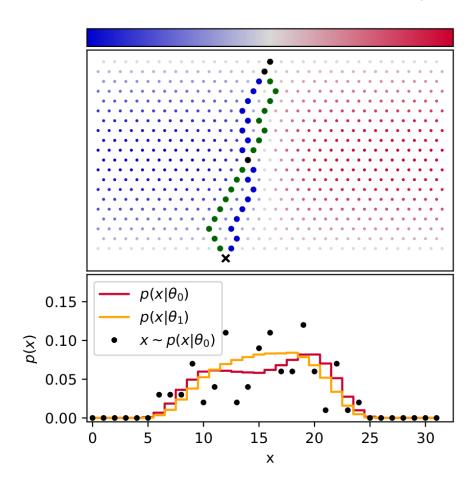


The probability of ending in bin x corresponds to the total probability of all the paths z from start to x.

$$p(x| heta) = \int p(x,z| heta) dz = inom{n}{x} heta^x (1- heta)^{n-x}$$

What if we shift or remove some of the pins?



The probability of ending in bin x still corresponds to the total probability of all the paths z from start to x:

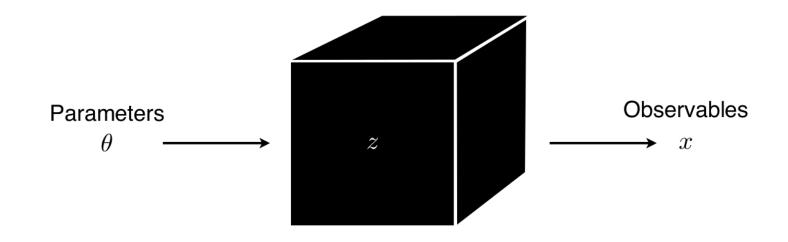
$$p(x| heta) = \int p(x,z| heta) dz$$

- But this integral can no longer be simplified analytically!
- As n grows larger, evaluating $p(x|\theta)$ becomes intractable since the number of paths grows combinatorially.
- Generating observations remains easy: drop balls.

The Galton board is a metaphore for the simulator-based scientific method:

- the Galton board device is the equivalent of the scientific simulator
- θ are parameters of interest
- z are stochastic execution traces through the simulator
- *x* are observables

Inference in this context requires likelihood-free algorithms.

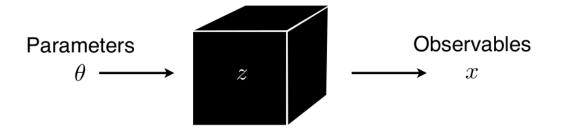


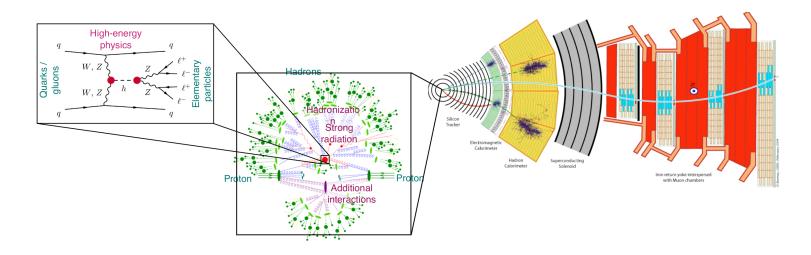
Prediction (simulation):

- Well-understood mechanistic model
- Simulator can generate samples

Inference:

- Likelihood function $p(x|\theta)$ is intractable
- Goal: estimator $\hat{p}(x|\theta)$



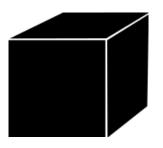


The Galton board of particle physics

Likelihood-free inference methods

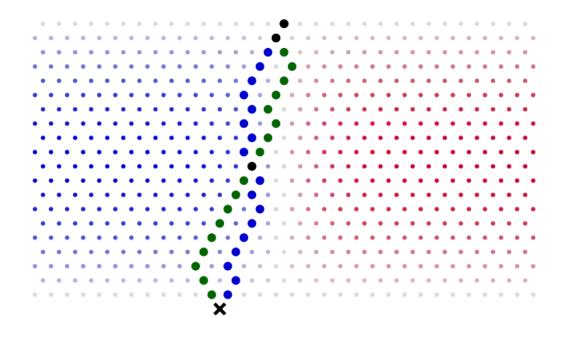
Treat the simulator as a black box Use latent structure

- Histograms of observables, Approximate Bayesian computation.
 - Rely on summary statistics.
- Machine learning algorithms
 - Density estimation, CARL, autoregressive models, normalizing flows, etc.



