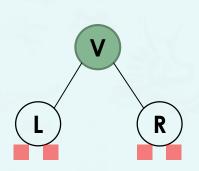
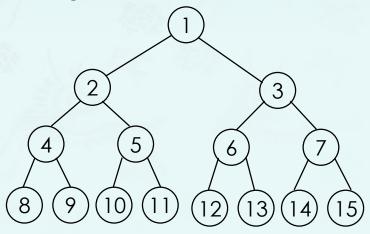
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## Data Structures Chapter 5 Tree

- 1. introduction
  - Definition and Terminology
- 2. Binary tree
  - Definition and Properties
  - Traversal
  - Coding
- 3. Binary search tree
- 4. Tree balancing

- Tree traversal (known as tree search) refers to the process of visiting each node in a tree, exactly once, in a systematic way.
- DFS (Depth-first Search)
  - There are three possible moves if we traverse left before right:
    - LVR inorder
    - LRV postorder
    - **VLR** preorder
  - They are named according to the position of V (the visiting node) with respect to the L and R.
  - These searches are referred to as depth-first search(DFS) since the search tree is deepened
    as much as possible on each child before going to the next sibling.

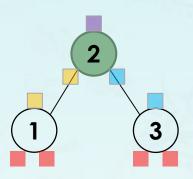




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  - These searches are referred to as depth-first search(DFS) since the search tree is deepened
    as much as possible on each child before going to the next sibling.
- BFS (Breadth-first search)
  - The **level order traversal** traverses in level-order, where it visit every node one a level before going to a lower level.
  - This search is referred as breadth-first search (DFS), as the search tree broadened as much as possible on each depth before going to the next depth.

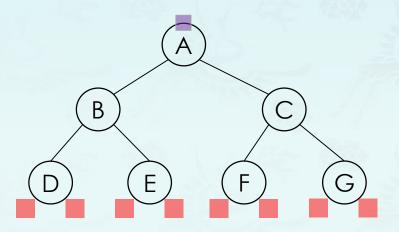
#### Example: Inorder traversal(LVR)

- Step 1 Recursively traverse left subtree.
- Step 2 Visit root node. (print or save it.)
- Step 3 Recursively traverse right subtree.



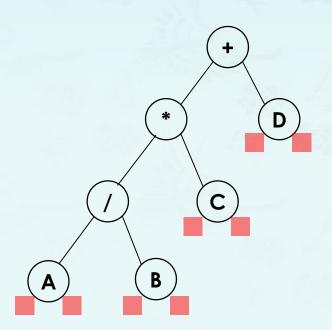
Output(LVR):123

- Example: Inorder traversal(LVR)
  - Step 1 Recursively traverse left subtree.
  - Step 2 Visit root node. (print or save it.)
  - Step 3 Recursively traverse right subtree.

