

Sumas de pares de listas y cuadrados

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codigo

Este modulo define dos programas, `sumlists/4` y `square_lists/3`.

Para el primero, dado un numero N par, se devuelven dos listas L1 y L2 que contienen entre las dos los numeros de Peano de 1 a N y cuya suma es la misma, S.

Ejemplos de `sumlists/4`:

1.

```
?- sumlists(s(s(s(s(0)))),L1,L2,S).
```

```
L1 = [s(s(s(0))),s(s(0))],
L2 = [s(s(s(s(0)))),s(0)],
S = s(s(s(s(s(0)))) ?
yes
?-
```

2.

```
?- sumlists(s(s(s(s(s(s(s(s(0)))))))),L1,L2,S).
```

```
L1 = [s(s(s(s(s(s(s(0))))))),s(s(s(s(s(0))))),s(s(s(s(0))),s(s(0))),
L2 = [s(s(s(s(s(s(0))))),s(s(s(s(s(s(s(s(0))))))),s(s(s(0))),s(0)],
S = s(s(s(s(s(s(s(s(s(s(s(s(s(s(s(s(0)))))))))))))) ?
yes
?-
```

Por otra parte, para `square_lists/4`, dado un numero N, se devuelve una matriz cuadrada de $N \times N$ que contiene todos los numeros de Peano del 1 a N^2 y cuyas filas suman lo mismo.

Ejemplos de `square_lists/3`:

1.

```
?- square_lists(s(s(0)),SQ,S).
```

```
S = s(s(s(s(s(0))))),
SQ = [[s(s(s(0))),s(s(0))],[s(s(s(s(0)))),s(0)]] ?
yes
?-
```

2.

```
?- square_lists(s(s(s(0))),SQ,S).
```

```
S = s(s(s(s(s(s(s(s(s(s(s(s(s(s(s(s(0))))))))))))),
SQ = [[s(s(s(s(s(s(s(s(0))))))),s(s(s(s(s(0)))),s(s(s(0))),
      [s(s(s(s(s(s(s(0))))),s(s(s(s(s(s(0))))),s(s(0))),
      [s(s(s(s(s(s(s(s(s(0))))))))),s(s(s(s(s(s(0))))),s(0)]] ?
yes
?-
```

A continuacion, se muestran los predicados y propiedades que se han utilizado.

Usage and interface

- **Library usage:**

```
:- use_
module(/home/guilogar/UPM/6semestre/ProDeclarativa/sumlistPeano/codigo.pl).
```
- **Exports:**
 - *Predicates:*

```
alumno_prode/4, plus/3, nums/2, sumlist/2, choose_one/3, perm/2, split/3,
sumlists/4, make_matrix/3, take_N/4, check_sum/2, times/3, exp/3, square_
lists/3.
```
 - *Properties:*

```
nat/1, lista/1, greater_zero/1.
```

Documentation on exports

alumno_prode/4: PREDICATE
 No further documentation available for this predicate.

nat/1: PROPERTY
Usage: nat(N)
 Cierto si N es un numero natural.

```
nat(0).
nat(s(X)) :-
    nat(X).
```

lista/1: PROPERTY
Usage: lista(L)
 Cierto si L es una lista.

```
lista([]).
lista([_1|Y]) :-
    lista(Y).
```

plus/3: PREDICATE
Usage: plus(A,B,C)
 Cierto si $A + B = C$.

```
plus(X,0,X) :-
    nat(X).
plus(X,s(Y),s(Z)) :-
    plus(X,Y,Z).
```

Other properties:**Test:** plus(A,B,C)Caso: $2 + 1 = 3$

- *If the following properties hold at call time:*

A=s(s(0)) (= /2)

B=s(0) (= /2)

then the following properties should hold upon exit:

C=s(s(s(0))) (= /2)

then the following properties should hold globally:

All the calls of the form plus(A,B,C) do not fail. (not_fails/1)

Test: plus(A,B,C)Caso: $0 + 1 = 1$

- *If the following properties hold at call time:*

A=0 (= /2)

