0}^{m_4} d_{N_1}^{n_1n_2n_3} d_{L_1}^{l_1l_2l_3} d_{M_1}^{m_1m_2m_3} d_{N_2}^{n_4} d_{L_2}^{l_4} d_{M_2}^{m_4} \left[ N_1L_1M_1 | N_2L_2M_2 \right] \\ \times \sum_{N_1=0}^{n_1+n_2+n_3} \sum_{L_1=0}^{l_1+l_2+l_3} \sum_{M_1=0}^{m_1+m_2+m_3} \sum_{N_2=0}^{n_4} \sum_{L_2=0}^{m_4} d_{N_1}^{n_1n_2n_3} d_{L_1}^{l_1l_2l_3} d_{M_1}^{m_1m_2m_3} d_{N_2}^{n_4} d_{L_2}^{l_4} d_{M_2}^{m_4} \left[ N_1L_1M_1 | N_2L_2M_2 \right] \\ \times \sum_{N_1=0}^{n_1+n_2+n_3} \sum_{L_1=0}^{l_1+l_2+l_3} \sum_{M_1=0}^{m_1+m_2+m_3} \sum_{N_2=0}^{n_4} \sum_{L_2=0}^{m_4} d_{N_1}^{n_1n_2n_3} d_{L_1}^{l_1l_2l_3} d_{M_1}^{m_1m_2m_3} d_{N_2}^{n_4} d_{L_2}^{l_4} d_{M_2}^{m_4} \left[ N_1L_1M_1 | N_2L_2M_2 \right] \\ \times \sum_{N_1=0}^{n_1+n_2+n_3} \sum_{L_1=0}^{l_1+l_2+l_3} \sum_{M_1=0}^{m_1+m_2+m_3} \sum_{N_2=0}^{n_4} \sum_{L_2=0}^{m_4} d_{N_1}^{n_1n_2n_3} d_{L_1}^{l_1l_2l_3} d_{M_1}^{m_1m_2m_3} d_{N_2}^{n_4} d_{M_2}^{m_4} \left[ N_1L_1M_1 | N_2L_2M_2 \right] \\ \times \sum_{N_1=0}^{n_1+n_2+n_3} \sum_{M_1=0}^{n_1+n_2+n_3} \sum_{N_2=0}^{n_1+n_2+n_3} \sum_{M_2=0}^{n_1+n_2+n_3} d_{N_2}^{n_1+n_2+n_3} d_{N_2}^{n_1+n_$$

In the above equation, the multiplicative constants are given as

$$E_{ijk}(\alpha_1, \alpha_2, \alpha_3) = \exp\left[-\frac{\alpha_1 \alpha_2}{\alpha_1 + \alpha_2} |\mathbf{A} - \mathbf{B}|^2\right] \exp\left[-\frac{(\alpha_1 + \alpha_2) \alpha_3}{\alpha_1 + \alpha_2 + \alpha_3} |\mathbf{P} - \mathbf{C}|^2\right]$$

The documentation for this class was generated from the following files:

- · oepdev/libints/eri.h
- · oepdev/libints/eri.cc

# 17.22 oepdev::ESPSolver Class Reference

Charges from Electrostatic Potential (ESP). A solver-type class.

#include <esp.h>

# **Public Member Functions**

ESPSolver (SharedScalarField3D field)

Construct from scalar field.

• ESPSolver (SharedScalarField3D field, psi::SharedMatrix centres)

Construct from scalar field.

virtual ∼ESPSolver ()

Destructor.

• virtual psi::SharedVector charges () const

Get the (fit) charges.

virtual psi::SharedMatrix centres () const

Get the charge distribution centres.

virtual void compute ()

Perform fitting of effective charges.

#### **Protected Attributes**

const int nCentres

Number of fit centres.

SharedScalarField3D field

Scalar field.

• psi::SharedVector charges\_

Charges to be fit.

psi::SharedMatrix centres\_

Centres, at which fit charges will reside.

# 17.22.1 Detailed Description

Charges from Electrostatic Potential (ESP). A solver-type class.

Solves the least-squares problem to fit the generalized charges  $q_m$ , that reproduce the reference generalized potential  $v^{\text{ref}}(\mathbf{r})$  supplied by the ScalarField3D object:

$$\int d\mathbf{r}' \left[ v^{\rm ref}(\mathbf{r}') - \sum_m \frac{q_m}{|\mathbf{r}' - \mathbf{r}_m|} \right]^2 \to {\rm minimize}$$

The charges are subject to the following constraint:

$$\sum_{m} q_{m} = 0$$

Method description.

M generalized charges is found by solving the matrix equation

$$\begin{pmatrix} \mathbf{A} & 0 \\ 0 & 1 \end{pmatrix}^{-1} \cdot \begin{pmatrix} \mathbf{b} \\ 0 \end{pmatrix} = \begin{pmatrix} \mathbf{q} \\ \lambda \end{pmatrix}$$

where the **A** matrix of dimension  $M \times M$  and b} vector or length M are given as

$$A_{mn} = \sum_{i} \frac{1}{r_{im}r_{in}}$$
  $b_m = \sum_{i} \frac{v^{\text{ref}}(\mathbf{r}_m)}{r_{im}}$ 

In the above equation, summations run over all sample points, at which reference potential is known.

Note

# Useful options:

- ESP\_PAD\_SPHERE Padding spherical radius for random points selection. Default: 10.0 [A.U.]
- ESP\_NPOINTS\_PER\_ATOM Number of random points per atom in a molecule. Detault: 1500
- ESP\_VDW\_RADIUS\_C The vdW radius for carbon atom. Default: 3.0 [A.U.]
- ESP\_VDW\_RADIUS\_H The vdW radius for hydrogen atom. Default: 4.0 [A.U.]
- ESP\_VDW\_RADIUS\_N The vdW radius for nitrogen atom. Default: 2.4 [A.U.]
- ESP\_VDW\_RADIUS\_O The vdW radius for oxygen atom. Default: 5 . 6 [A.U.]
- ESP\_VDW\_RADIUS\_F The vdW radius for fluorium atom. Default: 2.3 [A.U.]
- ESP\_VDW\_RADIUS\_CL The vdW radius for chlorium atom. Default: 2.9 [A.U.]

# 17.22.2 Constructor & Destructor Documentation

17.22.2.1 oepdev::ESPSolver::ESPSolver ( SharedScalarField3D field )

Construct from scalar field.

Assume that the centres are on atoms associated with the scalar field.

#### **Parameters**

field	- oepdev scalar field object

17.22.2.2 oepdev::ESPSolver::ESPSolver ( SharedScalarField3D field, psi::SharedMatrix centres )

Construct from scalar field.

Solve ESP equations for a custom set of charge distribution centres.

#### **Parameters**

field	- oepdev scalar field object
centres	- matrix with coordinates of charge distribution centres

The documentation for this class was generated from the following files:

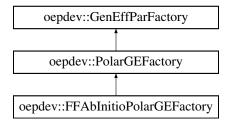
- · oepdev/lib3d/esp.h
- · oepdev/lib3d/esp.cc

# 17.23 oepdev::FFAbInitioPolarGEFactory Class Reference

Polarization GEFP Factory from First Principles: Finite-Difference Model. Arbitrary level of theory.

#include <gefp.h>

Inheritance diagram for oepdev::FFAbInitioPolarGEFactory:



# **Public Member Functions**

- FFAbInitioPolarGEFactory (std::shared\_ptr< psi::Wavefunction > wfn, psi::Options &opt)
- · virtual std::shared ptr

< GenEffPar > compute (void)

Compute the density matrix susceptibility tensors.

#### **Additional Inherited Members**

# 17.23.1 Detailed Description

Polarization GEFP Factory from First Principles: Finite-Difference Model. Arbitrary level of theory.

Implements creation of the density matrix susceptibility tensors. Does not guarantee the idempotency of the density matrix in LCAO-MO variation, but for weak electric fields the idempotency is to be expected up to first order. The density matrix susceptibility tensor is represented by:

$$\delta D_{\alpha\beta} = \mathbf{B}_{\alpha\beta}^{(1)} \cdot \mathbf{F} + \mathbf{B}_{\alpha\beta}^{(2)} : \mathbf{F} \otimes \mathbf{F}$$

where  $\mathbf{B}_{\alpha\beta}^{(1)}$  is the density matrix dipole polarizability defined as

$$\mathbf{B}_{\alpha\beta}^{(1)} = \frac{\partial D_{\alpha\beta}}{\partial \mathbf{F}} \Big|_{\mathbf{F}=\mathbf{0}}$$

whereas  $\mathbf{B}_{\alpha\beta}^{(2)}$  is the density matrix dipole-dipole hyperpolarizability,

$$\mathbf{B}_{\alpha\beta}^{(2)} = \frac{1}{2} \frac{\partial^2 D_{\alpha\beta}}{\partial \mathbf{F} \otimes \partial \mathbf{F}} \Big|_{\mathbf{F} = \mathbf{0}}$$

The first derivative is evaluated numerically from central finite-field 3-point formula,

$$f' = \frac{f(h) - f(-h)}{2h} + \mathfrak{O}(h^2)$$

where h is the differentiation step. Second derivatives are evaluated from the following formulae:

$$f_{uu} = \frac{f(h) + f(-h) - 2f(0)}{h^2} + \mathfrak{O}(h^2)$$

$$f_{uw} = \frac{f(h,h) + f(-h,-h) + 2f(0) - f(h,0) - f(-h,0) - f(0,h) - f(0,-h)}{2h^2} + \mathfrak{O}(h^2)$$

As long as the second-order susceptibility is considered, this susceptibility model works well for uniform weak, moderate and strong electric fields.

The documentation for this class was generated from the following files:

- · oepdev/libgefp/gefp.h
- oepdev/libgefp/gefp\_polar\_ffabinitio.cc

# 17.24 oepdev::Fourier9 Struct Reference

Simple structure to hold the Fourier series expansion coefficients for N=4.

#include <unitary\_optimizer.h>

### **Public Attributes**

- double a0
- double a1
- · double a2
- · double a3
- · double a4
- · double b1
- double b2
- · double b3
- · double b4

### 17.24.1 Detailed Description

Simple structure to hold the Fourier series expansion coefficients for *N*=4.

The documentation for this struct was generated from the following file:

· oepdev/libutil/unitary\_optimizer.h

# 17.25 oepdev::GenEffFrag Class Reference

Generalized Effective Fragment. Container Class.

```
#include <gefp.h>
```

### **Public Member Functions**

• GenEffFrag ()

Initialize with default name of GEFP (Default)

• GenEffFrag (std::string name)

Initialize with custom name of GEFP.

•  $\sim$ GenEffFrag ()

Destruct.

void rotate (std::shared\_ptr< psi::Matrix > R)

Rotate.

void translate (std::shared ptr< psi::Vector > T)

Translate

void superimpose (std::shared\_ptr< psi::Matrix > targetXYZ, std::vector< int > supList)

Superimpose.

void set\_gefp\_polarization (const std::shared\_ptr< GenEffPar > &par)

Set the Density Matrix Susceptibility Tensor Object.

void set\_dmat\_dipole\_polarizability (const std::vector< std::vector< std::shared\_ptr< psi::Matrix >>>
&susc)

Set the Density Matrix Dipole Polarizability.

void set\_dmat\_dipole\_dipole\_hyperpolarizability (const std::vector< std::vector< std::vector< std::shared\_ptr< psi::-</li>
 Matrix >>> &susc)

Set the Density Matrix Dipole-Dipole Hyperpolarizability.

void set\_dmat\_quadrupole\_polarizability (const std::vector< std::vector< std::shared\_ptr< psi::Matrix >>>
&susc)

Set the Density Matrix Quadrupole Polarizability.

std::shared\_ptr< psi::Matrix > susceptibility (int fieldRank, int fieldGradientRank, int i, int x) const

Grab the Density Matrix Susceptibility.

std::vector< std::shared\_ptr</li>

< psi::Matrix > > susceptibility (int fieldRank, int fieldGradientRank, int i) const

Grab the Density Matrix Susceptibility.

- std::vector< std::vector</li>
  - < std::shared\_ptr< psi::Matrix >> > susceptibility (int fieldRank, int fieldGradientRank) const

Grab the Density Matrix Susceptibility.

### **Public Attributes**

 std::map< std::string, std::shared\_ptr< GenEffPar >> parameters

Dictionary of All GEF Parameters.

#### **Protected Attributes**

std::string name

Name of GEFP.

std::shared\_ptr< GenEffPar > densityMatrixSusceptibilityGEF\_

Density Matrix Susceptibility Tensor.

std::shared\_ptr< GenEffPar > electrostaticEnergyGEF\_

Electrostatic Energy Effective One-Electron Potential.

std::shared\_ptr< GenEffPar > repulsionEnergyGEF\_

Exchange-Repulsion Effective One-Electron Potential.

std::shared\_ptr< GenEffPar > chargeTransferEnergyGEF\_

Charge-Transfer Effective One-Electron Potential.

std::shared\_ptr< GenEffPar > EETCouplingConstantGEF\_

EET Coupling Effective One-Electron Potential.

### 17.25.1 Detailed Description

Generalized Effective Fragment. Container Class.

Describes the GEFP fragment that is in principle designed to work at correlated levels of theory.

#### 17.25.2 Member Function Documentation

17.25.2.1 std::shared\_ptr<psi::Matrix> oepdev::GenEffFrag::susceptibility ( int fieldRank, int fieldGradientRank, int i, int x ) const [inline]

Grab the Density Matrix Susceptibility.

### **Parameters**

fieldRank	- power dependency with respect to the electric field
fieldGradient-	- power dependency with respect to the electric field gradient
Rank	
i	- id of the distributed site
X	- id of the composite Cartesian component

17.25.2.2 std::vector<std::shared\_ptr<psi::Matrix>> oepdev::GenEffFrag::susceptibility ( int fieldRank, int fieldGradientRank, int i ) const [inline]

Grab the Density Matrix Susceptibility.

#### **Parameters**

	fieldRank	- power dependency with respect to the electric field
ſ	fieldGradient-	- power dependency with respect to the electric field gradient
	Rank	
Ī	i	- id of the distributed site

17.25.2.3 std::vector<std::shared\_ptr<psi::Matrix>>> oepdev::GenEffFrag::susceptibility ( int fieldRank, int fieldGradientRank ) const [inline]

Grab the Density Matrix Susceptibility.

#### **Parameters**

fieldRank	- power dependency with respect to the electric field
fieldGradient-	- power dependency with respect to the electric field gradient
Rank	

The documentation for this class was generated from the following files:

- oepdev/libgefp/gefp.h
- · oepdev/libgefp/gefp.cc

# 17.26 oepdev::GenEffPar Class Reference

Generalized Effective Fragment Parameters. Container Class.

#include <gefp.h>

# **Public Member Functions**

• GenEffPar (std::string name)

Create with name of this parameter type.

∼GenEffPar ()

Destruct.

void set\_susceptibility (int fieldRank, int fieldGradientRank, const std::vector< std::vector< std::shared\_ptr<
psi::Matrix >>> &susc)

Set the Density Matrix Susceptibility.

- $\bullet \ \ void \ set\_dipole\_polarizability \ (const \ std::vector < std::vector < std::shared\_ptr < psi::Matrix >>> \&susc) \\$ 
  - Set The Density Matrix Dipole Polarizability.
- void set\_dipole\_dipole\_hyperpolarizability (const std::vector< std::vector< std::shared\_ptr< psi::Matrix >>> &susc)

Set The Density Matrix Dipole-Dipole Hyperpolarizability.

void set\_quadrupole\_polarizability (const std::vector< std::vector< std::shared\_ptr< psi::Matrix >>> &susc)

Set The Density Matrix Quadrupole Polarizability.

void set\_centres (const std::vector< std::shared\_ptr< psi::Vector >> &centres)

Set the distributed centres' positions.

· void allocate (int fieldRank, int fieldGradientRank, int nsites, int nbf)

Allocate the Density Matrix Susceptibility.

void allocate\_dipole\_polarizability (int nsites, int nbf)

Allocate The Density Matrix Dipole Polarizability.

void allocate\_dipole\_dipole\_hyperpolarizability (int nsites, int nbf)

Allocate The Density Matrix Dipole-Dipole Hyperpolarizability.

void allocate\_quadrupole\_polarizability (int nsites, int nbf)

Allocate The Density Matrix Quadrupole Polarizability.

- bool hasDensityMatrixDipolePolarizability () const
- bool hasDensityMatrixDipoleDipoleHyperpolarizability () const
- bool hasDensityMatrixQuadrupolePolarizability () const
- std::shared\_ptr< psi::Matrix > susceptibility (int fieldRank, int fieldGradientRank, int i, int x) const

Grab the Density Matrix Susceptibility.

- · std::vector< std::shared ptr
  - < psi::Matrix > > susceptibility (int fieldRank, int fieldGradientRank, int i) const

Grab the Density Matrix Susceptibility.

- std::vector< std::vector</li>
  - < std::shared\_ptr< psi::Matrix >> > susceptibility (int fieldRank, int fieldGradientRank) const

Grab the Density Matrix Susceptibility.

- std::vector< std::vector</li>
  - < std::shared\_ptr< psi::Matrix >> > dipole\_polarizability () const

Grab the density matrix dipole polarizability tensor.

- std::vector< std::shared ptr
  - < psi::Matrix > > dipole polarizability (int i) const

Grab the density matrix dipole polarizability tensor's x-th component.

std::shared\_ptr< psi::Matrix > dipole\_polarizability (int i, int x) const

Grab the density matrix dipole polarizability tensor's x-th component of the i-th distributed site.

- std::vector< std::vector</li>
  - < std::shared\_ptr< psi::Matrix >> > dipole\_dipole\_hyperpolarizability () const

Grab the density matrix dipole-dipole hyperpolarizability tensor.

- std::vector< std::shared ptr</li>
  - < psi::Matrix > > dipole\_dipole\_hyperpolarizability (int i) const

Grab the density matrix dipole-dipole hyperpolarizability tensor's x-th component.

• std::shared\_ptr< psi::Matrix > dipole\_dipole\_hyperpolarizability (int i, int x) const

Grab the density matrix dipole-dipole hyperpolarizability tensor's x-th component of the i-th distributed site.

- std::vector< std::vector</li>
  - < std::shared\_ptr< psi::Matrix > > quadrupole\_polarizability () const

Grab the density matrix quadrupole polarizability tensor.

- std::vector< std::shared\_ptr</li>
  - < psi::Matrix > > quadrupole polarizability (int i) const

Grab the density matrix quadrupole polarizability tensor's x-th component.

std::shared\_ptr< psi::Matrix > quadrupole\_polarizability (int i, int x) const

Grab the density matrix quadrupole polarizability tensor's x-th component of the i-th distributed site.

- std::vector< std::shared ptr</li>
  - < psi::Vector > > centres () const

Grab the centres' positions.

• std::shared\_ptr< psi::Vector > centre (int i) const

Grab the position of the i-th distributed site.

• std::shared\_ptr< psi::Matrix > compute\_density\_matrix (std::shared\_ptr< psi::Vector > field)

Compute the density matrix due to the uniform electric field perturbation.

• std::shared\_ptr< psi::Matrix > compute\_density\_matrix (double fx, double fy, double fz)

Compute the density matrix due to the uniform electric field perturbation.

std::shared\_ptr< psi::Matrix > compute\_density\_matrix (std::vector< std::shared\_ptr< psi::Vector >> fields)

Compute the density matrix due to the non-uniform electric field perturbation.

 std::shared\_ptr< psi::Matrix > compute\_density\_matrix (std::vector< std::shared\_ptr< psi::Vector >> fields, std::vector< std::shared\_ptr< psi::Matrix >> grads)

Compute the density matrix due to the non-uniform electric field perturbation.

### **Protected Attributes**

std::string name

The Name of Parameter Type.

- std::vector< std::vector</li>
  - < std::shared\_ptr< psi::Matrix >> > densityMatrixDipolePolarizability\_

The Density Matrix Dipole Polarizability.

- std::vector< std::vector</li>
  - < std::shared\_ptr< psi::Matrix >> > densityMatrixDipoleDipoleHyperpolarizability\_

The Density Matrix Dipole-Dipole Hyperpolarizability.

- std::vector< std::vector</li>
  - < std::shared\_ptr< psi::Matrix >> > densityMatrixQuadrupolePolarizability\_

The Density Matrix Quadrupole Polarizability.

- std::vector< std::shared ptr
  - < psi::Vector > > distributedCentres\_

The Positions of the Distributed Centres.

- bool hasDensityMatrixDipolePolarizability\_
- bool hasDensityMatrixDipoleDipoleHyperpolarizability\_
- bool hasDensityMatrixQuadrupolePolarizability

### 17.26.1 Detailed Description

Generalized Effective Fragment Parameters. Container Class.

### 17.26.2 Member Function Documentation

17.26.2.1 void oepdev::GenEffPar::allocate ( int fieldRank, int fieldGradientRank, int nsites, int nbf ) [inline]

Allocate the Density Matrix Susceptibility.

#### **Parameters**

fieldRank	- power dependency with respect to the electric field ${f F}$
fieldGradient-	- power dependency with respect to the electric field gradient $ abla\otimes \mathbf{F}$
Rank	
nsites	- number of distributed sites
nbf	- number of basis functions in the basis set

The following susceptibilities are supported (fieldRank, fieldGradientRank):

- (1,0) dipole polarizability, interacts with  ${\bf F}$
- (2, 0) dipole-dipole hyperpolarizability, interacts with  $F \otimes F$
- (0, 1) quadrupole polarizability, interacts with  $\nabla \otimes F$

17.26.2.2 std::shared\_ptr< psi::Matrix > oepdev::GenEffPar::compute\_density\_matrix ( std::shared\_ptr< psi::Vector > field )

Compute the density matrix due to the uniform electric field perturbation.

**Parameters** 

-		
	field	- the uniform electric field vector (A.U.)

17.26.2.3 std::shared\_ptr< psi::Matrix > oepdev::GenEffPar::compute\_density\_matrix ( double fx, double fy, double fz )

Compute the density matrix due to the uniform electric field perturbation.

#### **Parameters**

fx	- x-th Cartesian component of the uniform electric field vector (A.U.)
fy	- y-th Cartesian component of the uniform electric field vector (A.U.)
fz	- z-th Cartesian component of the uniform electric field vector (A.U.)

17.26.2.4 std::shared\_ptr< psi::Matrix > oepdev::GenEffPar::compute\_density\_matrix ( std::vector< std::shared\_ptr< psi::Vector >> fields )

Compute the density matrix due to the non-uniform electric field perturbation.

#### **Parameters**

fields	- the list of non-uniform electric field vector (A.U.) evaluated at the distributed DMatPol sites

17.26.2.5 std::shared\_ptr< psi::Matrix > oepdev::GenEffPar::compute\_density\_matrix ( std::vector< std::shared\_ptr< psi::Vector >> fields, std::vector< std::shared\_ptr< psi::Matrix >> grads )

Compute the density matrix due to the non-uniform electric field perturbation.

### **Parameters**

fields	- the list of electric field vectors (A.U.) evaluated at the distributed DMatPol sites
grads	- the list of electric field gradient matrices (A.U.) evaluated at the distributed DMatPol sites

17.26.2.6 void oepdev::GenEffPar::set\_susceptibility ( int *fieldRank*, int *fieldGradientRank*, const std::vector< std::vector< std::shared\_ptr< psi::Matrix >>> & susc ) [inline]

Set the Density Matrix Susceptibility.