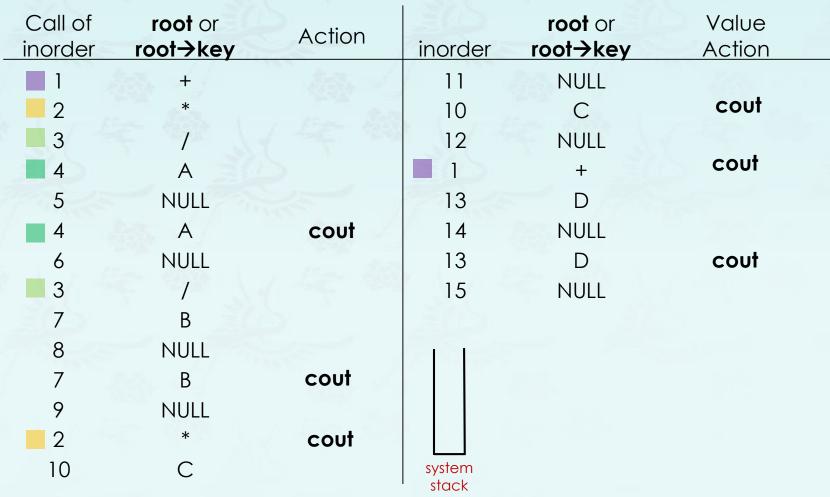


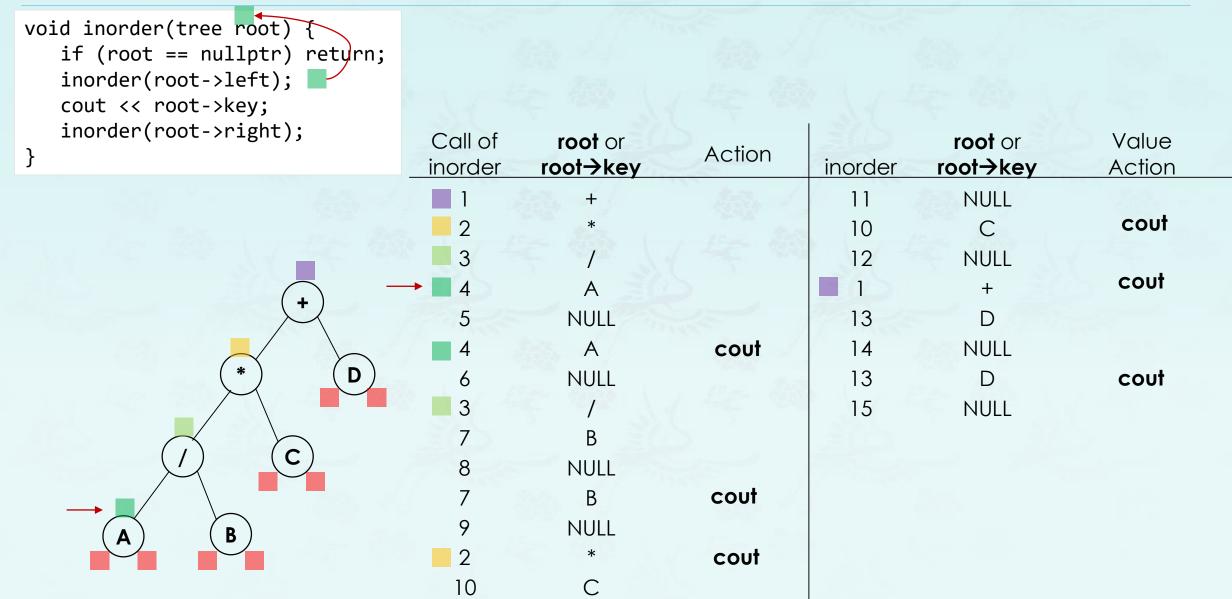
Output(LVR): DBEAFCG

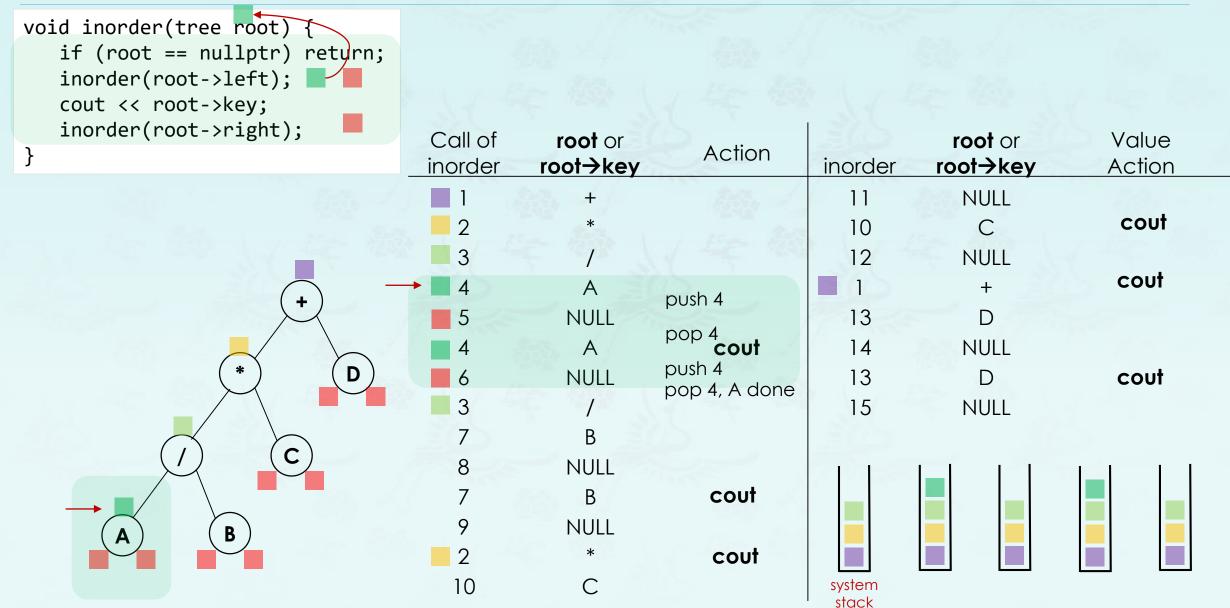
- Q1: Inorder Traversal(LVR):
- Q2: How many times is inorder() invoked for the complete traversal?
- A2: Every leaf node must visit (call the function) its left child and right child to make sure they don't have the child. 7 + 4 \* 2 = 15



