

# Graph Neural Networks for Power Systems

Balthazar Donon - 23/03/2023



# Balthazar DONON

## Deep Statistical Solvers & Power Systems Applications

- 2018 - 2022 : PhD student at RTE Research & Development and Université Paris-Saclay

## Graph Neural Networks for Voltage Management

- 2022-2024 : Post Doctoral Researcher at Institut Montefiore in a project for RTE Research & Development

# Deep Statistical Solvers

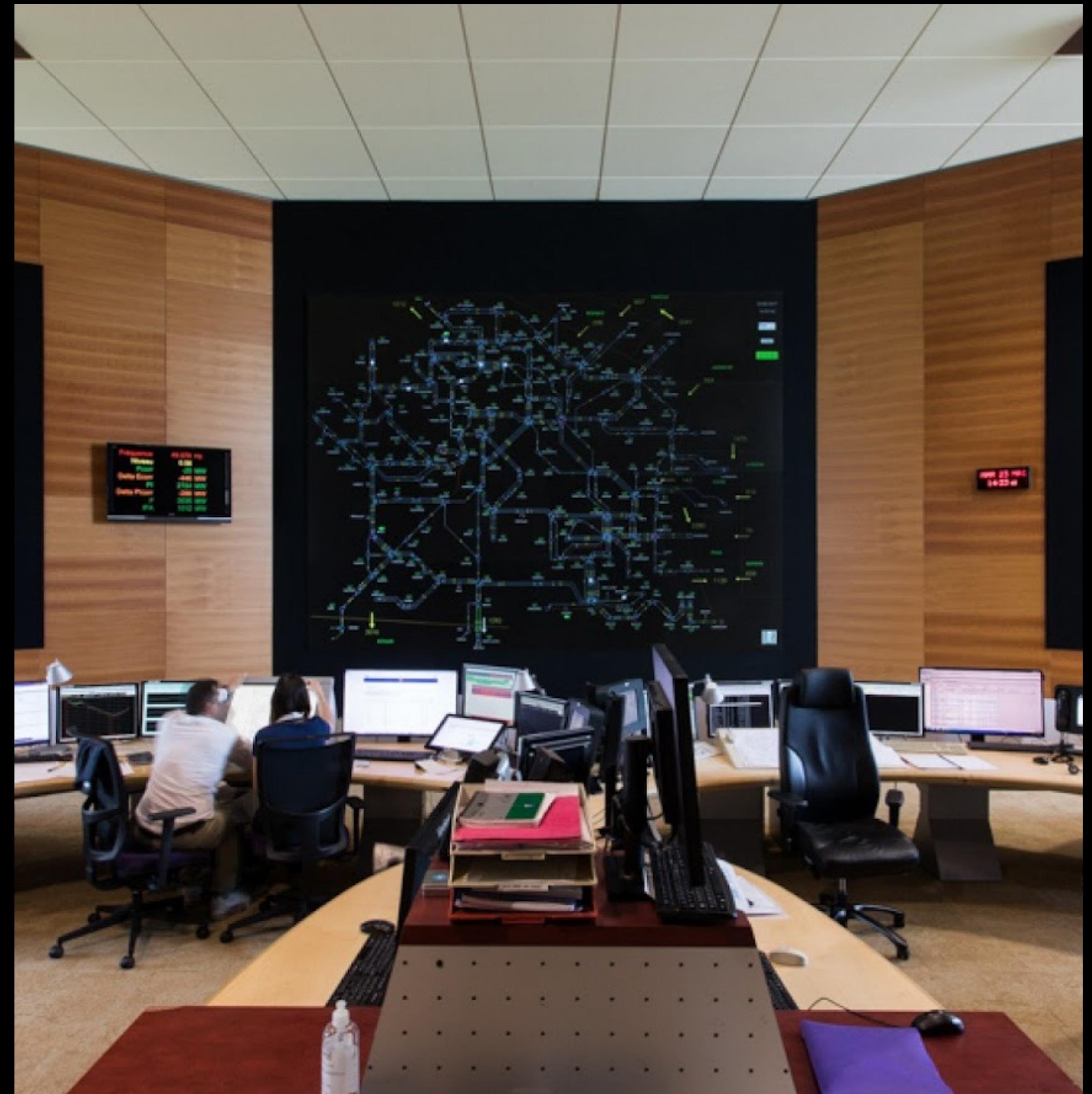
## & Power Systems Applications

# Introduction

# Introduction

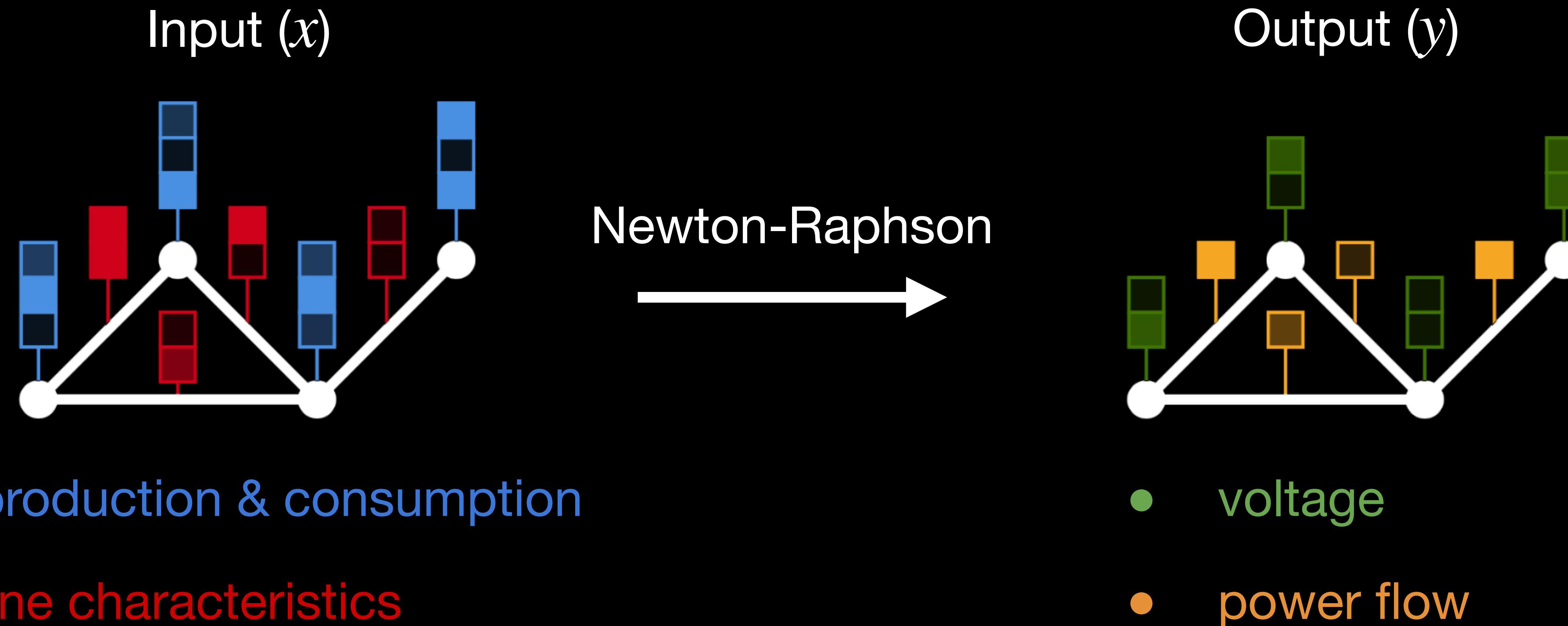
## Dispatchers

- Monitor and control transmission grids in real-time.
- Run security analyses.
- Anticipate the near future.



# Introduction

## AC Power Flow Problem



# Introduction

## An Increasing Complexity

- Power systems are facing an increasing uncertainty & complexity :
  - Intermittent renewables
  - New market mechanisms
  - New electricity uses

# Introduction Issue



Newton-Raphson too slow for probabilistic approaches (Monte-Carlo)...

→ Replace it with a fast approximation based on AI?

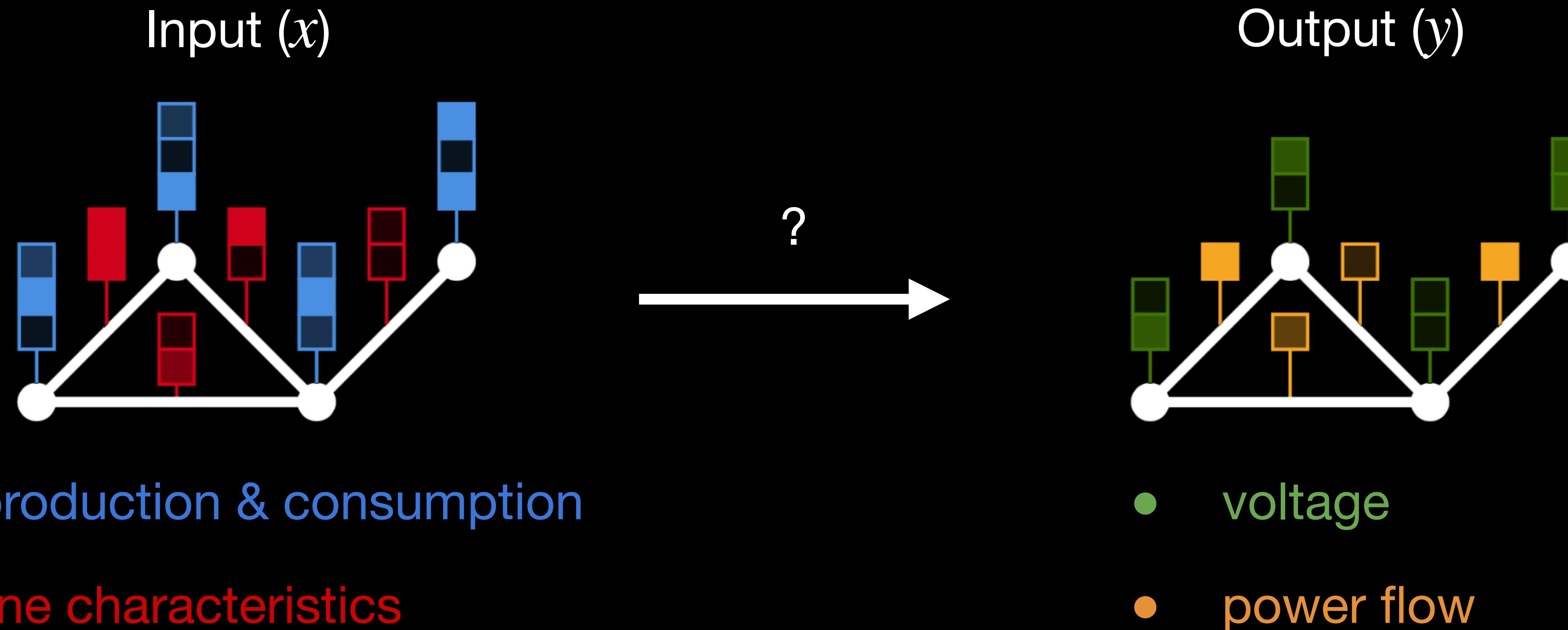
# Introduction

## The AI Opportunity

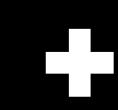
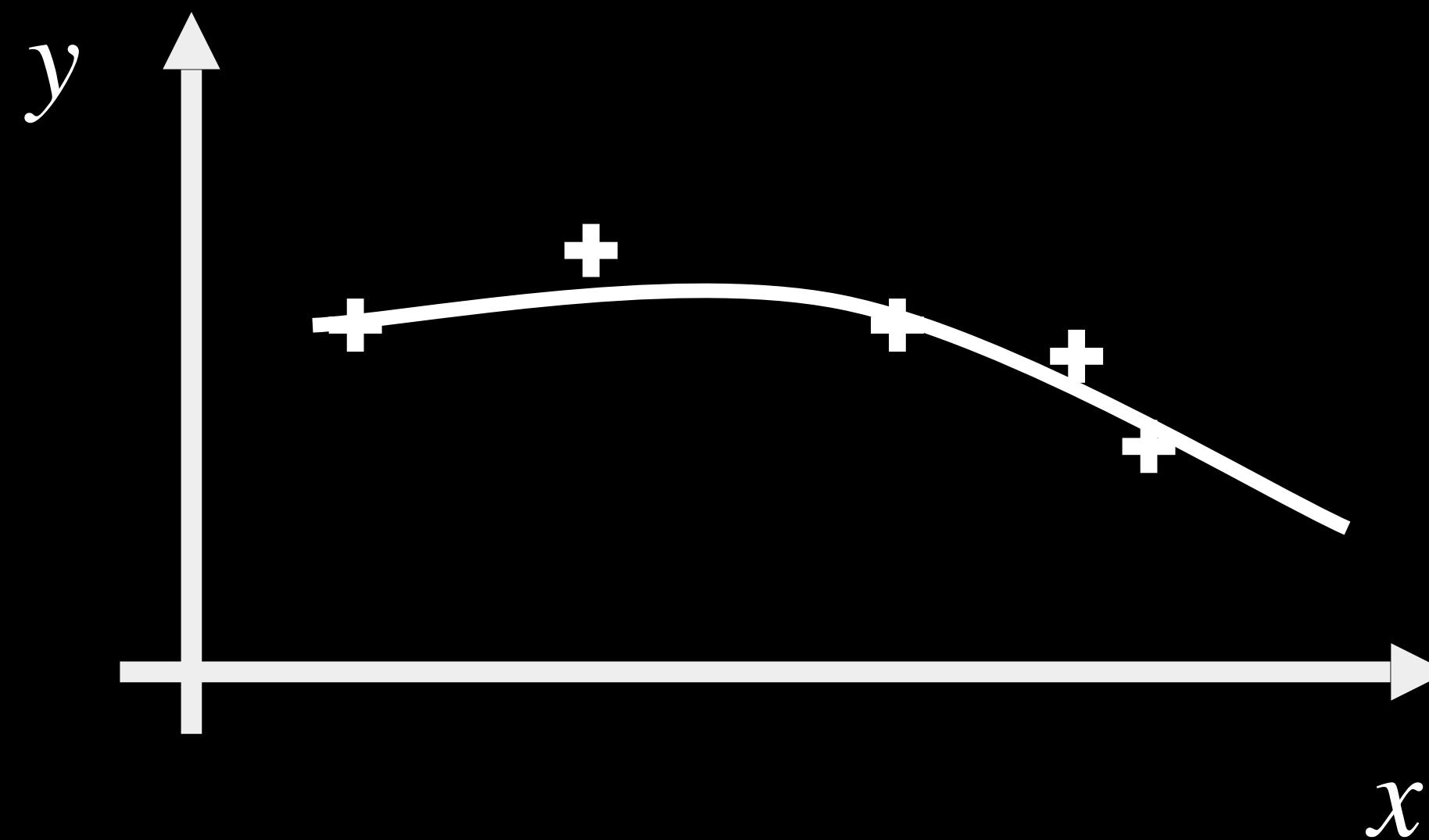
- AI / DL achieved tremendous successes in various domains :
  - Computer Vision
  - Natural language processing
  - Games (chess, go, etc.)
- Ability to solve complex problems that require a very high level of abstraction.

# Introduction

## The AC Power Flow Problem



# Introduction Machine Learning



Data  $(x, y)$

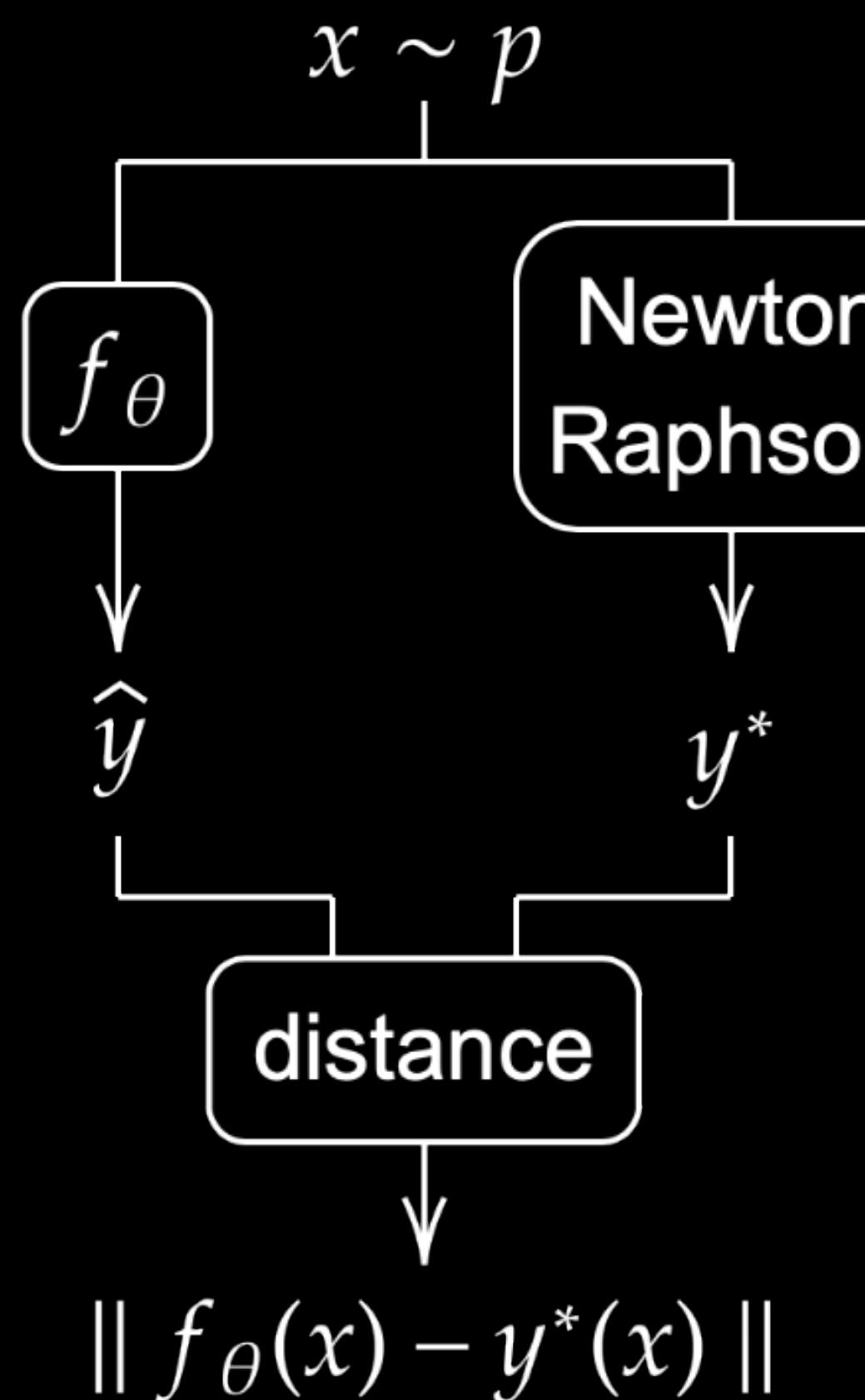
$x$  : Productions, Consumptions, Line Characteristics  
 $y$  : Voltage, Power Flows

Approximation  $f_\theta$

Learning = minimizing the error  $\|f_\theta(x) - y\|$  by modifying the parameter  $\theta$ .

