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H Applied Statistics  
8 February 2024

### Are Snakes Left-Handed?

#### 1) 1-Sample Mean T-test

$\mu$  = mean of lateral index values

$$H_o: \mu = 0.5$$

$$H_a: \mu \neq 0.5$$

$$\alpha = 0.05$$

Checks:

- Random: assume random selection
- Normal: CLT  $n > 30$ , sample size is large enough

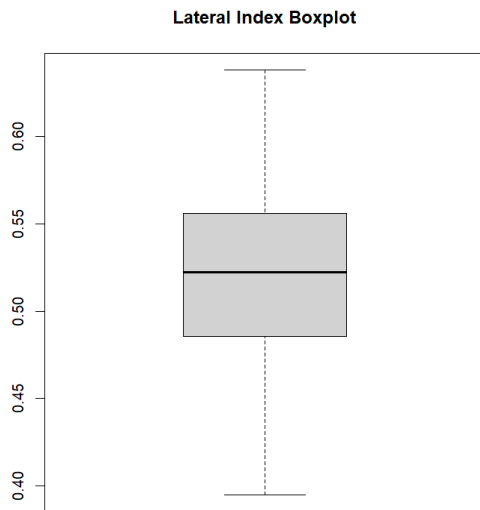
Calculations:

$$t = \frac{\bar{x} - \mu}{\frac{s}{\sqrt{n}}} = \frac{0.5183611 - 0.5}{\frac{0.05658983}{\sqrt{36}}} = 1.9468$$

$$p\text{-value} = p(t > 1.9468) \times 2 = 0.05962$$

Since the  $p\text{-value}(0.05962) > \alpha(0.05)$ , we fail to reject the null hypothesis. Therefore, there is not convincing evidence that snakes **do not** exhibit asymmetric coiling behavior (based on lateral index values).

Plot:



2) Categories and combinations of categories.

Model	Equation	$R^2$	$R^2$ (adjusted)	$S_e$	F-statistic
Length	$y = 0.50139 + 0.01471x$	0.008874	-0.02028	0.05716	0.3044
Gender	$y = 0.53644 - 0.03617x$	0.105	0.07871	0.05432	3.99
Age	$y = 0.54572 - 0.05472x$	0.2405	0.2181	0.05004	10.76
Age+Length	$y = 0.65768 - 0.09503x_1 - 0.07956x_2$	0.3696	0.3314	0.04627	9.673
Gender+Length	$y = 0.47529 - 0.06233x_1 + 0.06434x_2$	0.2198	0.1725	0.05148	4.649
Gender+Age	$y = 0.56381 - 0.03617x -$	0.3455	0.3058	0.04715	8.709

	0.05472x2				
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The chosen model has the highest  $R^2$  and  $R^2$ (adjusted) value, the lowest standard error, and the second highest F-statistic, which are all good things to have in a model.

3) Do adults differ from juveniles? Males from females?

## 2 2-Sample Difference in Means T-tests

First Test:

$\mu_1$  = lat index mean for juveniles

$\mu_2$  = lat index mean for adults

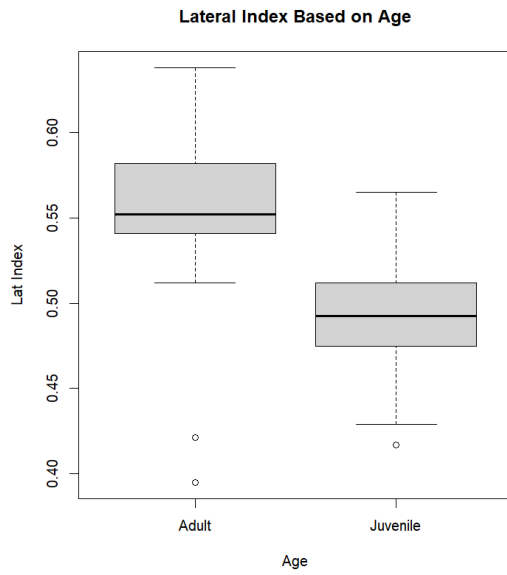
$$H_o : \mu_1 = \mu_2$$

$$H_a : \mu_1 \neq \mu_2$$

$$\alpha = 0.05$$

Checks:

- Normal: Box Plots do not appear normal. Two extreme outliers for adults, and one slight outlier for juveniles. Proceed with caution.



- Assume random selection.

Calculations:

$$t = \frac{(\bar{x}_1 - \bar{x}_2) - (\mu_1 - \mu_2)}{\sqrt{\frac{s_1^2}{n_1} + \frac{s_2^2}{n_2}}} = \frac{(0.491 - 0.5457222) - 0}{\sqrt{\frac{0.03917232^2}{18} + \frac{0.05893546^2}{18}}} = -3.2808 \quad \text{w/df} = 29.568$$

$$\text{p-value} = p(t > -3.2808) = 0.002657$$

Since the p-value(0.002657) < α(0.05), we reject the null hypothesis. Therefore, there is convincing evidence to suggest that the difference between the means of the lateral indexes for juveniles and adults are **not** equal to zero.