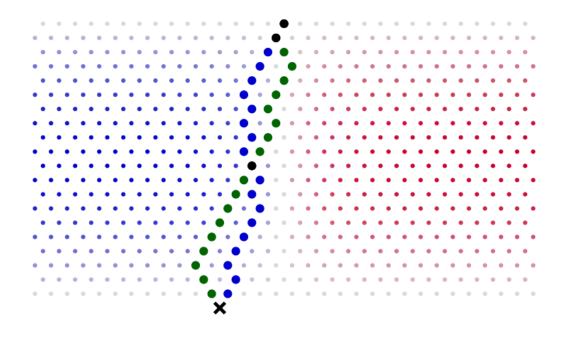
- Matrix Element Method, Optimal Observables, Shower deconstruction, Event Deconstruction.
 - Neglect or approximate shower + detector, explicitly calculate z integral.
- *new* Mining gold from the simulator.
 - Leverage matrix-element information + Machine Learning.

Mining gold from simulators



 $p(x|\theta)$ is usually intractable.

What about $p(x, z|\theta)$?



$$egin{aligned} p(x,z| heta) &= p(z_1| heta)p(z_2|z_1, heta)\dots p(z_T|z_{< T}, heta)p(x|z_{\leq T}, heta) \ &= p(z_1| heta)p(z_2| heta)\dots p(z_T| heta)p(x|z_T) \ &= p(x|z_T)\prod_t heta^{z_t}(1- heta)^{1-z_t} \end{aligned}$$

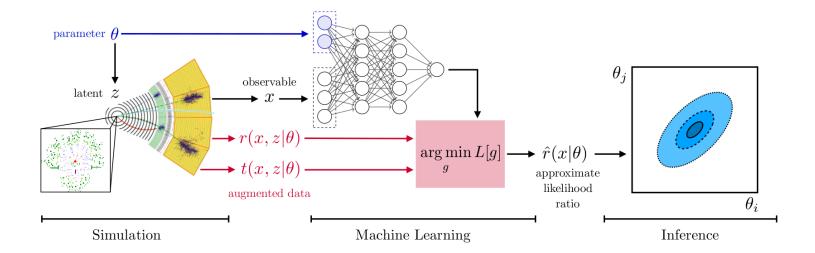
This can be computed as the ball falls down the board!

As the trajectory $z=z_1,...,z_T$ and the observable x are emitted, it is often possible:

- to calculate the joint likelihood $p(x, z|\theta)$;
- to calculate the joint likelihood ratio $r(x,z|\theta_0,\theta_1)$;
- ullet to calculate the joint score $t(x,z| heta_0) =
 abla_ heta \log p(x,z| heta)ig|_{ heta_0}.$

We call this process mining gold from your simulator!