B=s(0) (= /2)

then the following properties should hold upon exit:

C=s(0) (= /2)

then the following properties should hold globally:

All the calls of the form plus(A,B,C) do not fail. (not_fails/1)

Test: plus(A,B,C)Ejemplo de una resta: $4 - 2 = 2$

- *If the following properties hold at call time:*

A=s(s(0)) (= /2)

C=s(s(s(s(0)))) (= /2)

then the following properties should hold upon exit:

B=s(s(0)) (= /2)

then the following properties should hold globally:

All the calls of the form plus(A,B,C) do not fail. (not_fails/1)

nums/2:

PREDICATE

Usage: nums(N,L)

Cierta si L es una lista descendente de N a 1.

nums(0, []).

nums(s(N), [s(N) | Np]) :-

nums(N, Np).

Other properties:**Test:** nums(N,L)

Lista desde el 3 hasta a 1.

- *If the following properties hold at call time:*

N=s(s(s(0))) (= /2)

then the following properties should hold upon exit:

L=[s(s(s(0))), s(s(0)), s(0)] (= /2)

then the following properties should hold globally:

All the calls of the form nums(N,L) do not fail. (not_fails/1)

Test: `nums(N,L)`

Igual que el caso anterior pero nos dan la lista.

- *If the following properties hold at call time:*

`L=[s(s(s(0))),s(s(0)),s(0)]` (= /2)

then the following properties should hold upon exit:

`N=s(s(s(0)))` (= /2)

then the following properties should hold globally:

All the calls of the form `nums(N,L)` do not fail. (not_fails/1)

Test: `nums(N,L)`

Caso base.

- *If the following properties hold at call time:*

`N=0` (= /2)

then the following properties should hold upon exit:

`L=[]` (= /2)

then the following properties should hold globally:

All the calls of the form `nums(N,L)` do not fail. (not_fails/1)

sumlist/2:

PREDICATE

Usage: `sumlist(L,N)`

Cierto si N es la suma de elementos de L.

```
sumlist([],0).
sumlist([N|Np],S) :-
    sumlist(Np,Sp),
    plus(N,Sp,S).
```

Other properties:

Test: `sumlist(L,N)`

- *If the following properties hold at call time:*

`L=[s(0),s(0),s(s(0))]` (= /2)

then the following properties should hold upon exit:

`N=s(s(s(s(0))))` (= /2)

then the following properties should hold globally:

All the calls of the form `sumlist(L,N)` do not fail. (not_fails/1)

Test: `sumlist(L,N)`

- *If the following properties hold at call time:*

`L=[0,0,0]` (= /2)

then the following properties should hold upon exit:

`N=0` (= /2)

then the following properties should hold globally:

All the calls of the form `sumlist(L,N)` do not fail. (not_fails/1)

Test: `sumlist(L,N)`

Caso base.

- *If the following properties hold at call time:*
 $L=[]$ (= /2)
then the following properties should hold upon exit:
 $N=0$ (= /2)
then the following properties should hold globally:
All the calls of the form `sumlist(L,N)` do not fail. (not_fails/1)

choose_one/3:

PREDICATE

Usage: `choose_one(E,L,R)`

Cierto si R es igual a L sin el elemento E.

```

choose_one(E, [E|Lp], Lp) :-
    lista(Lp).
choose_one(E, [X|Lp], [X|Rp]) :-
    choose_one(E, Lp, Rp).

```

Other properties:**Test:** `choose_one(E,L,R)`

Se quita un elemento de la lista.

- *If the following properties hold at call time:*
 $E=s(0)$ (= /2)
 $L=[s(s(0)), s(s(s(0))), s(0)]$ (= /2)
then the following properties should hold upon exit:
 $R=[s(s(0)), s(s(s(0)))]$ (= /2)
then the following properties should hold globally:
All the calls of the form `choose_one(E,L,R)` do not fail. (not_fails/1)

Test: `choose_one(E,L,R)`

Se quita un elemento de la lista.