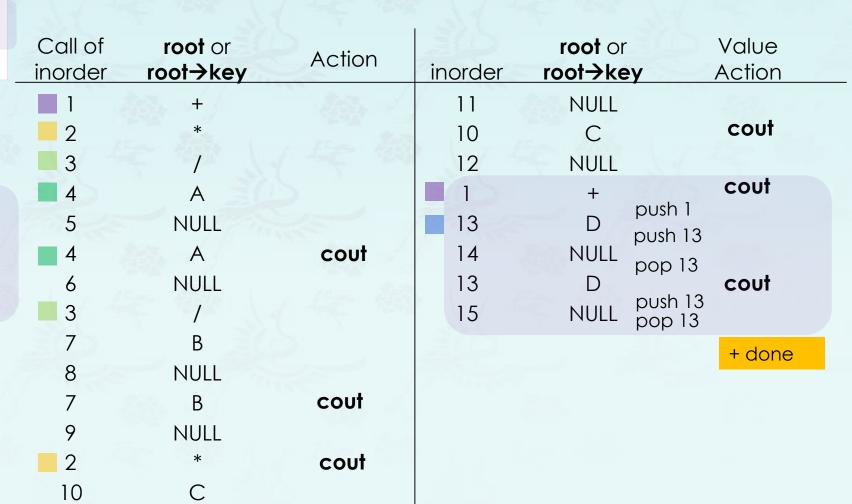
```
void inorder(tree root) {
   if (root == nullptr) return;
   inorder(root->left);
   cout << root->key;
   inorder(root->right);
}
```





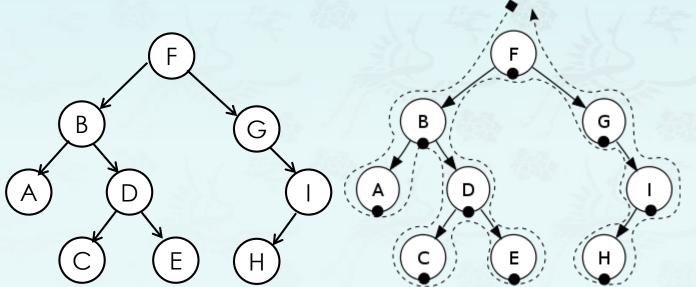


```
void inorder(tree root) {
   if (root == nullptr) return;
   inorder(root->left);
   cout << root->key;
   inorder(root->right);
}
```



#### Q: Inorder traversal(LVR)

- Traverse the left subtree.
- Visit the root.
- Traverse the right subtree.



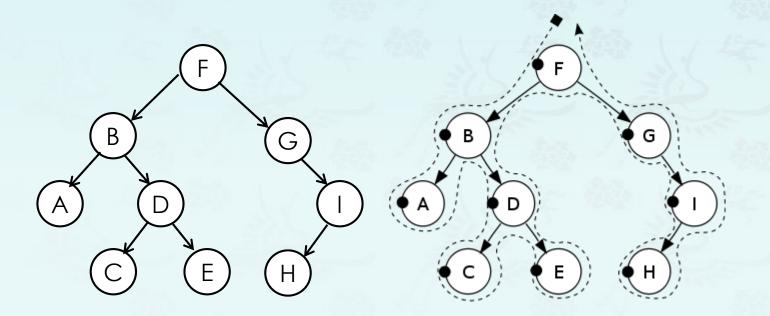
```
void inorder(tree root) {
   if (root == nullptr) return;

inorder(root->left);
   cout << root->key;
   inorder(root->right);
}
```

Output: A, B, C, D, E, F, G, H, I

#### Q: Preorder traversal(VLR)

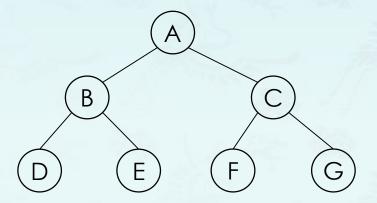
- Step 1 Visit root node.
- Step 2 Recursively traverse left subtree.
- Step 3 Recursively traverse right subtree.



Output: (VLR): F, B, A, D, C, E, G, I, H

#### Q: Preorder traversal(VLR)

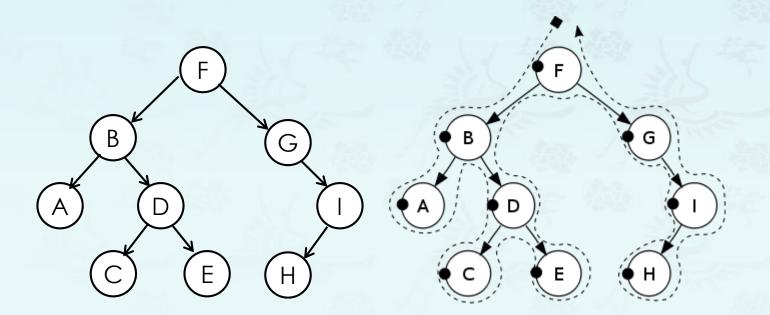
- Step 1 Visit root node.
- Step 2 Recursively traverse left subtree.
- Step 3 Recursively traverse right subtree.