RASCAL



Constraining Effective Field Theories, effectively

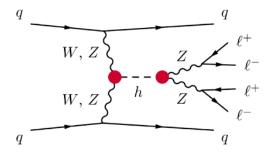
Latent variables

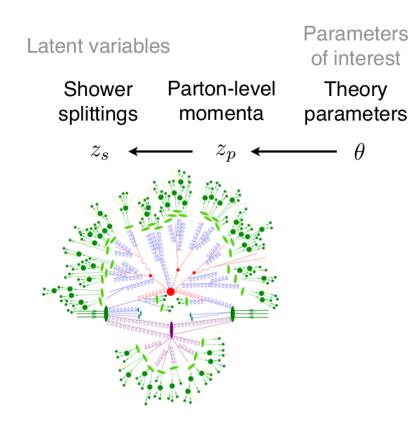
Parameters of interest

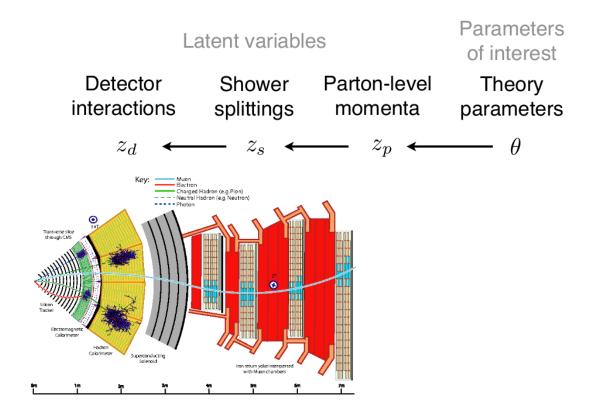
Parton-level momenta

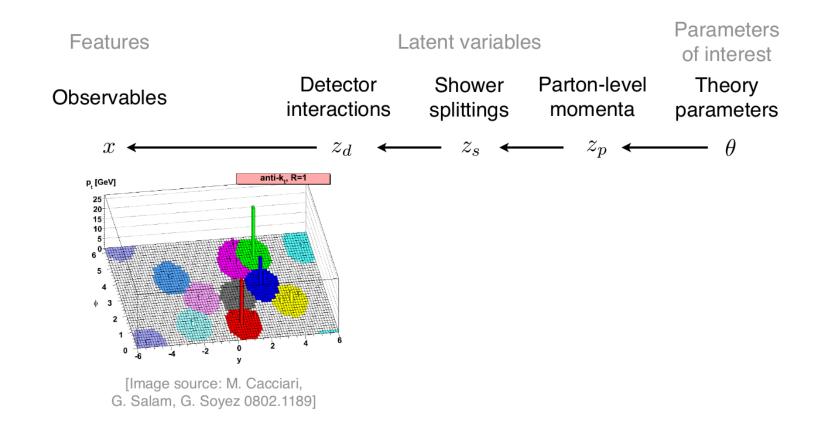
Theory parameters

 $z_p \leftarrow \theta$









$$p(x| heta) = \iiint p(z_p| heta)p(z_s|z_p)p(z_d|z_s)p(x|z_d)dz_pdz_sdz_d$$
 intractable

Key insights:

• The distribution of parton-level momenta

$$p(z_p| heta) = rac{1}{\sigma(heta)} rac{d\sigma(heta)}{dz_p},$$

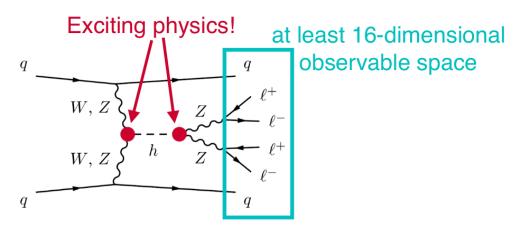
where $\sigma(\theta)$ and $\frac{d\sigma(\theta)}{dz_p}$ are the total and differential cross sections, is tractable.

• Downstream processes $p(z_s|z_p)$, $p(z_d|z_s)$ and $p(x|z_d)$ do not depend on θ .

 \Rightarrow This implies that both $r(x,z| heta_0, heta_1)$ and $t(x,z| heta_0)$ can be mined. E.g.,

$$r(x,z| heta_0, heta_1) = rac{p(z_p| heta_0)}{p(z_p| heta_1)} rac{p(z_s|z_p)}{p(z_s|z_p)} rac{p(z_d|z_s)}{p(z_d|z_s)} rac{p(x|z_d)}{p(x|z_d)} = rac{p(z_p| heta_0)}{p(z_p| heta_1)}$$

Proof of concept

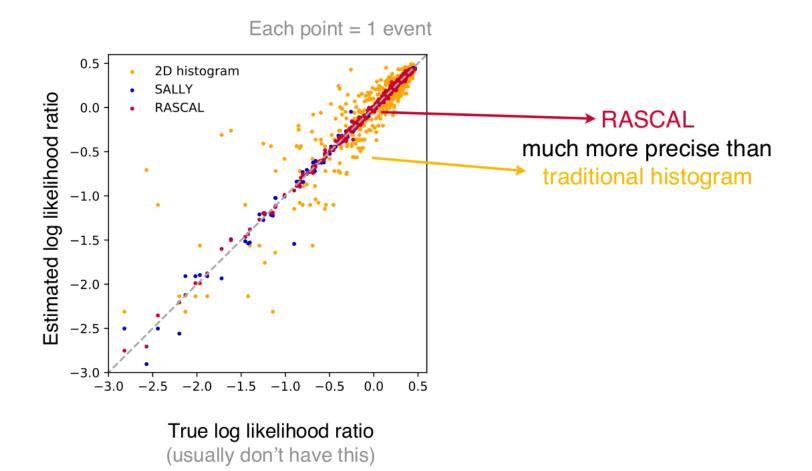


Higgs production in weak boson fusion

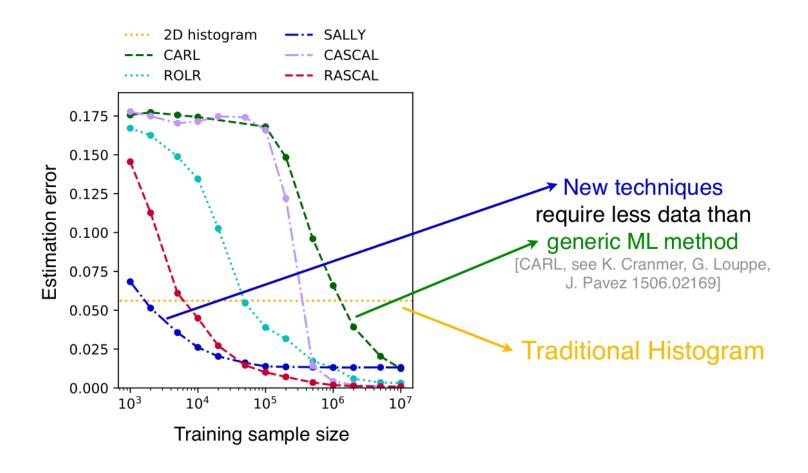
Goal: Constraints on two theory parameters:

$$\mathcal{L} = \mathcal{L}_{SM} + \underbrace{\frac{f_W}{\Lambda^2}} \, rac{ig}{2} \, (D^\mu \phi)^\dagger \, \sigma^a \, D^
u \phi \, W_{\mu
u}^a - \underbrace{\frac{f_{WW}}{\Lambda^2}} \, rac{g^2}{4} \, (\phi^\dagger \phi) \, W_{\mu
u}^a \, W^{\mu
u\,a}$$

Precise likelihood ratio estimates

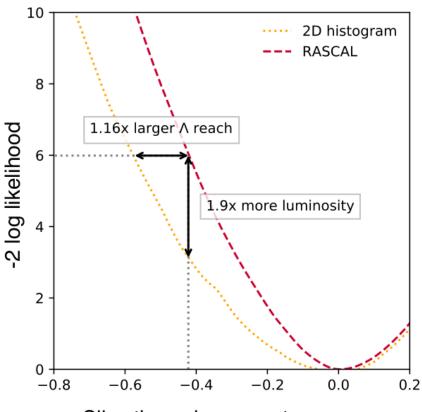


Increased data efficiency



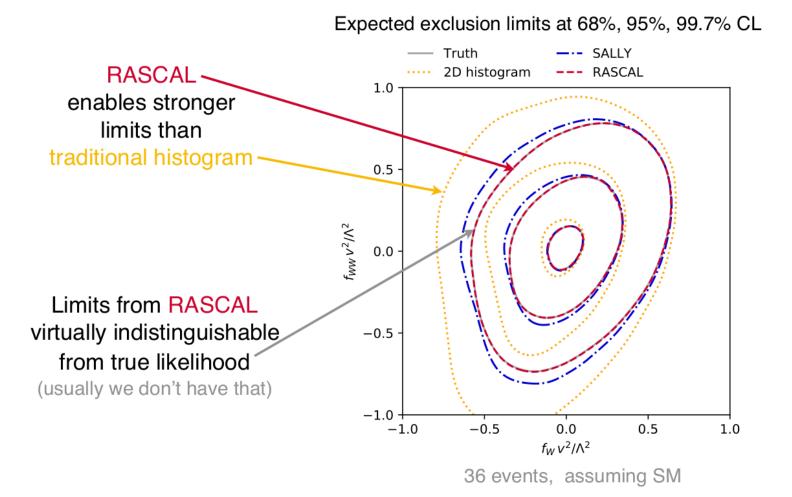
Better sensitivity

Likelihood function



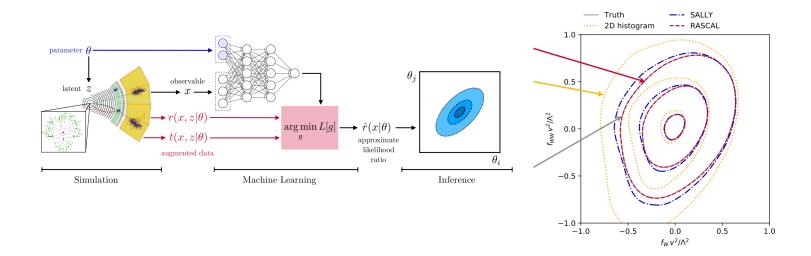
Slice through parameter space

Stronger bounds

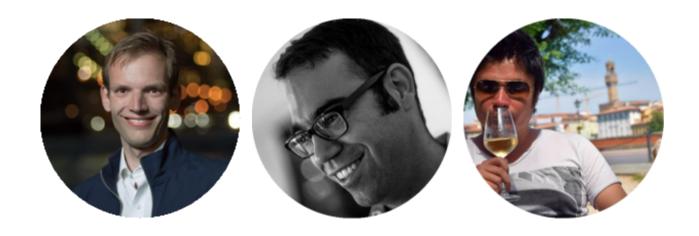


Summary

- Many LHC analysis (and much of modern science) are based on "likelihood-free" simulations.
- New inference algorithms:
 - Leverage more information from the simulator
 - Combine with the power of machine learning
- First application to LHC physics: stronger EFT constraints with less simulations.



Collaborators



Johann Brehmer, Kyle Cranmer and Juan Pavez

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The end.