- *If the following properties hold at call time:*
 $E=s(s(s(0)))$ (= /2)
 $L=[s(s(0)), s(s(s(0))), s(0)]$ (= /2)
then the following properties should hold upon exit:
 $R=[s(s(0)), s(0)]$ (= /2)
then the following properties should hold globally:
All the calls of the form `choose_one(E,L,R)` do not fail. (not_fails/1)

Test: `choose_one(E,L,R)`

Se quita un elemento de una lista de un elemento.

- *If the following properties hold at call time:*
 $E=s(s(0))$ (= /2)
 $L=[s(s(0))]$ (= /2)
then the following properties should hold upon exit:
 $R=[]$ (= /2)
then the following properties should hold globally:
All the calls of the form `choose_one(E,L,R)` do not fail. (not_fails/1)

perm/2:

PREDICATE

Usage: perm(L,Lp)

Cierto si Lp es una permutacion de L.

```
perm([], []).
perm([X|R],L) :-
    perm(R,Lp),
    choose_one(X,L,Lp).
```

Other properties:**Test:** perm(L,Lp)

Caso base.

- *If the following properties hold at call time:*

L=[] (= /2)

then the following properties should hold upon exit:

Lp=[] (= /2)

then the following properties should hold globally:

All the calls of the form perm(L,Lp) do not fail. (not_fails/1)

Test: perm(L,Lp)

Permutacion de una lista de 3 elementos. Al usar solutions en el test, LPdoc no genera bien la documentacion para este caso. En el codigo se muestra el test original.

- *If the following properties hold at call time:*

L=[a,b,c] (= /2)

then the following properties should hold globally:

For this test of perm(L,Lp) get at most 6 solutions (normally 2 solutions are generated, just enough to detect non-determinism). (

try_sols/2)

Goal perm(L,Lp) produces the solutions listed in
[perm([a,b,c],[a,b,c]),perm([a,b,c],[b,a,c]),perm([a,b,c],[b,c,a]),perm([a,b,c],

(solutions/2)

split/3:

PREDICATE

Usage: split(L,Lp,Li)

Cierto si Lp tiene los elementos de posicion par de L, y Li, los de posicion impar.

```
split([],[],[]).
split([X1,X2|Xn],[X1|Xp],[X2|Xpp]) :-
    split(Xn,Xp,Xpp).
```

Other properties:**Test:** split(L,L1,L2)

Caso base.

- *If the following properties hold at call time:*

L=[] (= /2)

then the following properties should hold upon exit:

L1=[] (= /2)

L2=[] (= /2)

then the following properties should hold globally:

All the calls of the form split(L,L1,L2) do not fail. (not_fails/1)

Test: `split(L,L1,L2)`

Caso normal dada una lista L.

– *If the following properties hold at call time:*

`L=[a,b,c,d]` (= /2)

then the following properties should hold upon exit:

`L1=[a,c]` (= /2)

`L2=[b,d]` (= /2)

then the following properties should hold globally:

All the calls of the form `split(L,L1,L2)` do not fail. (not_fails/1)

Test: `split(L,L1,L2)`

Dadas las dos listas devuelve la original.

– *If the following properties hold at call time:*

`L1=[a,c]` (= /2)

`L2=[b,d]` (= /2)

then the following properties should hold upon exit:

`L=[a,b,c,d]` (= /2)

then the following properties should hold globally:

All the calls of the form `split(L,L1,L2)` do not fail. (not_fails/1)

sumlists/4:

PREDICATE

Usage: `sumlists(N,L1,L2,S)`

Cierto si L1 y L2 contienen entre las dos los naturales de N hasta 1, y ambas suman lo mismo. Los ejemplos de uso se encuentran al principio del documento.

```
sumlists(N,L1,L2,S) :-
    nums(N,L),
    perm(L,Lp),
    split(Lp,L1,L2),
    sumlist(L1,S),
    sumlist(L2,S).
```

make_matrix/3:

PREDICATE

Usage: `make_matrix(L,N,M)`

Cierto si M es una matriz de N elementos por fila, formada por los elementos de L.

```
make_matrix([],_1,[]).
make_matrix(Lista,N,[Fila|Filas]) :-
    take_N(Lista,N,Fila,Rest),
    make_matrix(Rest,N,Filas).
```

Other properties:

Test: `make_matrix(L,N,M)`

Caso base.