# Introduction

## Proxy Approach



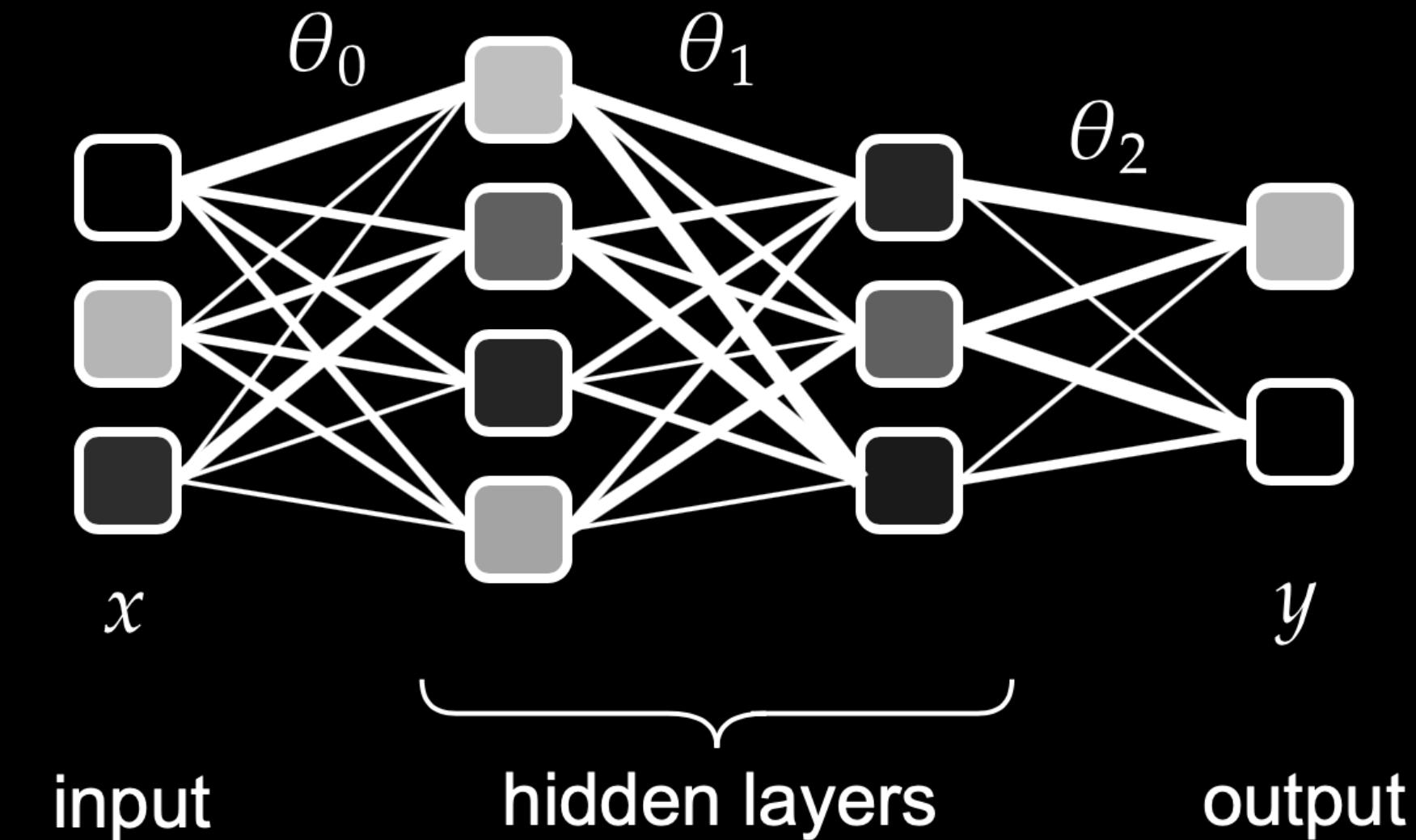
# Introduction Deep Learning

Deep Neural Network

$$\hat{y} = f_{\theta}(x)$$

Trainable weights

$$\theta = (\theta_0, \theta_1, \theta_2)$$



Learning = minimizing the error  $\|f_{\theta}(x) - y\|$  by modifying the parameter  $\theta$ .

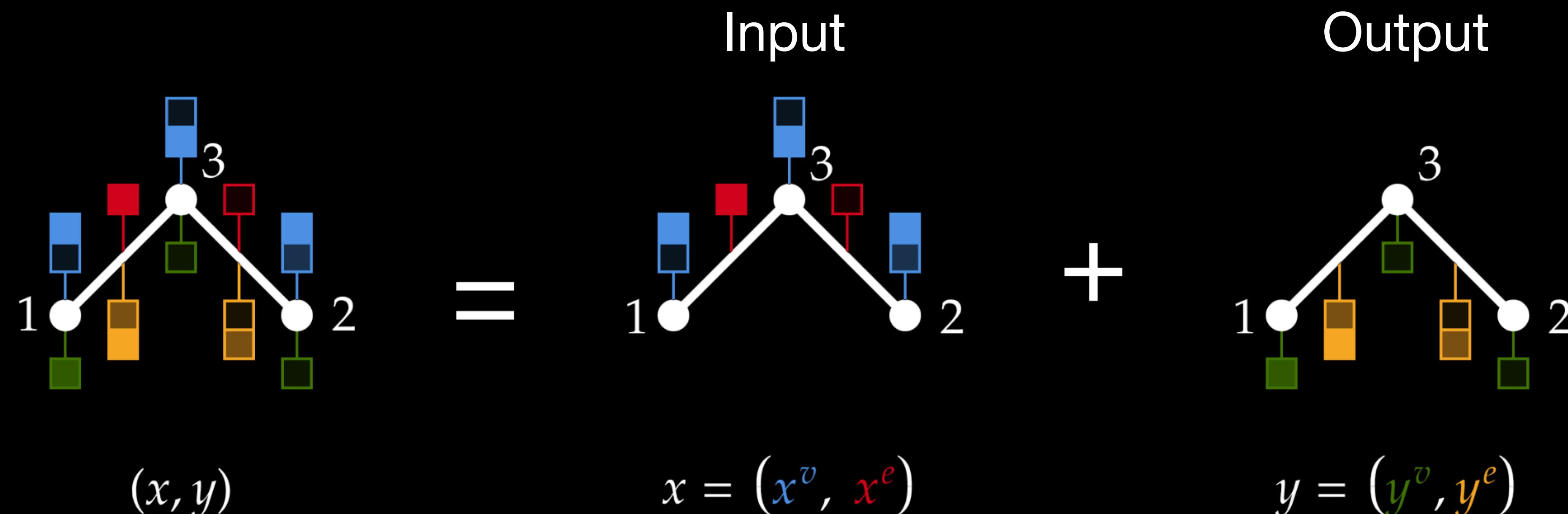
# Introduction

## Limitations



- Standard neural networks only work on **vector** data.
- Problem: power grids are **graphs**, and have a varying size and structure.

# Introduction Graph Data

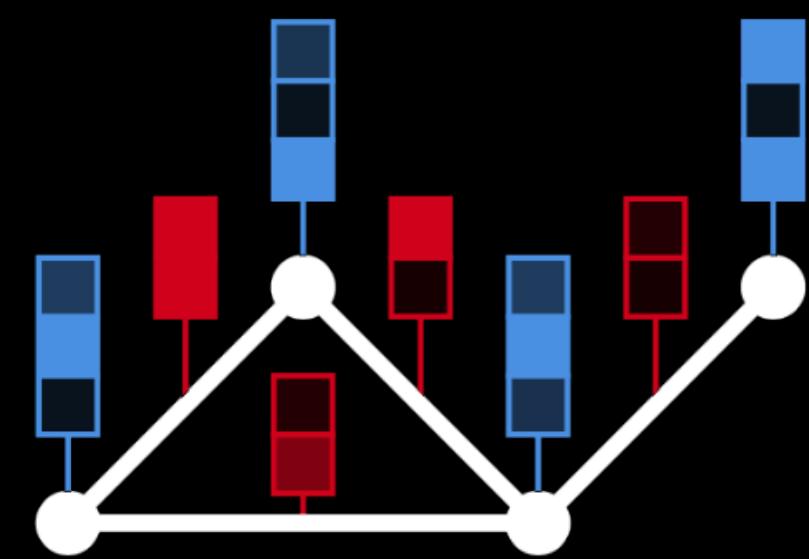


# Statistical Solver Problems

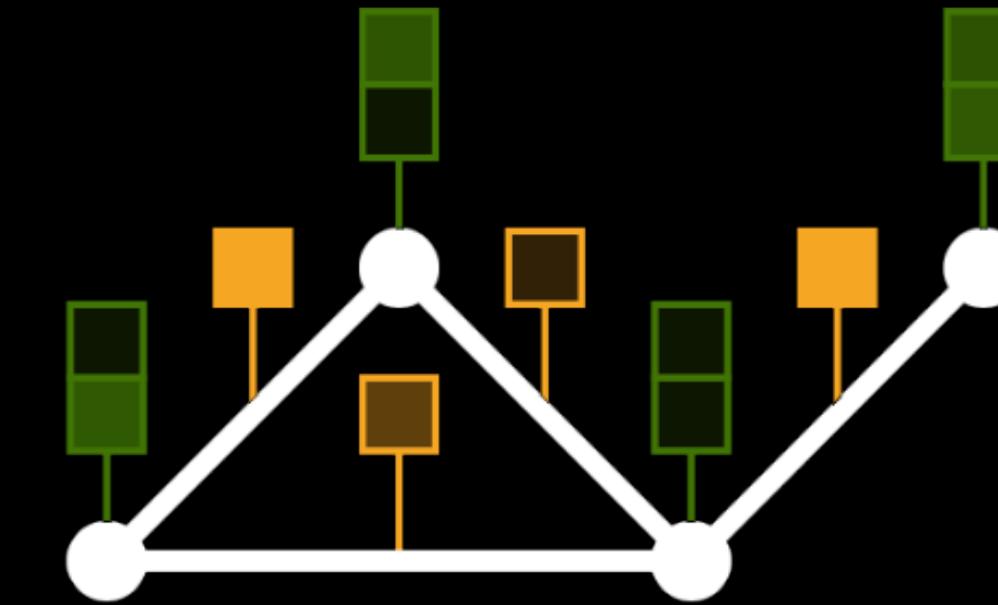
# Statistical Solver Problems

## Target Optimization Problem

Input ( $x$ )



Output ( $y$ )



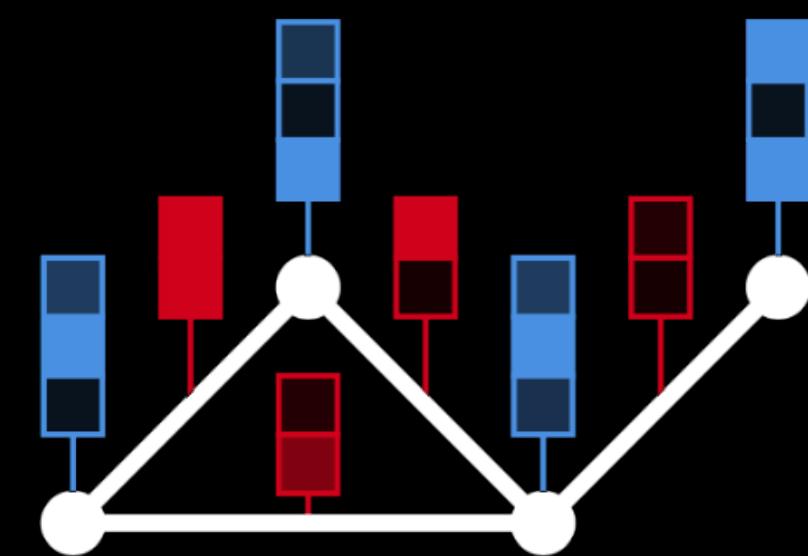
- production & consumption
- line characteristics

- voltage
- power flow

# Statistical Solver Problems

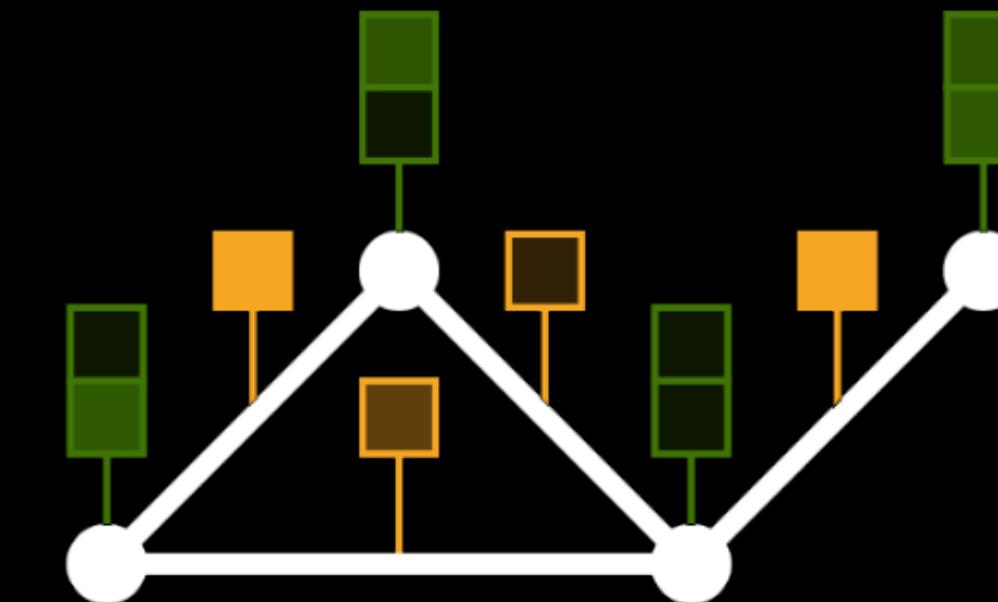
## Target Optimization Problem

Input ( $x$ )



- production & consumption
- line characteristics

Output ( $y$ )



- voltage
- power flow

$$y^*(x) = \arg \min_y \ell(x, y)$$

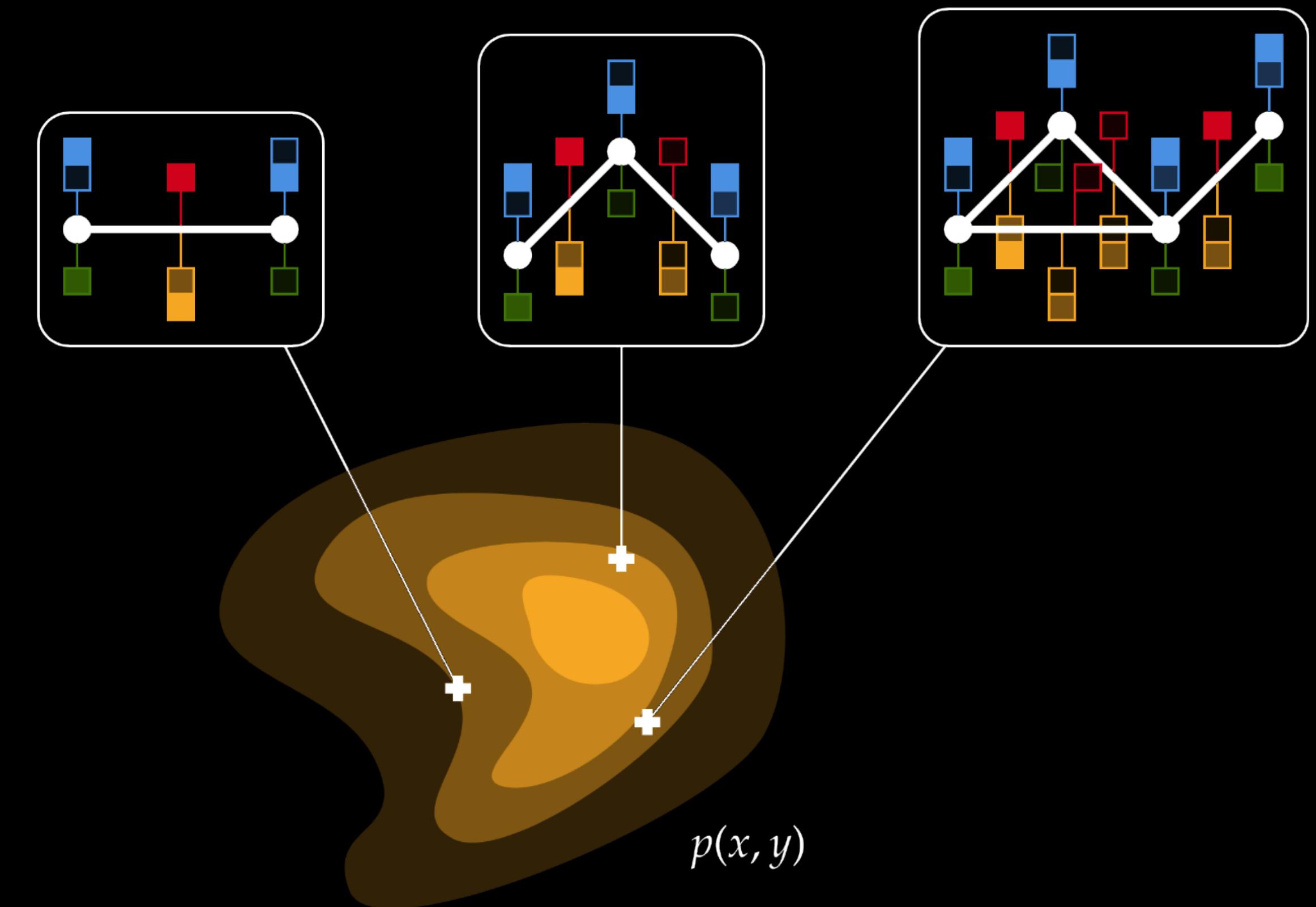
$\ell$  : Violation of Physical Laws (Kirchhoff)

# Statistical Solver Problems

## Statistical Conversion

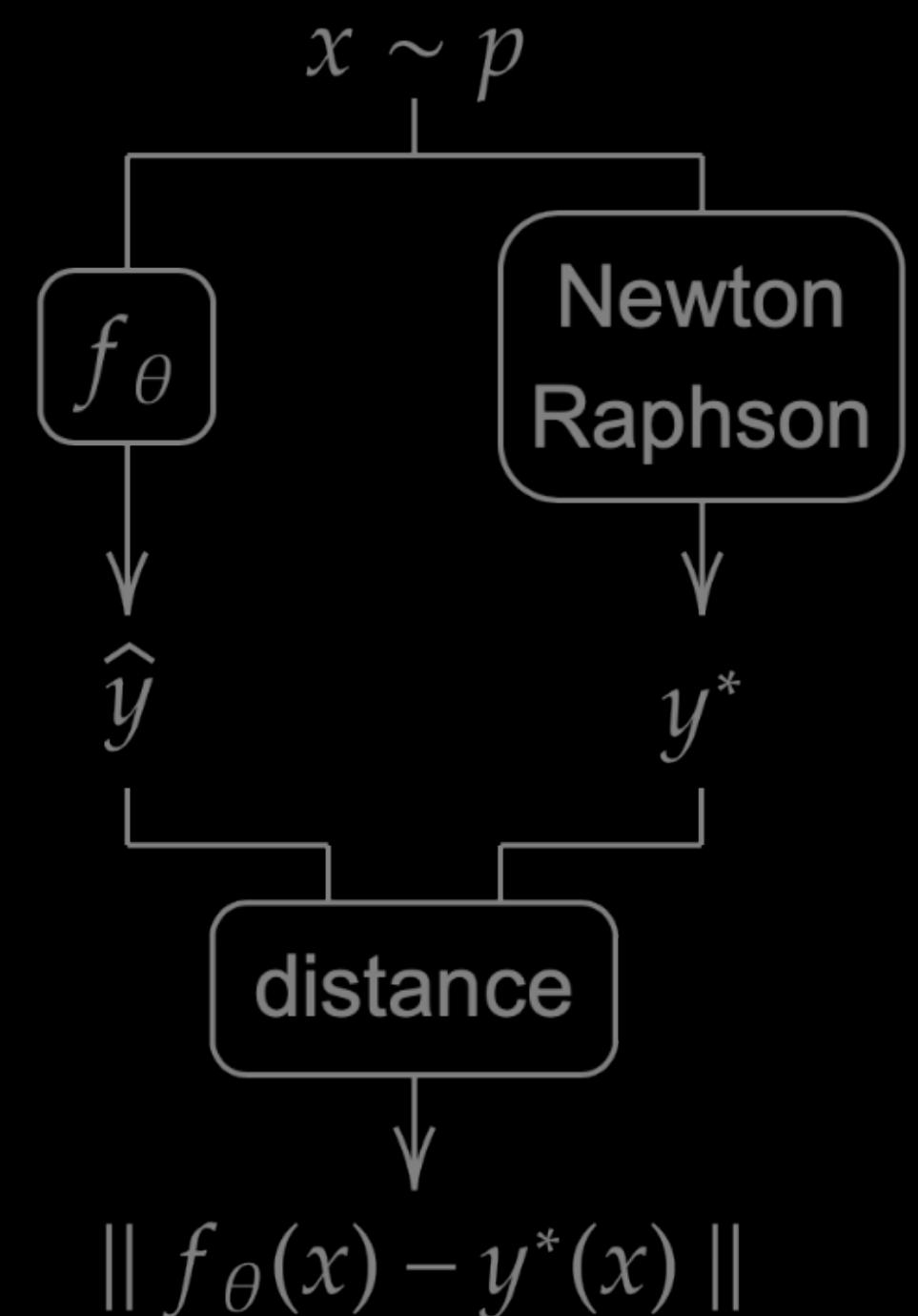
The holy grail :