### **Parameters**

	fieldRank	- power dependency with respect to the electric field ${f F}$
	fieldGradient-	- power dependency with respect to the electric field gradient $ abla\otimes \mathbf{F}$
	Rank	
Ì	susc	- the susceptibility tensor

The following susceptibilities are supported (fieldRank, fieldGradientRank):

- (1,0) dipole polarizability, interacts with  ${\bf F}$
- (2, 0) dipole-dipole hyperpolarizability, interacts with  $F \otimes F$
- (0, 1) quadrupole polarizability, interacts with  $\nabla \otimes F$
- 17.26.2.7 std::shared\_ptr<psi::Matrix> oepdev::GenEffPar::susceptibility ( int fieldRank, int fieldGradientRank, int i, int x ) const [inline]

Grab the Density Matrix Susceptibility.

#### **Parameters**

fieldRank	- power dependency with respect to the electric field
fieldGradient-	- power dependency with respect to the electric field gradient
Rank	
i	- id of the distributed site
X	- id of the composite Cartesian component

The following susceptibilities are supported (fieldRank, fieldGradientRank):

- (1, 0) dipole polarizability, interacts with F
- (2, 0) dipole-dipole hyperpolarizability, interacts with  $F \otimes F$
- (0, 1) quadrupole polarizability, interacts with  $\nabla \otimes \mathbf{F}$

The distributed sites are assumed to be atomic sites or molecular orbital centroids (depending on the polarization factory used). For the electric field, the composite Cartesian index is just an ordinary Cartesian index. For the electric field gradient and electric field squared, the composite Cartesian index is given as

$$I(x, y) = 3x + y$$

where the values of 0, 1 and 2 correspond to *x*, *y* and *z* Cartesian components, respectively. Therefore, in the latter case, there is 9 distinct composite Cartesian components.

17.26.2.8 std::vector<std::shared\_ptr<psi::Matrix>> oepdev::GenEffPar::susceptibility ( int fieldRank, int fieldGradientRank, int i ) const [inline]

Grab the Density Matrix Susceptibility.

#### **Parameters**

fieldRank	- power dependency with respect to the electric field
fieldGradient-	- power dependency with respect to the electric field gradient
Rank	
i	- id of the distributed site

The following susceptibilities are supported (fieldRank, fieldGradientRank):

- (1, 0) dipole polarizability, interacts with F
- (2, 0) dipole-dipole hyperpolarizability, interacts with  $F \otimes F$
- (0, 1) quadrupole polarizability, interacts with  $\nabla \otimes \mathbf{F}$

The distributed sites are assumed to be atomic sites or molecular orbital centroids (depending on the polarization factory used).

17.26.2.9 std::vector<std::vector<std::shared\_ptr<psi::Matrix>>> oepdev::GenEffPar::susceptibility ( int fieldRank, int fieldGradientRank ) const [inline]

Grab the Density Matrix Susceptibility.

### **Parameters**

fieldRank	- power dependency with respect to the electric field
fieldGradient-	- power dependency with respect to the electric field gradient
Rank	

The following susceptibilities are supported (fieldRank, fieldGradientRank):

• (1, 0) - dipole polarizability, interacts with F

- (2, 0) dipole-dipole hyperpolarizability, interacts with  ${f F}\otimes {f F}$
- (0, 1) quadrupole polarizability, interacts with  $\nabla \otimes \mathbf{F}$

The documentation for this class was generated from the following files:

- oepdev/libgefp/gefp.h
- · oepdev/libgefp/gefp.cc

# 17.27 oepdev::GenEffParFactory Class Reference

Generalized Effective Fragment Factory. Abstract Base.

```
#include <gefp.h>
```

Inheritance diagram for oepdev::GenEffParFactory:



### **Public Member Functions**

GenEffParFactory (std::shared\_ptr< psi::Wavefunction > wfn, psi::Options &opt)

Construct from wavefunction and Psi4 options.

virtual ~GenEffParFactory ()

Destruct.

- · virtual std::shared ptr
  - < GenEffPar > compute (void)=0

Compute the fragment parameters.

- virtual std::shared\_ptr
  - < psi::Wavefunction > wfn (void) const

Grab wavefunction.

• virtual psi::Options & options (void) const

Grab options.

- std::shared\_ptr<  $\ensuremath{\mathsf{CPHF}}\xspace > \ensuremath{\mathsf{cphf\_solver}}\xspace$  () const

Grab the CPHF object.

# **Static Public Member Functions**

static std::shared\_ptr

< GenEffParFactory > build (const std::string &type, std::shared\_ptr< psi::Wavefunction > wfn, psi::Options &opt)

Build Density Matrix Susceptibility Generalized Factory.

#### **Protected Member Functions**

• virtual double random double ()

Draw random number.

· virtual std::shared\_ptr

< psi::Vector > draw\_random\_point ()

Draw random point in 3D space, excluding the vdW region.

• virtual bool is\_in\_vdWsphere (double x, double y, double z) const

Is the point inside a vdW region?

### **Protected Attributes**

· std::shared ptr

< psi::Wavefunction > wfn\_

Wavefunction.

psi::Options & options\_

Psi4 Options.

std::default\_random\_engine\_randomNumberGenerator

Random number generators.

• std::uniform\_real\_distribution

< double > randomDistribution\_

std::shared\_ptr< psi::Matrix > excludeSpheres\_

Matrix with vdW sphere information.

std::map< std::string, double > vdwRadius\_

Map with vdW radii.

double cx

Centre-of-mass coordinates.

- double cy
- double cz
- double radius

Radius of padding sphere around the molecule.

const int nbf

Number of basis functions.

std::shared\_ptr< CPHF > cphfSolver\_

The CPHF object.

· std::shared\_ptr

 $< {\tt oepdev::} GenEffParFactory > {\tt abInitioPolarizationSusceptibilitiesFactory}\_$ 

Ab initio polarization susceptibility factory.

### 17.27.1 Detailed Description

Generalized Effective Fragment Factory. Abstract Base.

Describes the GEFP fragment that is in principle designed to work at correlated levels of theory.

### 17.27.2 Member Function Documentation

```
17.27.2.1 std::shared_ptr< oepdev::GenEffParFactory > oepdev::GenEffParFactory::build ( const std::string & type, std::shared_ptr< psi::Wavefunction > wfn, psi::Options & opt ) [static]
```

Build Density Matrix Susceptibility Generalized Factory.

### **Parameters**

type	- Type of factory
wfn	- Psi4 wavefunction
opt	- Psi4 options

### Available factory types:

• POLARIZATION - creates the polarization generalized effective fragment parameters' factory Factory subtype is specified in Psi4 options (input file).

Note

### Useful options:

- POLARIZATION factory type:
  - DMATPOL\_TRAINING\_MODE training mode. Default: EFIELD
  - DMATPOL\_NSAMPLES number of random samples (field or test charges sets). Default: 30
  - DMATPOL\_FIELD\_SCALE electric field scale factor (relevant if training mode is EFIELD).
     Default: 0.01 [au]
  - DMATPOL\_NTEST\_CHARGE number of test charges per sample (relevant if training mode is CHARGES). Default: 1
  - DMATPOL\_TEST\_CHARGE test charge value (relevant if training mode is CHARGES). Default:
     0.001 [au]
  - DMATPOL\_FIELD\_RANK electric field rank. Default: 1
  - DMATPOL\_GRADIENT\_RANK electric field gradient rank. Default: 0
  - DMATPOL\_TEST\_FIELD\_X test electric field in X direction. Default: 0.000 [au]
  - DMATPOL\_TEST\_FIELD\_Y test electric field in Y direction. Default: 0.000 [au]
  - DMATPOL\_TEST\_FIELD\_Z test electric field in Z direction. Default: 0.008 [au]
  - DMATPOL\_OUT\_STATS output file name for statistical evaluation results. Default: dmatpol. stats.dat
  - DMATPOL\_DO\_AB\_INITIO compute ab initio susceptibilities and evaluate statistics for it.
     Default: false
  - DMATPOL\_OUT\_STATS\_AB\_INITIO output file name for statistical evaluation results of ab initio model. Default: dmatpol.stats.abinitio.dat

The documentation for this class was generated from the following files:

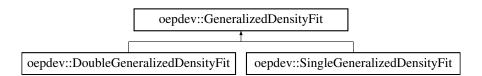
- · oepdev/libgefp/gefp.h
- oepdev/libgefp/gefp.cc

# 17.28 oepdev::GeneralizedDensityFit Class Reference

Generalized Density Fitting Scheme. Abstract Base.

#include <oep\_gdf.h>

Inheritance diagram for oepdev::GeneralizedDensityFit:



### **Public Member Functions**

GeneralizedDensityFit ()

Constructor. Initializes the pointers.

virtual ∼GeneralizedDensityFit ()

Destructor.

· virtual std::shared ptr

< psi::Matrix > compute (void)=0

Perform the generalized density fit.

std::shared\_ptr< psi::Matrix > G (void) const

Extract the  $G_{\xi_i}$  coefficients.

### **Static Public Member Functions**

```
· static std::shared ptr
```

< GeneralizedDensityFit > build (std::shared\_ptr< psi::BasisSet > bs\_auxiliary, std::shared\_ptr< psi::Matrix > v vector)

Factory for Single GDF Computer.

· static std::shared ptr

< GeneralizedDensityFit > build (std::shared\_ptr< psi::BasisSet > bs\_auxiliary, std::shared\_ptr< psi::BasisSet > bs\_intermediate, std::shared\_ptr< psi::Matrix > v\_vector)

Factory for Double GDF Computer.

#### **Protected Member Functions**

void invert\_matrix (std::shared\_ptr< psi::Matrix > &M)

Invert a square matrix and check if the inverse is acceptable.

### **Protected Attributes**

```
    std::shared_ptr< psi::Matrix > G_
```

The OEP coefficients  $G_{\mathcal{E}_i}$ .

std::shared\_ptr< psi::Matrix > H\_

The intermediate DF coefficients for  $\hat{v}|i\rangle$ .

std::shared\_ptr< psi::Matrix > V\_

The V matrix  $(\xi | \hat{v}i)$ .

int n\_a\_

Number of auxiliary basis set functions.

• int n i

Number of intermediate basis set functions.

• int n o

Number of OEP's.

•  $std::shared\_ptr < psi::BasisSet > bs\_a\_$ 

Basis set: auxiliary.

std::shared\_ptr< psi::BasisSet > bs\_i\_

Basis set: intermediate.

std::shared\_ptr

< oepdev::IntegralFactory > ints\_aa\_

Integral factory: aux - aux.

· std::shared ptr

< oepdev::IntegralFactory > ints\_ai\_

Integral factory: aux - int.

std::shared\_ptr

< oepdev::IntegralFactory > ints\_ii\_

Integral factory: int - int.

#### 17.28.1 Detailed Description

Generalized Density Fitting Scheme. Abstract Base.

Performs the following map:

$$\hat{v}|i)\cong\sum_{m{\eta}}G_{m{\eta}i}|m{\eta})$$

where  $\hat{v}$  is the effective one-electron potential (OEP) operator,  $|i\rangle$  is an arbitrary state vector and  $|\eta\rangle$  is an auxiliary basis vector. The coefficients  $G_{\eta i}$  are stored and define the OEP acting on the state i. The mapping onto the auxiliary space can be done in two ways:

- Single Density Fit. This method requires the auxiliary basis set to be nearly complete.
- Double Density Fit. This method can be used to arbitrary auxiliary basis sets.

#### 17.28.2 Member Function Documentation

17.28.2.1 std::shared\_ptr< GeneralizedDensityFit > GeneralizedDensityFit::build ( std::shared\_ptr< psi::BasisSet >  $bs_auxiliary$ , std::shared\_ptr< psi::Matrix >  $v_vector$  ) [static]

Factory for Single GDF Computer.

#### **Parameters**

bs_auxiliary	- auxiliary basis set
v_vector	- the matrix with $V_{\xi_i}$ elements

#### Returns

Generalized Density Fit Computer.

```
17.28.2.2 std::shared_ptr< GeneralizedDensityFit > GeneralizedDensityFit::build ( std::shared_ptr< psi::BasisSet > bs_auxiliary, std::shared_ptr< psi::BasisSet > bs_intermediate, std::shared_ptr< psi::Matrix > v_ivector ) [ static]
```

Factory for Double GDF Computer.

#### **Parameters**

bs_auxiliary	- auxiliary basis set
bs_intermediate	- intermediate basis set
v_vector	- the matrix with $V_{arepsilon i}$ elements

### Returns

Generalized Density Fit Computer.

```
17.28.2.3 std::shared_ptr< psi::Matrix > GeneralizedDensityFit::compute( void ) [pure virtual]
```

Perform the generalized density fit.

### Returns

The OEP coefficients  $G_{\xi_i}$ 

 $Implemented\ in\ oepdev:: Double Generalized Density Fit,\ and\ oepdev:: Single Generalized Density Fit.$ 

The documentation for this class was generated from the following files:

- oepdev/liboep/oep\_gdf.h
- · oepdev/liboep/oep\_gdf.cc

# 17.29 oepdev::GeneralizedPolarGEFactory Class Reference

Polarization GEFP Factory with Least-Squares Parameterization.

```
#include <gefp.h>
```

Inheritance diagram for oepdev::GeneralizedPolarGEFactory:



### Classes

struct StatisticalSet

A structure to handle statistical data.

### **Public Member Functions**

GeneralizedPolarGEFactory (std::shared ptr< psi::Wavefunction > wfn, psi::Options &opt)

Construct from Psi4 wavefunction and options.

virtual ∼GeneralizedPolarGEFactory ()

Destruct.

virtual std::shared ptr

< GenEffPar > compute (void)

Pefrorm Least-Squares Fit.

· bool has\_dipole\_polarizability () const

Dipole Polarizability (interacting with F)

• bool has\_dipole\_dipole\_hyperpolarizability () const

Dipole-Dipole Hyperpolarizability (interacting with  $\mathbf{F}^2$ )

• bool has\_quadrupole\_polarizability () const

Quadrupole Polarizability (interacting with  $\nabla \otimes \mathbf{F}$ )

bool has\_ab\_initio\_dipole\_polarizability () const

Ab Initio Dipole Polarizability (interacting with F)

· double Zinit () const

Grab initial summaric Z value.

double Z () const

Grab final summaric Z value.

### **Protected Member Functions**

void allocate (void)

Allocate memory.

void invert\_hessian (void)

Invert Hessian (do also the identity test)

• void compute\_electric\_field\_sums (void)

Compute electric field sum set.

void compute\_electric\_field\_gradient\_sums (void)

Compute electric field gradient sum set.

• void compute\_statistics (void)

Run the statistical evaluation of results.

void set\_distributed\_centres (void)

Set the distributed centres.

· void compute parameters (void)

Compute the parameters.

void fit (void)

Perform least-squares fit.

void compute\_ab\_initio (void)

Compute ab initio parameters.

• void save (int i, int j)

Save susceptibility tensors associated with the i-th and j-th basis set function.

virtual void compute\_samples (void)=0

Compute samples of density matrices and select electric field distributions.

virtual void compute gradient (int i, int j)=0

Compute Gradient vector associated with the i-th and j-th basis set function.

virtual void compute\_hessian (void)=0

Compute Hessian matrix (independent on the parameters)

#### **Protected Attributes**

· int nBlocks\_

Number of parameter blocks.

int nSites

Number of distributed sites.

int nSitesAbInitio

Number of distributed sites of Ab Initio model (FF - single site (com); distributed: LMO sites)

int nParameters

Dimensionality of entire parameter space.

std::vector< int > nParametersBlock

Dimensionality of parameter space per block.

const int nSamples\_

Number of statistical samples.

const double symmetryNumber\_ [6]

Symmetry number for matrix susceptibilities.

std::shared\_ptr< psi::Matrix > Gradient\_

Gradient.

std::shared\_ptr< psi::Matrix > Hessian\_

Hessian.

std::shared\_ptr< psi::Matrix > Parameters\_

Parameters.

std::shared\_ptr

< oepdev::GenEffPar > PolarizationSusceptibilities\_

Density Matrix Susceptibility Tensors Object.

· std::shared ptr

< oepdev::GenEffPar > abInitioPolarizationSusceptibilities\_

Density Matrix Susceptibility Tensors Object for Ab Initio Model.

· bool hasDipolePolarizability\_

Has Dipole Polarizability?

bool hasDipoleDipoleHyperpolarizability\_

Has Dipole-Dipole Hyperpolarizability?

bool hasQuadrupolePolarizability

Has Quadrupole Polarizability?

bool hasAbInitioDipolePolarizability\_

Has Ab Initio Dipole Polarizability?

StatisticalSet referenceStatisticalSet

Reference statistical data.

• StatisticalSet referenceDpolStatisticalSet\_

Multipole reference statistical data.

StatisticalSet modelStatisticalSet\_

Model statistical data.

StatisticalSet abInitioModelStatisticalSet

Ab Initio Model statistical data.

- std::vector< std::shared\_ptr
  - < psi::Matrix > > VMatrixSet

Potential matrix set.

- std::vector< std::vector</li>
  - < std::shared\_ptr< Vector >> > electricFieldSet\_

Electric field set.

- std::vector< std::vector</li>
  - < std::shared\_ptr< Matrix >> > electricFieldGradientSet\_

Electric field gradient set.

- std::vector< std::vector</li>
  - < double > > electricFieldSumSet

Electric field sum set.

- std::vector< std::vector</li>
  - < std::shared\_ptr< psi::Vector >> > electricFieldGradientSumSet\_

Electric field gradient sum set.

- std::vector< std::vector</li>
  - < std::shared\_ptr< Vector >> > abInitioModelElectricFieldSet\_

Electric field set for Ab Initio Model (LMO-distributed)

const double mField

Level shifters for Hessian blocks.

double Zinit

Initial summaric Z value.

double Z\_

Final summaric Z value.

std::shared\_ptr< psi::JK > jk\_

Computer of generalized JK objects.

### **Additional Inherited Members**

## 17.29.1 Detailed Description

Polarization GEFP Factory with Least-Squares Parameterization.

Implements a general class of methods for the density matrix susceptibility tensors represented by:

$$\delta D_{\alpha\beta} = \sum_{i} \left\{ \mathbf{B}_{i;\alpha\beta}^{(10)} \cdot \mathbf{F}(\mathbf{r}_{i}) + \mathbf{B}_{i;\alpha\beta}^{(20)} : \mathbf{F}(\mathbf{r}_{i}) \otimes \mathbf{F}(\mathbf{r}_{i}) + \mathbf{B}_{i;\alpha\beta}^{(01)} : \nabla_{i} \otimes \mathbf{F}(\mathbf{r}_{i}) + \ldots \right\}$$

where:

- $\mathbf{B}_{i;lphaeta}^{(10)}$  is the density matrix dipole polarizability
- ${f B}^{(20)}_{i:lphaeta}$  is the density matrix dipole-dipole hyperpolarizability
- $\mathbf{B}_{i:\alpha\beta}^{(01)}$  is the density matrix quadrupole polarizability

all defined for the generalized distributed site at  $\mathbf{r}_i$ .

Available models:

- 1. Training against uniform electric fields
  - · oepdev::LinearUniformEFieldPolarGEFactory linear with respect to electric field
  - oepdev::QuadraticUniformEFieldPolarGEFactory quadratic with respect to electric field
- 2. Training against non-uniform electric fields
  - oepdev::LinearNonUniformEFieldPolarGEFactory linear with respect to electric field, distributed site model
  - oepdev::QuadraticNonUniformEFieldPolarGEFactory quadratic with respect to electric field, distributed site model
  - oepdev::LinearGradientNonUniformEFieldPolarGEFactory linear with respect to electric field and linear with respect to electric field gradient, distributed site model. This model does not function now.
  - oepdev::QuadraticGradientNonUniformEFieldPolarGEFactory linear with respect to electric field and linear with respect to electric field gradient, distributed site model. This model does not function now.

For the non-linear field training, a set of point charges in each training sample is assumed. Distributed models use atomic centers as expansion points.

Determination of the generalized susceptibilities

Let  $\left\{\mathbf{F}^{(1)}(\mathbf{r}), \mathbf{F}^{(2)}(\mathbf{r}), \dots, \mathbf{F}^{(N)}(\mathbf{r}), \dots\right\}$  be a set of  $N_{\text{max}}$  distinct and randomly sampled spatial distributions of electric field. It is assumed that the exact difference one-particle density matrices (with respect to the unperturbed state) defined as

 $\delta \overline{\mathbf{D}}^{(N)} \equiv \overline{\mathbf{D}}^{(N)} - \overline{\mathbf{D}}^{(0)}$ 

are known for each sample (overline symbolizes the exact estimate). Now, for each pair of the AO indices the following parameterization is constructed:

$$\delta D^{(N)} = \sum_{i}^{M} \left\{ \sum_{u}^{x,y,z} s_{iu}^{[1]} F_{iu}^{(N)} + \sum_{u}^{x,y,z} \sum_{w < u} r_{uw} s_{iuw}^{[2]} F_{iu}^{(N)} F_{iw}^{(N)} + \dots \right\}$$

(the Greek subscripts were omitted here for notational simplicity). In the above equation,  $B_u^{(i;1)} = s_{iu}^{[1]}$  and  $B_{uw}^{(i;2)} = r_{uw} s_{iuw}^{[2]}$ , where  $r_{uw}$  is the symmetry factor equal to 1 for diagonal elements and 2 for off-diagonal elements of  $B_{uw}^{(i;2)}$ . The multiple parameter blocks ( $\mathbf{s}^{[1]}$ ,  $\mathbf{s}^{[2]}$  and so on) appear in the first power, allowing for linear least-squares regression. The square bracket superscripts denote the block of the parameter space.

To determine the optimum set,  $\mathbf{s} = \begin{pmatrix} \mathbf{s}^{[1]} & \mathbf{s}^{[2]} & \cdots \end{pmatrix}^T$ , a loss function Z that is subject to the least-squares minimization, is defined as

$$Z(\mathbf{s}) = \sum_{N}^{N_{\mathrm{max}}} \left( \delta D^{(N)} - \delta \overline{D}^{(N)} \right)^2 \,.$$

The Hessian of Z computed with respect to the parameters is parameter-independent (constant) and generally non-singular as long as the electric fields on all distributed sites are different. Therefore, the exact solution for the optimal parameters is given by the Newton equation

$$\mathbf{s} = -\mathbf{H}^{-1} \cdot \mathbf{g}$$

where  $\mathbf{g}$  and  $\mathbf{H}$  are the gradient vector and the Hessian matrix, respectively. Note that in this case the dimensions of parameter space for the block 1 and 2 are equal to 3M and 6M, respectively. The explicit forms of the gradient and Hessian up to second-order are given in the next section.