- *If the following properties hold at call time:*
 - $L=[]$ (= /2)
 - $N=s(0)$ (= /2)
- then the following properties should hold upon exit:*
 - $M=[]$ (= /2)
- then the following properties should hold globally:*
 - All the calls of the form `make_matrix(L,N,M)` do not fail. (not_fails/1)

Test: `make_matrix(L,N,M)`

Caso con una lista de 4 elementos y filas de 2.

- *If the following properties hold at call time:*
 - $L=[a,b,c,d]$ (= /2)
 - $N=s(s(0))$ (= /2)
- then the following properties should hold upon exit:*
 - $M=[[a,b],[c,d]]$ (= /2)
- then the following properties should hold globally:*
 - All the calls of the form `make_matrix(L,N,M)` do not fail. (not_fails/1)

Test: `make_matrix(L,N,M)`

Caso con una lista de 8 elementos y filas de 4.

- *If the following properties hold at call time:*
 - $L=[a,b,c,d,e,f,g,h]$ (= /2)
 - $N=s(s(s(s(0))))$ (= /2)
- then the following properties should hold upon exit:*
 - $M=[[a,b,c,d],[e,f,g,h]]$ (= /2)
- then the following properties should hold globally:*
 - All the calls of the form `make_matrix(L,N,M)` do not fail. (not_fails/1)

take_N/4:

PREDICATE

Usage: `take_N(L1,N,L2,Resto)`

Cierto si L2 es una lista formada por los primeros N elementos de L1. Resto contiene el resto de elementos de L1.

```
take_N(Rest,0,[],Rest).
take_N([Elem|Lista],s(N),[Elem|Lista2],Rest) :-
    take_N(Lista,N,Lista2,Rest).
```

Other properties:

Test: `take_N(L1,N,L2,Resto)`

Se toman 2 elementos de una lista de 5.

- *If the following properties hold at call time:*
 - $L1=[a,b,c,d,e]$ (= /2)
 - $N=s(s(0))$ (= /2)
 - $L2=[a,b]$ (= /2)
- then the following properties should hold upon exit:*
 - $Resto=[c,d,e]$ (= /2)
- then the following properties should hold globally:*
 - All the calls of the form `take_N(L1,N,L2,Resto)` do not fail. (not_fails/1)

Test: take_N(L1,N,L2,Resto)

Se toman 0 elementos de una lista de 5.

– *If the following properties hold at call time:*

L1=[a,b,c,d,e] (= /2)

N=0 (= /2)

then the following properties should hold upon exit:

L2=[] (= /2)

Resto=[a,b,c,d,e] (= /2)

then the following properties should hold globally:

All the calls of the form take_N(L1,N,L2,Resto) do not fail. (not_fails/1)

check_sum/2:

PREDICATE

Usage: check_sum(M,S)

Cierto si la suma de todas las filas de M suman S.

```
check_sum([],_1).
check_sum([Fila|Filas],Sum) :-
    sumlist(Fila,Sum),
    check_sum(Filas,Sum).
```

Other properties:

Test: check_sum(M,S)

Matriz de 2*2 cuyos elementos suman 5.

– *If the following properties hold at call time:*

M=[[s(s(0)),s(s(s(0)))],[s(0),s(s(s(s(0))))]] (= /2)

then the following properties should hold upon exit:

S=s(s(s(s(s(0)))) (= /2)

then the following properties should hold globally:

All the calls of the form check_sum(M,S) do not fail. (not_fails/1)

Test: check_sum(M,S)

Matriz de 3*1 cuyos elementos suman 2.