$$\theta^* = \arg \min_{\theta} \mathbb{E}_{x \sim p} [\ell(x, f_{\theta}(x))]$$

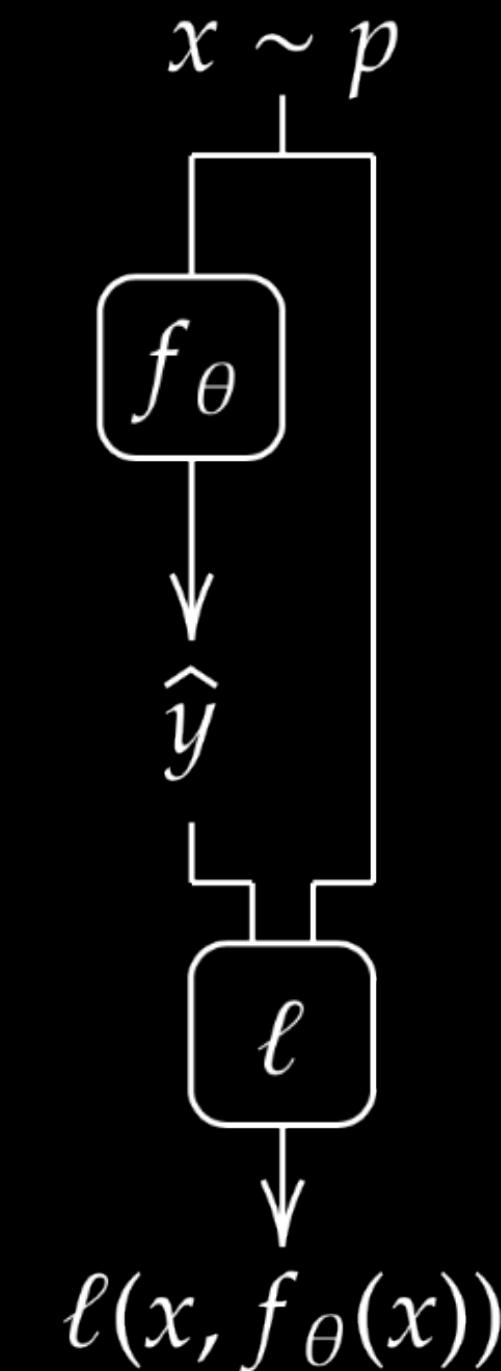


# Statistical Solver Problems

## Statistical Conversion



Proxy Approach



Statistical Solver

# Statistical Solver Problems

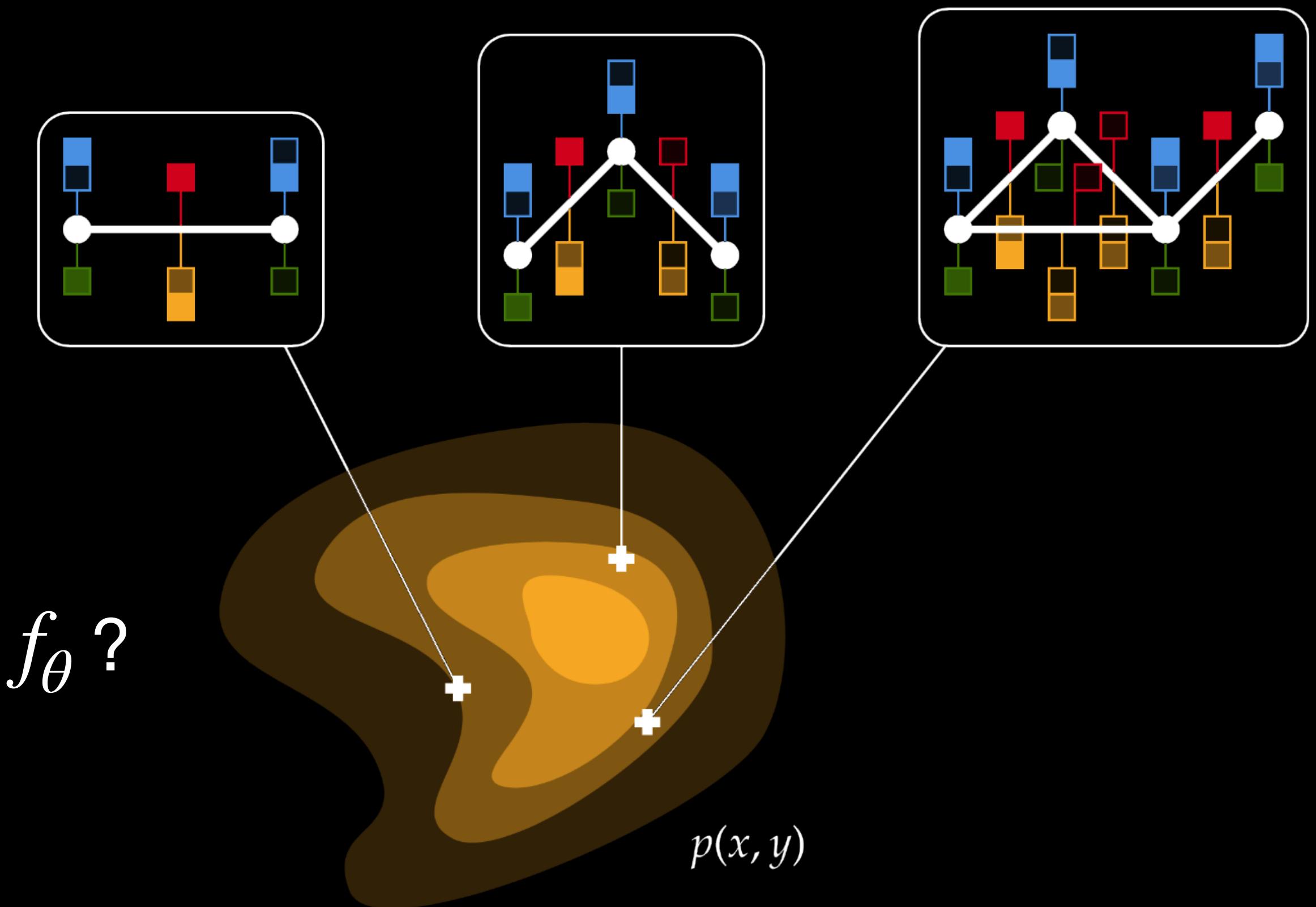
## Statistical Conversion

The holy grail :

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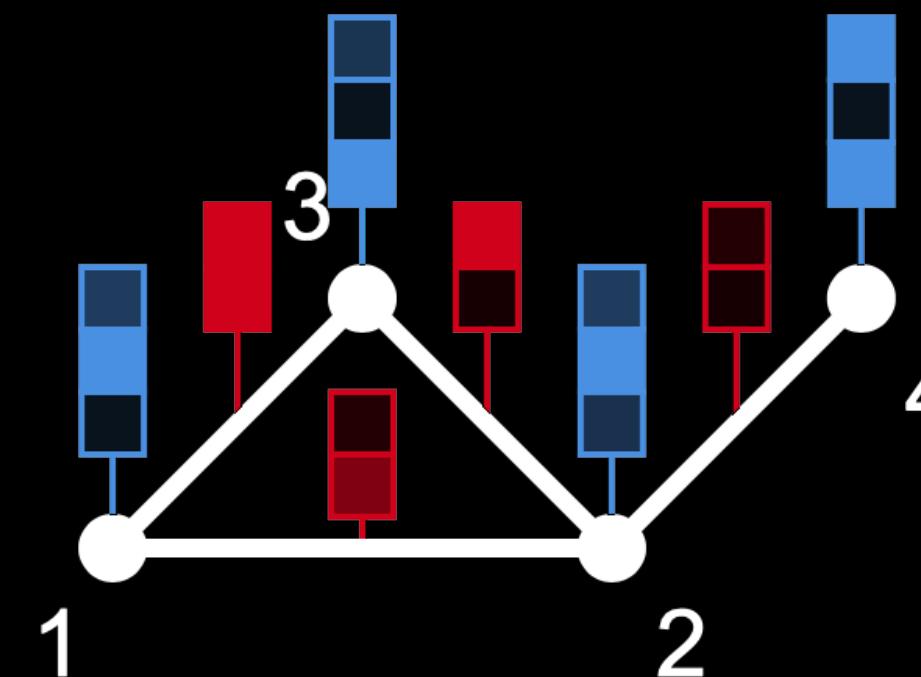
What kind of function should we use for  $f_{\theta}$  ?

- Standard Neural Networks ?

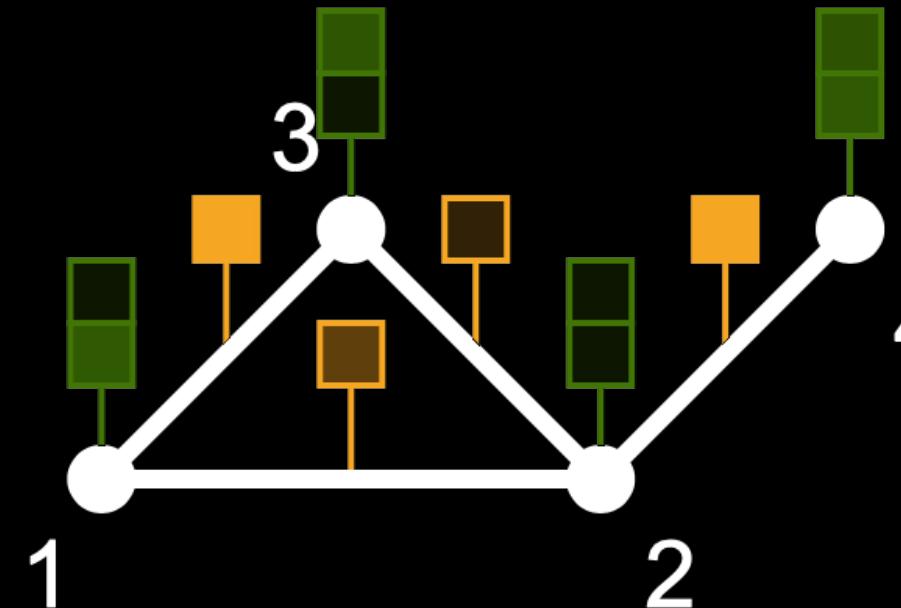


# Statistical Solver Problems

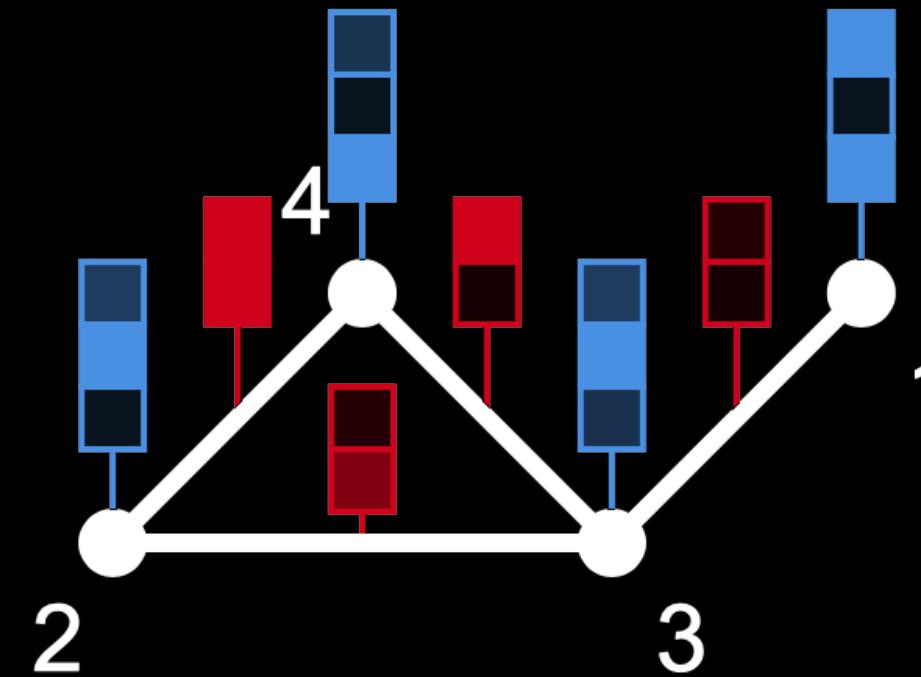
## Limits of Standard Neural Networks



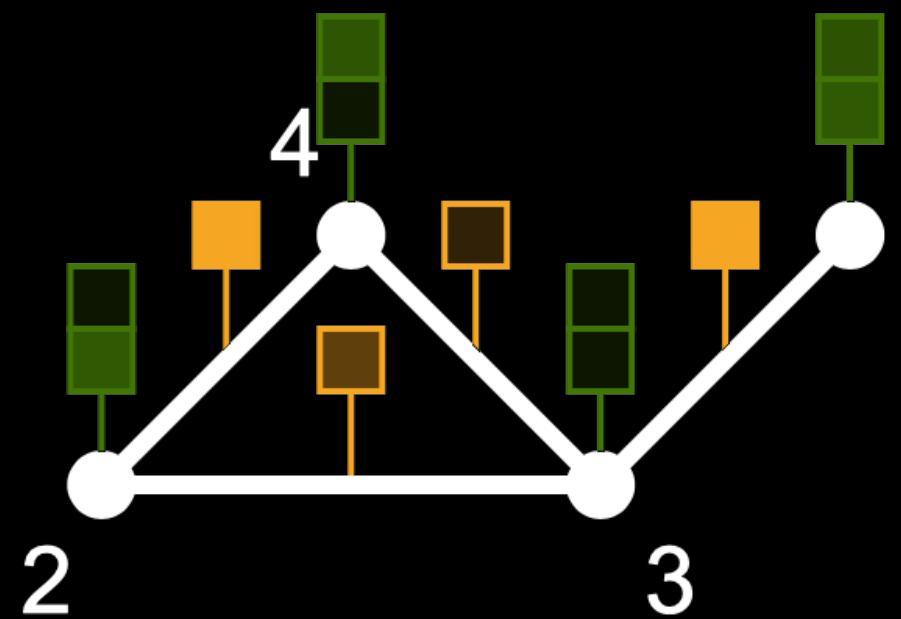
Newton  
Raphson



$$\ell(x, y) \approx 0$$



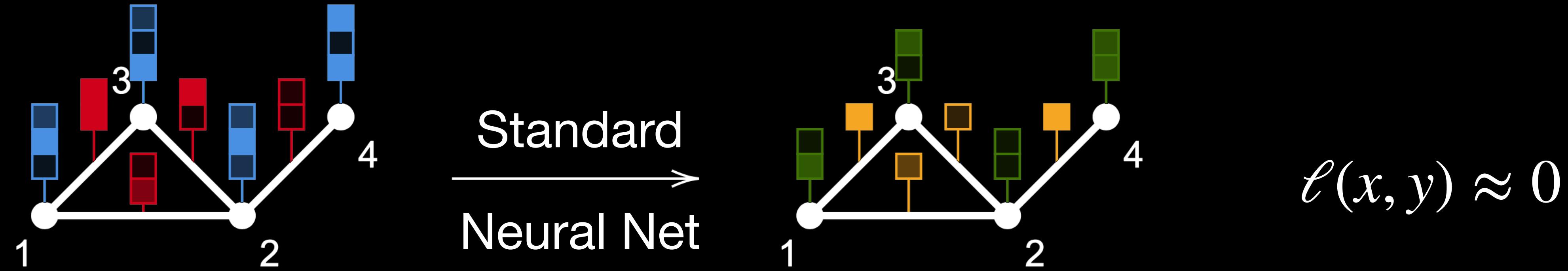
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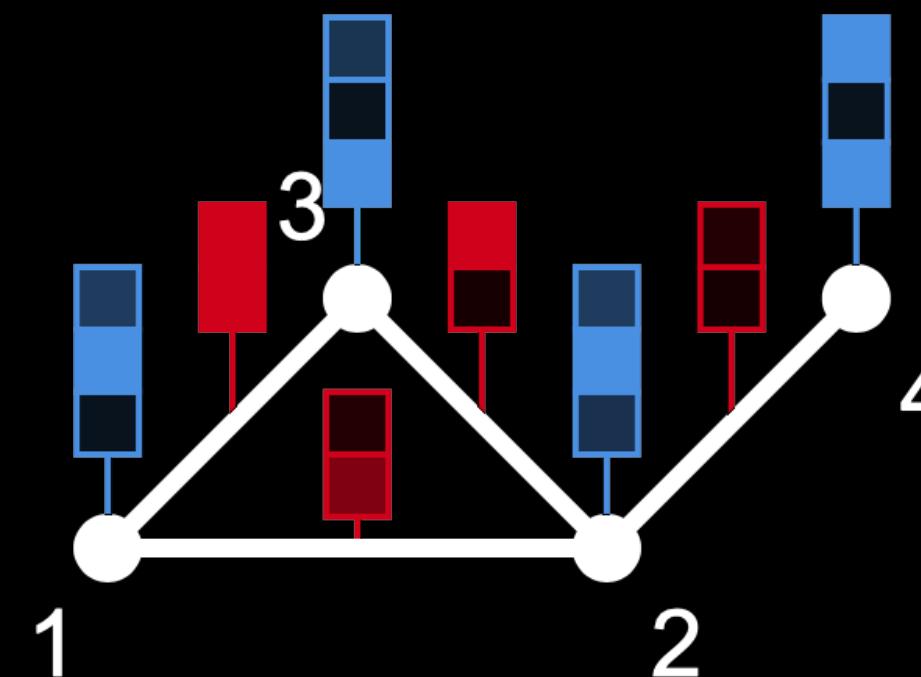
# Statistical Solver Problems

## Limits of Standard Neural Networks



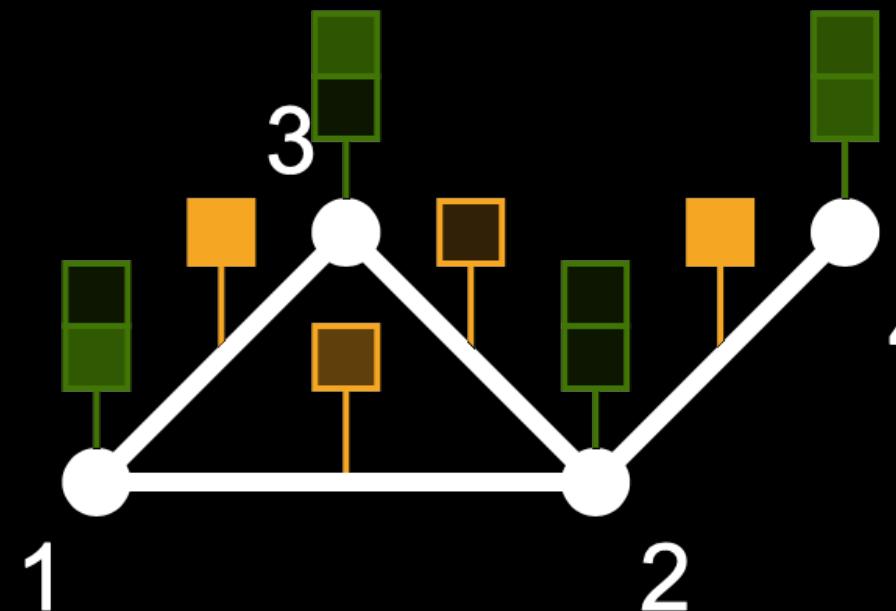
# Statistical Solver Problems

## Limits of Standard Neural Networks

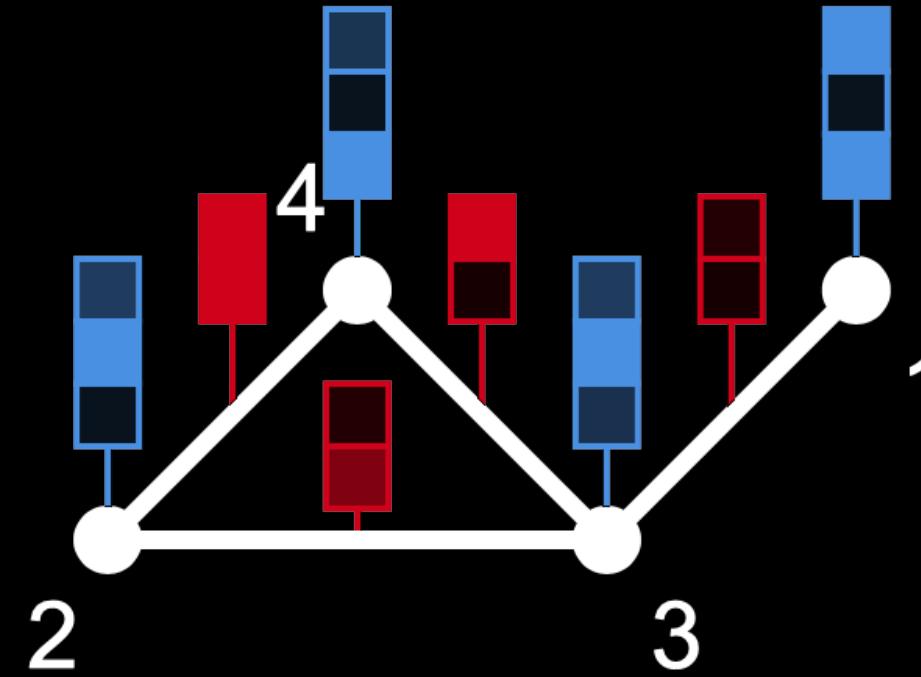


$1 \rightarrow 2$   
 $2 \rightarrow 3$   
 $3 \rightarrow 4$   
 $4 \rightarrow 1$

