

## CS1555 Recitation 5 – Solution

---

Objective: To practice relational algebra, especially aggregations, joins, and division.

---

Consider the following relation schemas:

STUDENT (sid, name, class, major)  
STUDENT\_DIR (id, address, phone)  
FK: (id) → STUDENT (sid)  
COURSES\_TAKEN (course\_no, term, sid, grade)  
FK: (course\_no) → COURSE (course\_no); (sid) → STUDENT (sid)  
COURSE (course\_no, course\_name, level)  
INSTRUCTOR (id, fname, lname)  
COURSES\_OFFERED(course\_no, term, instructor\_id)  
FK: (course\_no) → COURSE (course\_no); (instructor\_id) → INSTRUCTOR (id)

---

Write a relational algebra query using the nested notation for each of the queries below:

1. Find for each instructor, the course names of the courses he/she was teaching in Fall 19.  
List in addition to the course name, the first name and the last names of the instructor.

$\pi_{\text{COURSE.name, INSTRUCTOR.fname, INSTRUCTOR.lname}} (\sigma_{\text{term='Fall 19'}}$   
 $(\text{INSTRUCTOR} \bowtie \text{INSTRUCTOR.id} = \text{COURSES\_OFFERED.instructor\_id}$   
 $(\text{COURSE} * \text{COURSES\_OFFERED})))$

2. List the sid, name, and address (if available) of all students.

$\pi_{\text{sid, name, address}} (\text{STUDENT} \bowtie \text{STUDENT.sid} = \text{STUDENT\_DIR.id} \text{ STUDENT\_DIR})$

*(note the left outer join)*

Write a relational algebra query using the sequence notation for each of the queries below:

1. Find the total number of students who have enrolled in the course “Operating Systems”.

$$\begin{aligned} \text{OS\_TAKING} &\leftarrow \pi_{\text{sid}}(\sigma_{\text{COURSE.name} = \text{'Operating Systems'}}(\text{COURSE\_TAKEN} * \text{COURSE})) \\ \text{RSLT} &\leftarrow \mathcal{F}_{\text{COUNT sid}}(\text{OS\_TAKING}) \end{aligned}$$

*(or you can combine the two steps into one expression (nested operations))*

2. Find the sid(s) of the student(s) who has/have the highest GPA

$$\begin{aligned} \text{STUDENT\_GPA}(\text{sid}, \text{gpa}) &\leftarrow \pi_{\text{sid}} \mathcal{F}_{\text{AVERAGE grade}}(\text{COURSE\_TAKEN}) \\ \text{HIGHEST\_GPA}(\text{max\_gpa}) &\leftarrow \mathcal{F}_{\text{MAX gpa}}(\text{STUDENT\_GPA}) \\ \text{RSLT} &\leftarrow \pi_{\text{sid}}(\text{STUDENT\_GPA} \bowtie_{\text{gpa} = \text{max\_gpa}}(\text{HIGHEST\_GPA})) \end{aligned}$$

3. Find the sid (s) of the student(s) who has/have taken all courses at the UGrad level

$$\begin{aligned} \text{COURSE\_DENOMINATOR} &\leftarrow \pi_{\text{course\_no}}(\sigma_{\text{level} = \text{'UGrad'}}(\text{COURSE})) \\ \text{RSLT} &\leftarrow (\pi_{\text{sid, course\_no}}(\text{COURSE\_TAKEN})) \div \text{COURSE\_DENOMINATOR} \end{aligned}$$

4. Find for each instructor the number of courses he/she has taught or is teaching. List the first name and the last name of each instructor along with his/her ID and number of courses.

$$\begin{aligned} \text{COURSES\_TAUGHT}(\text{id}, \text{n\_courses}) &\leftarrow \pi_{\text{instructor\_id}} \mathcal{F}_{\text{COUNT course\_no}}(\text{COURSES\_OFFERED}) \\ \text{RSLT} &\leftarrow \text{COURSES\_TAUGHT} * \text{INSTRUCTOR} \end{aligned}$$

5. List the SID of the students who did not enroll in any course in Fall 19.

$SID\_ENROLL\_FALL19 \leftarrow \pi_{sid}(\sigma_{term = 'Fall\ 19'}(COURSE\_TAKEN))$

$SID\_ALL \leftarrow \pi_{sid}(STUDENT)$

$RSLT \leftarrow SID\_ALL - SID\_ENROLL\_FALL19$