Explicit Formulae for Gradient and Hessian Blocks in Linear Regression DMS Model

The gradient vector  $\mathbf{g}$  and the Hessian matrix  $\mathbf{H}$  are built from blocks associated with a particular type of parameters, i.e.,

$$\mathbf{g} = \begin{pmatrix} \mathbf{g}^{[1]} \\ \mathbf{g}^{[2]} \end{pmatrix}, \quad \mathbf{H} = \begin{pmatrix} \mathbf{H}^{[11]} & \mathbf{H}^{[12]} \\ \mathbf{H}^{[21]} & \mathbf{H}^{[22]} \end{pmatrix} \,,$$

where the block indices 1 and 2 correspond to the first- and second-order susceptibilities, respectively. Note that the second derivatives of  $\delta D^{(N)}$  with respect to the adjustable parameters vanish due to the linear functional form of

the parameterization formula given in the previous section. Thus, the gradient element of the r-th block and Hessian element of the (rs)-th block read

$$\begin{split} g^{[r]} &\equiv \frac{\partial Z}{\partial s^{[r]}} = -2 \sum_{N} \overline{\delta D}^{(N)} \frac{\partial \left[ \delta D^{(N)} \right]}{\partial s^{[r]}} \;, \\ H^{[rs]} &\equiv \frac{\partial^{2} Z}{\partial s^{[r]} \partial s^{[s]}} = 2 \sum_{N} \frac{\partial \left[ \delta D^{(N)} \right]}{\partial s^{[r]}} \frac{\partial \left[ \delta D^{(N)} \right]}{\partial s^{[s]}} \;. \end{split}$$

The explicit formulae for the gradient are

$$\begin{split} g_{ku}^{[1]} &= -2 \sum_{N} \overline{\delta D}^{(N)} F_{ku}^{(N)} \;, \\ g_{kuw}^{[2]} &= -2 r_{uw} \sum_{N} \overline{\delta D}^{(N)} F_{ku}^{(N)} F_{kw}^{(N)} \;. \end{split}$$

The Hessian subsequently follows to be %

$$\begin{split} H_{ku,lw}^{[11]} &= 2 \sum_{N} F_{ku}^{(N)} F_{lw}^{(N)} \;, \\ H_{ku,lu'w'}^{[12]} &= 2 r_{u'w'} \sum_{N} F_{ku}^{(N)} F_{lu'}^{(N)} F_{lw'}^{(N)} \;, \\ H_{kuw,lu'w'}^{[22]} &= 2 r_{uw} r_{u'w'} \sum_{N} F_{ku}^{(N)} F_{kw}^{(N)} F_{lu'}^{(N)} F_{lw'}^{(N)} \;. \end{split}$$

Note that due to the symmetry of the Hessian matrix, the block 21 is a transpose of the block 12. The composite indices ku and kuw are constructed from the distributed site index k and the appropriate symmetry-adapted (w < u) Cartesian component of a particular DMS tensor: u for the first-order, and uw for the second-order susceptibility tensor, respectively. The method described above can be easily extended to third and higher orders.

The documentation for this class was generated from the following files:

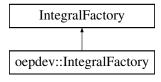
- oepdev/libgefp/gefp.h
- · oepdev/libgefp/gefp polar base.cc

## 17.30 oepdev::IntegralFactory Class Reference

Extended IntegralFactory for computing integrals.

#include <integral.h>

Inheritance diagram for oepdev::IntegralFactory:



#### **Public Member Functions**

IntegralFactory (std::shared\_ptr< psi::BasisSet > bs1, std::shared\_ptr< psi::BasisSet > bs2, std::shared\_ptr< psi::BasisSet > bs3, std::shared\_ptr< psi::BasisSet > bs4)

Initialize integral factory given a BasisSet for each center. Becomes (bs1 bs2 | bs3 bs4).

 $\bullet \ \, \textbf{IntegralFactory} \ \, (\textbf{std}::\textbf{shared\_ptr} < \ \, \textbf{psi}::\textbf{BasisSet} > \textbf{bs1}, \, \textbf{std}::\textbf{shared\_ptr} < \ \, \textbf{psi}::\textbf{BasisSet} > \textbf{bs2}) \\$ 

Initialize integral factory given a BasisSet for two centres. Becomes (bs1 bs2 | bs1 bs2).

```
    IntegralFactory (std::shared_ptr< psi::BasisSet > bs1)
        Initialize integral factory given a BasisSet for two centres. Becomes (bs1 bs1 | bs1 bs1).
    virtual ~IntegralFactory ()
        Destructor.
    virtual oepdev::TwoBodyAOInt * eri_1_1 (int deriv=0, bool use_shell_pairs=false)
        Returns an ERI_1_1 integral object.
    virtual oepdev::TwoBodyAOInt * eri_2_1 (int deriv=0, bool use_shell_pairs=false)
        Returns an ERI_2_1 integral object.
    virtual oepdev::TwoBodyAOInt * eri_2_2 (int deriv=0, bool use_shell_pairs=false)
        Returns an ERI_2_2 integral object.
    virtual oepdev::TwoBodyAOInt * eri_3_1 (int deriv=0, bool use_shell_pairs=false)
        Returns an ERI_3_1 integral object.
```

### 17.30.1 Detailed Description

Extended IntegralFactory for computing integrals.

In addition to integrals available in Psi4, oepdev::IntegralFactory enables to compute also:

- OEl's:
  - none at that moment
- ERI's:

```
integrals of type (a|b) - oepdev::ERI_1_1
integrals of type (ab|c) - oepdev::ERI_2_1
integrals of type (abc|d) - oepdev::ERI_3_1
integrals of type (ab|cd) - oepdev::ERI_2_2 (also in Psi4 as psi::ERI)
```

The documentation for this class was generated from the following files:

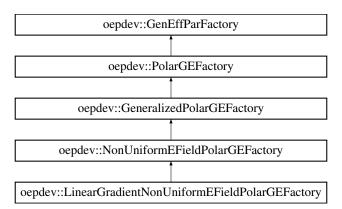
- oepdev/libpsi/integral.h
- · oepdev/libpsi/integral.cc

# 17.31 oepdev::LinearGradientNonUniformEFieldPolarGEFactory Class Reference

Polarization GEFP Factory with Least-Squares Parameterization.

```
#include <gefp.h>
```

Inheritance diagram for oepdev::LinearGradientNonUniformEFieldPolarGEFactory:



### **Public Member Functions**

• LinearGradientNonUniformEFieldPolarGEFactory (std::shared\_ptr< psi::Wavefunction > wfn, psi::Options & opt)

void compute\_gradient (int i, int j)

Compute Gradient vector associated with the i-th and j-th basis set function.

void compute\_hessian (void)

Compute Hessian matrix (independent on the parameters)

### **Additional Inherited Members**

### 17.31.1 Detailed Description

Polarization GEFP Factory with Least-Squares Parameterization.

Implements the generalized density matrix susceptibility model of the form

$$\delta D_{lphaeta}pprox\sum_{i}\left\{\mathbf{B}_{i;lphaeta}^{(10)}\cdot\mathbf{F}(\mathbf{r}_{i})+\mathbf{B}_{i;lphaeta}^{(01)}:
abla_{i}\otimes\mathbf{F}(\mathbf{r}_{i})
ight\}$$

where:

- ${f B}_{i;\alpha\beta}^{(10)}$  is the density matrix dipole polarizability
- $\mathbf{B}_{i:\alpha\beta}^{(01)}$  is the density matrix quadrupole polarizability all defined for the distributed site at  $\mathbf{r}_i$ .

Note

This model is not available now and probably will be deprecated in the future.

The documentation for this class was generated from the following files:

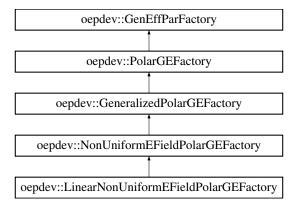
- · oepdev/libgefp/gefp.h
- oepdev/libgefp/gefp\_polar\_nonuniform\_field\_1\_grad\_1.cc

# 17.32 oepdev::LinearNonUniformEFieldPolarGEFactory Class Reference

Polarization GEFP Factory with Least-Squares Parameterization.

#include <gefp.h>

Inheritance diagram for oepdev::LinearNonUniformEFieldPolarGEFactory:



### **Public Member Functions**

- LinearNonUniformEFieldPolarGEFactory (std::shared\_ptr< psi::Wavefunction > wfn, psi::Options &opt)
- void compute\_gradient (int i, int j)

Compute Gradient vector associated with the i-th and j-th basis set function.

void compute\_hessian (void)

Compute Hessian matrix (independent on the parameters)

#### **Additional Inherited Members**

### 17.32.1 Detailed Description

Polarization GEFP Factory with Least-Squares Parameterization.

Implements the generalized density matrix susceptibility model of the form

$$\delta D_{\alpha\beta} \approx \sum_{i} \mathbf{B}_{i;\alpha\beta}^{(10)} \cdot \mathbf{F}(\mathbf{r}_i)$$

where:

•  $\mathbf{B}_{i:\alpha\beta}^{(10)}$  is the density matrix dipole polarizability defined for the distributed site at  $\mathbf{r}_i$ .

The documentation for this class was generated from the following files:

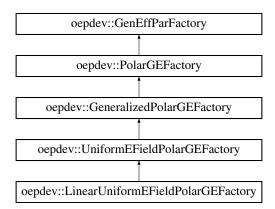
- · oepdev/libgefp/gefp.h
- oepdev/libgefp/gefp\_polar\_nonuniform\_field\_1.cc

# 17.33 oepdev::LinearUniformEFieldPolarGEFactory Class Reference

Polarization GEFP Factory with Least-Squares Parameterization.

#include <gefp.h>

Inheritance diagram for oepdev::LinearUniformEFieldPolarGEFactory:



### **Public Member Functions**

- LinearUniformEFieldPolarGEFactory (std::shared\_ptr< psi::Wavefunction > wfn, psi::Options &opt)
- void compute\_gradient (int i, int j)

Compute Gradient vector associated with the i-th and j-th basis set function.

void compute\_hessian (void)

Compute Hessian matrix (independent on the parameters)

### **Additional Inherited Members**

### 17.33.1 Detailed Description

Polarization GEFP Factory with Least-Squares Parameterization.

Implements the generalized density matrix susceptibility model of the form

$$\delta D_{\alpha\beta} \approx \mathbf{B}_{\alpha\beta}^{(10)} \cdot \mathbf{F}$$

where:

•  ${\bf B}_{\alpha\beta}^{(10)}$  is the density matrix dipole polarizability

The documentation for this class was generated from the following files:

- oepdev/libgefp/gefp.h
- oepdev/libgefp/gefp polar uniform field 1.cc

# 17.34 oepdev::NonUniformEFieldPolarGEFactory Class Reference

Polarization GEFP Factory with Least-Squares Parameterization.

#include <gefp.h>

Inheritance diagram for oepdev::NonUniformEFieldPolarGEFactory:



### **Public Member Functions**

- NonUniformEFieldPolarGEFactory (std::shared\_ptr< psi::Wavefunction > wfn, psi::Options &opt)
- void compute\_samples (void)

Compute samples of density matrices and select electric field distributions.

• virtual void compute\_gradient (int i, int j)=0

Compute Gradient vector associated with the i-th and j-th basis set function.

virtual void compute\_hessian (void)=0

Compute Hessian matrix (independent on the parameters)

### **Additional Inherited Members**

# 17.34.1 Detailed Description

Polarization GEFP Factory with Least-Squares Parameterization.

Implements a class of density matrix susceptibility models for parameterization in the non-uniform electric field generated by point charges.

The documentation for this class was generated from the following files:

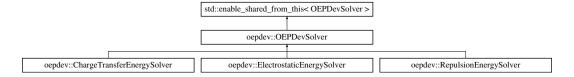
- oepdev/libgefp/gefp.h
- · oepdev/libgefp/gefp\_polar\_nonuniform\_base.cc

# 17.35 oepdev::OEPDevSolver Class Reference

Solver of properties of molecular aggregates. Abstract base.

#include <solver.h>

Inheritance diagram for oepdev::OEPDevSolver:



### **Public Member Functions**

OEPDevSolver (SharedWavefunctionUnion wfn\_union)

Take wavefunction union and initialize the Solver.

virtual ∼OEPDevSolver ()

Destroctor.

virtual double compute\_oep\_based (const std::string &method="DEFAULT")=0

Compute property by using OEP's.

virtual double compute\_benchmark (const std::string &method="DEFAULT")=0

Compute property by using benchmark method.

### **Static Public Member Functions**

• static std::shared\_ptr

< OEPDevSolver > build (const std::string &target, SharedWavefunctionUnion wfn\_union)

Build a solver of a particular property for given molecular cluster.

### **Protected Attributes**

• SharedWavefunctionUnion wfn\_union\_

Wavefunction union.

std::vector< std::string > methods oepBased

Names of all OEP-based methods implemented for a solver.

std::vector< std::string > methods\_benchmark\_

Names of all benchmark methods implemented for a solver.

### 17.35.1 Detailed Description

Solver of properties of molecular aggregates. Abstract base.

Uses only a wavefunction union object to initialize. Available solvers:

- ELECTROSTATIC ENERGY
- REPULSION ENERGY
- CHARGE TRANSFER ENERGY

Options controlling the generalized density fitting (GDF):

- OEPDEV\_DF\_TYPE type of the GDF. Default: DOUBLE.
- DF\_BASIS\_OEP auxiliary basis set. Default: sto-3q.
- DF\_BASIS\_INT intermediate basis set. Relevant only if double GDF is used. Default: aug-cc-pVD-Z-jkfit. Note that intermediate basis set should be nearly complete.

#### 17.35.2 Constructor & Destructor Documentation

17.35.2.1 OEPDevSolver::OEPDevSolver ( SharedWavefunctionUnion wfn\_union )

Take wavefunction union and initialize the Solver.

#### **Parameters**

wfn_union	- wavefunction union of isolated molecular wavefunctions

### 17.35.3 Member Function Documentation

17.35.3.1 std::shared\_ptr< OEPDevSolver > OEPDevSolver::build ( const std::string & target, SharedWavefunctionUnion wfn\_union ) [static]

Build a solver of a particular property for given molecular cluster.

#### **Parameters**

target	- target property
wfn_union	- wavefunction union of isolated molecular wavefunctions

Implemented target properties:

- ELECTROSTATIC\_ENERGY Coulombic interaction energy between unperturbed wavefunctions.
- REPULSION\_ENERGY Pauli repulsion interaction energy between unperturbed wavefunctions.

### See Also

ElectrostaticEnergySolver

```
17.35.3.2 double OEPDevSolver::compute_benchmark ( const std::string & method = "DEFAULT" ) [pure virtual]
```

Compute property by using benchmark method.

Each solver object has one DEFAULT benchmark method

#### **Parameters**

```
method - benchmark method
```

Implemented in oepdev::ChargeTransferEnergySolver, oepdev::RepulsionEnergySolver, and oepdev::Electrostatic-EnergySolver.

17.35.3.3 double OEPDevSolver::compute\_oep\_based ( const std::string & method = "DEFAULT" ) [pure virtual]

Compute property by using OEP's.

Each solver object has one  $\mathtt{DEFAULT}$  OEP-based method.

#### **Parameters**

method - flavour of OEP model

Implemented in oepdev::ChargeTransferEnergySolver, oepdev::RepulsionEnergySolver, and oepdev::Electrostatic-EnergySolver.

The documentation for this class was generated from the following files:

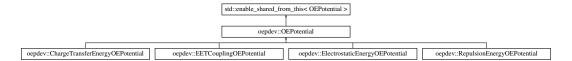
- oepdev/libutil/solver.h
- · oepdev/libutil/solver.cc

# 17.36 oepdev::OEPotential Class Reference

Generalized One-Electron Potential: Abstract base.

#include <oep.h>

Inheritance diagram for oepdev::OEPotential:



### **Public Member Functions**

• OEPotential (SharedWavefunction wfn, Options & options)

Fully ESP-based OEP object.

 OEPotential (SharedWavefunction wfn, SharedBasisSet auxiliary, SharedBasisSet intermediate, Options &options)

General OEP object.

virtual ∼OEPotential ()

Destructor.

· virtual void compute (void)

Compute matrix forms of all OEP's within all OEP types.

virtual void compute (const std::string &oepType)=0

Compute matrix forms of all OEP's within a specified OEP type.

virtual void compute\_3D (const std::string &oepType, const double &x, const double &y, const double &z, double &v)=0

Compute value of potential in point x, y, z and save at v.

virtual void write\_cube (const std::string &oepType, const std::string &fileName)

Write potential to a cube file.

virtual void rotate (const Matrix &rotmat)

Rotate

virtual void translate (const Vector &trans)

Translate

virtual void superimpose (const Matrix &refGeometry, const std::vector< int > &supList, const std::vector< int > &reordList)

Superimpose.

• std::string name () const

Retrieve name of this OEP.

OEPType oep (const std::string &oepType) const

Retrieve the potentials.

SharedMatrix matrix (const std::string &oepType) const

Retrieve the potentials in a matrix form.

SharedWavefunction wfn () const

Retrieve wavefunction object.

- void set\_name (const std::string &name)
- virtual void print\_header () const =0

#### Static Public Member Functions

- · static std::shared ptr
  - < OEPotential > build (const std::string &category, SharedWavefunction wfn, Options &options)

Build fully ESP-based OEP object.

- · static std::shared\_ptr
  - < OEPotential > build (const std::string &category, SharedWavefunction wfn, SharedBasisSet auxiliary, SharedBasisSet intermediate, Options &options)

Build general OEP object.

### **Protected Attributes**

· Options options\_

Psi4 options.

SharedWavefunction wfn\_

Wavefunction.

SharedBasisSet primary

Promary Basis set.

SharedBasisSet auxiliary\_

Auxiliary Basis set.

• SharedBasisSet intermediate\_

Intermediate Basis set.

• std::string name\_

Name of this OEP;.

std::map< std::string, OEPType > oepTypes\_

Types of OEP's within the scope of this object.

- · std::shared\_ptr
  - < psi::IntegralFactory > intsFactory

Integral factory.

std::shared\_ptr< psi::Matrix > potMat\_

Matrix of potential one-electron integrals.

- std::shared\_ptr
  - < psi::OneBodyAOInt > OEInt\_

One-electron integral shared pointer.

std::shared\_ptr< PotentialInt > potInt\_

One-electron potential shared pointer.

## 17.36.1 Detailed Description

Generalized One-Electron Potential: Abstract base.

Manages OEP's in matrix and 3D forms. Available OEP categories:

• ELECTROSTATIC ENERGY

- REPULSION ENERGY
- CHARGE TRANSFER ENERGY
- EET COUPLING CONSTANT

### 17.36.2 Constructor & Destructor Documentation

17.36.2.1 OEPotential::OEPotential (SharedWavefunction wfn, Options & options)

Fully ESP-based OEP object.

#### **Parameters**

wfn	- wavefunction
options	- Psi4 options

17.36.2.2 OEPotential::OEPotential ( SharedWavefunction wfn, SharedBasisSet auxiliary, SharedBasisSet intermediate, Options & options )

General OEP object.

### **Parameters**

wfn	- wavefunction
auxiliary	- auxiliary basis set for density fitting of OEP's
intermediate	- intermediate basis set for density fitting of OEP's
options	- Psi4 options

### 17.36.3 Member Function Documentation

17.36.3.1 std::shared\_ptr< OEPotential > OEPotential::build ( const std::string & category, SharedWavefunction wfn, Options & options ) [static]

Build fully ESP-based OEP object.

### **Parameters**

type	- OEP category
wfn	- wavefunction
options	- Psi4 options

17.36.3.2 std::shared\_ptr< OEPotential > OEPotential::build ( const std::string & category, SharedWavefunction wfn, SharedBasisSet auxiliary, SharedBasisSet intermediate, Options & options ) [static]

Build general OEP object.

### **Parameters**

type	- OEP category
wfn	- wavefunction
auxiliary	- auxiliary basis set for density fitting of OEP's
intermediate	- intermediate basis set for density fitting of OEP's

```
options - Psi4 options
```

The documentation for this class was generated from the following files:

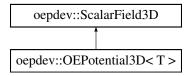
- · oepdev/liboep/oep.h
- · oepdev/liboep/oep.cc

# 17.37 oepdev::OEPotential3D< T > Class Template Reference

Class template for OEP scalar fields.

```
#include <space3d.h>
```

Inheritance diagram for oepdev::OEPotential3D< T >:



#### **Public Member Functions**

- OEPotential3D (const int &np, const double &padding, std::shared\_ptr< T > oep, const std::string &oepType)
   Construct random spherical collection of scalar field of type T.
- OEPotential3D (const int &nx, const int &ny, const int &nz, const double &px, const double &py, const double &px, std::shared\_ptr< T > oep, const std::string &oepType, psi::Options &options)

Construct ordered 3D collection of scalar field of type T.

virtual ∼OEPotential3D ()

Destructor.

• virtual double compute xyz (const double &x, const double &y, const double &z)

Compute a value of scalar field at point (x, y, z)

• virtual void print () const

Print information of the object to Psi4 output.

### **Protected Attributes**

std::shared\_ptr< T > oep\_

Shared pointer to the instance of class T

std::string oepType\_

Descriptor of the scalar field type stored in instance of  ${\it T}$ 

### **Additional Inherited Members**

### 17.37.1 Detailed Description

template < class T> class oepdev:: OEPotential 3D < T>

Class template for OEP scalar fields.

Used for special type of classes T that contain following public member functions:

with the descriptor of a certain scalar field type, x, y, z the points in 3D space in which the scalar field has to be computed and stored at v. Instances of T should store shared pointer to wavefunction object. List of classes T that are compatible with this class template and are currently implemented in oepdev is given below:

• oepdev::OEPotential abstract base (do not use derived classes as T)

Template parameters:

**Template Parameters** 

```
T | the compatible class (e.g. oepdev::OEPotential)
```

The documentation for this class was generated from the following file:

oepdev/lib3d/space3d.h

# 17.38 oepdev::OEPType Struct Reference

Container to handle the type of One-Electron Potentials.

```
#include <oep.h>
```

### **Public Attributes**

· std::string name

Name of this type of OEP.

• bool is\_density\_fitted

Is this OEP DF-based?

• int n

Number of OEP's within a type.

· SharedMatrix matrix

All OEP's of this type gathered in a matrix form.

# 17.38.1 Detailed Description

Container to handle the type of One-Electron Potentials.

The documentation for this struct was generated from the following file:

· oepdev/liboep/oep.h

# 17.39 oepdev::PerturbCharges Struct Reference

Structure to hold perturbing charges.

```
#include <scf_perturb.h>
```

### **Public Attributes**

std::vector< double > charges

Vector of charge values.

 $\bullet \ \, std::vector < std::shared\_ptr$ 

< psi::Vector > > positions

Vector of charge position vectors.

## 17.39.1 Detailed Description

Structure to hold perturbing charges.

The documentation for this struct was generated from the following file:

• oepdev/libutil/scf\_perturb.h

# 17.40 oepdev::Points3Dlterator::Point Struct Reference

### **Public Attributes**

- double x
- · double y
- double z
- int index

The documentation for this struct was generated from the following file:

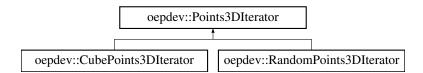
· oepdev/lib3d/space3d.h

# 17.41 oepdev::Points3Dlterator Class Reference

Iterator over a collection of points in 3D space. Abstract base.

```
#include <space3d.h>
```

Inheritance diagram for oepdev::Points3DIterator:



### Classes

struct Point

# **Public Member Functions**

• Points3DIterator (const int &np)

Plain constructor. Initializes the abstract features.

virtual ∼Points3DIterator ()

Destructor.

virtual bool is\_done ()

Check if iteration is finished.

virtual void first ()=0

Initialize first iteration.

virtual void next ()=0

Step to next iteration.

- virtual double x () const
- virtual double y () const
- virtual double z () const
- · virtual int index () const

### **Static Public Member Functions**

- · static shared ptr
  - < Points3DIterator > build (const int &nx, const int &ny, const int &nz, const double &dx, const double &dx, const double &dx, const double &ox, const double &oz)

Build G09 Cube collection iterator.

- static shared\_ptr
  - < Points3Dlterator > build (const int &np, const double &radius, const double &cx, const double &cy, const double &cz)

Build random collection iterator.

- · static shared\_ptr
  - < Points3Dlterator > build (const int &np, const double &pad, psi::SharedMolecule mol)

Build random collection iterator.

### **Protected Attributes**

· const int np\_

Number of points.

bool done\_

Status of the iterator.

• int index\_

Current index.

Point current\_

### 17.41.1 Detailed Description

Iterator over a collection of points in 3D space. Abstract base.

Points3DIterators are constructed either as iterators over:

- · a random collections or
- an ordered (g09 cube-like) collections. Note: Always create instances by using static factory methods.

### 17.41.2 Constructor & Destructor Documentation

17.41.2.1 oepdev::Points3Dlterator::Points3Dlterator ( const int & np )

Plain constructor. Initializes the abstract features.