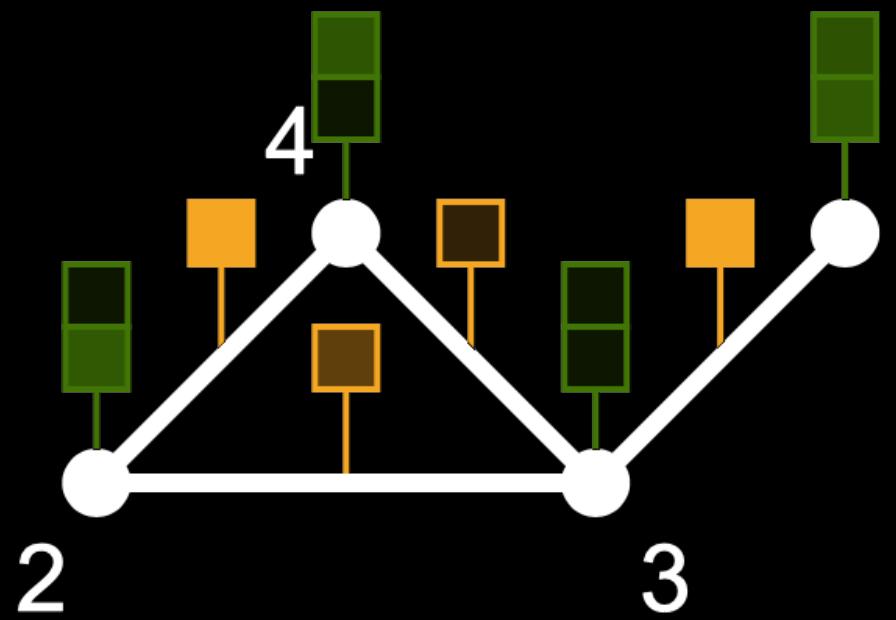
Standard  
Neural Net



$$\ell(x, y) \approx 0$$



Standard  
Neural Net



$$\ell(x, y) \gg 0$$

# Standard Neural Networks are not permutation-equivariant.

# Graph Neural Networks

# Graph Neural Networks

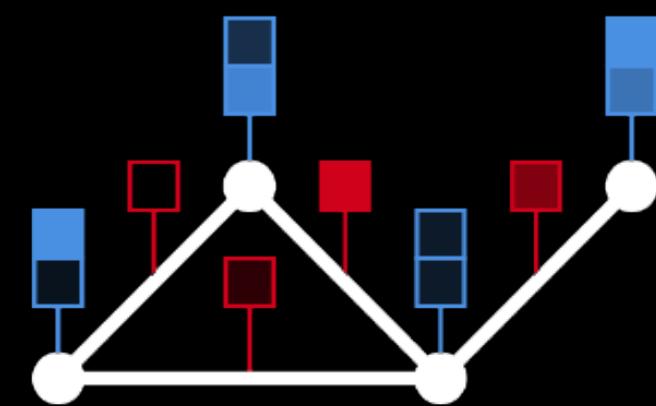
## Message Passing GNN



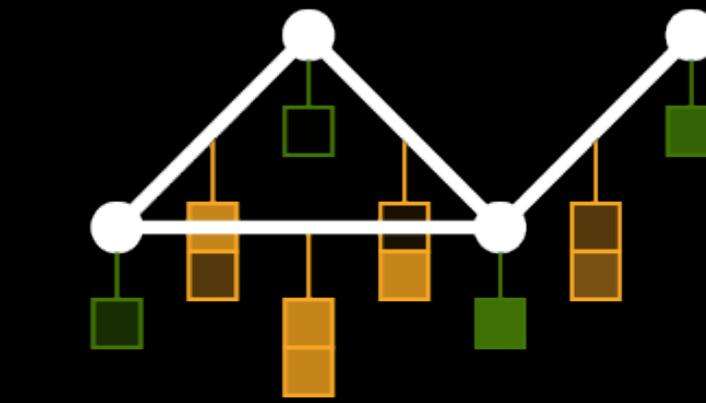
- Message Passing Graph Neural Networks :
  - Iterative process
  - Propagates information locally

# Graph Neural Networks

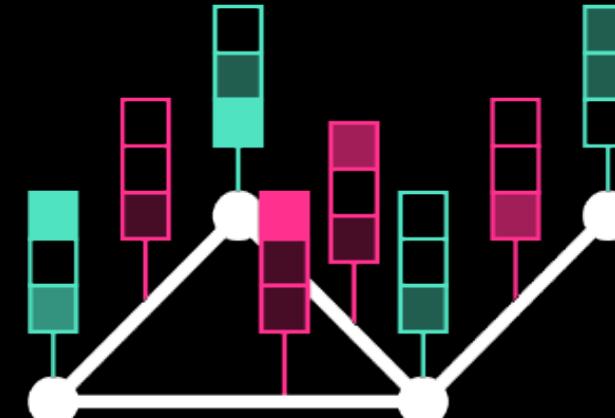
## Message Passing GNN



↓ Encoding

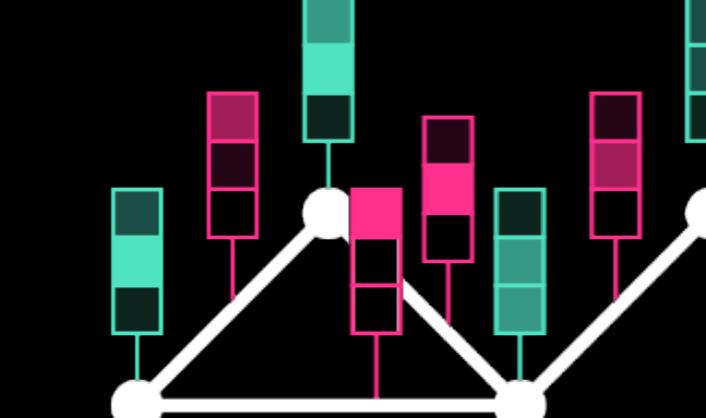
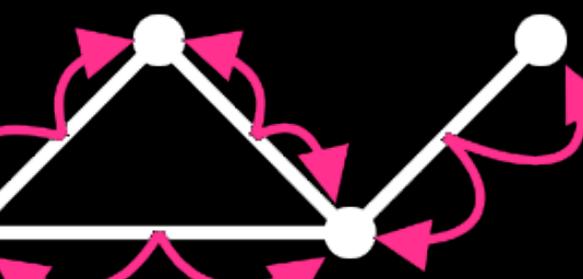
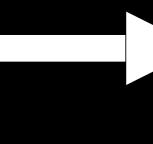
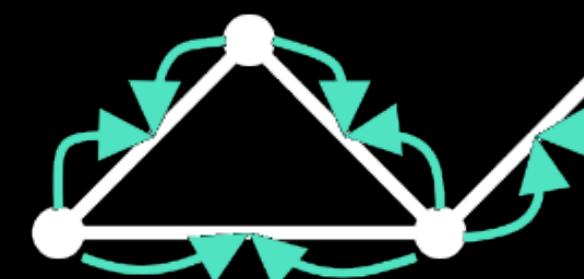