Second Test:

$\mu_1$  = lat index mean for males

$\mu_2$  = lat index mean for females

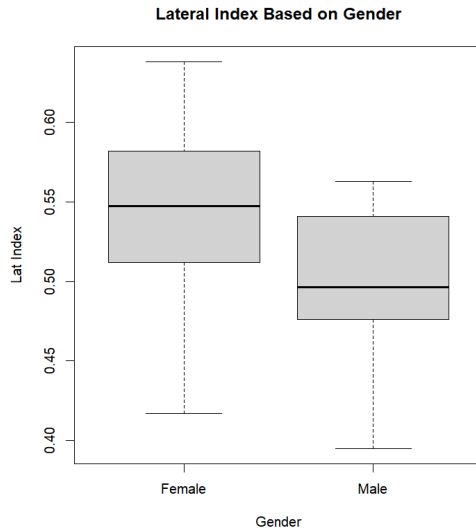
$$H_o : \mu_1 = \mu_2$$

$$H_a : \mu_1 \neq \mu_2$$

$$\alpha = 0.05$$

Checks:

- Normal: The female box plot appears relatively normal, but the male box plot appears skewed left. Proceed with caution.



- Assume random selection.

Calculations:

$$t = \frac{(\bar{x}_1 - \bar{x}_2) - (\mu_1 - \mu_2)}{\sqrt{\frac{s_1^2}{n_1} + \frac{s_2^2}{n_2}}} = \frac{(0.5002778 - 0.5364444) - 0}{\sqrt{\frac{0.04560677^2}{18} + \frac{0.06181207^2}{18}}} = -1.9975 \quad w/df = 31.278$$

$$p\text{-value} = p(t > -1.9975) = 0.05453$$

Since the p-value(0.05453) <  $\alpha(0.05)$ , we fail to reject the null hypothesis. Therefore, there is not convincing evidence to suggest that the difference between the means of the lateral indexes for males and females is **not** equal to zero.

4) Is there a difference in mean coiling laterality index per each categorical pairing of snake?

$\mu_1$  = lat index mean for adults/females (AF)

$\mu_2$  = lat index mean for juveniles/females (JF)

$\mu_3$  = lat index mean for adults/males (AM)

$\mu_4$  = lat index mean for juveniles/males (JM)

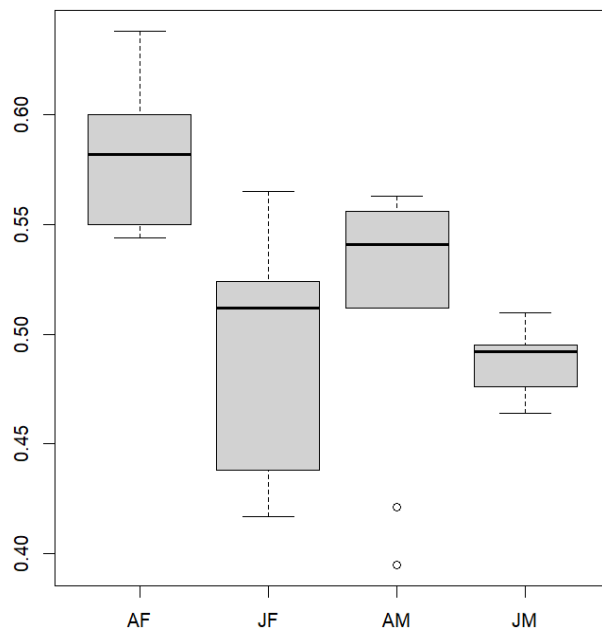
$$H_o: \mu_1 = \mu_2 = \mu_3 = \mu_4$$

$H_o$ : At least 2 means are different

$$\alpha = 0.05$$

Checks:

- Normality: Boxplots do not appear normal. AM has extreme outliers, and JM looks the closest to approximately normal. Proceed with caution.



- Equal Variance: the largest standard deviation ( $S_3$ ) is more than two times the smallest standard deviation ( $S_4$ ). Proceed with caution.

$$S_3 = 0.06218007$$

$$S_4 = 0.01399107$$

- Independence: assume independence.
- Random: assume random selection.

Calculations:

	$\bar{x}$	S	n
$\mu_1(\text{AF})$	0.5785556	0.03300042	9
$\mu_2(\text{JF})$	0.4943333	0.0551362	9
$\mu_3(\text{AM})$	0.5128889	0.06218007	9
$\mu_4(\text{JM})$	0.4876667	0.01399107	9

$$N = 9(4) = 36$$

$$T = 9(0.5785556) + 9(0.4943333) + 9(0.5128889) + 9(0.4876667) = 18.661$$

$$\bar{x} = \frac{18.661}{36} = 0.5184$$

$$\text{SSTr} = 9(0.5785556 - 0.5184)^2 + 9(0.4943333 - 0.5184)^2 + 9(0.5128889 - 0.5184)^2 + 9(0.4876667 - 0.5184)^2 = 0.046555$$

$$\text{SSE} = 8(0.03300042)^2 + 8(0.0551362)^2 + 8(0.06218007)^2 + 8(0.01399107)^2 = 0.065529$$

$$\text{MSTr} = \frac{0.046555}{3} = 0.015518$$

$$\text{MSE} = \frac{0.065529}{32} = 0.00205$$

$$\text{F-stat.} = \frac{0.015518}{0.00205} = 7.5698$$

$$\text{p-value} = p(F > 7.5698) = 0.00058075$$

Check means:

AF	AM	JF	JM
0.5785556	0.5128889	0.4943333	0.4876667

Check standard deviations:

AF	AM	JF	JM
0.03300042	0.06218007	0.05513620	0.01399107

ANOVA Test:

Df	Sum Sq	Mean Sq	F value	Pr(>F)
Treatment	3	0.04656	0.015518	7.578 0.000577 ***
Residuals	32	0.06553	0.002048	

Since the p-value(0.00058075) <  $\alpha(0.05)$ , we reject the null hypothesis. Therefore, there is convincing evidence to suggest that at least two of the mean coiling laterality indexes per each categorical pairing of snakes are **not** equal.