#### **Parameters**

_		
ſ	np	- number of points this iterator is constructed for

### 17.41.3 Member Function Documentation

17.41.3.1 std::shared\_ptr< Points3Dlterator > oepdev::Points3Dlterator::build ( const int & nx, const int & ny, const int & nz, const double & dx, const double & dx, const double & dx, const double & ox, const double & ox, const double & ox, const double & oz ) [static]

Build G09 Cube collection iterator.

The points are generated according to Gaussian cube file format.

#### **Parameters**

nx	- number of points along x direction
ny	- number of points along y direction
nz	- number of points along z direction
dx	- spacing distance along x direction
dy	- spacing distance along y direction
dz	- spacing distance along y direction
OX	- coordinate x of cube origin
oy	- coordinate y of cube origin
OZ	- coordinate z of cube origin

17.41.3.2 std::shared\_ptr< Points3Dlterator > oepdev::Points3Dlterator::build ( const int & np, const double & radius, const double & cx, const double & cy, const double & cz ) [static]

Build random collection iterator.

The points are drawn according to uniform distrinution in 3D space.

#### **Parameters**

np	- number of points to draw
radius	- sphere radius inside which points are to be drawn
CX	- coordinate x of sphere's centre
су	- coordinate y of sphere's centre
CZ	- coordinate z of sphere's centre

17.41.3.3 shared\_ptr< Points3Dlterator > oepdev::Points3Dlterator::build ( const int & np, const double & pad, psi::SharedMolecule mol ) [static]

Build random collection iterator.

The points are drawn according to uniform distrinution in 3D space enclosing a molecule given. All drawn points lie outside the van der Waals volume.

### Parameters

	number of points to droug
np	- number of points to draw
pad	- radius padding of a minimal sphere enclosing the molecule
mol	- Psi4 molecule object

The documentation for this class was generated from the following files:

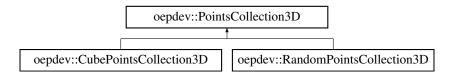
- · oepdev/lib3d/space3d.h
- · oepdev/lib3d/space3d.cc

# 17.42 oepdev::PointsCollection3D Class Reference

Collection of points in 3D space. Abstract base.

#include <space3d.h>

Inheritance diagram for oepdev::PointsCollection3D:



### **Public Types**

• enum Collection { Random, Cube }

Public descriptior of collection type.

#### **Public Member Functions**

• PointsCollection3D (Collection collectionType, int &np)

Initialize abstract features.

- PointsCollection3D (Collection collectionType, const int &np)
- virtual ~PointsCollection3D ()

Destructor.

· virtual int npoints () const

Get the number of points.

- · virtual shared\_ptr
  - < Points3Dlterator > points\_iterator () const

Get the iterator over this collection of points.

• virtual Collection get\_type () const

Get the collection type.

virtual void print () const =0

Print the information to Psi4 output file.

#### **Static Public Member Functions**

· static shared ptr

< PointsCollection3D > build (const int &npoints, const double &radius, const double &cx=0.0, const double &cz=0.0)

Build random collection of points.

- static shared\_ptr
  - < PointsCollection3D > build (const int &npoints, const double &padding, psi::SharedMolecule mol)

Build random collection of points.

- · static shared\_ptr
  - < PointsCollection3D > build (const int &nx, const int &ny, const int &nz, const double &px, const double &px, const double &px, psi::Options &options)

Build G09 Cube collection of points.

### **Protected Attributes**

const int np

Number of points.

Collection collectionType

Collection type.

shared\_ptr< Points3Dlterator > pointsIterator\_

iterator over points collection

### 17.42.1 Detailed Description

Collection of points in 3D space. Abstract base.

Create random or ordered (g09 cube-like) collections of points in 3D space.

Note: Always create instances by using static factory methods.

### 17.42.2 Constructor & Destructor Documentation

17.42.2.1 oepdev::PointsCollection3D::PointsCollection3D ( Collection collectionType, int & np )

Initialize abstract features.

#### **Parameters**

np	- number of points to be created
----	----------------------------------

### 17.42.3 Member Function Documentation

17.42.3.1 std::shared\_ptr< PointsCollection3D > oepdev::PointsCollection3D::build ( const int & npoints, const double & radius, const double & cx = 0.0, const double & cy = 0.0, const double & cz = 0.0) [static]

Build random collection of points.

Points uniformly span a sphere.

### **Parameters**

npoints	- number of points to draw
radius	- sphere radius inside which points are to be drawn
CX	- coordinate x of sphere's centre
су	- coordinate y of sphere's centre
CZ	- coordinate z of sphere's centre

17.42.3.2 std::shared\_ptr< PointsCollection3D > oepdev::PointsCollection3D::build ( const int & *npoints*, const double & *padding*, psi::SharedMolecule *mol* ) [static]

Build random collection of points.

Points uniformly span space inside a sphere enclosing a molecule. exluding the van der Waals volume.

## Parameters

np	- number of points to draw

padding	- radius padding of a minimal sphere enclosing the molecule
mol	- Psi4 molecule object

17.42.3.3 std::shared\_ptr< PointsCollection3D > oepdev::PointsCollection3D::build ( const int & nx, const int & ny, const int & nz, const double & px, const double & px, psi::SharedBasisSet bs, psi::Options & options ) [static]

Build G09 Cube collection of points.

The points span a parallelpiped according to Gaussian cube file format.

#### **Parameters**

nx	- number of points along x direction
ny	- number of points along y direction
nz	- number of points along z direction
рх	- padding distance along x direction
ру	- padding distance along y direction
pz	- padding distance along z direction
bs	- Psi4 basis set object
options	- Psi4 options object

The documentation for this class was generated from the following files:

- · oepdev/lib3d/space3d.h
- · oepdev/lib3d/space3d.cc

# 17.43 oepdev::PolarGEFactory Class Reference

Polarization GEFP Factory. Abstract Base.

#include <gefp.h>

Inheritance diagram for oepdev::PolarGEFactory:



### **Public Member Functions**

- PolarGEFactory (std::shared\_ptr< psi::Wavefunction > wfn, psi::Options & opt)
  - Construct from Psi4 options.
- virtual ~PolarGEFactory ()

Destruct.

- virtual std::shared ptr
  - < GenEffPar > compute (void)=0

Compute the density matrix susceptibility tensors.

### **Protected Member Functions**

- std::shared\_ptr< psi::Vector > draw\_field ()

Randomly draw electric field value.

double draw\_charge ()

Randomly draw charge value.

std::shared ptr

< oepdev::RHFPerturbed > perturbed\_state (const std::shared\_ptr< psi::Vector > &field)

Solve SCF equations to find perturbed state due to uniform electric field.

std::shared ptr

< oepdev::RHFPerturbed > perturbed\_state (const std::shared\_ptr< psi::Vector > &pos, const double &charge)

Solve SCF equations to find perturbed state due to point charge.

· std::shared ptr

< oepdev::RHFPerturbed > perturbed\_state (const std::shared\_ptr< psi::Matrix > &charges)

Solve SCF equations to find perturbed state due to set of point charges.

• std::shared\_ptr< psi::Vector > field\_due\_to\_charges (const std::shared\_ptr< psi::Matrix > &charges, const double &x, const double &z)

Evaluate electric field at point (x,y,z) due to point charges.

- std::shared\_ptr< psi::Vector > **field\_due\_to\_charges** (const std::shared\_ptr< psi::Matrix > &charges, const std::shared\_ptr< psi::Vector > &pos)
- std::shared\_ptr< psi::Matrix > field\_gradient\_due\_to\_charges (const std::shared\_ptr< psi::Matrix > &charges, const double &x, const double &y, const double &z)

Evaluate electric field gradient at point (x,y,z) due to point charges.

std::shared\_ptr< psi::Matrix > field\_gradient\_due\_to\_charges (const std::shared\_ptr< psi::Matrix > &charges, const std::shared\_ptr< psi::Vector > &pos)

### **Additional Inherited Members**

### 17.43.1 Detailed Description

Polarization GEFP Factory. Abstract Base.

Basic interface for the polarization density matrix susceptibility parameters.

The documentation for this class was generated from the following files:

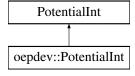
- oepdev/libgefp/gefp.h
- · oepdev/libgefp/gefp polar base.cc

# 17.44 oepdev::PotentialInt Class Reference

Computes potential integrals.

#include <potential.h>

Inheritance diagram for oepdev::PotentialInt:



### **Public Member Functions**

PotentialInt (std::vector< psi::SphericalTransform > &st, std::shared\_ptr< psi::BasisSet > bs1, std::shared\_ptr< psi::BasisSet > bs2, int deriv=0)

Constructor. Initialize identically like in psi::PotentilInt.

PotentialInt (std::vector< psi::SphericalTransform > &st, std::shared\_ptr< psi::BasisSet > bs1, std::shared\_ptr< psi::BasisSet > bs2, std::shared\_ptr< psi::Matrix > Qxyz, int deriv=0)

Constructor. Takes an arbitrary collection of charges.

PotentialInt (std::vector< psi::SphericalTransform > &, std::shared\_ptr< psi::BasisSet >, std::shared\_ptr< psi::BasisSet >, const double &x, const double &y, const double &z, const double &q=1.0, int deriv=0)

Constructor. Computes potential for one point x, y, z for a test particle of charge q.

void set\_charge\_field (const double &x, const double &y, const double &z, const double &q=1.0)

Mutator. Set the charge field to be a x, y, z point of charge q.

# 17.44.1 Detailed Description

Computes potential integrals.

## 17.44.2 Constructor & Destructor Documentation

17.44.2.1 oepdev::PotentialInt::PotentialInt ( std::vector< psi::SphericalTransform > & st, std::shared\_ptr< psi::BasisSet > bs1, std::shared\_ptr< psi::BasisSet > bs2, int deriv = 0 )

Constructor. Initialize identically like in psi::PotentilInt.

#### **Parameters**

st	- Spherical transform object
bs1	- basis set for first space
bs2	- basis set for second space
deriv	- derivative level

17.44.2.2 oepdev::PotentialInt::PotentialInt ( std::vector< psi::SphericalTransform > & st, std::shared\_ptr< psi::BasisSet > bs1, std::shared\_ptr< psi::BasisSet > bs2, std::shared\_ptr< psi::Matrix > Qxyz, int deriv = 0 )

Constructor. Takes an arbitrary collection of charges.

# Parameters

st	- Spherical transform object
bs1	- basis set for first space
bs2	- basis set for second space
Qxyz	- matrix with charges and their positions
deriv	- derivative level

17.44.2.3 oepdev::PotentialInt::PotentialInt ( std::vector < psi::SphericalTransform > & st, std::shared\_ptr < psi::BasisSet > bs1, std::shared\_ptr < psi::BasisSet > bs2, const double & x, const double & y, const double & z, const double & q = 1.0, int deriv = 0)

Constructor. Computes potential for one point x, y, z for a test particle of charge q.

#### **Parameters**

st	- Spherical transform object
bs1	- basis set for first space

bs2	- basis set for second space
X	- x coordinate of q
у	- y coordinate of q
Z	- z coordinate of q
q	- value of the probe charge
deriv	- derivative level

## 17.44.3 Member Function Documentation

17.44.3.1 void oepdev::PotentialInt::set\_charge\_field ( const double & x, const double & y, const double & z, const double & q = 1 . 0 )

Mutator. Set the charge field to be a x, y, z point of charge q.

## **Parameters**

X	- x coordinate of q
у	- y coordinate of q
Z	- z coordinate of q
q	- value of the probe charge

The documentation for this class was generated from the following files:

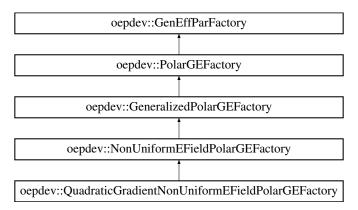
- · oepdev/libpsi/potential.h
- · oepdev/libpsi/potential.cc

# 17.45 oepdev::QuadraticGradientNonUniformEFieldPolarGEFactory Class Reference

Polarization GEFP Factory with Least-Squares Parameterization.

#include <gefp.h>

 $Inheritance\ diagram\ for\ oepdev:: Quadratic Gradient Non Uniform EField Polar GEF actory:$ 



## **Public Member Functions**

- QuadraticGradientNonUniformEFieldPolarGEFactory (std::shared\_ptr< psi::Wavefunction > wfn, psi::-Options &opt)
- void compute\_gradient (int i, int j)

Compute Gradient vector associated with the i-th and j-th basis set function.

void compute hessian (void)

Compute Hessian matrix (independent on the parameters)

# **Additional Inherited Members**

# 17.45.1 Detailed Description

Polarization GEFP Factory with Least-Squares Parameterization.

Implements the generalized density matrix susceptibility model of the form

$$\delta D_{\alpha\beta} \approx \sum_{i} \left\{ \mathbf{B}_{i;\alpha\beta}^{(10)} \cdot \mathbf{F}(\mathbf{r}_{i}) + \mathbf{B}_{i;\alpha\beta}^{(20)} : \mathbf{F} \otimes \mathbf{F}(\mathbf{r}_{i}) + \mathbf{B}_{i;\alpha\beta}^{(01)} : \nabla_{i} \otimes \mathbf{F}(\mathbf{r}_{i}) \right\}$$

where:

- $\mathbf{B}_{i:lphaeta}^{(10)}$  is the density matrix dipole polarizability
- ${f B}^{(20)}_{i:lphaeta}$  is the density matrix dipole-dipole hyperpolarizability
- $\mathbf{B}_{i:\alpha\beta}^{(01)}$  is the density matrix quadrupole polarizability all defined for the distributed site at  $\mathbf{r}_i$ .

Note

This model is not available now and probably will be deprecated in the future.

The documentation for this class was generated from the following files:

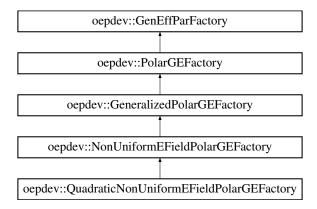
- · oepdev/libgefp/gefp.h
- oepdev/libgefp/gefp\_polar\_nonuniform\_field\_2\_grad\_1.cc

# 17.46 oepdev::QuadraticNonUniformEFieldPolarGEFactory Class Reference

Polarization GEFP Factory with Least-Squares Parameterization.

#include <gefp.h>

Inheritance diagram for oepdev::QuadraticNonUniformEFieldPolarGEFactory:



## **Public Member Functions**

- QuadraticNonUniformEFieldPolarGEFactory (std::shared\_ptr< psi::Wavefunction > wfn, psi::Options & opt)
- void compute\_gradient (int i, int j)

Compute Gradient vector associated with the i-th and j-th basis set function.

void compute\_hessian (void)

Compute Hessian matrix (independent on the parameters)

## **Additional Inherited Members**

# 17.46.1 Detailed Description

Polarization GEFP Factory with Least-Squares Parameterization.

Implements the generalized density matrix susceptibility model of the form

$$\delta D_{lphaeta} pprox \sum_{i} \left\{ \mathbf{B}_{i;lphaeta}^{(10)} \cdot \mathbf{F}(\mathbf{r}_{i}) + \mathbf{B}_{i;lphaeta}^{(20)} : \mathbf{F}(\mathbf{r}_{i}) \otimes \mathbf{F}(\mathbf{r}_{i}) 
ight\}$$

where:

- ${\bf B}_{i:\alpha\beta}^{(10)}$  is the density matrix dipole polarizability
- $\mathbf{B}_{i;\alpha\beta}^{(20)}$  is the density matrix dipole-dipole hyperpolarizability all defined for the distributed site at  $\mathbf{r}_i$ .

The documentation for this class was generated from the following files:

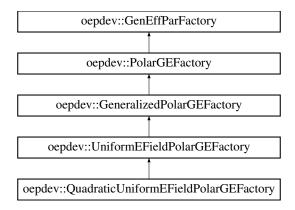
- oepdev/libgefp/gefp.h
- · oepdev/libgefp/gefp\_polar\_nonuniform\_field\_2.cc

# 17.47 oepdev::QuadraticUniformEFieldPolarGEFactory Class Reference

Polarization GEFP Factory with Least-Squares Parameterization.

#include <gefp.h>

Inheritance diagram for oepdev::QuadraticUniformEFieldPolarGEFactory:



# **Public Member Functions**

- QuadraticUniformEFieldPolarGEFactory (std::shared ptr< psi::Wavefunction > wfn, psi::Options &opt)
- void compute\_gradient (int i, int j)

Compute Gradient vector associated with the i-th and j-th basis set function.

void compute\_hessian (void)

Compute Hessian matrix (independent on the parameters)

# **Additional Inherited Members**

# 17.47.1 Detailed Description

Polarization GEFP Factory with Least-Squares Parameterization.

Implements the generalized density matrix susceptibility model of the form

$$\delta D_{\alpha\beta} \approx \mathbf{B}_{\alpha\beta}^{(10)} \cdot \mathbf{F} + \mathbf{B}_{\alpha\beta}^{(20)} : \mathbf{F} \otimes \mathbf{F}$$

where:

- ${f B}^{(10)}_{lphaeta}$  is the density matrix dipole polarizability
- $\mathbf{B}_{\alpha\beta}^{(20)}$  is the density matrix dipole-dipole hyperpolarizability

The documentation for this class was generated from the following files:

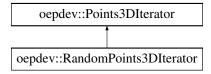
- oepdev/libgefp/gefp.h
- oepdev/libgefp/gefp\_polar\_uniform\_field\_2.cc

# 17.48 oepdev::RandomPoints3DIterator Class Reference

Iterator over a collection of points in 3D space. Random collection.

#include <space3d.h>

Inheritance diagram for oepdev::RandomPoints3DIterator:



### **Public Member Functions**

- RandomPoints3Dlterator (const int &np, const double &radius, const double &cx, const double &cy, const double &cz)
- RandomPoints3DIterator (const int &np, const double &pad, psi::SharedMolecule mol)
- · virtual void first ()

Initialize first iteration.

· virtual void next ()

Step to next iteration.

# **Protected Member Functions**

- virtual double random\_double ()
- virtual void draw\_random\_point ()
- virtual bool is\_in\_vdWsphere (double x, double y, double z) const

# **Protected Attributes**

- double **cx**\_
- · double cy\_
- double cz\_
- · double radius\_
- double r
- double phi\_

- · double theta\_
- double x\_
- double y\_
- double z\_
- psi::SharedMatrix excludeSpheres\_
- std::map< std::string, double > vdwRadius\_
- std::default\_random\_engine randomNumberGenerator\_
- std::uniform\_real\_distribution
  - < double > randomDistribution\_

## **Additional Inherited Members**

## 17.48.1 Detailed Description

Iterator over a collection of points in 3D space. Random collection.

**Note:** Always create instances by using static factory method from Points3DIterator. Do not use constructors of this class.

The documentation for this class was generated from the following files:

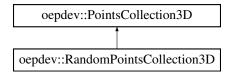
- oepdev/lib3d/space3d.h
- oepdev/lib3d/space3d.cc

# 17.49 oepdev::RandomPointsCollection3D Class Reference

Collection of random points in 3D space.

#include <space3d.h>

Inheritance diagram for oepdev::RandomPointsCollection3D:



# **Public Member Functions**

- RandomPointsCollection3D (Collection collectionType, const int &npoints, const double &radius, const double &cx, const double &cy, const double &cz)
- RandomPointsCollection3D (Collection collectionType, const int &npoints, const double &padding, psi::-SharedMolecule mol)
- · virtual void print () const

Print the information to Psi4 output file.

# **Additional Inherited Members**

# 17.49.1 Detailed Description

Collection of random points in 3D space.

**Note:** Do not use constructors of this class explicitly. Instead, use static factory methods of the superclass to create instances.

The documentation for this class was generated from the following files:

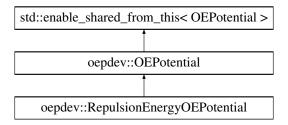
- · oepdev/lib3d/space3d.h
- · oepdev/lib3d/space3d.cc

# 17.50 oepdev::RepulsionEnergyOEPotential Class Reference

Generalized One-Electron Potential for Pauli Repulsion Energy.

#include <oep.h>

Inheritance diagram for oepdev::RepulsionEnergyOEPotential:



## **Public Member Functions**

- RepulsionEnergyOEPotential (SharedWavefunction wfn, SharedBasisSet auxiliary, SharedBasisSet intermediate, Options & options)
- RepulsionEnergyOEPotential (SharedWavefunction wfn, Options & options)
- virtual void compute (const std::string &oepType) override

Compute matrix forms of all OEP's within a specified OEP type.

virtual void compute\_3D (const std::string &oepType, const double &x, const double &y, const double &z, double &v) override

Compute value of potential in point x, y, z and save at v.

· virtual void print\_header () const override

## **Additional Inherited Members**

## 17.50.1 Detailed Description

Generalized One-Electron Potential for Pauli Repulsion Energy.

Contains the following OEP types:

- Murrell-etal.S1
- Otto-Ladik.S2

The documentation for this class was generated from the following files:

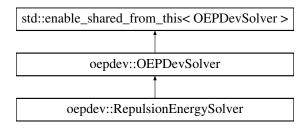
- · oepdev/liboep/oep.h
- · oepdev/liboep/oep.cc

# 17.51 oepdev::RepulsionEnergySolver Class Reference

Compute the Pauli-Repulsion interaction energy between unperturbed wavefunctions.

#include <solver.h>

Inheritance diagram for oepdev::RepulsionEnergySolver:



## **Public Member Functions**

- **RepulsionEnergySolver** (SharedWavefunctionUnion wfn\_union)
- virtual double compute\_oep\_based (const std::string &method="DEFAULT")
   Compute property by using OEP's.
- virtual double compute\_benchmark (const std::string &method="DEFAULT")

  Compute property by using benchmark method.

## **Additional Inherited Members**

# 17.51.1 Detailed Description

Compute the Pauli-Repulsion interaction energy between unperturbed wavefunctions.

The implemented methods are shown below Note:

Keyword	Method Description
Beno	chmark Methods
HAYES_STONE	*Default*. Pauli Repulsion energy at HF level from
	Hayes and Stone (1984).
DENSITY_BASED	Pauli Repulsion energy at HF level from Mandado and
	Hermida-Ramon (2012).
MURRELL_ETAL	Approximate Pauli Repulsion energy at HF level from
	Murrell et al (1967).
OTTO_LADIK	Approximate Pauli Repulsion energy at HF level from
	Otto and Ladik (1975).
EFP2	Approximate Pauli Repulsion energy at HF level from
	EFP2 model.
OEP	-Based Methods
MURRELL_ETAL_MIX	*Default*. OEP-Murrell et al's: S1 term via DF-OEP,
	S2 term via ESP-OEP.
MURRELL_ETAL_ESP	OEP-Murrell et al's: S1 and S2 via ESP-OEP

Table 17.3: Methods available in the Solver

- This solver also computes and prints the exchange energy at HF level (formulae are given below) for reference purposes.
- In order to construct this solver, always use the <code>OEPDevSolver::build</code> static factory method.

Below the detailed description of the implemented equations is given for each of the above provided methods. In the formulae across, it is assumed that the orbitals are real. The Coulomb notation for electron repulsion integrals (ERI's) is adopted; i.e,

$$(ac|bd) = \iint d\mathbf{r}_1 d\mathbf{r}_2 \phi_a(\mathbf{r}_1) \phi_c(\mathbf{r}_1) \frac{1}{r_{12}} \phi_b(\mathbf{r}_2) \phi_d(\mathbf{r}_2)$$

Greek subscripts denote basis set orbitals whereas Italic subscripts denote the occupied molecular orbitals.

#### **Benchmark Methods**

Pauli Repulsion energy at HF level by Hayes and Stone (1984).