Decoding ↑



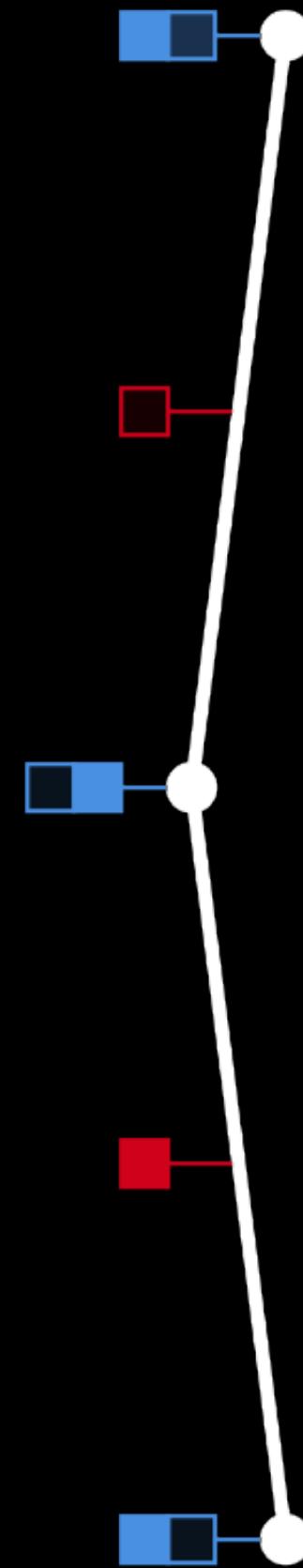
Message passing

D times



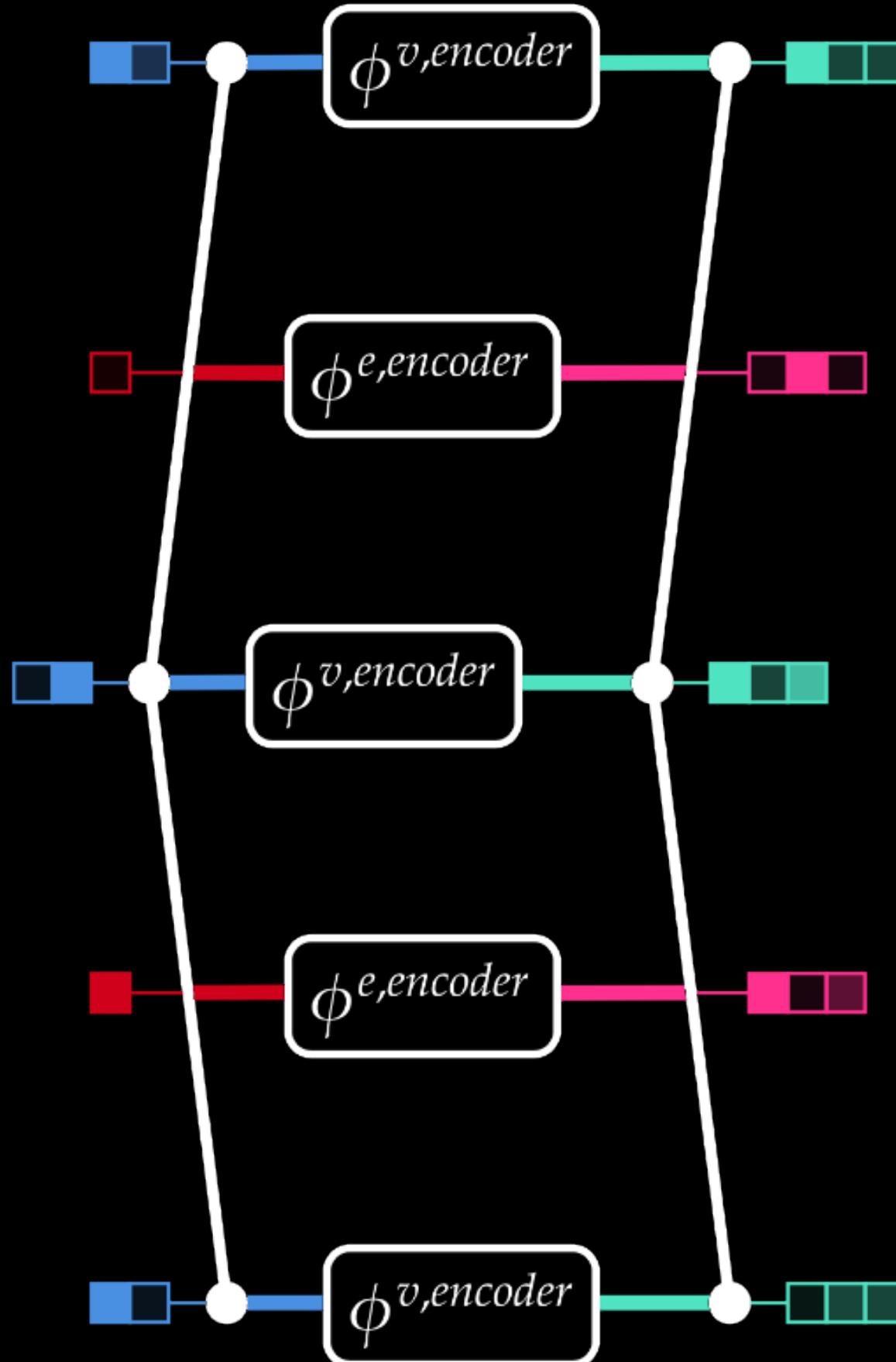
# Graph Neural Networks

## Example



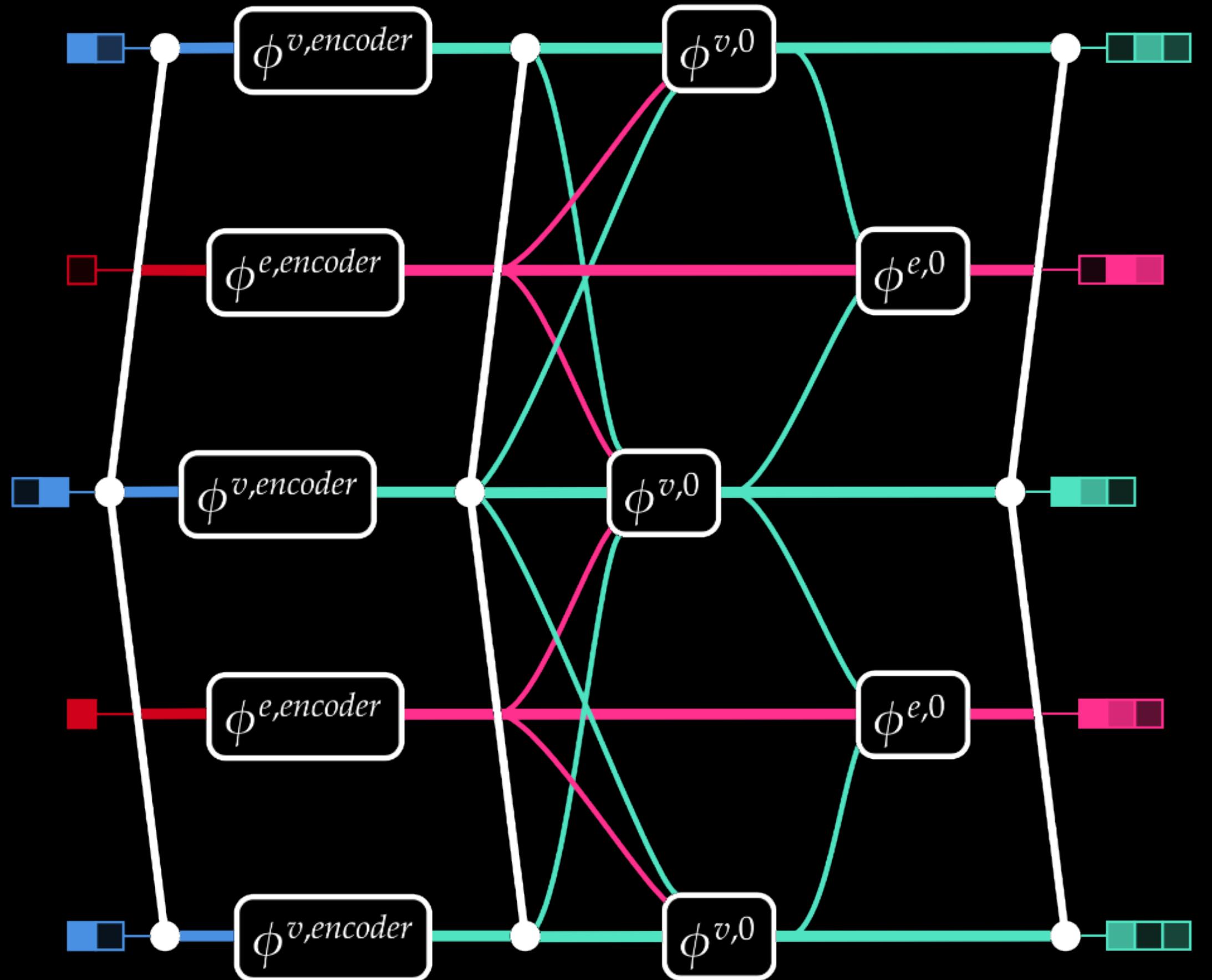
# Graph Neural Networks

## Example



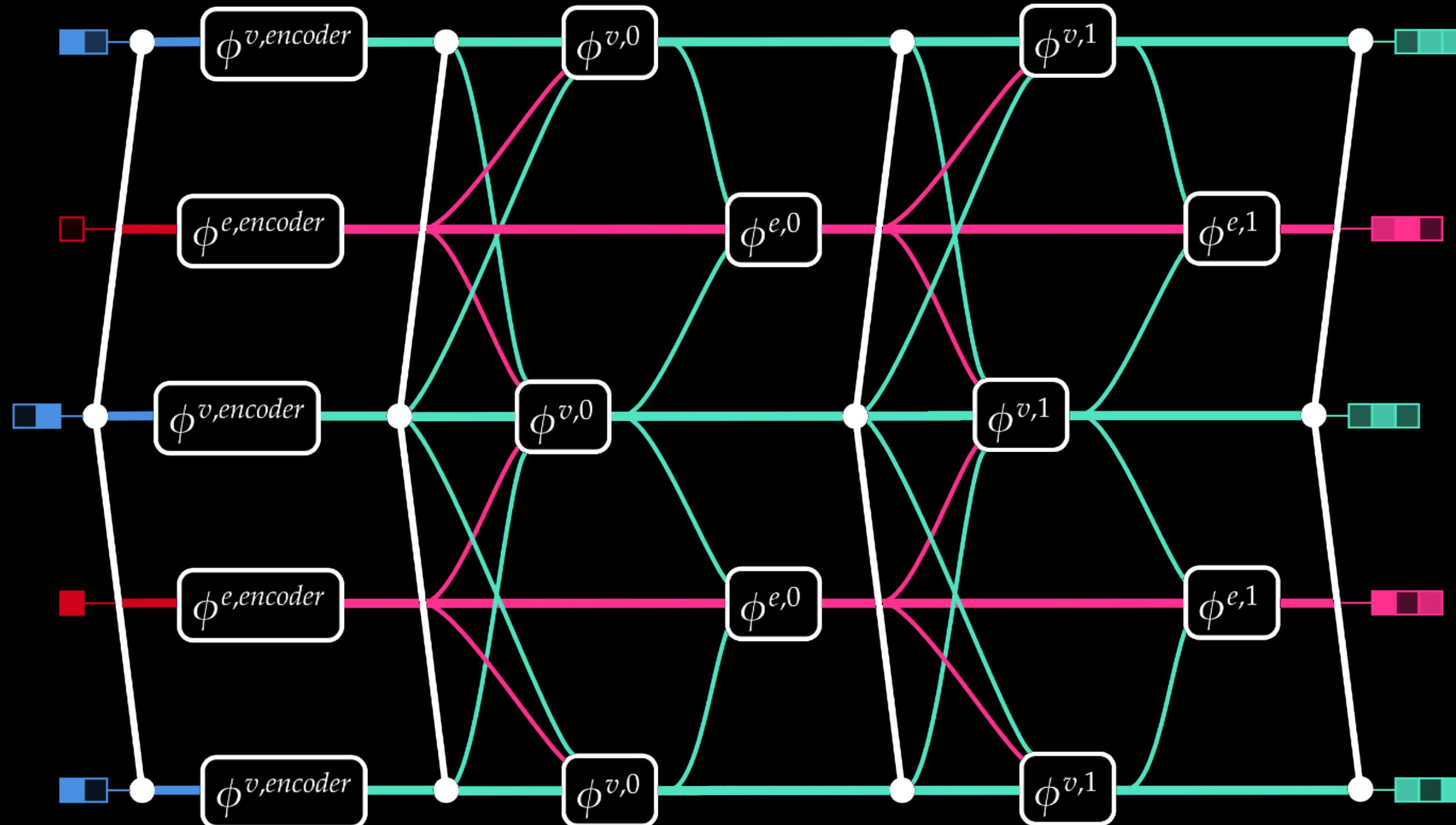
# Graph Neural Networks

## Example



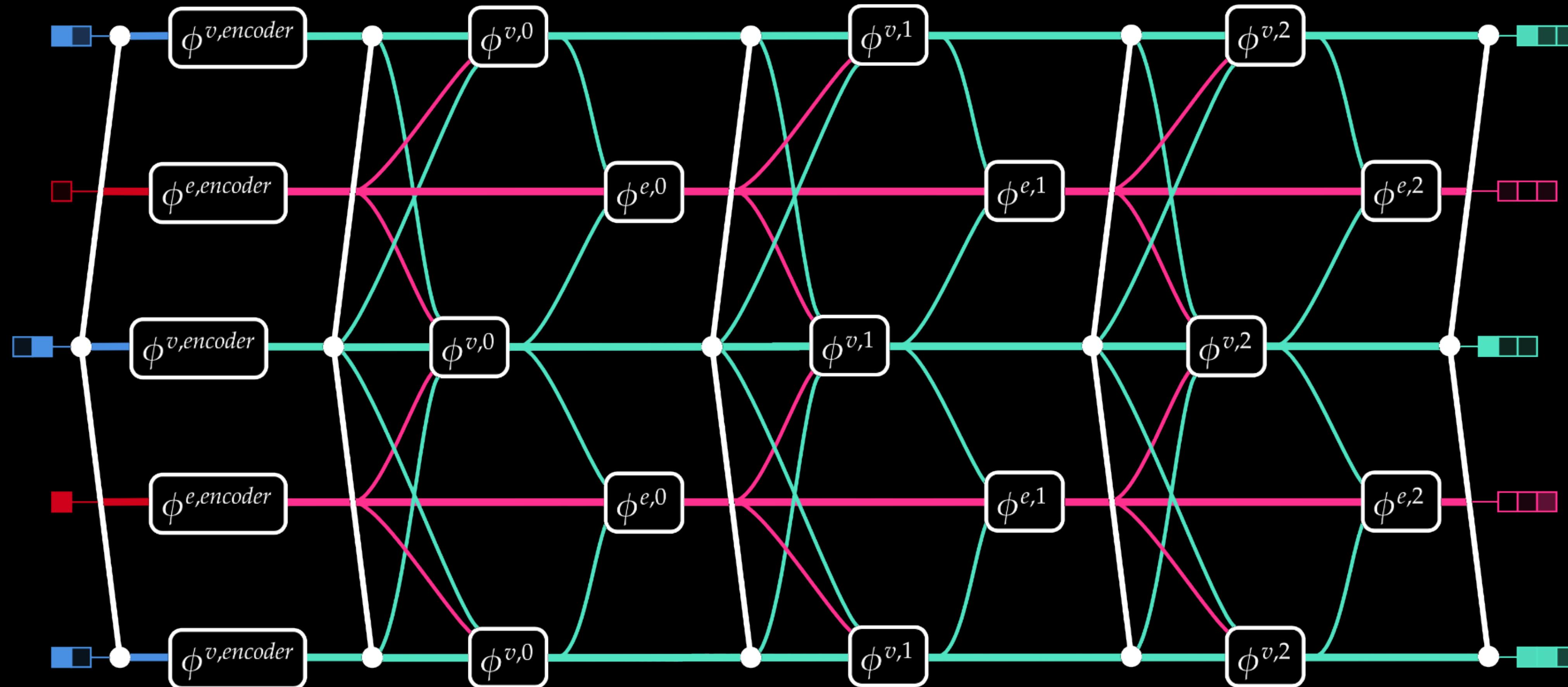
# Graph Neural Networks

## Example



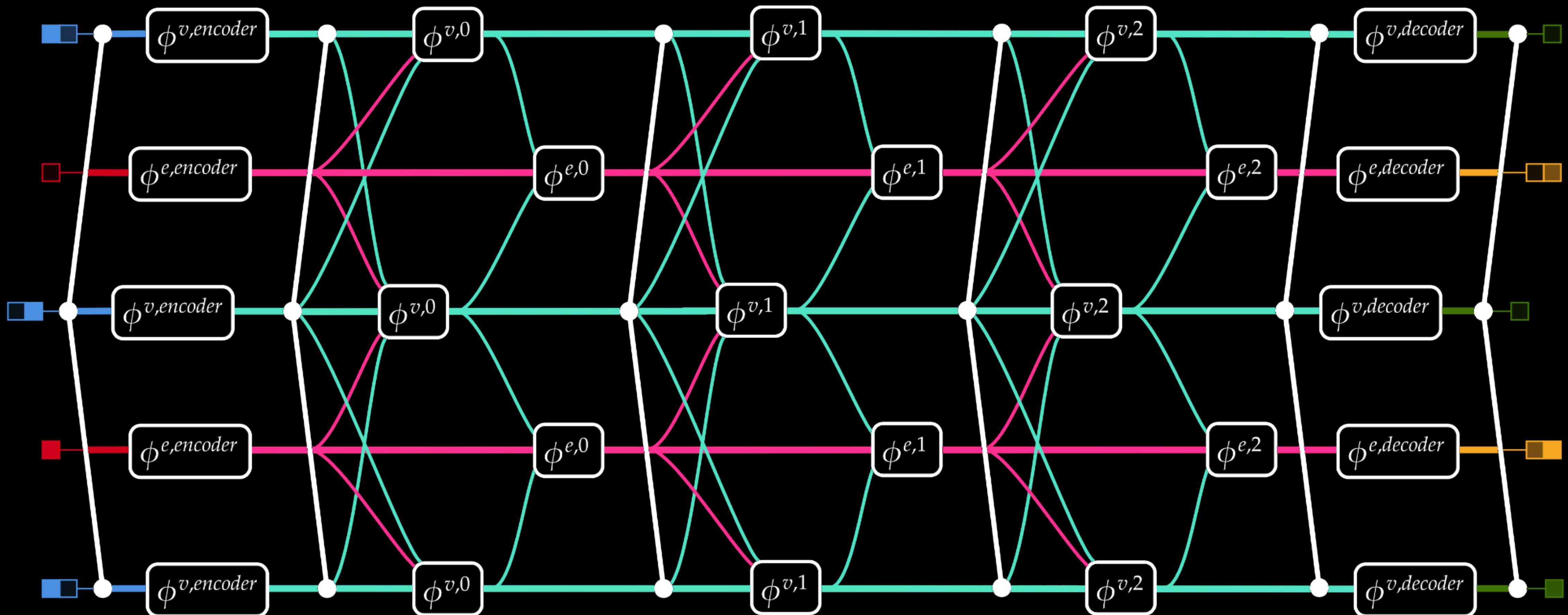
# Graph Neural Networks

## Example



# Graph Neural Networks

## Example



# Graph Neural Networks

## Properties



- Only local operations.
- Neural network blocks are trained jointly.
- Permutation equivariant.

# Graph Neural Networks

## Deep Statistical Solver



- A Deep Statistical Solver is a Graph Neural Network  $f_\theta$  trained so as to minimize

$$\mathbb{E}_{x \sim p} [\ell(x, f_\theta(x))]$$

# Universal Approximation Theorem

# Universal Approximation Theorem

## Summary



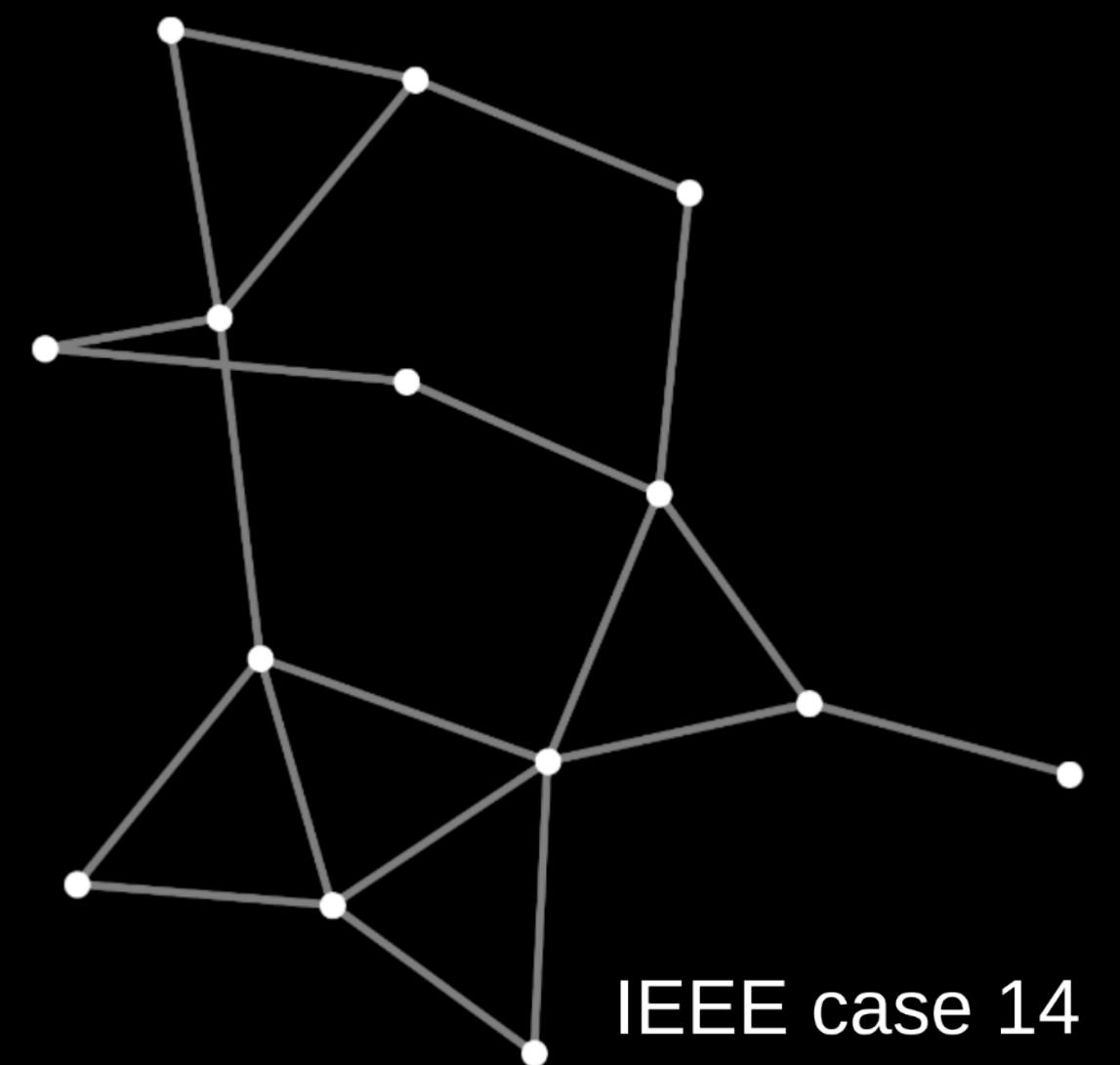
- GNNs can approximate an actual Newton-Raphson solver to an arbitrary precision.
- It requires more propagation steps than the largest graph diameter.

# Power Systems Experiments

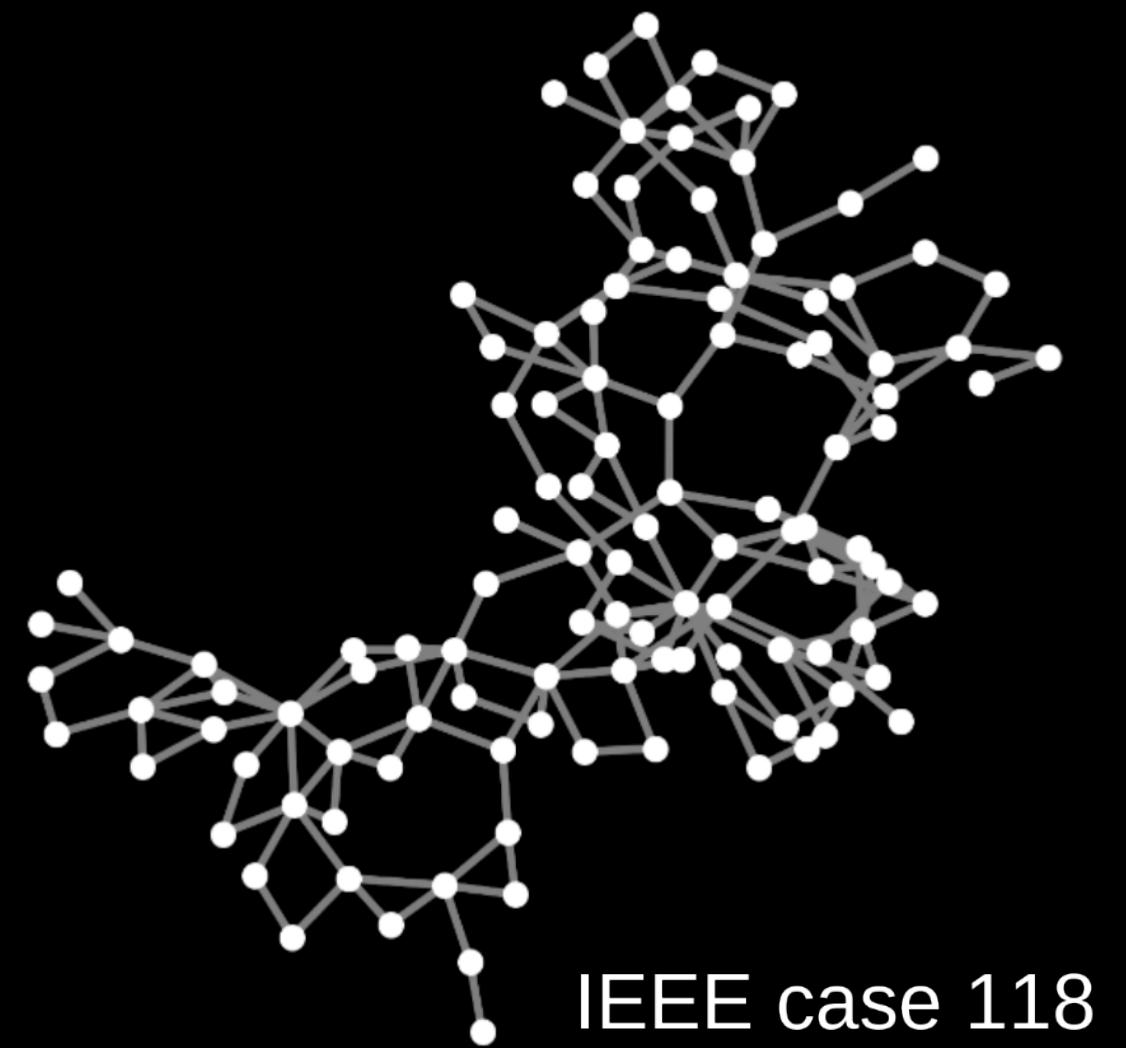
# Power Systems Experiments

## Setup

- Random injections
- Random line disconnections



IEEE case 14



IEEE case 118

# Power Systems Experiments

## Results



Dataset		IEEE 14 nodes			IEEE 118 nodes		
Method		DSS	Proxy	NR	DSS	Proxy	NR
Corr. w/ NR	$v_i$	.9993	> .9999	-	.9979	> .9999	-
	$\vartheta_i$	.9986	> .9999	-	.8131	> .9999	-
	$p_{ij}$	> .9999	> .9999	-	> .9999	> .9999	-
	$q_{ij}$	> .9999	> .9999	-	> .9999	> .9999	-
nRMSE w/ NR	$v_i$	2.0e-3	4.9e-4	-	1.4e-3	1.2e-3	-
	$\vartheta_i$	7.1e-3	1.7e-3	-	5.7e-2	4.5e-3	-
	$p_{ij}$	6.2e-4	2.6e-4	-	1.0e-3	3.9e-4	-
	$q_{ij}$	4.2e-4	2.0e-4	-	1.1e-4	1.7e-4	-
Loss 10 <sup>th</sup> p.		4.2e-6	2.3e-5	1e-12	1.3e-6	6.2e-6	3e-14
Loss 50 <sup>th</sup> p.		1.0e-5	4.0e-5	2e-12	1.7e-6	8.3e-6	4e-14
Loss 90 <sup>th</sup> p.		4.4e-5	1.2e-4	3e-12	2.5e-6	1.3e-5	6e-14

Our trained DSS models are highly correlated with the Newton-Raphson solutions.

# Summary

# PhD Summary

## Main Contributions



We have designed a full-fledged optimization method that

- is trained by direct minimization of physical laws;
- aims at solving a distribution of problem instances;
- respects the permutation-invariance of the problem;
- relies on the training of a graph neural network heuristics;
- is theoretically grounded by a Universal Approximation Theorem.



# GNNs for Voltage Management

## Post Doctoral Research Project

# Project Overview

# Project Overview

## Team

- Collaboration between **RTE R&D** and **Institut Montefiore** (Liège Université).



Louis  
Wehenkel

Professor - ULiège



François  
Cubelier

PhD student - ULiège



Efthymios  
Karangelos

Postdoc - ULiège



Laure  
Crochepierre

Researcher - RTE



Balthazar  
Donon

Postdoc - ULiège



# Project Overview

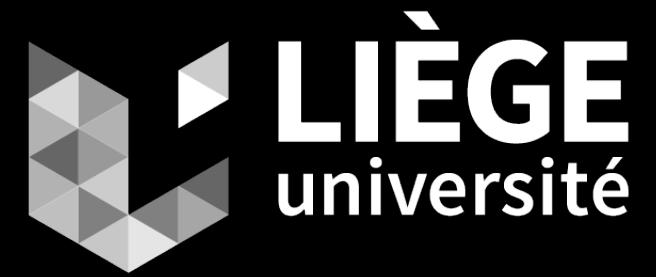
## Industrial Motivations



- Increasing amount of high voltage events.
- In the future, it may become even more complex.
  - We want to anticipate and develop real-time methods for voltage management, based on Graph Neural Networks (GNNs).