Output: (VLR): A B D E C F G

#### Q: Postorder traversal(LRV)

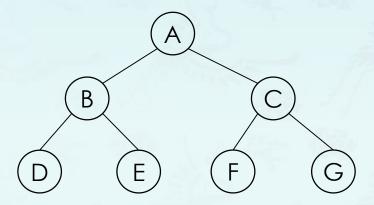
- Step 1 Recursively traverse left subtree.
- Step 2 Recursively traverse right subtree.
- Step 3 Visit root node.



Output(LRV): A C E D B H I G F

#### Q: Postorder traversal(LRV)

- Step 1 Recursively traverse left subtree.
- Step 2 Recursively traverse right subtree.
- Step 3 Visit root node.



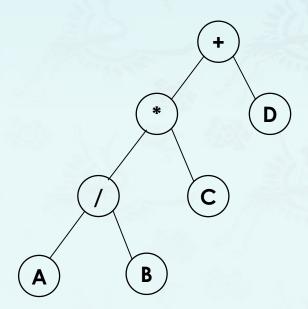
```
void postorder(tree root) {
   if (root == nullptr) return;

   postorder(root->left);
   postorder(root->right);
   cout << root->key;
}
```

Output(LRV): DEBFGCA

#### Q: Postorder traversal(LRV)

- Step 1 Recursively traverse left subtree.
- Step 2 Recursively traverse right subtree.
- Step 3 Visit root node.



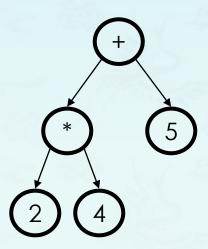
```
void postorder(tree root) {
   if (root == nullptr) return;

   postorder(root->left);
   postorder(root->right);
   cout << root->key;
}
```

Output(LRV): A B / C \* D +

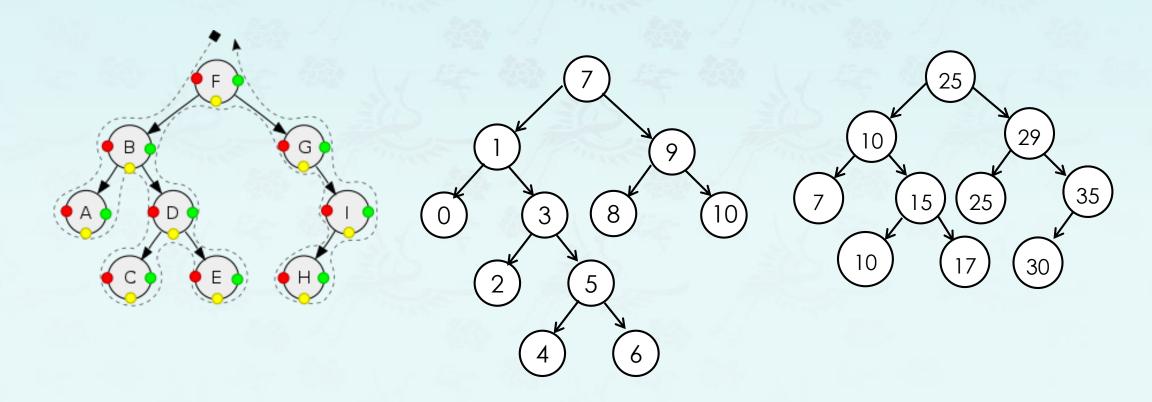
#### Exercise 1:

- preorder Traversal(VLR):
- inorder traversal(LVR) :
- postorder traversal(LRV):
- Level Order traversal:



#### Exercise 2:

- preorder Traversal(VLR)
- inorder traversal(LVR)
- postorder traversal(LRV)



#### Observations:

- 1. If you know you need to **explore the roots** before inspecting any leaves, you pick **preorder** because you will encounter all the roots before all of the leaves.
- 2. If you know you need to **explore all the leaves** before any nodes, you select **postorder** because you don't waste any time inspecting roots in search for leaves.
- 3. If you know that the tree has an inherent sequence in the nodes, and you want to flatten the tree back into its original sequence, than an **inorder** traversal should be used. The tree would be flattened in the same way it was created. A pre-order or post-order traversal might not unwind the tree back into the sequence which was used to create it.
- 4. In a <u>binary search tree</u> ordered such that in each node the key is greater than all keys in its left subtree and less than all keys in its right subtree, in-order traversal retrieves the keys in ascending sorted order.

### Summary & quaestio qo q ???

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