For a closed-shell system, equation of Hayes and Stone (1984) becomes

$$E^{\text{Rep}} = 2\sum_{kl} \left( V_{kl}^A + V_{kl}^B + T_{kl} \right) \left[ [\mathbf{S}^{-1}]_{lk} - \delta_{lk} \right] + \sum_{klmn} (kl|mn) \left\{ 2[\mathbf{S}^{-1}]_{kl} [\mathbf{S}^{-1}]_{mn} - [\mathbf{S}^{-1}]_{kn} [\mathbf{S}^{-1}]_{lm} - 2\delta_{kl}\delta_{mn} + \delta_{kn}\delta_{lm} \right\}$$

where S is the overlap matrix between the doubly-occupied orbitals. The exact, pure exchange energy is for a closed shell case given as

$$E^{\text{Ex,pure}} = -2\sum_{a \in A} \sum_{b \in B} (ab|ba)$$

Similarity transformation of molecular orbitals does not affect the resulting energies. The overall exchange-repulsion interaction energy is then (always net repulsive)

$$E^{\text{Ex-Rep}} = E^{\text{Ex,pure}} + E^{\text{Rep}}$$

Repulsion energy of Mandado and Hermida-Ramon (2011)

At the Hartree-Fock level, the exchange-repulsion energy from the density-based scheme of Mandado and Hermida-Ramon (2011) is fully equivalent to the method by Hayes and Stone (1984). However, density-based method enables to compute exchange-repulsion energy at any level of theory. It is derived based on the Pauli deformation density matrix.

$$\Delta \mathbf{D}^{\text{Pauli}} \equiv \mathbf{D}^{oo} - \mathbf{D}$$

where  $\mathbf{D}^{oo}$  and  $\mathbf{D}$  are the density matrix formed from mutually orthogonal sets of molecular orbitals within the entire aggregate (formed by symmetric orthogonalization of MO's) and the density matrix of the unperturbed system (that can be understood as a Hadamard sum  $\mathbf{D} \equiv \mathbf{D}^A \oplus \mathbf{D}^B$ ).

At HF level, the Pauli deformation density matrix is given by

$$\Delta \mathbf{D}^{Pauli} = \mathbf{C} \left[ \mathbf{S}^{-1} - \mathbf{1} \right] \mathbf{C}^{\dagger}$$

whereas the density matrix constructed from mutually orthogonal orbitals is

$$\mathbf{D}^{oo} = \mathbf{C}\mathbf{S}^{-1}\mathbf{C}^{\dagger}$$

In the above equations, S is the overlap matrix between doubly occupied molecular orbitals of the entire aggregate.

Here, the expressions for the exchange-repulsion energy at any level of theory are shown for the case of open-shell system. The net repulsive energy is given as

$$E^{\text{Ex-Rep}} = E^{\text{Rep},1} + E^{\text{Rep},2} + E^{\text{Ex}}$$

where the one- and two-electron part of the repulsion energy is

$$E^{\text{Rep,1}} = E^{\text{Rep,Kin}} + E^{\text{Rep,Nuc}}$$
  
 $E^{\text{Rep,2}} = E^{\text{Rep,el}-\Delta} + E^{\text{Rep},\Delta-\Delta}$ 

The kinetic and nuclear contributions are

$$\begin{split} E^{\text{Rep,Kin}} &= 2 \sum_{\alpha\beta \in A,B} \Delta D^{\text{Pauli}}_{\alpha\beta} T_{\alpha\beta} \\ E^{\text{Rep,Nuc}} &= 2 \sum_{\alpha\beta \in A,B} \Delta D^{\text{Pauli}}_{\alpha\beta} \sum_{z \in A,B} V^{(z)}_{\alpha\beta} \end{split}$$

whereas the electron-deformation and deformation-deformation interaction contributions are

$$\begin{split} E^{\text{Rep,el}-\Delta} &= 4 \sum_{\alpha\beta\gamma\delta \in A,B} \Delta D^{\text{Pauli}}_{\alpha\beta} D_{\gamma\delta}(\alpha\beta | \gamma\delta) \\ E^{\text{Rep,}\Delta-\Delta} &= 2 \sum_{\alpha\beta\gamma\delta \in A,B} \Delta D^{\text{Pauli}}_{\alpha\beta} \Delta D^{\text{Pauli}}_{\gamma\delta}(\alpha\beta | \gamma\delta) \end{split}$$

The associated exchange energy is given by

$$E^{\mathrm{Ex}} = -\sum_{\alpha\beta\gamma\delta\in A.B} \left[ D^{oo}_{\alpha\delta} D^{oo}_{\beta\gamma} - D^{A}_{\alpha\delta} D^{A}_{\beta\gamma} - D^{B}_{\alpha\delta} D^{B}_{\beta\gamma} \right] (\alpha\beta|\gamma\delta)$$

It is important to emphasise that, although, at HF level, the particular 'repulsive' and 'exchange' energies computed by using either Hayes and Stone or Mandado and Hermida-Ramon methods are not equal to each other, they sum up to exactly the same exchange-repulsion energy,  $E^{\rm Ex-Rep}$ . Therefore, these methods at HF level are fully equivalent but the nature of partitioning of repulsive and exchange parts is different. It is also noted that the orbital localization does *not* affect the resulting energies, as opposed to the few approximate methods described below (Otto-Ladik and EFP2 methods).

Approximate Pauli Repulsion energy at HF level from Murrell et al.

By expanding the overlap matrix in a Taylor series one can show that the Pauli repulsion energy is approximately given as

$$E^{\text{Rep}} = E^{\text{Rep}}(\mathscr{O}(S)) + E^{\text{Rep}}(\mathscr{O}(S^2))$$

where the first-order term is

$$E^{\mathrm{Rep}}(\mathscr{O}(S)) = -2\sum_{a \in A}\sum_{b \in B}S_{ab}\left\{V_{ab}^A + \sum_{c \in A}\left[2(ab|cc) - (ac|bc)\right] + V_{ab}^B + \sum_{d \in B}\left[2(ab|dd) - (ad|bd)\right]\right\}$$

whereas the second-order term is

$$E^{\text{Rep}}(\mathcal{O}(S^2)) = 2\sum_{a \in A} \sum_{b \in B} S_{ab} \left\{ \sum_{c \in A} S_{bc} \left[ V_{ac}^B + 2\sum_{d \in B} (ac|dd) \right] + \sum_{d \in B} S_{ad} \left[ V_{bd}^A + 2\sum_{c \in A} (bd|cc) \right] - \sum_{c \in A} \sum_{d \in B} S_{cd}(ac|bd) \right\}$$

Thus derived repulsion energy is invariant with respect to transformation of molecular orbitals, similarly as Hayes-Stone's method and density-based method. By using OEP technique, the above theory can be exactly re-cast *without* any further approximations.

Approximate Pauli Repulsion energy at HF level from Otto and Ladik (1975).

The Pauli repulsion energy is approximately given as

$$E^{\text{Rep}} = E^{\text{Rep}}(\mathscr{O}(S)) + E^{\text{Rep}}(\mathscr{O}(S^2))$$

where the first-order term is

$$E^{\mathsf{Rep}}(\mathscr{O}(S)) = -2\sum_{a \in A} \sum_{b \in B} S_{ab} \left\{ V_{ab}^A + 2\sum_{c \in A} (ab|cc) - (ab|aa) + V_{ab}^B + 2\sum_{d \in B} (ab|dd) - (ab|bb) \right\}$$

whereas the second-order term is

$$E^{\text{Rep}}(\mathscr{O}(S^2)) = 2\sum_{a \in A} \sum_{b \in B} S_{ab}^2 \left\{ V_{aa}^B + V_{bb}^A + 2\sum_{c \in A} (cc|bb) + 2\sum_{d \in B} (aa|dd) - (aa|bb) \right\}$$

Thus derived repulsion energy is *not* invariant with respect to transformation of molecular orbitals, in contrast to Hayes-Stone's method and density-based method. It was shown that good results are obtained when using localized molecular orbitals, whereas using canonical molecular orbitals brings poor results. By using OEP technique, the above theory can be exactly re-cast *without* any further approximations.

Approximate Pauli Repulsion energy at HF level from Jensen and Gordon (1996).

The Pauli repulsion energy used within the EFP2 approach is approximately given as

$$E^{\text{Rep}} = E^{\text{Rep}}(\mathscr{O}(S)) + E^{\text{Rep}}(\mathscr{O}(S^2))$$

where the first-order term is

$$E^{\text{Rep}}(\mathscr{O}(S)) = -2\sum_{a \in A} \sum_{b \in B} S_{ab} \left\{ \sum_{c \in A} F_{ac}^A S_{cb} + \sum_{d \in B} F_{bd}^B S_{da} - 2T_{ab} \right\}$$

whereas the second-order term is

$$E^{\text{Rep}}(\mathscr{O}(S^2)) = 2\sum_{a \in A} \sum_{b \in B} S_{ab}^2 \left\{ \sum_{x \in A} \frac{-Z_x}{R_{xb}} + \sum_{y \in B} \frac{-Z_y}{R_{ya}} + \sum_{c \in A} \frac{2}{R_{bc}} + \sum_{d \in B} \frac{2}{R_{ad}} - \frac{1}{R_{ab}} \right\}$$

Thus derived repulsion energy is *not* invariant with respect to transformation of molecular orbitals, in contrast to Hayes-Stone's method and density-based method. It was shown that good results are obtained when using localized molecular orbitals, whereas using canonical molecular orbitals brings poor results.

In EFP2, exchange energy is approximated by spherical Gaussian approximation (SGO). The result of this is the following formula for the exchange energy:

$$E^{\mathrm{Ex}} pprox -4 \sum_{a \in A} \sum_{b \in B} \sqrt{\frac{-2 \ln |S_{ab}|}{\pi}} \frac{S_{ab}^2}{R_{ab}}$$

In all the above formulas,  $R_{ij}$  are distances between position vectors of \*i\*th and \*j\*th point. The LMO centroids are defined by

$$\mathbf{r}_a = (a|\mathbf{r}|a)$$

where a denotes the occupied molecular orbital.

## **OEP-Based Methods**

The Murrell et al's theory of Pauli repulsion for S-1 term and the Otto-Ladik's theory for S-2 term is here re-cast by introducing OEP's. The S-1 term is expressed via DF-OEP, whereas the S-2 term via ESP-OEP.

S-1 term (Murrell et al.)

The OEP reduction without any approximations leads to the following formula

$$E^{\text{Rep}}(\mathscr{O}(S^1)) = -2\sum_{a \in A}\sum_{b \in B}S_{ab}\left\{\sum_{\xi \in A}S_{b\xi}G_{\xi a}^A + \sum_{\eta \in B}S_{a\eta}G_{\eta b}^B\right\}$$

where the OEP matrices are given as

$$G_{\xi a}^{A} = \sum_{\xi' \in A} \left[ \mathbf{S}^{-1} \right]_{\xi \xi'} \sum_{\alpha \in A} \left\{ C_{\alpha a} V_{\alpha \xi'}^{A} + \sum_{\mu \nu \in A} \left[ 2C_{\alpha a} D_{\mu \nu} - C_{\nu a} D_{\alpha \mu} \right] (\alpha \xi' | \mu \nu) \right\}$$

and analogously for molecule *B*. Here, the nuclear attraction integrals are denoted by  $V_{\alpha\xi'}^A$ .

S-2 term (Otto-Ladik)

After the OEP reduction, this contribution under Otto-Ladik approximation has the following form:

$$E^{\text{Rep}}(\mathcal{O}(S^2)) = 2 \sum_{a \in A} \sum_{b \in B} S_{ab}^2 \left\{ \sum_{x \in A} q_{xa} V_{bb}^{(x)} + \sum_{y \in B} q_{yb} V_{aa}^{(y)} \right\}$$

where the ESP charges associated with each occupied molecular orbital reproduce the *effective potential* of molecule in question, i.e.,

$$\sum_{x \in A} \frac{q_{xa}}{|\mathbf{r} - \mathbf{r}_x|} \cong v_a^A(\mathbf{r})$$

where the potential is given by

$$v_a^A(\mathbf{r}) = \sum_{x \in A} \frac{-Z_x}{|\mathbf{r} - \mathbf{r}_x|} + 2\sum_{c \in A} \int \frac{\phi_c(\mathbf{r}')\phi_c(\mathbf{r}')}{|\mathbf{r} - \mathbf{r}'|} d\mathbf{r}' - \frac{1}{2} \int \frac{\phi_a(\mathbf{r}')\phi_a(\mathbf{r}')}{|\mathbf{r} - \mathbf{r}'|} d\mathbf{r}'$$

## 17.51.2 Member Function Documentation

17.51.2.1 double RepulsionEnergySolver::compute\_benchmark ( const std::string & method = "DEFAULT" )
[virtual]

Compute property by using benchmark method.

Each solver object has one DEFAULT benchmark method

**Parameters** 

method - benchmark method

Implements oepdev::OEPDevSolver.

17.51.2.2 double RepulsionEnergySolver::compute\_oep\_based ( const std::string & method = "DEFAULT" )
[virtual]

Compute property by using OEP's.

Each solver object has one DEFAULT OEP-based method.

**Parameters** 

method - flavour of OEP model

Implements oepdev::OEPDevSolver.

The documentation for this class was generated from the following files:

- oepdev/libutil/solver.h
- · oepdev/libutil/solver.cc

# 17.52 oepdev::RHFPerturbed Class Reference

RHF theory under electrostatic perturbation.

#include <scf\_perturb.h>

Inheritance diagram for oepdev::RHFPerturbed:

RHF
oepdev::RHFPerturbed

# **Public Member Functions**

RHFPerturbed (std::shared\_ptr< psi::Wavefunction > ref\_wfn, std::shared\_ptr< psi::SuperFunctional > functional)

Build from wavefunction and superfunctional.

• RHFPerturbed (std::shared\_ptr< psi::Wavefunction > ref\_wfn, std::shared\_ptr< psi::SuperFunctional > functional, psi::Options &options, std::shared\_ptr< psi::PSIO > psio)

Build from wavefunction and superfunctional + options and psio.

virtual ∼RHFPerturbed ()

Clear memory.

• virtual double compute\_energy ()

Compute total energy.

virtual void set\_perturbation (std::shared\_ptr< psi::Vector > field)

Perturb the system with external electric field.

• virtual void set\_perturbation (const double &fx, const double &fy, const double &fz)

This is an overloaded member function, provided for convenience. It differs from the above function only in what argument(s) it accepts.

virtual void set\_perturbation (std::shared\_ptr< psi::Vector > position, const double &charge)

Perturb the system with a point charge.

• virtual void set\_perturbation (const double &rx, const double &ry, const double &rz, const double &charge)

This is an overloaded member function, provided for convenience. It differs from the above function only in what argument(s) it accepts.

std::shared\_ptr< psi::Matrix > Vpert () const

Get a copy of the perturbation potential one-electron matrix.

· double nuclear\_interaction\_energy () const

Get the interaction energy of the nuclei with the perturbing potential.

## **Protected Member Functions**

• virtual void perturb Hcore ()

Add the electrostatic perturbation to the Hcore matrix.

# **Protected Attributes**

std::shared ptr< psi::Vector > perturbField

Perturbing electric field.

std::shared ptr< PerturbCharges > perturbCharges

Perturbing charges.

std::shared ptr< psi::Matrix > Vpert

Perturbation potential one-electron matrix.

double nuclearInteractionEnergy\_

Electrostatic interaction energy due to nuclei.

# 17.52.1 Detailed Description

RHF theory under electrostatic perturbation.

Compute RHF wavefunction under the following conditions:

- · external uniform electric field
- · set of point charges The mixed conditions can also be used.

Theory

The electrostatic perturbation is here understood as a distribution of external (generally non-uniform) electric field. It is assumed that this perturbation is one-electron in nature. Therefore, the one-electron Hamiltonian is changed according to the following

$$\mathbf{H}^{\text{core}} \to \mathbf{H}^{\text{core}} + \sum_{n} q_n \mathbf{V}^{(n)} - \mathbb{M} \cdot \mathbf{F}$$

where  $q_n$  is the external classical point charge,  $\mathbf{V}^{(n)}$  is the associated matrix of potential integrals,  $\mathbb{M}$  is the vector of dipole integrals and  $\mathbf{F}$  is an external uniform electric field. The total energy is then computed by performing an SCF procedure on the above one-electron Hamiltonian. The contribution due to nuclei is included, i.e.,

$$E_{\mathrm{Nuc}} \to E_{\mathrm{Nuc-Nuc}} + \sum_{In} \frac{q_n Z_I}{r_{In}} - \mu_{\mathrm{Nuc}} \cdot \mathbf{F}$$

where  $\mu_{\mathrm{Nuc}}$  is the nuclear dipole moment and  $Z_{l}$  is the atomic number of the Ith nucleus. It is added in the nuclear repulsion energy  $E_{\mathrm{Nuc-Nuc}}$  (note that the resulting energy can be negative as well depending on the electric field direction and configuration of point charges.

The documentation for this class was generated from the following files:

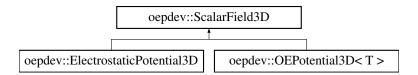
- · oepdev/libutil/scf perturb.h
- · oepdev/libutil/scf perturb.cc

# 17.53 oepdev::ScalarField3D Class Reference

Scalar field in 3D space. Abstract base.

#include <space3d.h>

Inheritance diagram for oepdev::ScalarField3D:



### **Public Member Functions**

- ScalarField3D (const int &np, const double &pad, psi::SharedWavefunction wfn, psi::Options &options)

  Construct potential on random grid by providing wavefunction.
- ScalarField3D (const int &nx, const int &ny, const int &nz, const double &px, const double &py, const double &px, std::shared\_ptr< psi::Wavefunction > wfn, psi::Options &options)

Construct potential on cube grid by providing wavefunction.

virtual ∼ScalarField3D ()

Destructor.

• virtual int npoints () const

Get the number of points at which the scalar field is defined.

- · virtual std::shared ptr
  - < PointsCollection3D > points\_collection () const

Get the collection of points.

- · virtual std::shared\_ptr
  - < psi::Matrix > data () const

Get the data matrix in a form  $\{[x, y, z, f(x, y, z)]\}$ .

```
virtual std::shared_ptr< psi::Wavefunction > wfn () const
```

Get the wavefunction.

· virtual bool is computed () const

Get the information if data is already computed or not.

virtual void compute ()

Compute the scalar field in each point from the point collection.

virtual double compute\_xyz (const double &x, const double &y, const double &z)=0

Compute a value of scalar field at point (x, y, z)

virtual void write\_cube\_file (const std::string &name)

Write the cube file (only for Cube collections, otherwise does nothing)

• virtual void print () const =0

Print information of the object to Psi4 output.

## **Static Public Member Functions**

• static shared\_ptr< ScalarField3D > build (const std::string &type, const int &np, const double &pad, psi::SharedWavefunction wfn, psi::Options &options)

Build scalar field of random points.

static shared\_ptr< ScalarField3D > build (const std::string &type, const int &nx, const int &ny, const int &nz, const double &px, const double &px, psi::SharedWavefunction wfn, psi::Options &options)

Build scalar field of points on a g09-cube grid.

#### **Protected Attributes**

```
    std::shared ptr
```

< PointsCollection3D > pointsCollection\_

Collection of points at which the scalar field is to be computed.

std::shared\_ptr< psi::Matrix > data\_

The data matrix in a form  $\{[x, y, z, f(x, y, z)]\}$ .

· std::shared\_ptr

< psi::Wavefunction > wfn\_

Wavefunction.

psi::Matrix geom

Geometry of a molecule.

std::shared\_ptr

< psi::IntegralFactory > fact\_

Integral factory.

std::shared\_ptr< psi::Matrix > pot\_

Matrix of potential one-electron integrals.

· std::shared\_ptr

< psi::OneBodyAOInt > oneInt\_

One-electron integral shared pointer.

std::shared\_ptr< PotentialInt > potInt\_

One-electron potential shared pointer.

std::shared\_ptr< psi::BasisSet > primary\_

Basis set.

int nbf

Number of basis functions.

bool isComputed\_

Has data already computed?

# 17.53.1 Detailed Description

Scalar field in 3D space. Abstract base.

Create scalar field defined at points distributed randomly or as an ordered g09 cube-like collection. Currently implemented scalar fields are:

- Electrostatic potential computes electrostatic potential (requires wavefunction)
- Template of generic classes compute custom scalar fields (requires generic object that is able to compute the field in 3D space)

**Note:** Always create instances by using static factory methods build. The following types of scalar field are currently implemented:

• ELECTROSTATIC POTENTIAL

#### 17.53.2 Member Function Documentation

17.53.2.1 std::shared\_ptr< ScalarField3D > oepdev::ScalarField3D::build ( const std::string & type, const int & np, const double & pad, psi::SharedWavefunction wfn, psi::Options & options ) [static]

Build scalar field of random points.

#### **Parameters**

type	- type of scalar field
np	- number of points
pad	- radius padding of a minimal sphere enclosing the molecule
wfn	- Psi4 Wavefunction containing the molecule
options	- Psi4 options

17.53.2.2 std::shared\_ptr< ScalarField3D > oepdev::ScalarField3D::build ( const std::string & type, const int & nx, const int & ny, const int & ny, const double & px, const double & py, const double & pz, psi::SharedWavefunction wfn, psi::Options & options ) [static]

Build scalar field of points on a g09-cube grid.

### **Parameters**

type	- type of scalar field
nx	- number of points along x direction
ny	- number of points along y direction
nz	- number of points along z direction
рх	- padding distance along x direction
ру	- padding distance along y direction
pz	- padding distance along z direction
wfn	- Psi4 Wavefunction containing the molecule
options	- Psi4 options

The documentation for this class was generated from the following files:

- · oepdev/lib3d/space3d.h
- · oepdev/lib3d/space3d.cc

# 17.54 oepdev::ShellCombinationsIterator Class Reference

Iterator for Shell Combinations. Abstract Base.

```
#include <integrals_iter.h>
```

Inheritance diagram for oepdev::ShellCombinationsIterator:

```
oepdev::ShellCombinationsIterator

oepdev::AllAOShellCombinationsIterator_2 oepdev::AllAOShellCombinationsIterator_4
```

# **Public Member Functions**

· ShellCombinationsIterator (int nshell)

Constructor.

virtual ∼ShellCombinationsIterator ()

Destructor.

virtual void first (void)=0

First iteration.

virtual void next (void)=0

Next iteration.

- · virtual std::shared ptr
  - < psi::BasisSet > bs\_1 (void) const

Grab the basis set of axis 1.

- · virtual std::shared\_ptr
  - < psi::BasisSet > bs\_2 (void) const

Grab the basis set of axis 2.

- virtual std::shared ptr
  - < psi::BasisSet > bs\_3 (void) const

Grab the basis set of axis 3.

- virtual std::shared ptr
  - < psi::BasisSet > bs 4 (void) const

Grab the basis set of axis 4.

virtual int P (void) const

Grab the current shell P index.

virtual int Q (void) const

Grab the current shell Q index.

virtual int R (void) const

Grab the current shell R index.

virtual int S (void) const

Grab the current shell S index.

virtual bool is\_done (void)

Return status of an iterator.

· virtual const int nshell (void) const

Return number of shells this iterator is for.

- · virtual std::shared\_ptr
  - < AOIntegralsIterator > ao\_iterator (std::string mode="ALL") const
- virtual void compute\_shell (std::shared\_ptr< oepdev::TwoBodyAOInt > tei) const =0
- virtual void compute\_shell (std::shared\_ptr< psi::TwoBodyAOInt > tei) const =0

## **Static Public Member Functions**

- · static std::shared ptr
  - < ShellCombinationsIterator > build (const IntegralFactory &ints, std::string mode="ALL", int nshell=4)

    Build shell iterator from oepdev::IntegralFactory.
- · static std::shared ptr
  - < ShellCombinationsIterator > build (std::shared\_ptr< IntegralFactory > ints, std::string mode="ALL", int nshell=4)

This is an overloaded member function, provided for convenience. It differs from the above function only in what argument(s) it accepts.