# Project Overview

## Industrial Motivations



- To ensure that voltages are admissible, dispatchers can adjust :
  - Voltage set points at pilot buses (secondary voltage control)
  - The opening / closing of transmission lines
  - Activate / deactivate shunts
  - Activate / deactivate synchronous condensers
  - Set points of static VAR compensators

# Project Overview

## Research Motivations

- Prove the viability of GNNs for real-life industrial problems
- GNN-based control policy for voltage management



# Project Overview

## Research Motivations

$x$  - Power Grid Snapshot

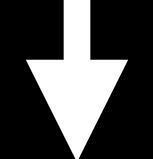


# Project Overview

## Research Motivations

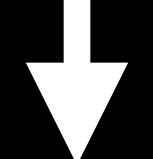
$x$  - Power Grid Snapshot

$\Pi_\theta$  - Control Policy



$y$  - Action

AC Power Flow Simulator



$r$  - Reward

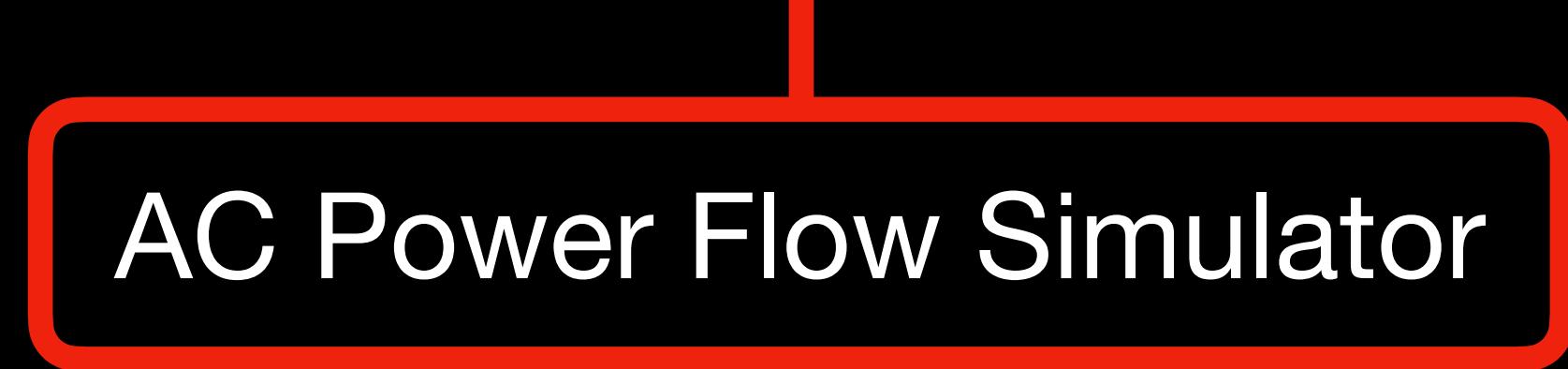
# Project Overview

## Research Motivations

$x$  - Power Grid Snapshot



$y$  - Action



Non-differentiable

$r$  - Reward

# Project Overview

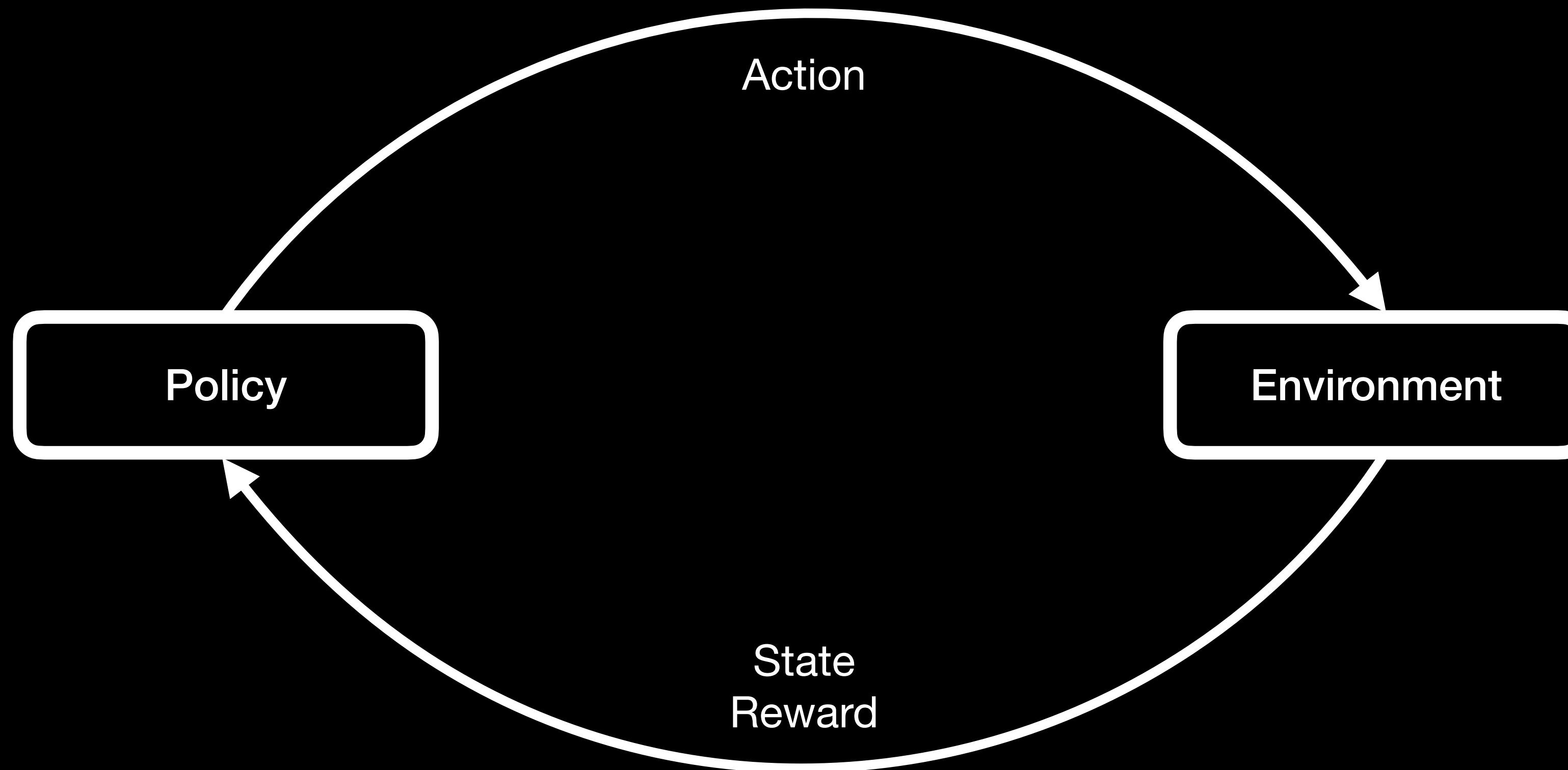
## Simulator



- Non-differentiable simulator
  - Discrete control variables
  - Divergence issues
  - Easier to replace
- Need to use gradient-free methods (Reinforcement Learning literature)

# Project Overview

## Simulator



# Project Overview

## Reward

- Primary objective : Joule losses
- Relaxed constraints :
  - Voltage in admissible range
  - No line overflow
  - Generator reactive margins

Can we train a GNN-based policy to solve  
real-life voltage management problems in  
an unsupervised and gradient-free way ?

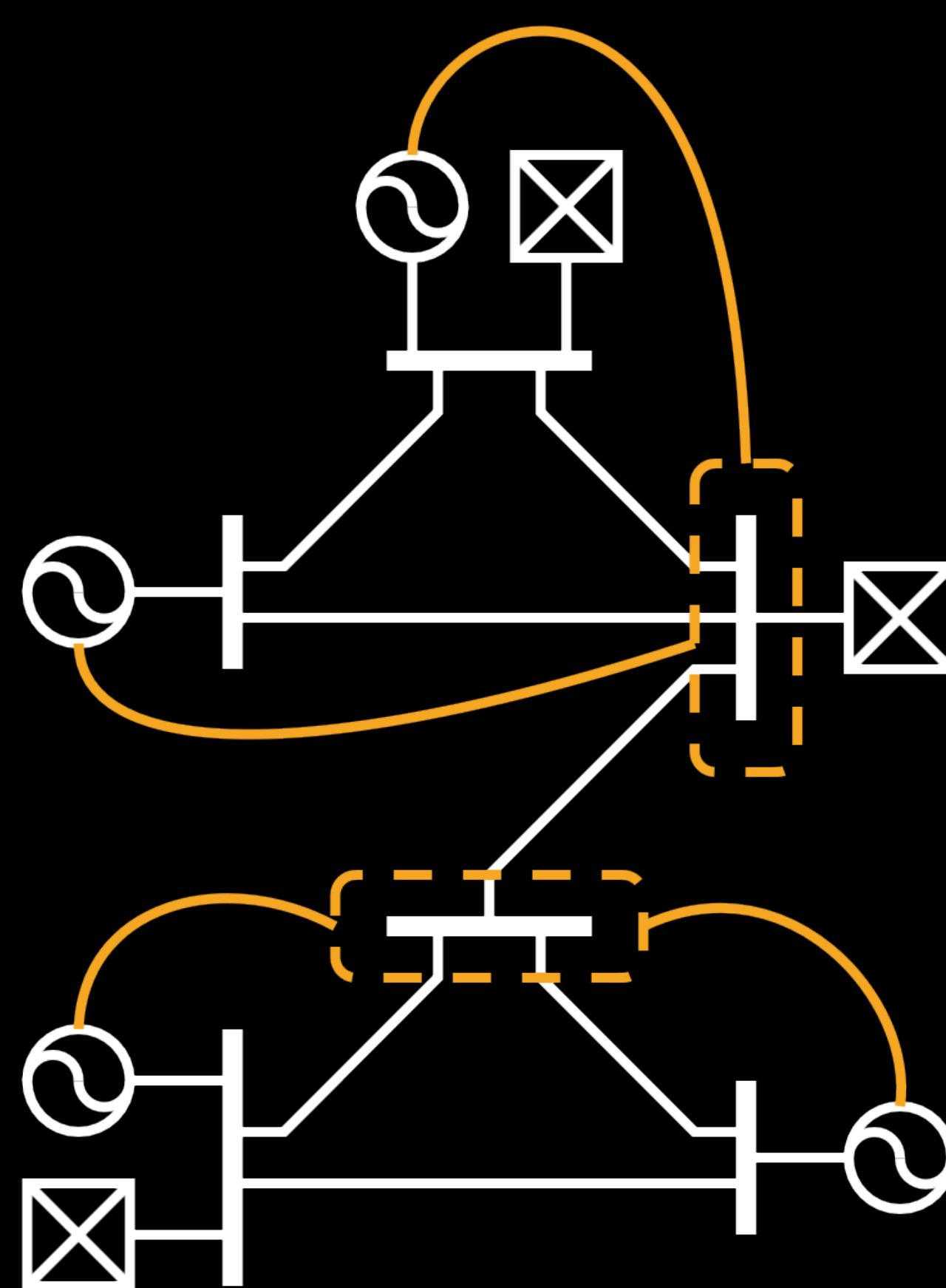
# Data & Neural Networks

# Data & Neural Networks

## Power Grid vs. Hyper Heterogeneous Multi Graph (H2MG)

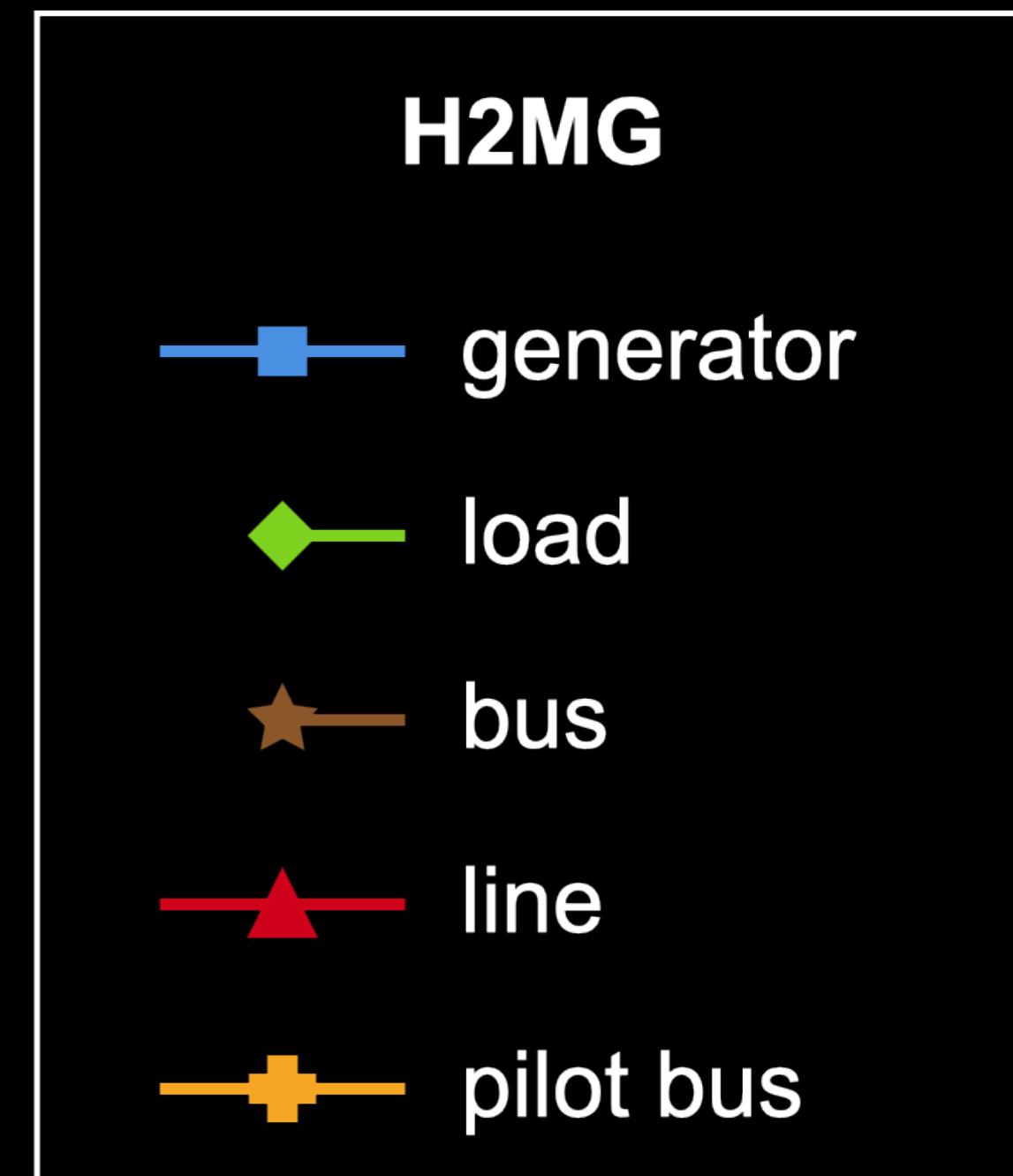
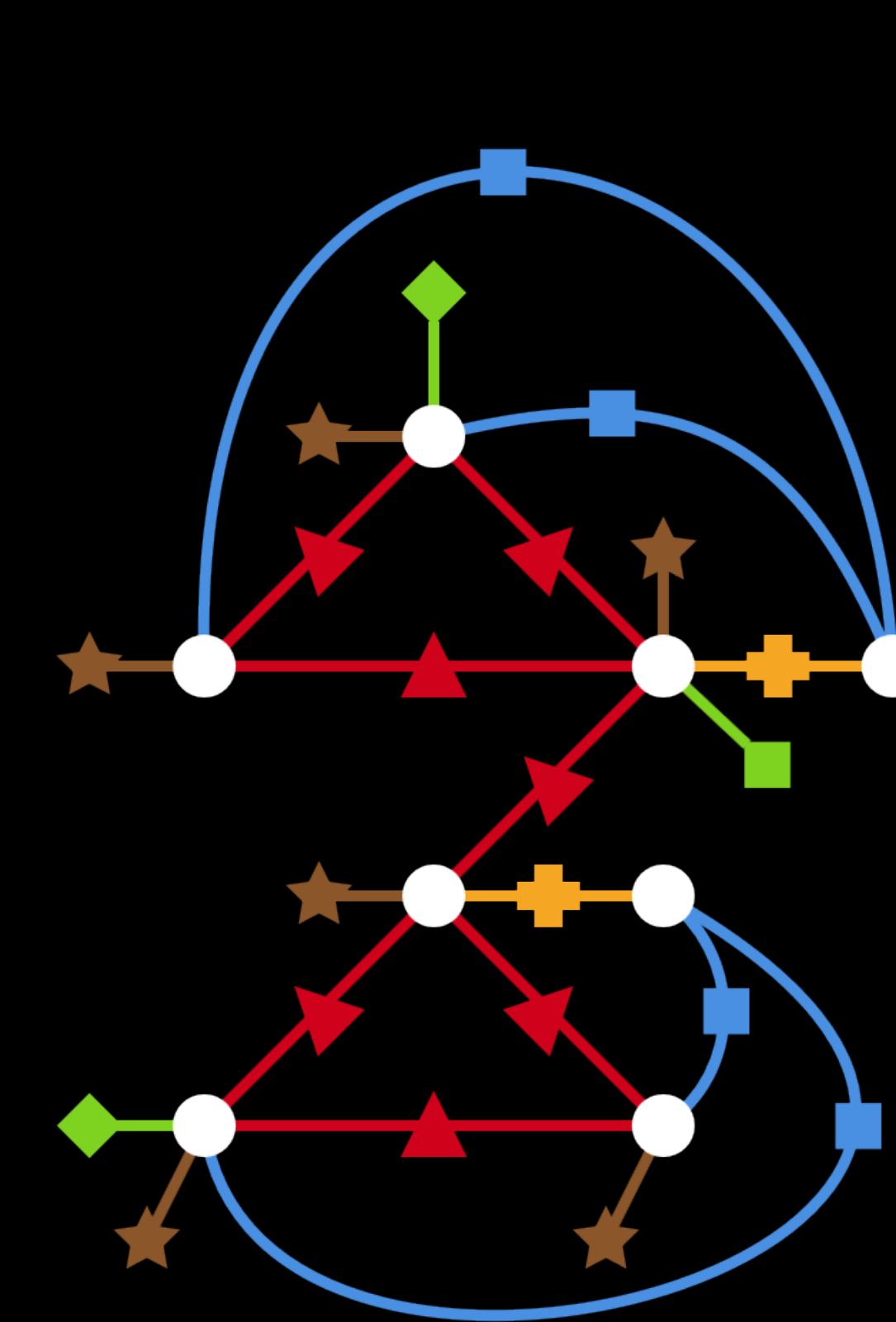
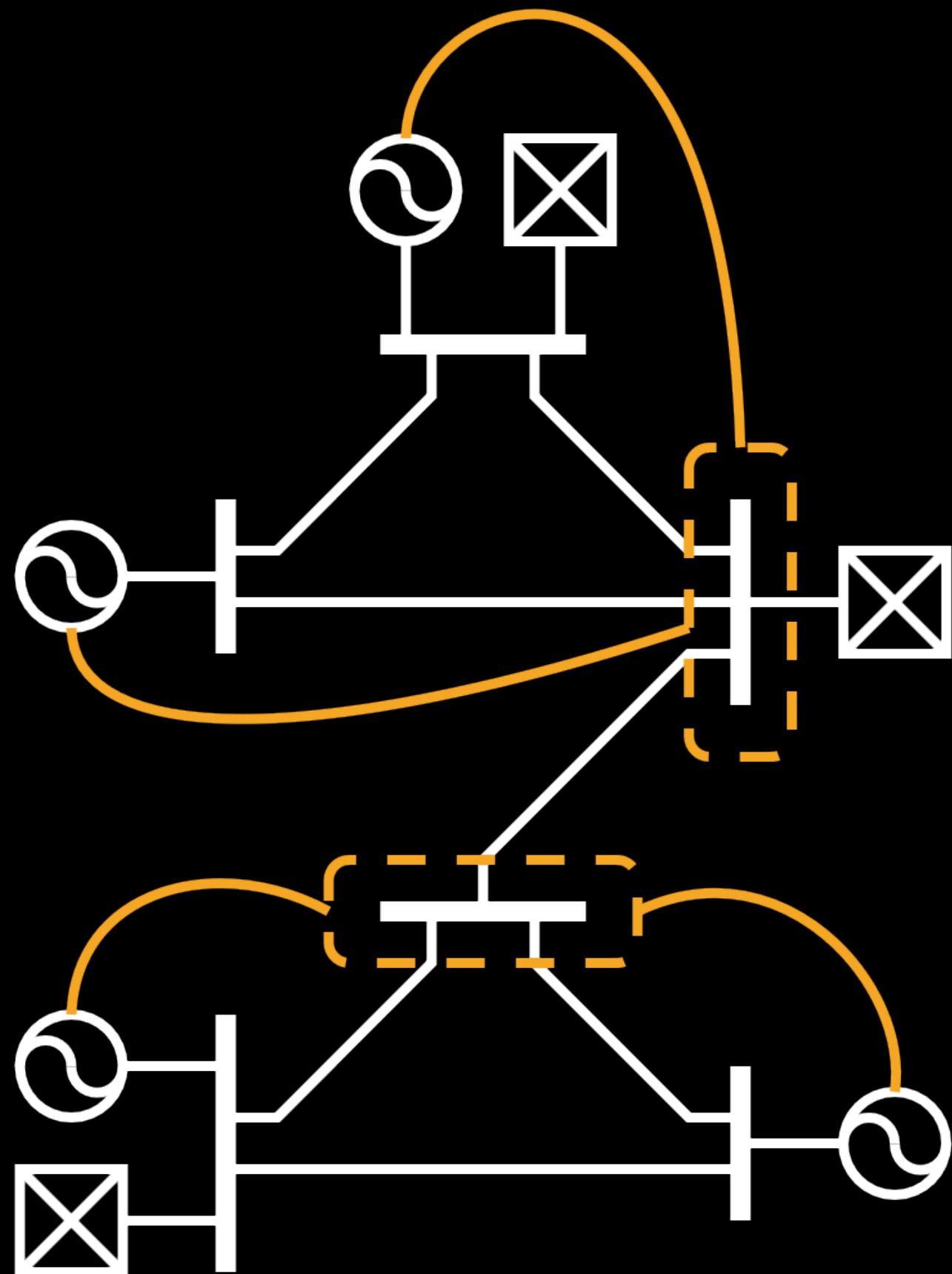
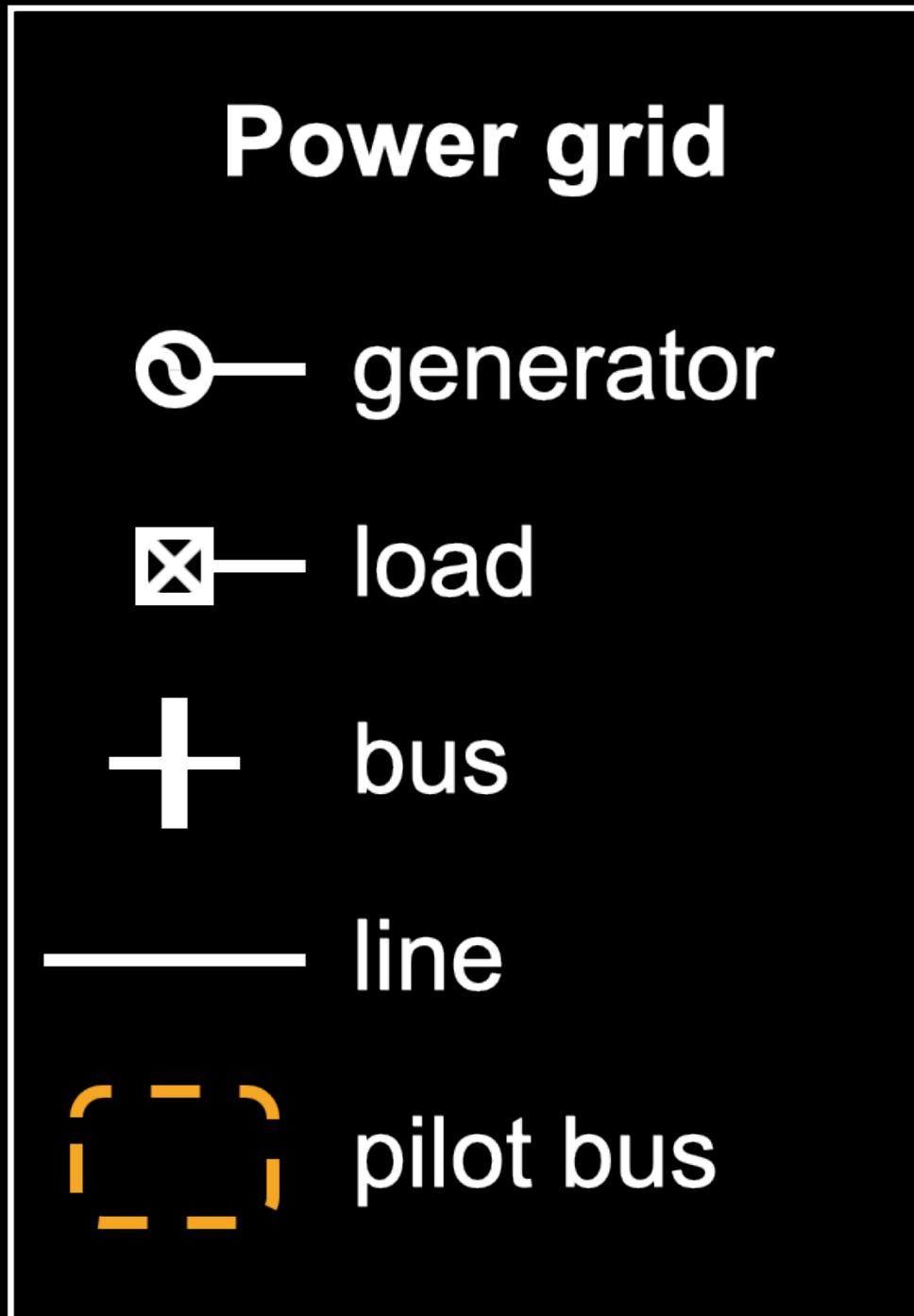
### Power grid

