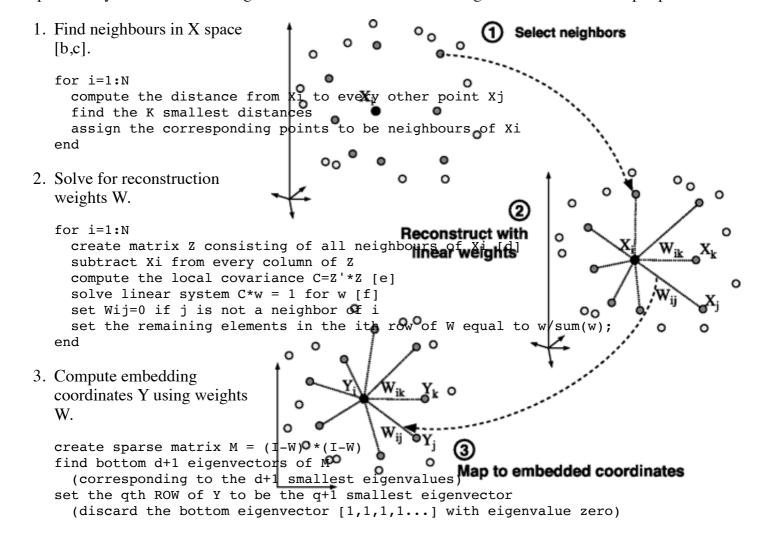
## [home] [algorithm] [publications] [gallery] [code] [related work]

## **LLE Algorithm Pseudocode**

(Notes, e.g. [a] appear below)

Input X: D by N matrix consisting of N data items in D dimensions.

Output Y: d by N matrix consisting of d < D dimensional embedding coordinates for the input points.



## **Notes**

- [a] Notation
   Xi and Yi denote the ith column of X and Y
   (in other words the data and embedding coordinates of the ith point)
   M' denotes the transpose of matrix M
   \* denotes matrix multiplication
   (e.g. M'\*M is the matrix product of M left multiplied by its transpose)
   I is the identity matrix
   1 is a column vector of all ones
- [b] This can be done in a variety of ways, for example above we compute the K nearest neighbours using Euclidean distance. Other methods such as epsilon-ball include all points within a

- certain radius or more sophisticated domain specific and/or adaptive local distance metrics.
- [c] Even for simple neighbourhood rules like K-NN or epsilon-ball using Euclidean distance, there are highly efficient techniques for computing the neighbours of every point, such as KD trees.
- [d] Z consists of all columns of X corresponding to the neighbours of Xi but not Xi itself
- [e] If K>D, the local covariance will not be full rank, and it should be regularized by seting C=C+eps\*I where I is the identity matrix and eps is a small constant of order 1e-3\*trace(C). This ensures that the system to be solved in step 2 has a unique solution.
- [f] 1 denotes a column vector of all ones

Sam T. Roweis..... roweis at cs dot toronto dot edu ..... <u>www.cs.toronto.edu/~roweis/</u> Lawrence K. Saul...... Isaul@research.att.com..... <u>www.research.att.com/~lsaul/</u>