- · static std::shared ptr
  - < ShellCombinationsIterator > build (const psi::IntegralFactory &ints, std::string mode="ALL", int nshell=4)

    Build shell iterator from psi::IntegralFactory.
- · static std::shared ptr
  - < ShellCombinationsIterator > build (std::shared\_ptr< psi::IntegralFactory > ints, std::string mode="ALL", int nshell=4)

This is an overloaded member function, provided for convenience. It differs from the above function only in what argument(s) it accepts.

## **Protected Attributes**

SharedBasisSet bs 1

Basis set of axis 1.

SharedBasisSet bs 2

Basis set of axis 2.

SharedBasisSet bs 3

Basis set of axis 3.

SharedBasisSet bs\_4\_

Basis set of axis 4.

const int nshell\_

Number of shells this iterator is for.

· bool done

Status of an iterator.

# 17.54.1 Detailed Description

Iterator for Shell Combinations. Abstract Base.

Date

2018/03/01 17:22:00

# 17.54.2 Constructor & Destructor Documentation

17.54.2.1 ShellCombinationsIterator::ShellCombinationsIterator (int nshell)

Constructor.

**Parameters** 

nshell	- number of shells this iterator is for

### 17.54.3 Member Function Documentation

17.54.3.1 std::shared\_ptr< AOIntegralsIterator > ShellCombinationsIterator::ao\_iterator ( std::string mode = "ALL" ) const [virtual]

Make an AO integral iterator based on current shell

#### Parameters 4 8 1

mode	- either "ALL" or "UNIQUE" (iterate over all or unique integrals)

## Returns

iterator over AO integrals

17.54.3.2 std::shared\_ptr< ShellCombinationsIterator > ShellCombinationsIterator::build ( const IntegralFactory & ints, std::string mode = "ALL", int nshell = 4) [static]

Build shell iterator from oepdev::IntegralFactory.

#### **Parameters**

ints	- integral factory
mode	- mode of iteration (either ALL or UNIQUE)
nshell	- number of shells to iterate through

# Returns

shell iterator

## **Examples:**

example\_integrals\_iter.cc.

17.54.3.3 std::shared\_ptr< ShellCombinationsIterator > ShellCombinationsIterator::build ( const psi::IntegralFactory & ints, std::string mode = "ALL", int nshell = 4 ) [static]

Build shell iterator from psi::IntegralFactory.

### **Parameters**

ints	- integral factory
mode	- mode of iteration (either ALL or UNIQUE)
nshell	- number of shells to iterate through

### Returns

shell iterator

17.54.3.4 void ShellCombinationsIterator::compute\_shell ( std::shared\_ptr< oepdev::TwoBodyAOInt > tei ) const [pure virtual]

Compute integrals in a current shell. Works both for oepdev::TwoBodyAOInt and psi::TwoBodyAOInt

#### **Parameters**

tei - two body integral object

Implemented in oepdev::AllAOShellCombinationsIterator\_2, and oepdev::AllAOShellCombinationsIterator\_4.

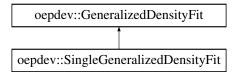
The documentation for this class was generated from the following files:

- · oepdev/libutil/integrals iter.h
- · oepdev/libutil/integrals\_iter.cc

# 17.55 oepdev::SingleGeneralizedDensityFit Class Reference

Generalized Density Fitting Scheme - Single Fit.

Inheritance diagram for oepdev::SingleGeneralizedDensityFit:



## **Public Member Functions**

- SingleGeneralizedDensityFit (std::shared\_ptr< psi::BasisSet > bs\_auxiliary, std::shared\_ptr< psi::Matrix > v\_vector)
- std::shared\_ptr< psi::Matrix > compute (void)
   Perform the generalized density fit.

### **Additional Inherited Members**

# 17.55.1 Detailed Description

Generalized Density Fitting Scheme - Single Fit.

The density fitting map projects the OEP onto the auxiliary, nearly complete basis set space through application of the resolution of identity. Refer to density fitting in complete space for more details.

## 17.55.2 Determination of the OEP matrix

Coefficients G are computed by using the following relation

$$\mathbf{G}^{(i)} = \mathbf{v}^{(i)} \cdot \mathbf{S}^{-1}$$

where

$$S_{\xi\eta}=(\xi|\eta)$$

$$v_{\xi}^{(i)} = (\xi \,|\, \hat{v}i)$$

In the above, | denotes the single integration over electron coordinate, i.e.,

$$(a|b) \equiv \int d\mathbf{r} \phi_a^*(\mathbf{r}) \phi_b(\mathbf{r})$$

whereas the spatial form of the potential operator  $\hat{v}$  can be expressed by

$$v(\mathbf{r}) \equiv \int d\mathbf{r}' \frac{\rho(\mathbf{r}')}{|\mathbf{r}' - \mathbf{r}|}$$

with  $\rho(\mathbf{r})$  being the effective one-electron density associated with  $\hat{v}$ .

# 17.55.3 Member Function Documentation

17.55.3.1 std::shared\_ptr< psi::Matrix > SingleGeneralizedDensityFit::compute ( void ) [virtual]

Perform the generalized density fit.

Returns

The OEP coefficients  $G_{\xi_i}$ 

Implements oepdev::GeneralizedDensityFit.

The documentation for this class was generated from the following files:

- oepdev/liboep/oep\_gdf.h
- oepdev/liboep/oep\_gdf.cc

# 17.56 oepdev::GeneralizedPolarGEFactory::StatisticalSet Struct Reference

A structure to handle statistical data.

#include <gefp.h>

# **Public Attributes**

• std::vector< double > InducedInteractionEnergySet

Interaction energy set.

- std::vector< std::shared\_ptr</li>
  - < psi::Matrix >> DensityMatrixSet

Density matrix set.

- std::vector< std::shared\_ptr</li>
  - < psi::Vector > > InducedDipoleSet

Induced dipole moment set.

- std::vector< std::shared\_ptr
  - < psi::Vector > > InducedQuadrupoleSet

Induced quadrupole moment set.

- std::vector< std::shared\_ptr
  - < psi::Matrix > > JKMatrixSet

Sum of J and K matrix set.

# 17.56.1 Detailed Description

A structure to handle statistical data.

The documentation for this struct was generated from the following file:

· oepdev/libgefp/gefp.h

# 17.57 oepdev::test::Test Class Reference

### Manages test routines.

```
#include <test.h>
```

#### **Public Member Functions**

Test (std::shared\_ptr< psi::Wavefunction > wfn, psi::Options &options)
 Construct the tester.

• ∼Test ()

Destructor.

· double run (void)

Pefrorm the test.

# **Protected Member Functions**

```
• double test_basic (void)
```

Test the basic functionalities of OEPDev.

double test cphf (void)

Test the CPHF method.

double test\_dmatPol (void)

Test the density matrix susceptibility (X = 1)

double test\_dmatPolX (void)

Test the density matrix susceptibility.

double test\_eri\_1\_1 (void)

Test the oepdev::ERI\_1\_1 class against psi::ERI.

double test\_eri\_2\_2 (void)

Test the oepdev::ERI\_2\_2 class against psi::ERI.

double test\_eri\_3\_1 (void)

Test the oepdev::ERI\_3\_1 class against psi::ERI.

double test\_unitaryOptimizer (void)

 ${\it Test the oepdev::} {\it UnitaryOptimizer class}.$ 

double test\_unitaryOptimizer\_4\_2 (void)

Test the oepdev::UnitaryOptimizer\_4\_2 class.

double test\_scf\_perturb (void)

Test the oepdev::RHFPerturbed class.

# **Protected Attributes**

```
std::shared_ptr
```

< psi::Wavefunction > wfn\_

Wavefunction object.

• psi::Options & options\_

Psi4 Options.

# 17.57.1 Detailed Description

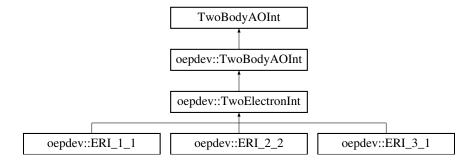
Manages test routines.

The documentation for this class was generated from the following files:

- · oepdev/libtest/test.h
- · oepdev/libtest/test.cc

# 17.58 oepdev::TwoBodyAOInt Class Reference

Inheritance diagram for oepdev::TwoBodyAOInt:



## **Public Member Functions**

- virtual void compute (std::shared\_ptr< psi::Matrix > &result, int ibs1=0, int ibs2=2)
   Compute two-body two-centre integral and put it into matrix.
- virtual void compute (psi::Matrix &result, int ibs1=0, int ibs2=2)
- virtual size t compute\_shell (int, int, int, int)=0
- virtual size\_t **compute\_shell** (int, int, int)=0
- virtual size t compute\_shell (int, int)=0
- virtual size t compute shell deriv1 (int, int, int, int)=0
- virtual size\_t compute\_shell\_deriv2 (int, int, int, int)=0
- virtual size\_t compute\_shell\_deriv1 (int, int, int)=0
- virtual size\_t compute\_shell\_deriv2 (int, int, int)=0
- virtual size\_t compute\_shell\_deriv1 (int, int)=0
- virtual size\_t compute\_shell\_deriv2 (int, int)=0

## **Protected Member Functions**

- TwoBodyAOInt (const IntegralFactory \*intsfactory, int deriv=0)
- TwoBodyAOInt (const TwoBodyAOInt &rhs)

## 17.58.1 Member Function Documentation

17.58.1.1 void oepdev::TwoBodyAOInt::compute ( std::shared\_ptr< psi::Matrix > & result, int ibs1 = 0, int ibs2 = 2 )

[virtual]

Compute two-body two-centre integral and put it into matrix.

# **Parameters**

result	- matrix where to store (i $  $ j) two-body integrals		
ibs1	- first basis set axis		
ibs2	- second basis set axis		

17.58.1.2 void oepdev::TwoBodyAOInt::compute ( psi::Matrix & result, int ibs1 = 0, int ibs2 = 2 ) [virtual]

This is an overloaded member function, provided for convenience. It differs from the above function only in what argument(s) it accepts.

The documentation for this class was generated from the following files:

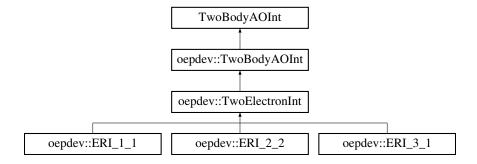
- · oepdev/libpsi/integral.h
- · oepdev/libpsi/integral.cc

# 17.59 oepdev::TwoElectronInt Class Reference

General Two Electron Integral.

#include <eri.h>

Inheritance diagram for oepdev::TwoElectronInt:



## **Public Member Functions**

- TwoElectronInt (const IntegralFactory \*integral, int deriv, bool use\_shell\_pairs)
- virtual size\_t compute\_shell (int, int)

Compute ERI's between 2 shells. Result is stored in buffer.

virtual size\_t compute\_shell (int, int, int)

Compute ERI's between 3 shells. Result is stored in buffer.

virtual size\_t compute\_shell (int, int, int, int)

Compute ERI's between 4 shells. Result is stored in buffer.

- virtual size\_t compute\_shell (const psi::AOShellCombinationsIterator &)
- virtual size\_t compute\_shell\_deriv1 (int, int)

Compute first derivatives of ERI's between 2 shells.

virtual size\_t compute\_shell\_deriv2 (int, int)

Compute second derivatives of ERI's between 2 shells.

· virtual size t compute shell deriv1 (int, int, int)

Compute first derivatives of ERI's between 3 shells.

• virtual size\_t compute\_shell\_deriv2 (int, int, int)

Compute second derivatives of ERI's between 3 shells.

virtual size\_t compute\_shell\_deriv1 (int, int, int, int)

Compute first derivatives of ERI's between 4 shells.

• virtual size\_t compute\_shell\_deriv2 (int, int, int, int)

Compute second derivatives of ERI's between 4 shells.

## **Protected Member Functions**

• int get\_cart\_am (int am, int n, int x)

Get the angular momentum per Cartesian component.

double get R (int N, int L, int M)

Get the (N,L,M)th McMurchie-Davidson coefficient.

virtual size\_t compute\_doublet (int, int)

Computes the ERI's between three shells.

virtual size\_t compute\_triplet (int, int, int)

Computes the ERI's between three shells.

virtual size t compute quartet (int, int, int, int)

Computes the ERI's between four shells.

### **Protected Attributes**

const int max am

Maximum angular momentum.

const int n\_max\_am\_

Maximum number of angular momentum functions.

psi::Fjt \* fjt\_

Computes the fundamental: Boys function value at T for degree v.

bool use shell pairs

Should we use shell pair information?

const double cartMap\_ [60]

Map of Cartesian components per each am.

· const double df\_ [8]

Double factorial array.

double \* mdh buffer R

Buffer for the McMurchie-Davidson-Hermite R coefficents.

## 17.59.1 Detailed Description

General Two Electron Integral.

Implements the McMurchie-Davidson recursive scheme for all integral types. The integral can be defined for any number of Gaussian centres, thus it is not limited to 2-by-2 four-centre ERI. Currently implemented subtypes are:

- oepdev::ERI\_1\_1 2-centre electron-repulsion integral (i|j)
- oepdev::ERI\_2\_2 4-centre electron-repulsion integral (ij|kl)
- oepdev::ERI\_3\_1 4-centre electron-repulsion integral (ijk|I)

### See Also

The Integral Package Library

## 17.59.2 Member Function Documentation

```
17.59.2.1 size_t oepdev::TwoElectronInt::compute_shell ( const psi::AOShellCombinationsIterator & shellIter )
[virtual]
```

Compute ERIs between 4 shells. Result is stored in buffer. Only for use with ERI\_2\_2 and the same basis sets, otherwise shell pairs won't be compatible.

The documentation for this class was generated from the following files:

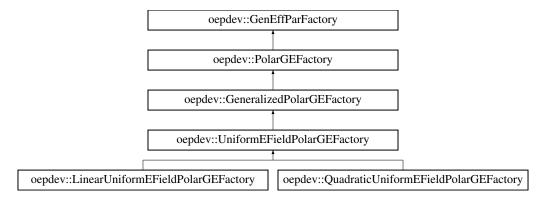
- · oepdev/libints/eri.h
- · oepdev/libints/eri.cc

# 17.60 oepdev::UniformEFieldPolarGEFactory Class Reference

Polarization GEFP Factory with Least-Squares Parameterization.

#include <gefp.h>

Inheritance diagram for oepdev::UniformEFieldPolarGEFactory:



#### **Public Member Functions**

- UniformEFieldPolarGEFactory (std::shared\_ptr< psi::Wavefunction > wfn, psi::Options &opt)
- void compute\_samples (void)

Compute samples of density matrices and select electric field distributions.

• virtual void compute\_gradient (int i, int j)=0

Compute Gradient vector associated with the i-th and j-th basis set function.

virtual void compute\_hessian (void)=0

Compute Hessian matrix (independent on the parameters)

## **Additional Inherited Members**

## 17.60.1 Detailed Description

Polarization GEFP Factory with Least-Squares Parameterization.

Implements a class of density matrix susceptibility models for parameterization in the uniform electric field.

The documentation for this class was generated from the following files:

- oepdev/libgefp/gefp.h
- · oepdev/libgefp/gefp\_polar\_uniform\_base.cc

# 17.61 oepdev::UnitaryOptimizer Class Reference

Find the optimim unitary matrix of quadratic matrix equation.

```
#include <unitary_optimizer.h>
```

## **Public Member Functions**

• UnitaryOptimizer (double \*R, double \*P, int n, double conv=1.0e-6, int maxiter=100, bool verbose=true)

Create from R and P matrices and optimization options.

• UnitaryOptimizer (std::shared\_ptr< psi::Matrix > R, std::shared\_ptr< psi::Vector > P, double conv=1.0e-6, int maxiter=100, bool verbose=true)

Create from R and P matrices and optimization options.

∼UnitaryOptimizer ()

Clear memory.

· bool maximize ()

Run the minimization.

• bool minimize ()

Run the maximization.

std::shared\_ptr< psi::Matrix > X ()

Get the unitary matrix (solution)

double \* get\_X () const

Get the unitary matrix (pointer to solution)

• double Z ()

Get the actual value of Z function.

• bool success () const

Get the status of the optimization.

#### **Protected Member Functions**

• UnitaryOptimizer (int n, double conv, int maxiter, bool verbose)

Initialize the basic memory.

void common\_init\_ ()

Prepare the optimizer.

• void run\_ (const std::string &opt)

Run the optimization (intermediate interface)

• void optimize\_ (const std::string &opt)

Run the optimization (inner interface)

void refresh\_ ()

Restore the initial state of the optimizer.

void update\_conv\_()

Update the convergence.

void update\_iter\_ ()

Update the iterates.

void update\_Z\_ ()

Update Z value.

void update\_RP\_ ()

Uptade R and P matrices.

void update\_X\_ ()

Update the solution matrix X.

double eval Z (double \*X, double \*R, double \*P)

Evaluate the objective Z function.

- double eval\_Z\_ ()
- double eval\_dZ\_ (double g, double \*R, double \*P, int i, int j)

Evaluate the change in Z.

• double eval\_Z\_trial\_ (int i, int j, double gamma)

Evaluate the trial Z value.

void form\_X0\_()

Create identity matrix.

void form\_X\_ (int i, int j, double gamma)

```
Form unitary matrix X (store in buffer Xnew_)

    void form_next_X_ (const std::string &opt)

          Form the next unitary matrix X.
    • ABCD get_ABCD_ (int i, int j)
          Retrieve ABCD parameters for root search.

    void find_roots_boyd_ (const ABCD &abcd)

          Solve for all roots of equation A*sin(g) + B*cos(g) + C*sin(2*g) + D*cos(2*g) = 0 -> implements Boyd's method.

    double find_root_halley_ (double x0, const ABCD &abcd)

          Solve for root of equation A*sin(g) + B*cos(g) + C*sin(2*g) + D*cos(2*g) = 0 -> implements Halley's method.
    • double find_gamma_ (const ABCD &abcd, int i, int j, const std::string &opt)
          Compute gamma from roots of base equations.
    • bool It_ (double a, double b)
          less-than function
    • bool gt_ (double a, double b)
          greater-than function

    double func_0_ (double g, const ABCD &abcd)

          Function f(gamma) = d(dZ)/dgamma.
    • double func_1_ (double g, const ABCD &abcd)
          Gradient of f(gamma)

    double func_2_ (double g, const ABCD &abcd)

          Hessian of f(gamma) - used only for Halley method (not implemented since Boyd method is more suitable here)
    std::shared_ptr< psi::Matrix > psi_X_ ()
          Form the Psi4 matrix with the transformation matrix.
Protected Attributes

 const int n

          Dimension of the problem.
    · const double conv_
          Convergence.

    const int maxiter

          Maximum number of iterations.

    const bool verbose

          Verbose mode.

    double * R

          R matrix.
    double * P
          P vector.

 double * R0

          Reference R matrix.
    double * P0_
          Reference P vector.
    double * X
          X Matrix (accumulated solution)

 double * W

          Work place.
    double * Xold_
```

Temporary X matrix.

Temporary X matrix.

double \* Xnew\_

int niter\_

Current number of iterations.

double S\_ [4]

Current solutions.

double Zinit

Initial Z value.

• double Zold\_

Old Z value.

double Znew\_

New Z value.

• double conv\_current\_

Current convergence.

bool success\_

Status of optimization.

## 17.61.1 Detailed Description

Find the optimim unitary matrix of quadratic matrix equation.

The objective function of the orthogonal matrix X

$$Z(\mathbf{X}) \equiv \sum_{ijkl} X_{ij} X_{kl} R_{jl} - \sum_{ij} X_{ij} P_j$$

is optimized by using the Jacobi iteration algorithm. In the above equation,  $\mathbf{R}$  is a square, general real matrix of size  $N \times N$  whereas  $\mathbf{P}$  is a real vector of length N.

Algorithm.

Optimization of X is factorized into a sequence of 2-dimensional rotations with one real parameter  $\gamma$ :

$$\mathbf{X}^{\text{New}} = \mathbf{U}(\gamma) \cdot \mathbf{X}^{\text{Old}}$$

where

$$\mathbf{U}(\gamma) \equiv egin{pmatrix} \ddots & & & & & & \\ & \cos(\gamma) & \cdots & \sin(\gamma) & & & \\ & \vdots & \ddots & \vdots & & \\ & -\sin(\gamma) & \cdots & \cos(\gamma) & & & & \\ & & & \ddots & & & \\ & & & & & \ddots \end{pmatrix}$$

is the Jacobi transformation matrix constructed for the Ith and Jth element from the entire N-dimensional set. For the sake of algirithmic simplicity, every iteration after  $\mathbf{U}(\gamma)$  has been formed,  $\mathbf{X}^{\mathrm{Old}}$  is for a while assumed to be an identity matrix and the  $\mathbf{R}$  matrix and  $\mathbf{P}$  vector are transformed according to the following formulae

$$\mathbf{R} \to \mathbf{U}\mathbf{R}\mathbf{U}^T$$
$$\mathbf{P} \to \mathbf{U}\mathbf{P}$$

The full transformation matrix is accumulated in the memory buffer until convergence.

In each iteration, the optimum angle  $\gamma$  is found as follows: First, the roots of the finite Fourier series

$$A\sin(\gamma) + B\cos(\gamma) + C\sin(2\gamma) + D\cos(2\gamma) = 0$$

are found. In the above equations, the expansion coefficients are given as

$$A = P_I + P_J - \sum_{k \neq I, J} (R_{Ik} + R_{Jk} + R_{kI} + R_{kJ})$$

$$B = P_I - P_J - \sum_{k \neq I, J} (R_{Ik} - R_{Jk} + R_{kI} - R_{kJ})$$

$$C = -2(R_{IJ} + R_{JI})$$

$$D = -2(R_{IJ} - R_{JJ})$$

and I,J are the chosen indices in the Jacobi iteration subspace. The roots are evaluated by applying the Boyd's method[1], in which they are given as

$$\gamma_n = \Re\left[-i\ln(\lambda_n)\right]$$

where  $\lambda_n$  is an eivenvalue of the following 4 by 4 complex matrix:

$$\begin{pmatrix} 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \\ -\frac{D+iC}{D-iC} & -\frac{B+iC}{D-iC} & 0 & -\frac{B-iC}{D-iC} \end{pmatrix}$$

Once the four roots of the Fourier series equation are found, one solution out of four is chosen which satisfies the global optimum condition, i.e., the largest increase/decrease in the objective function given by

$$\delta Z = A(1 - \cos(\gamma)) + B\sin(\gamma) + C\sin^2(\gamma) + \frac{D}{2}\sin(2\gamma)$$

The discrimination between the minimae/maximae is performed based on the evaluation of the Hessian of Z with respect to  $\gamma$ ,

$$\frac{\partial^2 Z}{\partial \gamma^2} = A\cos(\gamma) - B\sin(\gamma) + 2C\cos(2\gamma) - 2D\sin(2\gamma)$$

All the N(N-1)/2 unique pairs of molecular orbitals are checked and the optimal set of  $\gamma, I, J$  is chosen to construct  $\mathbf{X}^{\mathrm{New}}$ .

References:

[1] Boyd, J.P.; J. Eng. Math. (2006) 56, pp. 203-219

## 17.61.2 Constructor & Destructor Documentation

17.61.2.1 oepdev::UnitaryOptimizer::UnitaryOptimizer ( double \* R, double \* P, int n, double conv = 1.0e-6, int maxiter = 100, bool verbose = true )

Create from R and P matrices and optimization options.