- generator
- load
- bus
- line
- pilot bus



# Data & Neural Networks

## Power Grid vs. Hyper Heterogeneous Multi Graph (H2MG)

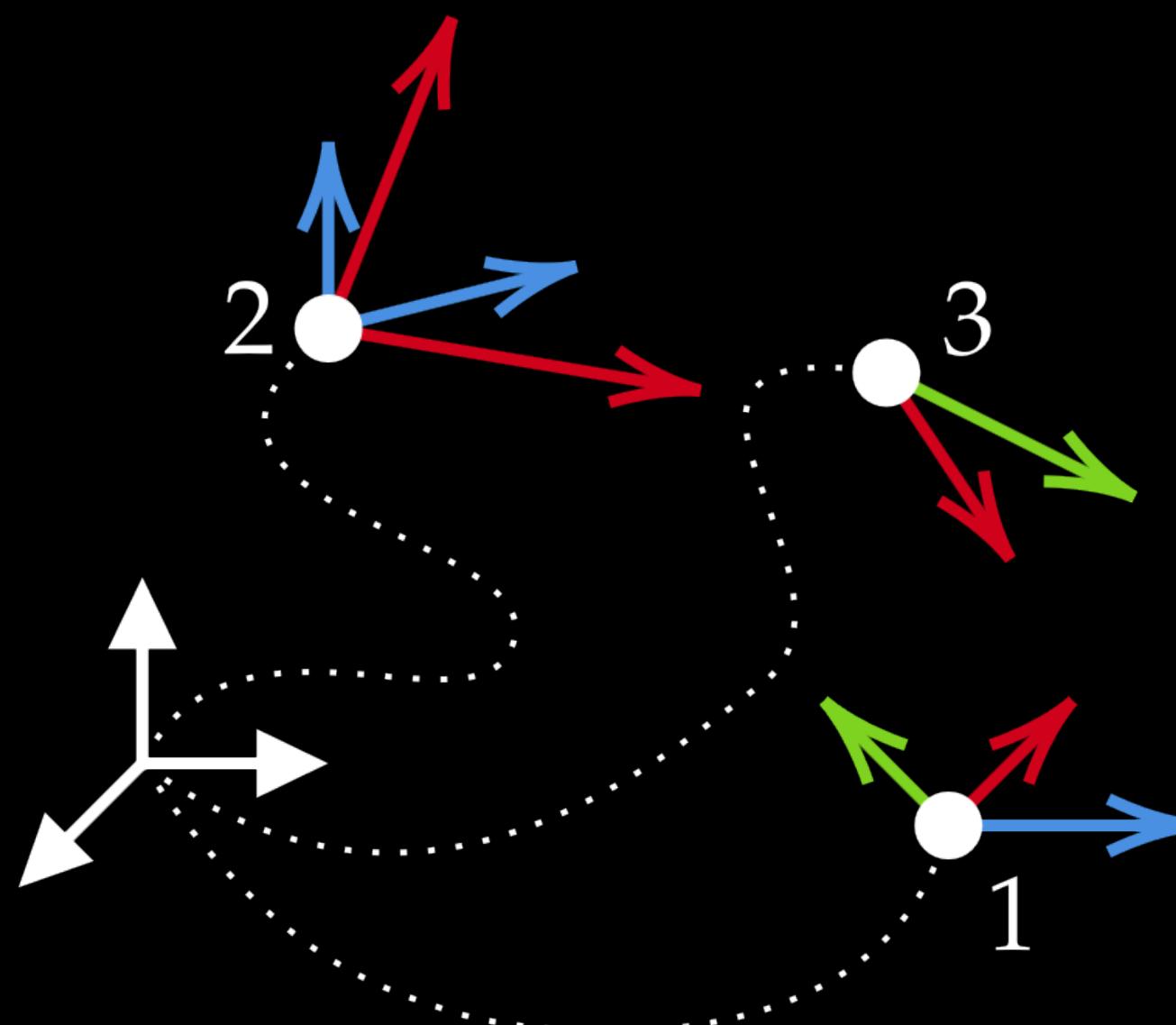
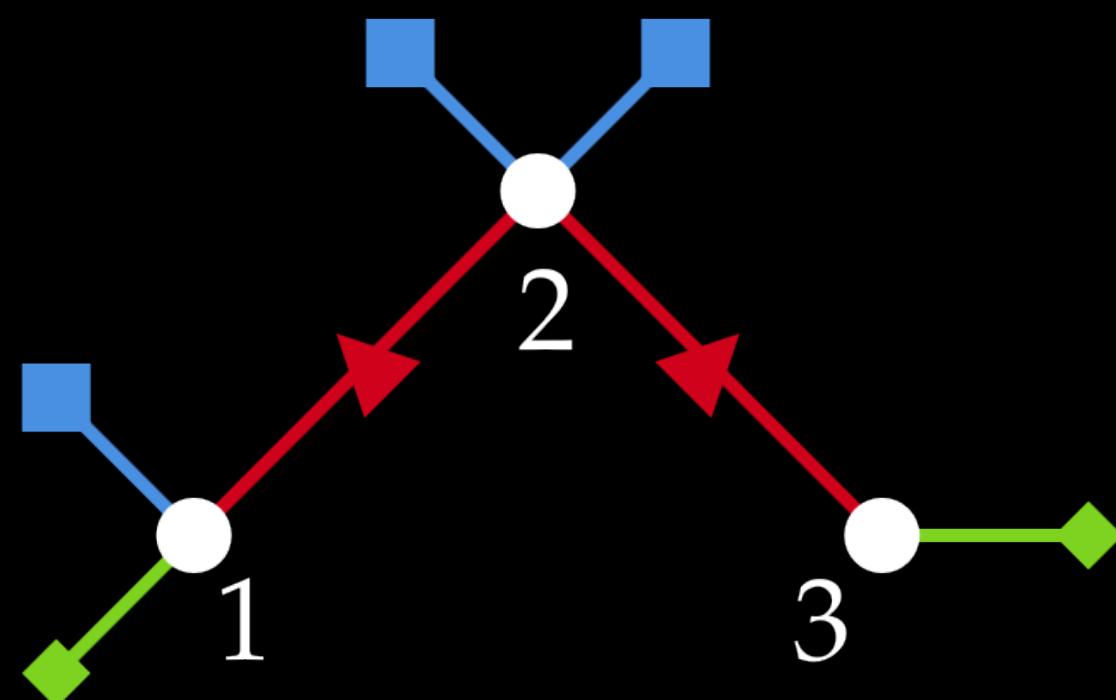


# Data & Neural Networks

## Example

Latent trajectories

Input data



$$\frac{dh_i}{ds} = \tanh \left[ \sum_{(c,e,o) \in \mathcal{N}(i)} \Phi_{\theta}^{c,o}(x^g, x_e^c, h^g, (h_{o(e)})_{o \in \mathcal{O}^c}, t) \right]$$

# Data & Neural Networks

## Trajectories



!

# Data & Neural Networks

## Main Novelties

- Hyper Heterogeneous Multi Graph (H2MG)
  - Seamless representation of power grids.
  - Cyber-physical graph structure.
- Hyper Heterogeneous Multi Graph Neural Ordinary Differential Equation (H2MGNODE)
  - Dynamical system defined over H2MGs.



# Artificial Data

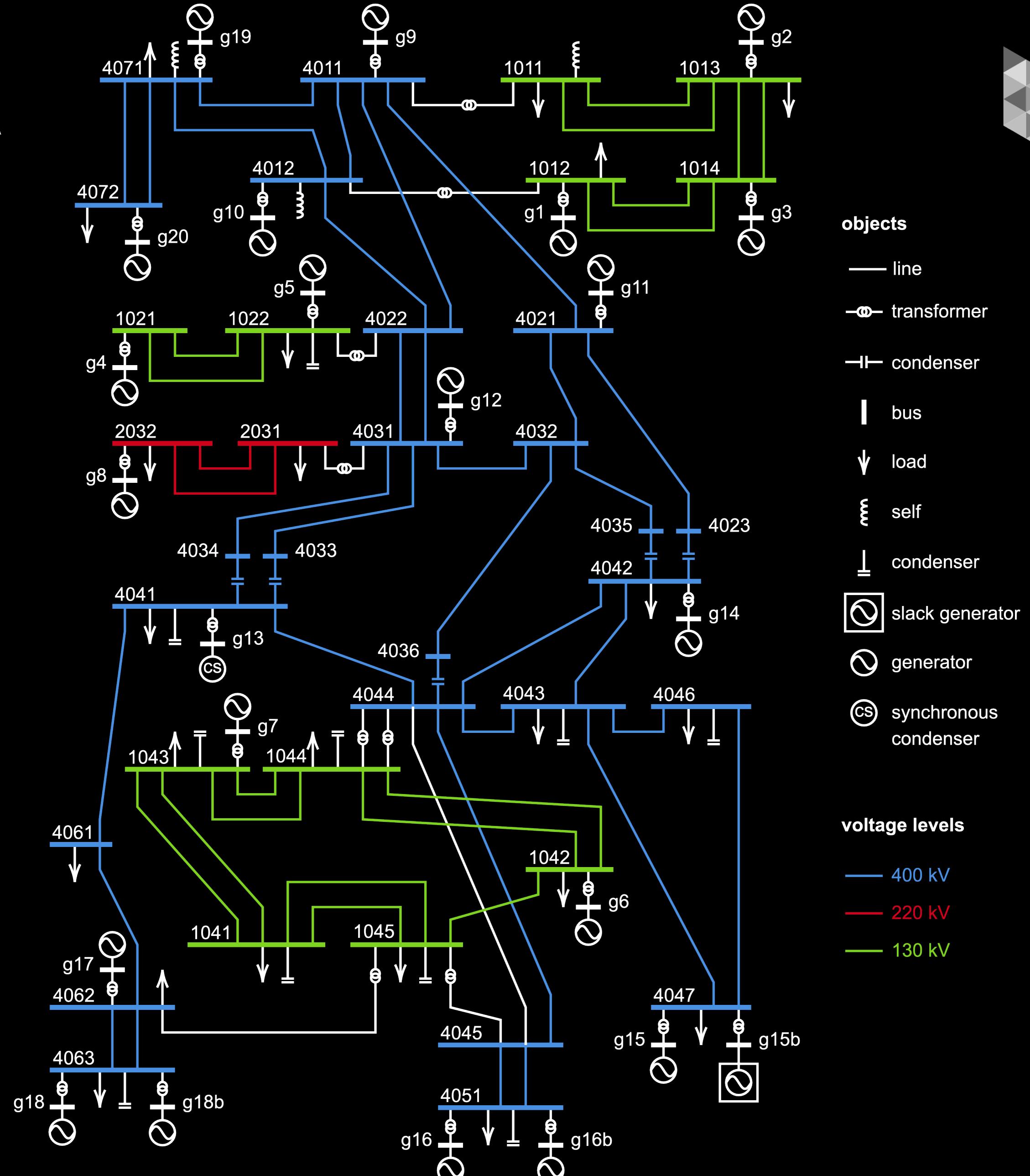
# Artificial Data Summary



- Swedish transmission system.
- Stems from and extends the Nordic32 test case (CIGRE Task Force 38.02.08).
- Enriched first by the research group of Thierry Van Cutsem, and then by Florin Capitanescu.
- 60 buses, 23 generators, 57 lines, 31 transformers, 22 loads, 12 shunts.

*Suppressing ineffective control actions in optimal power flow problems*, F. Capitanescu, IET Generation, Transmission & Distribution, 14 (13), pp. 2520-2527, 2020. doi: 10.1049/iet-gtd.2019.1783

# Artificial Data Diagram



objects

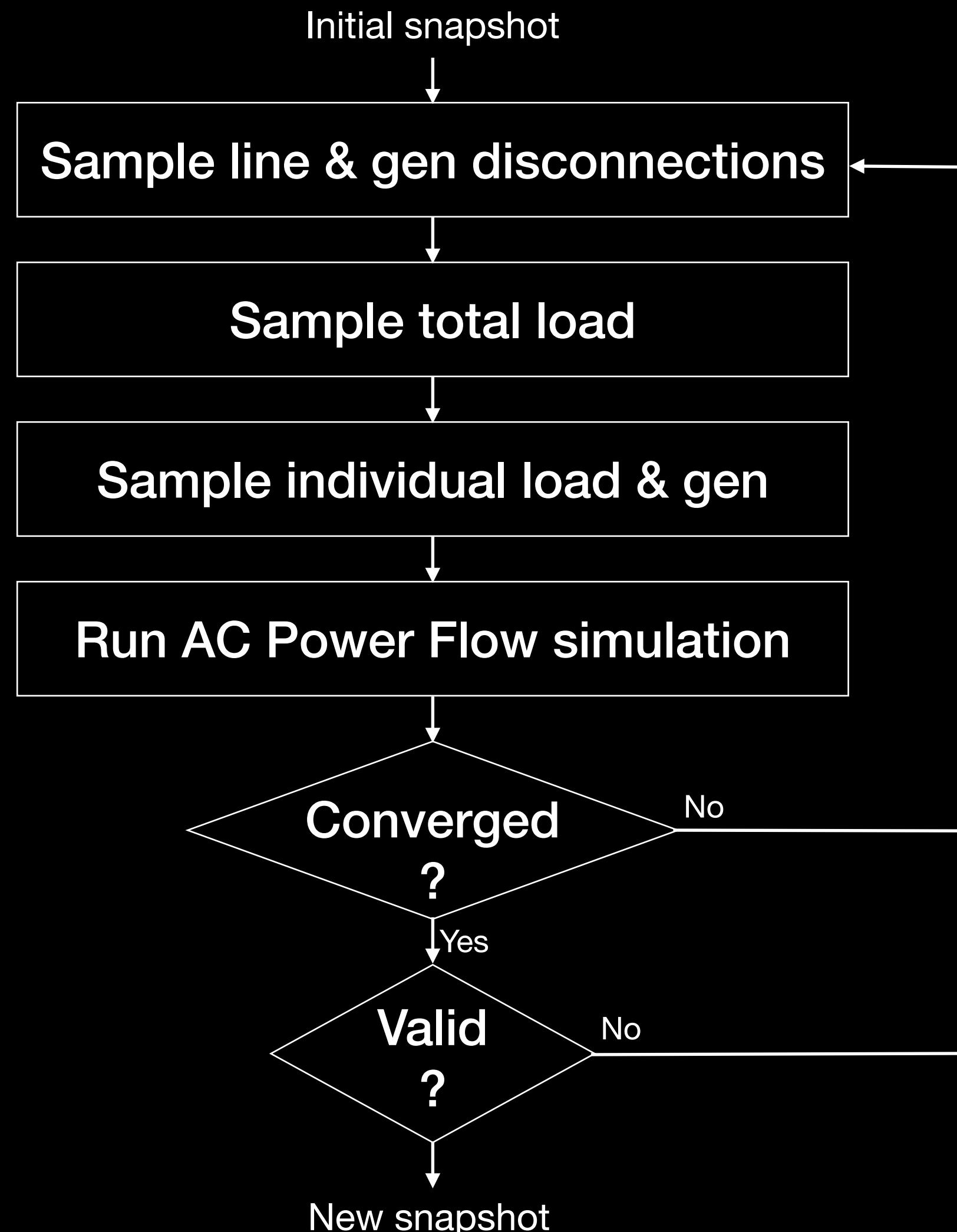
- line
- $\omega$ - transformer
- II- condenser
- | bus
- ↓ load
- $\xi$  self
- $\perp$  condenser
- slack generator
- generator
- cs synchronous condenser