– *If the following properties hold at call time:*

M=[[s(s(0))],[s(s(0))],[s(s(0))]] (= /2)

then the following properties should hold upon exit:

S=s(s(0)) (= /2)

then the following properties should hold globally:

All the calls of the form check_sum(M,S) do not fail. (not_fails/1)

times/3:

PREDICATE

Usage: times(A,B,C)

Cierto si $A * B = C$

```
times(X,0,0) :-
    nat(X).
times(X,s(Y),Z) :-
    times(X,Y,W),
    plus(X,W,Z).
```

Other properties:**Test:** times(A,B,C)Caso base: $2 * 0 = 0$

- *If the following properties hold at call time:*

A=s(s(0)) (= /2)

B=0 (= /2)

then the following properties should hold upon exit:

S=0 (= /2)

then the following properties should hold globally:

All the calls of the form times(A,B,C) do not fail. (not_fails/1)

Test: times(A,B,C)Caso: $2 * 3 = 6$

- *If the following properties hold at call time:*

A=s(s(0)) (= /2)

B=s(s(s(0))) (= /2)

then the following properties should hold upon exit:

S=s(s(s(s(s(s(0)))))) (= /2)

then the following properties should hold globally:

All the calls of the form times(A,B,C) do not fail. (not_fails/1)

exp/3:

PREDICATE

Usage: exp(Exp,N,S)Cierta si $N^{\text{Exp}} = S$

exp(0,X,s(0)) :-
 nat(X).

exp(s(N),X,Y) :-
 exp(N,X,W),
 times(W,X,Y).

Other properties:**Test:** exp(Exp,N,S)Caso base: $2^0 = 1$

- *If the following properties hold at call time:*

Exp=0 (= /2)

N=s(s(0)) (= /2)

then the following properties should hold upon exit:

S=s(0) (= /2)

then the following properties should hold globally:

All the calls of the form exp(Exp,N,S) do not fail. (not_fails/1)

Test: exp(Exp,N,S)Caso: $2^3 = 8$

- *If the following properties hold at call time:*
`Exp=s(s(s(0)))` (= /2)
`N=s(s(0))` (= /2)
then the following properties should hold upon exit:
`S=s(s(s(s(s(s(s(s(0))))))))` (= /2)
then the following properties should hold globally:
All the calls of the form `exp(Exp,N,S)` do not fail. (not_fails/1)

greater_zero/1: PROPERTY

Usage: `greater_zero(N)`

Cierto si N es un natural mayor que 0.

```
greater_zero(s(0)).
greater_zero(s(N)) :-
    greater_zero(N).
```

square_lists/3: PREDICATE

Usage: `square_lists(N,SQ,S)`

Cierto si SQ es una matriz de $N \times N$, cuyas filas suman S, y entre todas contienen los numeros de N^2 hasta 1. Los tests se encuentran al principio del documento.

```
square_lists(N,SQ,S) :-
    greater_zero(N),
    exp(s(s(0)),N,N2),
    nums(N2,Lista),
    perm(Lista,ListaP),
    make_matrix(ListaP,N,SQ),
    check_sum(SQ,S).
```

Documentation on imports

This module has the following direct dependencies:

- *Application modules:*

`native_props`, `unittest_props`.

- *Internal (engine) modules:*

`term_basic`, `arithmetic`, `atomic_basic`, `basiccontrol`, `exceptions`, `term_compare`,
`term_typing`, `debugger_support`, `basic_props`.

- *Packages:*

`prelude`, `initial`, `condcomp`, `assertions`, `assertions/assertions_basic`,
`nativeprops`.

References

(this section is empty)

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(Index is nonexistent)

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This is a global index containing pointers to places where concepts, predicates, modes, properties, types, applications, authors, etc., are referred to in the text of the document.

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 R=[s(s(0)),s(s(s(0)))] 5
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 Resto=[c,d,e] 8

S

S=0 10
 S=s(0) 10
 S=s(s(0)) 9

S=s(s(s(s(s(0))))) 9
 S=s(s(s(s(s(s(0))))) 10
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