## **Parameters**

R	- R matrix
Р	- P vector
n	- dimensionality of the problem ( $N$ )
conv	- convergence in the Z function
maxiter	- maximum number of iterations
verbose	- whether print information of iteration process or not Sets up the optimizer.

17.61.2.2 oepdev::UnitaryOptimizer::UnitaryOptimizer ( std::shared\_ptr< psi::Matrix > R, std::shared\_ptr< psi::Vector > P, double conv = 1 . 0e-6, int maxiter = 100, bool verbose = true )

Create from R and P matrices and optimization options.

#### **Parameters**

R	- R matrix
Р	- P vector
conv	- convergence in the ${\it Z}$ function
maxiter	- maximum number of iterations
verbose	- whether print information of iteration process or not Sets up the optimizer.

17.61.2.3 oepdev::UnitaryOptimizer::UnitaryOptimizer ( int n, double conv, int maxiter, bool verbose ) [protected]

Initialize the basic memory.

## **Parameters**

n	- dimensionality of the problem ( $N$ )
conv	- convergence in the Z function
maxiter	- maximum number of iterations
verbose	- whether print information of iteration process or not Sets up the optimizer.

The documentation for this class was generated from the following files:

- · oepdev/libutil/unitary\_optimizer.h
- · oepdev/libutil/unitary\_optimizer.cc

# 17.62 oepdev::UnitaryOptimizer\_4\_2 Class Reference

Find the optimim unitary matrix for quartic-quadratic matrix equation with trace.

#include <unitary\_optimizer.h>

## **Public Member Functions**

- UnitaryOptimizer\_4\_2 (double \*R, double \*P, int n, double conv=1.0e-6, int maxiter=100, bool verbose=true)

  Create from R and P matrices and optimization options.
- ∼UnitaryOptimizer\_4\_2 ()

Clear memory.

• bool maximize ()

Run the minimization.

• bool minimize ()

Run the maximization.

•  $std::shared\_ptr < psi::Matrix > X ()$ 

Get the unitary matrix (solution)

double \* get\_X () const

Get the unitary matrix (pointer to solution)

• double Z ()

Get the actual value of Z function.

• bool success () const

Get the status of the optimization.

## **Protected Member Functions**

```
    UnitaryOptimizer_4_2 (int n, double conv, int maxiter, bool verbose)

      Initialize the basic memory.
void common_init_ ()
     Prepare the optimizer.

    void run (const std::string &opt)

      Run the optimization (intermediate interface)

    void optimize_ (const std::string &opt)

      Run the optimization (inner interface)
• void refresh_()
      Restore the initial state of the optimizer.
void update_conv_ ()
      Update the convergence.
void update_iter_()
      Update the iterates.
void update_Z_ ()
      Update Z value.
void update_RP_()
      Uptade R and P matrices.

    void update_X_ ()

      Update the solution matrix X.

    double eval_Z_ (double *X, double *R, double *P)

      Evaluate the objective Z function.

    double eval_Z_()

    double eval_dZ_ (double g, double *R, double *P, int I, int J)

      Evaluate the change in Z.

    double eval_Z_trial_ (int I, int J, double gamma)

      Evaluate the trial Z value.

    void form_X0_()

      Create identity matrix.

    void form X (int I, int J, double gamma)

      Form unitary matrix X (store in buffer Xnew )

    void form_next_X_ (const std::string &opt)

     Form the next unitary matrix X.

    Fourier9 get_fourier_ (int I, int J)

      Retrieve ABCD parameters for root search.

    void find_roots_boyd_ (const Fourier9 &abcd)

      Solve for all roots of equation A*sin(g) + B*cos(g) + C*sin(2*g) + D*cos(2*g) = 0 -> implements Boyd's method.

    double find_root_halley_ (double x0, const Fourier9 &abcd)

      Solve for root of equation A*sin(g) + B*cos(g) + C*sin(2*g) + D*cos(2*g) = 0 -> implements Halley's method.

    double find_gamma_ (const Fourier9 &abcd, int i, int j, const std::string &opt)

      Compute gamma from roots of base equations.
• bool It_ (double a, double b)
     less-than function

    bool gt_ (double a, double b)

     greater-than function

    std::shared ptr< psi::Matrix > psi X ()

      Form the Psi4 matrix with the transformation matrix.
```

# **Protected Attributes**

const int n

Dimension of the problem.

const double conv

Convergence.

· const int maxiter\_

Maximum number of iterations.

const bool verbose

Verbose mode.

double \* R\_

R tensor.

double \* P\_

P tensor.

double \* R0

Reference R tensor.

double \* P0\_

Reference P tensor.

double \* X\_

X Matrix (accumulated solution)

• double \* W\_

Work place.

double \* Xold\_

Temporary X matrix.

double \* Xnew

Temporary X matrix.

int niter\_

Current number of iterations.

double S\_ [8]

Current solutions.

double Zinit\_

Initial Z value.

• double Zold\_

Old Z value.

double Znew

New Z value.

double conv\_current\_

Current convergence.

· bool success\_

Status of optimization.

# 17.62.1 Detailed Description

Find the optimim unitary matrix for quartic-quadratic matrix equation with trace.

The objective function of the orthogonal matrix  $\boldsymbol{X}$ 

$$Z(\mathbf{X}) \equiv \sum_{ijklmn} X_{ki} X_{lj} X_{mi} X_{nj} R_{ijklmn} + \sum_{ijk} X_{ji} X_{ki} P_{ijk}$$

is optimized by using the Jacobi iteration algorithm. In the above equation,  $\mathbf{R}$  is a general real sixth-rank tensor of size  $N^6$  whereas  $\mathbf{P}$  is a general real third-rank tensor of size  $N^3$ .

Algorithm.

Optimization of X is factorized into a sequence of 2-dimensional rotations with one real parameter  $\gamma$ :

$$\mathbf{X}^{\text{New}} = \mathbf{X}^{\text{Old}} \cdot \mathbf{U}(\gamma)$$

where

$$\mathbf{U}(\gamma) \equiv egin{pmatrix} \ddots & & & & & & \\ & \cos(\gamma) & \cdots & \sin(\gamma) & & & \\ & \vdots & \ddots & \vdots & & \\ & -\sin(\gamma) & \cdots & \cos(\gamma) & & & \ddots \end{pmatrix}$$

is the Jacobi transformation matrix constructed for the Ith and Jth element from the entire N-dimensional set. For the sake of algirithmic simplicity, every iteration after  $\mathbf{U}(\gamma)$  has been formed,  $\mathbf{X}^{Old}$  is for a while assumed to be an identity matrix and the  $\mathbf{R}$  as well as  $\mathbf{P}$  tensors are transformed according to the following formulae

$$R_{ijklmn} 
ightarrow \sum_{k'l'm'n'} R_{ijk'l'm'n'} X_{k'k} X_{l'l} X_{m'm} X_{n'n} \ P_{ijk} 
ightarrow \sum_{i'k'} P_{ij'k'} X_{j'j} X_{k'k}$$

The full transformation matrix is accumulated in the memory buffer until convergence.

In each iteration, the optimum angle  $\gamma$  is found as follows: First, the roots of the finite Fourier series

$$a_0 + \sum_{p=1}^{4} \left\{ a_p \cos(px) + b_p \sin(px) \right\} = 0$$

are found. In the above equations, the expansion coefficients are calculated analytically as a function of I, J - the chosen indices in the Jacobi iteration subspace. The roots are evaluated by applying the Boyd's method[1], in which they are given as

$$\gamma_n = \Re\left[-i\ln(\lambda_n)\right]$$

where  $\lambda_n$  is an eivenvalue of the following 8 by 8 complex matrix:

1	0	1	0	0	0	0	0	0	\
1	0	0	1	0	0	0	0	0	1
1	0	0	0	1	0	0	0	0	1
1	0	0	0	0	1	0	0	0	
1	0	0	0	0	0	1	0	0	
1	0	0	0	0	0	0	1	0	
\.	$-\frac{a_4+ib_4}{a_4-ib_4}$	$-\frac{a_3+ib_3}{a_4-ib_4}$	$-\frac{a_2+ib_2}{a_4-ib_4}$	$-\frac{a_1+ib_1}{a_4-ib_4}$	$-\frac{2a_0}{a_4-ib_4}$	$-\frac{a_1-ib_1}{a_4-ib_4}$	$-\frac{a_2-ib_2}{a_4-ib_4}$	$-\frac{a_3-ib_3}{a_4-ib_4}$	

Once the eight roots of the Fourier series equation are found, one solution out of eight is chosen which satisfies the global optimum condition, i.e., the largest increase/decrease in the objective function given by

$$\delta Z = Z(\mathbf{U}(\gamma)) - Z(\mathbf{1})$$

The Hessian is not computed. All the N(N-1)/2 unique pairs of molecular orbitals are checked and the optimal set of  $\gamma, I, J$  is chosen to construct  $\mathbf{X}^{\mathrm{New}}$ .

References:

[1] Boyd, J.P.; J. Eng. Math. (2006) 56, pp. 203-219

# 17.62.2 Constructor & Destructor Documentation

17.62.2.1 oepdev::UnitaryOptimizer\_4\_2::UnitaryOptimizer\_4\_2 ( double \* R, double \* P, int n, double conv = 1 . 0e-6, int maxiter = 100, bool verbose = true )

Create from R and P matrices and optimization options.

#### **Parameters**

R	- R tensor (flattened row-wise)
Р	- P tensor (flattened row-wise)
n	- dimensionality of the problem ( $N$ )
conv	- convergence in the ${\it Z}$ function
maxiter	- maximum number of iterations
verbose	- whether print information of iteration process or not Sets up the optimizer.

17.62.2.2 oepdev::UnitaryOptimizer\_4\_2::UnitaryOptimizer\_4\_2 ( int *n*, double *conv*, int *maxiter*, bool *verbose* )

[protected]

Initialize the basic memory.

## **Parameters**

n	- dimensionality of the problem ( $N$ )
conv	- convergence in the $Z$ function
maxiter	- maximum number of iterations
verbose	- whether print information of iteration process or not Sets up the optimizer.

The documentation for this class was generated from the following files:

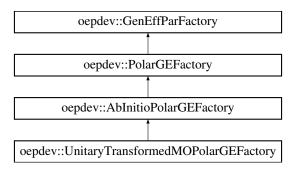
- · oepdev/libutil/unitary\_optimizer.h
- · oepdev/libutil/unitary\_optimizer.cc

# 17.63 oepdev::UnitaryTransformedMOPolarGEFactory Class Reference

Polarization GEFP Factory with Least-Squares Scaling of MO Space.

#include <gefp.h>

Inheritance diagram for oepdev::UnitaryTransformedMOPolarGEFactory:



# **Public Member Functions**

- UnitaryTransformedMOPolarGEFactory (std::shared\_ptr< psi::Wavefunction > wfn, psi::Options & opt)
   Construct from CPHF object and Psi4 options.
- $\bullet \ \, \text{virtual} \sim \! \text{UnitaryTransformedMOPolarGEFactory ()} \\$

Destruct.

std::shared\_ptr< GenEffPar > compute (void)

Pefrorm Least-Squares Fit.

## **Additional Inherited Members**

# 17.63.1 Detailed Description

Polarization GEFP Factory with Least-Squares Scaling of MO Space.

Implements creation of the density matrix susceptibility tensors for which  $X \neq 1$ . Guarantees the idempotency of the density matrix up to first-order in LCAO-MO variation.

Note

This method does not give better results than the X=1 method and is extremely time and memory consuming. Therefore, it is placed here only for future reference about solving unitary optimization problem in case it occurs.

The documentation for this class was generated from the following files:

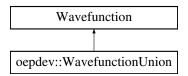
- · oepdev/libgefp/gefp.h
- oepdev/libgefp/gefp\_polar\_abinitio.cc

# 17.64 oepdev::WavefunctionUnion Class Reference

Union of two Wavefunction objects.

```
#include <wavefunction_union.h>
```

Inheritance diagram for oepdev::WavefunctionUnion:



# **Public Member Functions**

WavefunctionUnion (SharedWavefunction ref\_wfn, Options & options)

Constructor.

virtual ∼WavefunctionUnion ()

Destructor.

• virtual double compute\_energy ()

Compute Energy (now blank)

virtual double nuclear\_repulsion\_interaction\_energy ()

Compute Nuclear Repulsion Energy between unions.

• void localize orbitals ()

Localize Molecular Orbitals.

void transform\_integrals ()

Transform Integrals (2- and 4-index transformations)

• int I\_nmo (int n) const

Get number of molecular orbitals of the \*n\*th fragment.

• int I\_nso (int n) const

Get number of symmetry orbitals of the \*n\*th fragment.

• int l\_ndocc (int n) const

Get number of doubly occupied orbitals of the \*n\*th fragment.

int l\_nvir (int n) const

Get number of virtual orbitals of the \*n\*th fragment.

int l\_nalpha (int n) const

Get the number of the alpha electrons of the \*n\*th fragment.

int l\_nbeta (int n) const

Get the number of the beta electrons of the \*n\*th fragment.

• int I nbf (int n) const

Get number of basis functions of the \*n\*th fragment.

• int l\_noffs\_ao (int n) const

Get the basis set offset of the \*n\*th fragment.

· double I energy (int n) const

Get the reference energy of the \*n\*th fragment.

SharedMolecule | molecule (int n) const

Get the molecule object of the \*n\*th fragment.

SharedBasisSet I primary (int n) const

Get the primary basis set object of the \*n\*th fragment.

SharedBasisSet I auxiliary (int n) const

Get the auxiliary basis set object of the \*n\*th fragment.

• SharedBasisSet I intermediate (int n) const

Get the intermediate basis set object of the \*n\*th fragment.

• SharedWavefunction I wfn (int n) const

Get the wavefunction object of the \*n\*th fragment.

• SharedMOSpace I\_mospace (int n, const std::string &label) const

Get the MO space named label (either OCC or VIR) of the \*n\*th fragment.

• SharedLocalizer l\_localizer (int n) const

Get the orbital localizer object of the \*n\*th fragment.

· SharedIntegralTransform integrals (void) const

Get the integral transform object of the entire union.

bool has\_localized\_orbitals (void) const

If union got its molecular orbital localized or not.

· SharedBasisSet primary (void) const

Get the primary basis set for the entire union.

• SharedMOSpace mospace (const std::string &label) const

Get the MO space named label (either OCC or VIR)

- SharedMatrix Ca\_subset (const std::string &basis="SO", const std::string &subset="ALL")
- SharedMatrix Cb\_subset (const std::string &basis="SO", const std::string &subset="ALL")
- SharedMatrix C\_subset\_helper (SharedMatrix C, const Dimension &noccpi, SharedVector epsilon, const std::string &basis, const std::string &subset)

Helpers for Ca\_ and Cb\_ matrix transformers.

SharedVector epsilon\_subset\_helper (SharedVector epsilon, const Dimension &noccpi, const std::string &basis, const std::string &subset)

Helper for epsilon transformer.

void print\_header (void)

Print information about this wavefunction union.

void print\_mo\_integrals (void)

Print the MO ingegrals.

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#### **Protected Attributes**

int nlsolatedMolecules\_

Number of isolated molecules.

SharedWavefunction dimer\_wavefunction\_

The wavefunction for a dimer (electrons relaxed in the field of monomers)

· SharedIntegralTransform integrals\_

Integral transform object (2- and 4-index transformations)

· bool hasLocalizedOrbitals\_

whether orbitals of the union were localized (or not)

std::map< const std::string,</li>

SharedMOSpace > mospacesUnion\_

Dictionary of MO spaces for the entire union (OCC and VIR)

std::vector< SharedMolecule > I\_molecule\_

List of molecules.

std::vector< SharedBasisSet > I primary

List of primary basis functions per molecule.

std::vector< SharedBasisSet > I auxiliary

List of auxiliary basis functions per molecule.

std::vector < SharedBasisSet > I\_intermediate\_

List of intermediate basis functions per molecule.

std::vector < SharedWavefunction > I wfn

List of original isolated wavefunctions (electrons unrelaxed)

std::vector< std::string > I name

List of names of isolated wavefunctions.

std::vector< int > I nbf

List of basis function numbers per molecule.

std::vector< int > I nmo

List of numbers of molecular orbitals (MO's) per molecule.

std::vector< int > l\_nso\_

List of numbers of SO's per molecule.

std::vector< int > l\_ndocc\_

List of numbers of doubly occupied orbitals per molecule.

std::vector< int > I\_nvir\_

List of numbers of virtual orbitals per molecule.

std::vector< int > l\_noffs\_ao\_

List of basis set offsets per molecule.

std::vector< double > l\_energy\_

List of energies of isolated wavefunctions.

•  $std::vector < double > l_efzc_$ 

List of frozen-core energies per isolated wavefunction.

std::vector< bool > l\_density\_fitted\_

List of information per wfn whether it was obtained using DF or not.

std::vector< int > l\_nalpha\_

List of numbers of alpha electrons per isolated wavefunction.

std::vector< int > l\_nbeta\_

List of numbers of beta electrons per isolated wavefunction.

std::vector< int > I nfrzc

List of numbers of frozen-core orbitals per isolated molecule.

std::vector < SharedLocalizer > I\_localizer\_

List of orbital localizers.

std::vector< std::map< const</li>

std::string, SharedMOSpace > > I\_mospace\_

List of dictionaries of MO spaces.

## 17.64.1 Detailed Description

Union of two Wavefunction objects.

The WavefunctionUnion is the union of two unperturbed Wavefunctions.

#### Notes:

- 1. Works only for C1 symmetry! Therefore this->nirrep() = 1.
- 2. Does not set reference\_wavefunction\_
- 3. Sets oeprop\_ for the union of uncoupled molecules
- 4. Performs Hadamard sums on H\_, Fa\_, Da\_, Ca\_ and S\_ based on uncoupled wavefunctions.
- 5. Since it is based on shallow copy of the original Wavefunction, it **changes** contents of this wavefunction. Reallocate and copy if you want to keep the original wavefunction.

#### Warnings:

- 1. Gradients, Hessians and frequencies are not touched, hence they are wrong!
- 2. Lagrangian (if present) is not touched, hence its wrong!
- Ca/Cb and epsilon subsets were reimplemented from psi::Wavefunction to remove sorting of orbitals. However, the corresponding member functions are not virtual in psi::Wavefunction. This could bring problems when upcasting.

The following variables are *shallow* copies of variables inside the Wavefunction object, that is created for the *whole* molecule cluster:

- basissets\_(DF/RI/F12/etc basis sets)\_
- basisset\_(ORBITAL basis set)
- sobasisset\_ (Primary basis set for SO integrals)
- AO2SO\_ (AO2SO conversion matrix (AO in rows, SO in cols)
- molecule (Molecule that this wavefunction is run on)
- options\_(Options object)
- psio\_ (PSI file access variables)
- integral\_(Integral factory)
- factory\_ (Matrix factory for creating standard sized matrices)
- memory\_ (How much memory you have access to)
- nalpha\_, nbeta\_ (Total alpha and beta electrons)
- nfrzc\_ (Total frozen core orbitals)
- doccpi\_ (Number of doubly occupied per irrep)
- soccpi\_ (Number of singly occupied per irrep)
- frzcpi\_ (Number of frozen core per irrep)
- frzvpi\_ (Number of frozen virtuals per irrep)
- nalphapi\_(Number of alpha electrons per irrep)
- nbetapi\_ (Number of beta electrons per irrep)

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- nsopi\_ (Number of so per irrep)
- nmopi\_ (Number of mo per irrep)
- nso\_(Total number of SOs)
- nmo\_ (Total number of MOs)
- nirrep\_(Number of irreps; must be equal to 1 due to symmetry reasons)
- same\_a\_b\_dens\_ and same\_a\_b\_orbs\_ The rest is altered so that the Wavefunction parameters reflect a cluster of non-interacting (uncoupled, isolated, unrelaxed) molecular electron densities.

#### 17.64.2 Constructor & Destructor Documentation

17.64.2.1 oepdev::WavefunctionUnion::WavefunctionUnion ( SharedWavefunction ref\_wfn, Options & options )

#### Constructor.

Provide wavefunction with molecule containing at least 2 fragments.

#### **Parameters**

ref_wfn	- reference wavefunction
options	- Psi4 options

#### 17.64.3 Member Function Documentation

17.64.3.1 SharedMatrix oepdev::WavefunctionUnion::Ca\_subset ( const std::string & basis = "SO", const std::string & subset = "ALL")

Return a subset of the Ca matrix in a desired basis

#### **Parameters**

basis	the symmetry basis to use AO, SO
subset	the subset of orbitals to return ALL, ACTIVE, FROZEN, OCC, VIR, FROZEN_OCC, ACTIV-
	E_OCC, ACTIVE_VIR, FROZEN_VIR

#### Returns

the matrix in Pitzer order in the desired basis

17.64.3.2 SharedMatrix oepdev::WavefunctionUnion::Cb\_subset ( const std::string & basis = "SO", const std::string & subset = "ALL" )

Return a subset of the Cb matrix in a desired basis

## **Parameters**

basis	the symmetry basis to use AO, SO
subset	the subset of orbitals to return ALL, ACTIVE, FROZEN, OCC, VIR, FROZEN_OCC, ACTIV-
	E_OCC, ACTIVE_VIR, FROZEN_VIR

#### Returns

the matrix in Pitzer order in the desired basis

The documentation for this class was generated from the following files:

- oepdev/libutil/wavefunction\_union.h
- oepdev/libutil/wavefunction\_union.cc

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# **Chapter 18**

# **File Documentation**

# 18.1 include/oepdev\_files.h File Reference

#### **Macros**

• #define OEPDEV\_USE\_PSI4\_DIIS\_MANAGER 0

Use DIIS from Psi4 (1) or OEPDev (0)?

• #define OEPDEV\_MAX\_AM 8

L max.

• #define OEPDEV\_N\_MAX\_AM 17

2L\_max+1

• #define OEPDEV\_CRIT\_ERI 1e-9

ERI criterion for E12, E34, E123 and lambda\*EXY coefficients.

• #define OEPDEV\_SIZE\_BUFFER\_R 250563

Size of R buffer (OEPDEV\_N\_MAX\_AM\*OEPDEV\_N\_MAX\_AM\*OEPDEV\_N\_MAX\_AM\*3)

• #define OEPDEV\_SIZE\_BUFFER\_D2 3264

Size of D2 buffer (3\*(OEPDEV\_MAX\_AM+1)\*(OEPDEV\_MAX\_AM+1)\*OEPDEV\_N\_MAX\_AM)

# 18.2 include/oepdev\_options.h File Reference

# **Namespaces**

• psi

Psi4 package namespace.

## **Functions**

• int psi::read\_options (std::string name, Options &options)

Options for the OEPDev plugin.

## 18.3 main.cc File Reference

```
#include <string>
#include "include/oepdev_files.h"
#include "psi4/liboptions/liboptions.h"
#include "psi4/libmints/wavefunction.h"
#include "include/oepdev_options.h"
#include "oepdev/liboep/oep.h"
#include "oepdev/libgefp/gefp.h"
#include "oepdev/libutil/wavefunction_union.h"
#include "oepdev/libutil/solver.h"
#include "oepdev/libtest/test.h"
```

## **Namespaces**

• psi

Psi4 package namespace.

## **Typedefs**

- using SharedWavefunction = std::shared\_ptr< psi::Wavefunction >
- using SharedUnion = std::shared\_ptr< oepdev::WavefunctionUnion >
- using SharedOEPotential = std::shared\_ptr< oepdev::OEPotential >
- using **SharedGEFPFactory** = std::shared\_ptr< oepdev::GenEffParFactory >
- using **SharedGEFPParameters** = std::shared\_ptr< oepdev::GenEffPar >

#### **Functions**

• SharedWavefunction psi::oepdev (SharedWavefunction ref\_wfn, Options & options)

Main routine of the OEPDev plugin.