voltage levels

- 400 kV
- 220 kV
- 130 kV

# Artificial Data

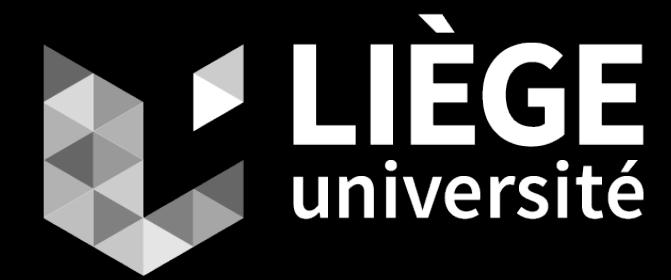
## Overview



# Cétautomatix

# Cétautomatix

## OPF Solver

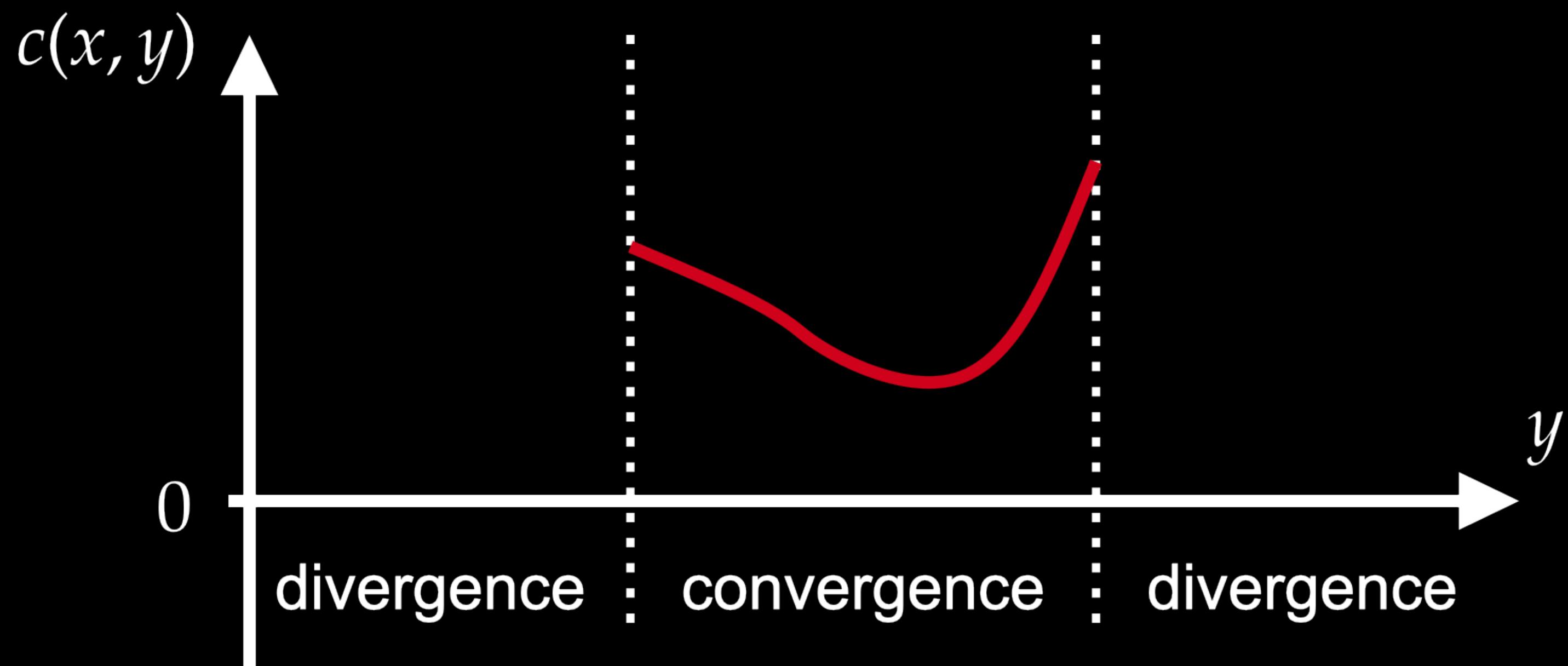


- Knitro (RTE License)
- 2 modes :
  - Constrained (if no feasible solution, solve the Relaxed version)
  - Relaxed (quadratic penalization of constraint violations)

# Idéfix

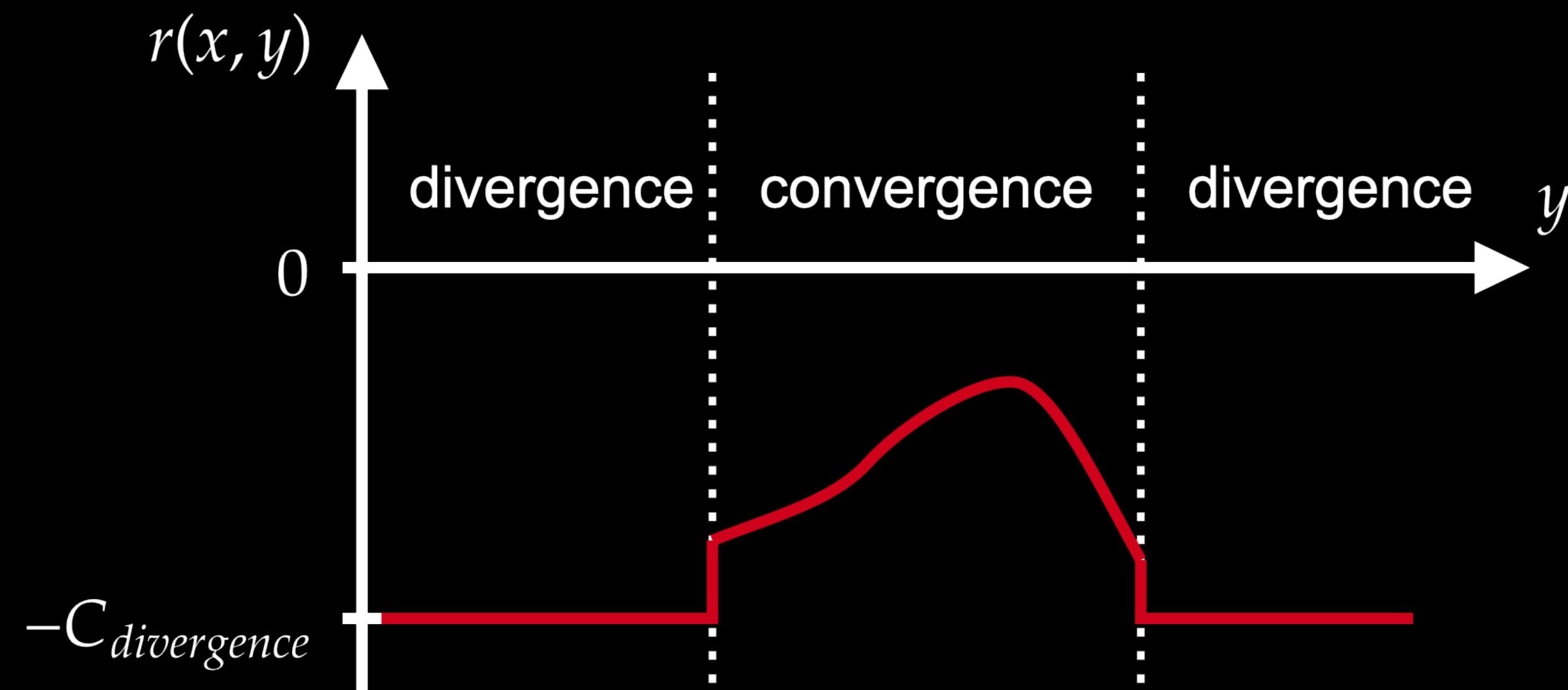
## Early Experiments

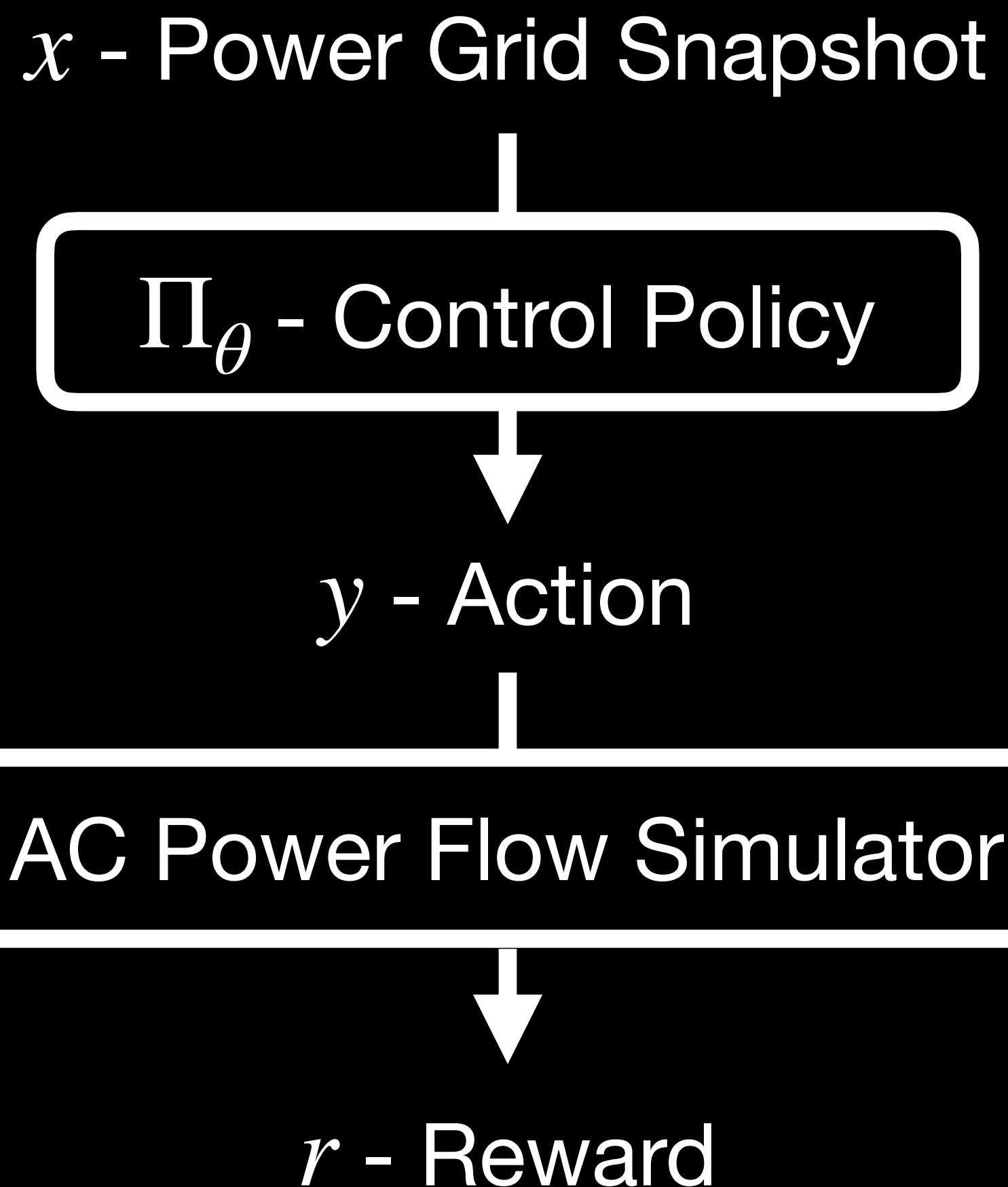
- Only continuous action variables:
  - Generator Voltage Setpoints
- Reward : Joule losses + quadratic penalization of constraint violations.
- Requires to run a power flow simulation.

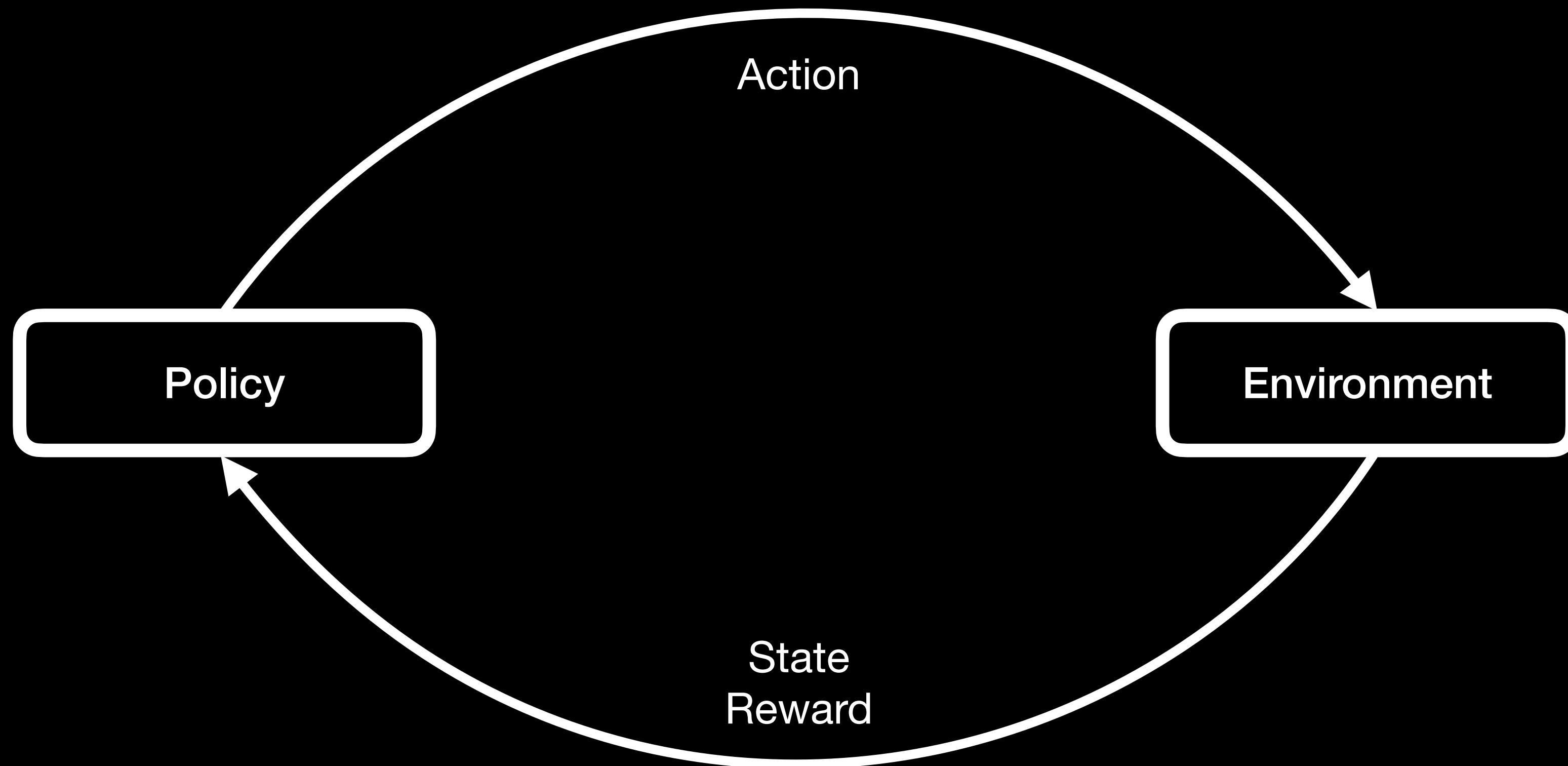


## Reward Function - Opposite of Cost

$$r(x, y) = \begin{cases} -c(x, y) & \text{if } (x, y) \text{ converges} \\ -C_{\text{div}} & \text{otherwise} \end{cases}$$

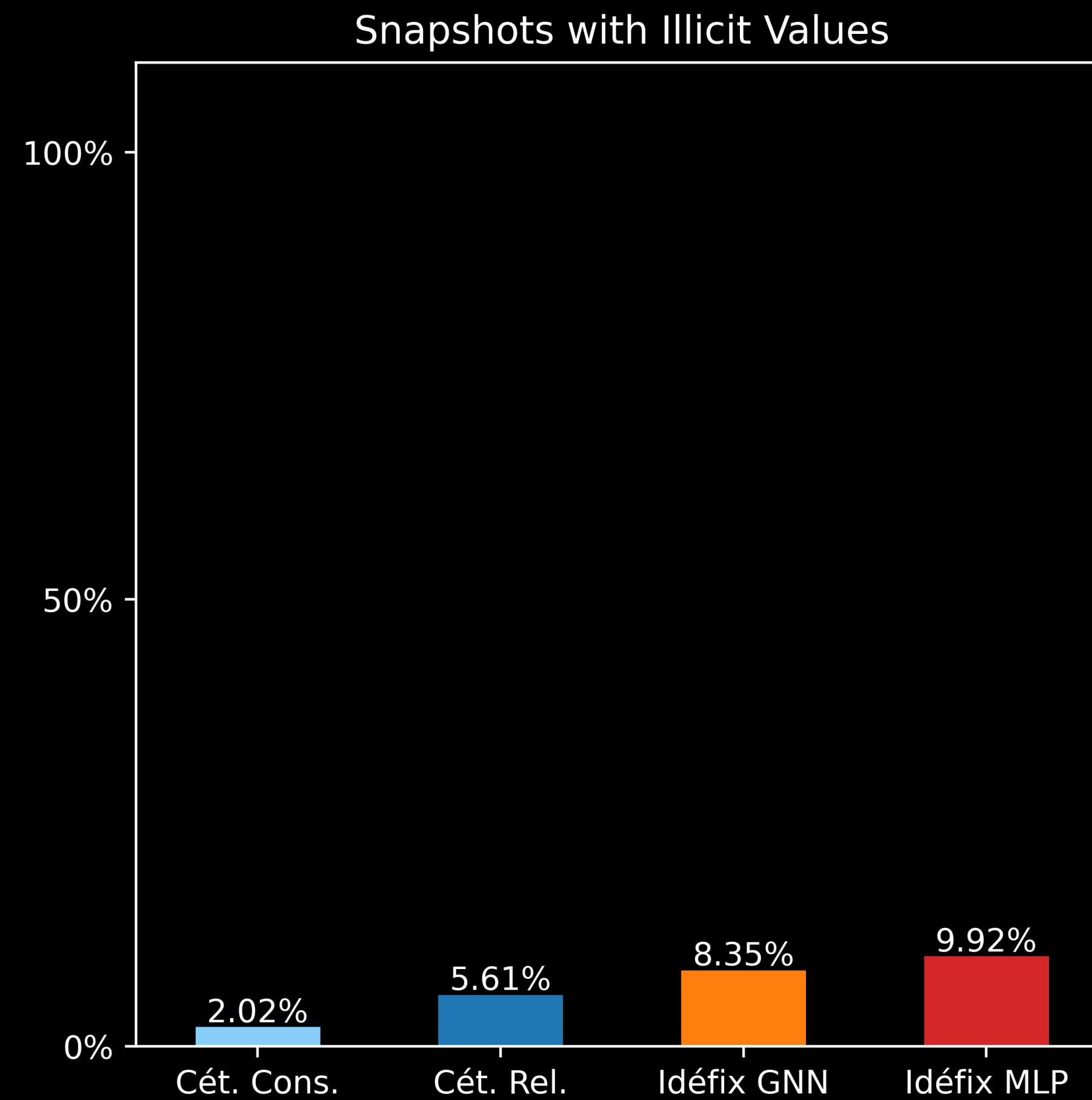






# Idéfix

## Illicit Snapshots



# Questions ?

# Thank you !