# 18.4 oepdev/lib3d/esp.h File Reference

```
#include "psi4/libmints/vector.h"
#include "space3d.h"
```

## **Classes**

· class oepdev::ESPSolver

Charges from Electrostatic Potential (ESP). A solver-type class.

#### **Namespaces**

• psi

Psi4 package namespace.

· oepdev

## **Typedefs**

- using psi::SharedVetor = std::shared\_ptr< Vector >
- using oepdev::SharedScalarField3D = std::shared\_ptr< ScalarField3D >

# 18.5 oepdev/libgefp/gefp.h File Reference

```
#include <vector>
#include <string>
#include <random>
#include <cmath>
#include "psi4/libmints/wavefunction.h"
#include "psi4/libmints/matrix.h"
#include "psi4/libmints/vector.h"
#include "psi4/libmints/vector3.h"
#include "../liboep/oep.h"
#include "../libutil/util.h"
#include "../libutil/cphf.h"
#include "../libutil/scf_perturb.h"
```

## Classes

class oepdev::GenEffPar

Generalized Effective Fragment Parameters. Container Class.

class oepdev::GenEffFrag

Generalized Effective Fragment. Container Class.

· class oepdev::GenEffParFactory

Generalized Effective Fragment Factory. Abstract Base.

class oepdev::PolarGEFactory

Polarization GEFP Factory. Abstract Base.

· class oepdev::AbInitioPolarGEFactory

Polarization GEFP Factory from First Principles. Hartree-Fock Approximation.

class oepdev::FFAbInitioPolarGEFactory

Polarization GEFP Factory from First Principles: Finite-Difference Model. Arbitrary level of theory.

• class oepdev::GeneralizedPolarGEFactory

Polarization GEFP Factory with Least-Squares Parameterization.

struct oepdev::GeneralizedPolarGEFactory::StatisticalSet

A structure to handle statistical data.

class oepdev::UniformEFieldPolarGEFactory

Polarization GEFP Factory with Least-Squares Parameterization.

· class oepdev::NonUniformEFieldPolarGEFactory

Polarization GEFP Factory with Least-Squares Parameterization.

class oepdev::LinearUniformEFieldPolarGEFactory

Polarization GEFP Factory with Least-Squares Parameterization.

· class oepdev::QuadraticUniformEFieldPolarGEFactory

Polarization GEFP Factory with Least-Squares Parameterization.

class oepdev::LinearNonUniformEFieldPolarGEFactory

Polarization GEFP Factory with Least-Squares Parameterization.

class oepdev::QuadraticNonUniformEFieldPolarGEFactory

Polarization GEFP Factory with Least-Squares Parameterization.

• class oepdev::LinearGradientNonUniformEFieldPolarGEFactory

Polarization GEFP Factory with Least-Squares Parameterization.

• class oepdev::QuadraticGradientNonUniformEFieldPolarGEFactory

Polarization GEFP Factory with Least-Squares Parameterization.

class oepdev::UnitaryTransformedMOPolarGEFactory

Polarization GEFP Factory with Least-Squares Scaling of MO Space.

## **Namespaces**

oepdev

OEPDev module namespace.

## 18.6 oepdev/libints/eri.h File Reference

```
#include "psi4/libpsi4util/exception.h"
#include "psi4/libmints/integral.h"
#include "psi4/libmints/basisset.h"
#include "psi4/libmints/fjt.h"
#include "../libpsi/integral.h"
#include "recurr.h"
```

#### Classes

```
    class oepdev::TwoElectronInt
```

General Two Electron Integral.

```
class oepdev::ERI_1_1
```

2-centre ERI of the form (a|O(2)|b) where O(2) = 1/r12.

class oepdev::ERI\_2\_2

4-centre ERI of the form (ab|O(2)|cd) where O(2) = 1/r12.

class oepdev::ERI\_3\_1

4-centre ERI of the form (abc|O(2)|d) where O(2) = 1/r12.

## **Namespaces**

oepdev

OEPDev module namespace.

## 18.7 oepdev/libints/recurr.h File Reference

## **Namespaces**

· oepdev

#### **Macros**

• #define D1\_INDEX(x, i, n) ((81\*(x))+(9\*(i))+(n))

Get the index of McMurchie-Davidson-Hermite D1 coefficient stored in the mdh\_buffer\_, that is attributed to the x Cartesian coordinate from angular momentum i of function 1, and the Hermite index n.

#define D2\_INDEX(x, i, j, n) ((1377\*(x))+(153\*(i))+(17\*(j))+(n))

Get the index of McMurchie-Davidson-Hermite D2 coefficient stored in the mdh\_buffer\_, that is attributed to the x Cartesian coordinate from angular momenta i, j of function 1 and 2, and the Hermite index n.

#define D3 INDEX(x, i, j, k, n) ((18225\*(x))+(2025\*(i))+(225\*(j))+(25\*(k))+(n))

Get the index of McMurchie-Davidson-Hermite D3 coefficient stored in the  $mdh\_buffer\_$ , that is attributed to the x Cartesian coordinate from angular momenta i, j and k of function 1, 2 and 3, and the Hermite index n.

• #define R\_INDEX(n, I, m, j) ((14739\*(n))+(867\*(l))+(51\*(m))+(j))

Get the index of McMurchie-Davidson R coefficient stored in the mdh\_buffer\_R\_ from angular momenta n, I and m and the Boys index j.

#### **Functions**

• double oepdev::d\_N\_n1\_n2 (int N, int n1, int n2, double PA, double PB, double aP)

Compute McMurchie-Davidson-Hermite (MDH) coefficient for binomial expansion.

• void oepdev::make mdh D1 coeff (int n1, double aPd, double \*buffer)

Compute the McMurchie-Davidson-Hermite coefficients for monomial expansion.

• void oepdev::make\_mdh\_D2\_coeff (int n1, int n2, double aPd, double \*PA, double \*PB, double \*buffer)

Compute the McMurchie-Davidson-Hermite coefficients for binomial expansion.

• void oepdev::make\_mdh\_D3\_coeff (int n1, int n2, int n3, double aPd, double \*PA, double \*PB, double \*PC, double \*buffer)

Compute the McMurchie-Davidson-Hermite coefficients for trinomial expansion.

• void oepdev::make\_mdh\_D2\_coeff\_explicit\_recursion (int n1, int n2, double aP, double \*PA, double \*PB, double \*buffer)

Compute the McMurchie-Davidson-Hermite coefficients for binomial expansion by explicit recursion. This function makes the same changes to buffers as oepdev::make\_mdh\_D2\_coeff, but implements it through explicit recursion by calls to oepdev::d N n1 n2. Therefore, it is slightly slower. Here for debugging purposes.

• void oepdev::make\_mdh\_R\_coeff (int N, int L, int M, double alpha, double a, double b, double c, double \*F, double \*buffer)

Compute the McMurchie-Davidson R coefficients.

## 18.8 oepdev/liboep/oep.h File Reference

```
#include <cstdio>
#include <string>
#include <vector>
#include <map>
#include "psi4/libparallel/parallel.h"
#include "psi4/liboptions/liboptions.h"
#include "psi4/libmints/wavefunction.h"
#include "psi4/libmints/basisset.h"
#include "psi4/libmints/matrix.h"
#include "psi4/libmints/vector.h"
#include "psi4/libthce/thce.h"
#include "psi4/libthce/thce.h"
#include "../lib3d/space3d.h"
```

#### Classes

struct oepdev::OEPType

Container to handle the type of One-Electron Potentials.

· class oepdev::OEPotential

Generalized One-Electron Potential: Abstract base.

· class oepdev::ElectrostaticEnergyOEPotential

Generalized One-Electron Potential for Electrostatic Energy.

· class oepdev::RepulsionEnergyOEPotential

Generalized One-Electron Potential for Pauli Repulsion Energy.

• class oepdev::ChargeTransferEnergyOEPotential

Generalized One-Electron Potential for Charge-Transfer Interaction Energy.

class oepdev::EETCouplingOEPotential

Generalized One-Electron Potential for EET coupling calculations.

### **Namespaces**

· oepdev

OEPDev module namespace.

## **Typedefs**

- using oepdev::SharedWavefunction = std::shared ptr< Wavefunction >
- using oepdev::SharedBasisSet = std::shared\_ptr< BasisSet >
- using oepdev::SharedTensor = std::shared\_ptr< Tensor >
- using oepdev::SharedMatrix = std::shared\_ptr< Matrix >
- using oepdev::SharedVector = std::shared\_ptr< Vector >

# 18.9 oepdev/liboep/oep\_gdf.h File Reference

```
#include <cstdio>
#include <string>
#include "psi4/liboptions/liboptions.h"
#include "psi4/libmints/wavefunction.h"
#include "psi4/libmints/basisset.h"
#include "psi4/libmints/matrix.h"
#include "../libpsi/integral.h"
```

#### Classes

· class oepdev::GeneralizedDensityFit

Generalized Density Fitting Scheme. Abstract Base.

· class oepdev::SingleGeneralizedDensityFit

Generalized Density Fitting Scheme - Single Fit.

· class oepdev::DoubleGeneralizedDensityFit

Generalized Density Fitting Scheme - Double Fit.

## **Namespaces**

oepdev

OEPDev module namespace.

# 18.10 oepdev/libpsi/integral.h File Reference

```
#include "psi4/libmints/integral.h"
#include "psi4/libmints/basisset.h"
#include "psi4/libmints/matrix.h"
```

#### **Classes**

- · class oepdev::TwoBodyAOInt
- · class oepdev::IntegralFactory

Extended IntegralFactory for computing integrals.

## **Namespaces**

· oepdev

OEPDev module namespace.

# 18.11 oepdev/libpsi/potential.h File Reference

```
#include <vector>
#include "psi4/psi4-dec.h"
#include "psi4/libparallel/parallel.h"
#include "psi4/liboptions/liboptions.h"
#include "psi4/libpsio/psio.h"
#include "psi4/libmints/typedefs.h"
#include "psi4/libmints/onebody.h"
#include "psi4/libmints/potential.h"
#include "psi4/libmints/sointegral_onebody.h"
#include "psi4/libmints/osrecur.h"
```

## Classes

· class oepdev::PotentialInt

Computes potential integrals.

#### **Namespaces**

· oepdev

## 18.12 oepdev/libtest/test.h File Reference

```
#include <vector>
#include "psi4/psi4-dec.h"
#include "psi4/libparallel/parallel.h"
#include "psi4/liboptions/liboptions.h"
#include "psi4/libpsio/psio.h"
#include "psi4/libmints/integral.h"
#include "psi4/libmints/wavefunction.h"
#include "psi4/libmints/basisset.h"
#include "psi4/libqt/qt.h"
#include "../libpsi/integral.h"
#include "../libpsi/integrals_iter.h"
```

#### Classes

class oepdev::test::Test

Manages test routines.

## **Namespaces**

· oepdev

OEPDev module namespace.

# 18.13 oepdev/libutil/diis.h File Reference

```
#include <cstdio>
#include <string>
#include <vector>
#include "psi4/libparallel/parallel.h"
#include "psi4/libciomr/libciomr.h"
#include "psi4/libmints/vector.h"
#include "psi4/libmints/matrix.h"
#include "psi4/libqt/qt.h"
```

#### **Classes**

class oepdev::DIISManager

DIIS manager.

## **Namespaces**

oepdev

## 18.14 oepdev/libutil/integrals\_iter.h File Reference

```
#include <cstdio>
#include "psi4/libparallel/parallel.h"
#include "psi4/libmints/basisset.h"
#include "psi4/libmints/integral.h"
#include "../libpsi/integral.h"
```

#### **Classes**

- · class oepdev::ShellCombinationsIterator
  - Iterator for Shell Combinations. Abstract Base.
- · class oepdev::AOIntegralsIterator
  - Iterator for AO Integrals. Abstract Base.
- class oepdev::AllAOShellCombinationsIterator\_4
  - Loop over all possible ERI shells in a shell quartet.
- class oepdev::AllAOShellCombinationsIterator 2
  - Loop over all possible ERI shells in a shell doublet.
- class oepdev::AllAOIntegralsIterator\_4
  - Loop over all possible ERI within a particular shell quartet.
- · class oepdev::AllAOIntegralsIterator 2

Loop over all possible ERI within a particular shell doublet.

#### **Namespaces**

oepdev

OEPDev module namespace.

## **Typedefs**

- using **oepdev::SharedIntegralFactory** = std::shared ptr< IntegralFactory >
- using oepdev::SharedTwoBodyAOInt = std::shared\_ptr< TwoBodyAOInt >
- using oepdev::SharedShellsIterator = std::shared\_ptr< ShellCombinationsIterator >
   Iterator over shells as shared pointer.
- using oepdev::SharedAOIntsIterator = std::shared\_ptr< AOIntegralsIterator >
   Iterator over AO integrals as shared pointer.

## 18.15 oepdev/libutil/scf\_perturb.h File Reference

```
#include "psi4/libmints/vector.h"
#include "psi4/libmints/matrix.h"
#include "psi4/libscf_solver/rhf.h"
```

#### Classes

• struct oepdev::PerturbCharges

Structure to hold perturbing charges.

class oepdev::RHFPerturbed

RHF theory under electrostatic perturbation.

## **Namespaces**

oepdev

OEPDev module namespace.

# 18.16 oepdev/libutil/solver.h File Reference

```
#include <cstdio>
#include <string>
#include <map>
#include "psi4/psi4-dec.h"
#include "psi4/libparallel/parallel.h"
#include "psi4/libparallel/parallel.h"
#include "psi4/libpsio/psio.h"
#include "psi4/libmints/potential.h"
#include "psi4/libmints/integral.h"
#include "wavefunction_union.h"
#include "integrals_iter.h"
#include "../libpsi/integral.h"
#include "../libpsi/integral.h"
```

#### Classes

· class oepdev::OEPDevSolver

Solver of properties of molecular aggregates. Abstract base.

class oepdev::ElectrostaticEnergySolver

Compute the Coulombic interaction energy between unperturbed wavefunctions.

· class oepdev::RepulsionEnergySolver

Compute the Pauli-Repulsion interaction energy between unperturbed wavefunctions.

· class oepdev::ChargeTransferEnergySolver

Compute the Charge-Transfer interaction energy between unperturbed wavefunctions.

## **Namespaces**

oepdev

OEPDev module namespace.

# **Typedefs**

- using oepdev::SharedWavefunctionUnion = std::shared\_ptr< WavefunctionUnion >
- using oepdev::SharedOEPotential = std::shared\_ptr< OEPotential >

# 18.17 oepdev/libutil/unitary\_optimizer.h File Reference

```
#include <string>
#include <complex>
#include "psi4/libmints/vector.h"
#include "psi4/libmints/matrix.h"
```

## Classes

• struct oepdev::ABCD

Simple structure to hold the Fourier series expansion coefficients.

• struct oepdev::Fourier9

Simple structure to hold the Fourier series expansion coefficients for N=4.

· class oepdev::UnitaryOptimizer

Find the optimim unitary matrix of quadratic matrix equation.

class oepdev::UnitaryOptimizer\_4\_2

Find the optimim unitary matrix for quartic-quadratic matrix equation with trace.

## **Namespaces**

oepdev

OEPDev module namespace.

## Macros

- #define IDX(i, j, n) ((n)\*(i)+(j))
- #define **IDX3**(i, j, k) (n2\_\*(i)+n\_\*(j)+(k))
- #define IDX6(i, j, k, l, m, n)  $(n5_*(i)+n4_*(j)+n3_*(k)+n2_*(l)+n_*(m)+(n))$

## **Functions**

- constexpr std::complex< double > oepdev::operator'''\_i (unsigned long long d)
- constexpr std::complex< double > oepdev::operator'''\_i (long double d)

## 18.18 oepdev/libutil/util.h File Reference

```
#include <cstdio>
#include <string>
#include <cmath>
#include <map>
#include "psi4/psi4-dec.h"
#include "psi4/libparallel/parallel.h"
#include "psi4/liboptions/liboptions.h"
#include "psi4/libpsio/psio.h"
#include "psi4/libciomr/libciomr.h"
#include "psi4/libpsio/psio.hpp"
#include "psi4/libiwl/iwl.h"
#include "psi4/libqt/qt.h"
#include "psi4/libmints/molecule.h"
#include "psi4/libmints/writer.h"
#include "psi4/libmints/writer_file_prefix.h"
#include "psi4/libmints/wavefunction.h"
#include "psi4/libmints/basisset.h"
#include "psi4/libmints/vector.h"
#include "psi4/libmints/matrix.h"
#include "psi4/libmints/oeprop.h"
#include "psi4/libmints/local.h"
#include "psi4/libfunctional/superfunctional.h"
#include "psi4/libtrans/mospace.h"
#include "psi4/libtrans/integraltransform.h"
#include "psi4/libscf_solver/rhf.h"
#include "psi4/libdpd/dpd.h"
```

## **Namespaces**

oepdev

OEPDev module namespace.

# **Typedefs**

- using oepdev::SharedMolecule = std::shared ptr< Molecule >
- using **oepdev::SharedSuperFunctional** = std::shared ptr< SuperFunctional >
- using oepdev::SharedMOSpace = std::shared\_ptr< MOSpace >
- using oepdev::SharedMOSpaceVector = std::vector < std::shared\_ptr < MOSpace >>
- using **oepdev::SharedIntegralTransform** = std::shared\_ptr< IntegralTransform >
- using oepdev::SharedLocalizer = std::shared ptr< Localizer >

#### **Functions**

void oepdev::preambule (void)

Print preambule for module OEPDEV.

 template<typename... Args> std::string oepdev::string\_sprintf (const char \*format, Args...args)

Format string output. Example: std::string text = oepdev::string\_sprinff("Test %3d, %13.5f", 5, -10.5425);.

• std::shared\_ptr< SuperFunctional > oepdev::create\_superfunctional (std::string name, Options & options)

Set up DFT functional.

 std::shared\_ptr< Molecule > oepdev::extract\_monomer (std::shared\_ptr< const Molecule > molecule\_dimer, int id)

Extract molecule from dimer.

std::shared\_ptr< Wavefunction > oepdev::solve\_scf (std::shared\_ptr< Molecule > molecule, std::shared\_ptr< BasisSet > primary, std::shared\_ptr< SuperFunctional > functional, Options &options, std::shared\_ptr< PSIO > psio)

Solve RHF-SCF equations for a given molecule in a given basis set.

double oepdev::average\_moment (std::shared\_ptr< psi::Vector > moment)

Compute the scalar magnitude of multipole moment.

# 18.19 oepdev/libutil/wavefunction\_union.h File Reference

```
#include <cstdio>
#include <string>
#include <map>
#include "psi4/psi4-dec.h"
#include "psi4/libparallel/parallel.h"
#include "psi4/liboptions/liboptions.h"
#include "psi4/libpsio/psio.h"
#include "psi4/libciomr/libciomr.h"
#include "psi4/libpsio/psio.hpp"
#include "psi4/libqt/qt.h"
#include "psi4/libmints/molecule.h"
#include "psi4/libmints/writer.h"
#include "psi4/libmints/writer_file_prefix.h"
#include "psi4/libmints/wavefunction.h"
#include "psi4/libmints/basisset.h"
#include "psi4/libmints/vector.h"
#include "psi4/libmints/matrix.h"
#include "psi4/libmints/oeprop.h"
#include "psi4/libmints/local.h"
#include "psi4/libfunctional/superfunctional.h"
#include "psi4/libtrans/mospace.h"
#include "psi4/libtrans/integraltransform.h"
#include "psi4/libscf_solver/rhf.h"
#include "psi4/libdpd/dpd.h"
```

#### Classes

· class oepdev::WavefunctionUnion

Union of two Wavefunction objects.

## **Namespaces**

oepdev

# **Chapter 19**

# **Example Documentation**

# 19.1 example\_cphf.cc

Shows how to use the oepdev::CPHF solver to compute molecular and LMO-distributed polarizabilities at RHF level of theory.

```
void example_cphf(std::shared_ptr<psi::Wavefunction> wfn, psi::Options& opt){
    // build the solver
    std::shared_ptr<oepdev::CPHF> solver = std::make_shared<oepdev::CPHF>(wfn, opt);

    // run the solver to converge CPHF equations
    solver->compute();

    // print the LMO-distributed polarizabilities
    for (int i=0; i<solver->nocc(); i++) {
        solver->polarizability(i)->print();
    }

    // print the molecular polarizability
    solver->polarizability()->print();

    // grab 4th LMO-distributed polarizability and its associated LMO centroid
    psi::SharedMatrix pol_4 = solver->polarizability(3);
    psi::SharedVector rmo_4 = solver->lmo_centroid(3);
};
```

# 19.2 example\_integrals\_iter.cc

Iterations over electron repulsion integrals in AO basis. This is an example of how to use

- the oepdev::ShellCombinationsIterator class
- the oepdev::AOIntegralsIterator class.

```
void iterate(std::shared_ptr<oepdev::IntegralFactory> ints)
{
    // Prepare for direct calculation of ERI's (shell by shell)
    std::shared_ptr<psi::TwoBodyAoInt> tei(ints->eri());

    // Grab the buffer where the integrals for a current shell will be placed
    const double* buffer = tei->buffer();

    // Create iterator to go through all shell quartet combinations
    oepdev::SharedShellsIterator shellIter =
        oepdev::ShellCombinationsIterator::build(ints, "ALL", 4);

    // Iterate over shells, and then over all integrals in each shell quartet
    for (shellIter->first(); shellIter->is_done() == false; shellIter->next())
    {
            // Compute all integrals between shells in the current quartet
            shellIter->compute_shell(tei);
```

```
// Create iterator to go through all integrals within a shell quartet
oepdev::SharedAOIntsIterator intsIter = shellIter->ao_iterator("ALL");

for (intsIter->first(); intsIter->is_done() == false; intsIter->next())
{
    // Grab current (ij|kl) indices here
    int i = intsIter->i();
    int j = intsIter->j();
    int k = intsIter->k();
    int l = intsIter->l();

    // Grab the (ij|kl) integral
    double integral = buffer[intsIter->index()];
}
}
```

# 19.3 example\_scf\_perturb.cc

Perturb HF Hamiltonian with external electrostatic potential. This is an example of how to use the oepdev::RHF-Perturbed class.

```
void scf_perturb(std::shared_ptr<psi::Wavefunction> wfn, psi::Options& opt)
   // Set up HF superfunctional
   std::shared_ptr<psi::SuperFunctional> func = oepdev::create_superfunctional
      ("HF", opt);
   // Initialize the perturbed wavefunction
   std::shared_ptr<oepdev::RHFPerturbed> scf = std::make_shared<oepdev::RHFPerturbed>(wfn, func, opt, wfn->
      psio());
   /* Perturb the system with the uniform electric field [Fx, Fy, Fz].
      Then, add two point charges of charge qi placed at [Rxi, Ryi, Rzi].
   Provide all these values in atomic units! * const double Fx = 0.04, Fy = 0.05, Fz = -0.09; const double Rx1= 0.00, Rx2= 1.30, Rx3= -1.00;
   const double Rx1= 0.10, Rx2=-0.30, Rx3= 3.50; const double q1 = 0.30, q2=-0.09;
   scf->set_perturbation(Fx, Fy, Fz);
                                                 /\star set it only once, setting it again will overwrite the
       field, not add */
   scf->set_perturbation(Rx1, Ry1, Rz1, q1); scf->set_perturbation(Rx2, Ry2, Rz2, q2); /* more charges can be added */
   // Solve perturbed SCF equations
   scf->compute_energy();
   // Grab some data
   /\star Note that the external field and charges perturb only one-electron Hamiltonian.\star/
```

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