Image Registries

Glyn Normington

May 29, 2019

This document provides a formal model of some aspects of Docker image registries.

I am indebted to Chris Frost and Steve Powell for their helpful feedback.

ii	Version 0.3
1	version 0.3

Contents

1	Introduction	1
2	Fundamentals	1
3	Content Digests	2
4	Repositories	3
5	Registries	5
6	Image References	8
A	Bibliography	10
В	Z Notation	11

Introduction 1

This document provides a formal model of image registries.

Docker Inc. [1] introduced container images and registries to hold them and these were later standardised as part of the Open Container Initiative [2]. The reader is assumed to have a basic understanding of how images are used.

This document models image references, repositories, and registries. It covers digests and tags.

The Z specification language is used to describe the model, but sufficient English text is also provided that readers who do not know Z should be able to understand what's going on. Appendix B contains a summary of the Z notation. For more information about Z, please consult the Z Manual [3]. The model was type checked using fuzz [4].

2 **Fundamentals**

Images are opaque blobs as far as we are concerned here - the decomposition into layers is ignored. Similarly, cryptographic hashes (or hexes, to use the terminology of the OCI Distribution specification), tags, and (registry) hostnames and paths are modelled in terms of their usage, but not their implementation.

[Image, Hex, Tag, Hostname, Path]

There is a special reserved tag.

Latest: Tag

¹See the bibliography in Appendix A.

3 Content Digests

A content digest is a combination of a cryptographic hash function (such as SHA-256) or "algorithm", and the hash output by such a function.

```
\_ContentDigest \_
alg: Image \rightarrow Hex
hash: Hex
```

The algorithm in a content digest is represented as a string which names one of a limited set of algorithms, but we ignore that here and pretend the algorithm is part of the content digest.

The idea is that a content digest d identifies an image i if and only if applying the hash function (from the content digest) to the image produces the hash output in the content digest:

$$d.alg i = d.hash$$

The limited set of algorithms is chosen so that given an image i with a content digest d, it is extremely difficult, if not impossible, to construct a distinct image j with the same content digest:

$$i \neq j \land d.alg i = d.hash = d.alg j$$

An optional content digest is modelled as a datatype.

```
OptionalContentDigest ::= None \mid Dig \langle \langle ContentDigest \rangle \rangle
```

We add a convenient function for extracting the content digest from an optional content digest which is "present".

$$Cd == Dig^{\sim}$$

4 Repositories

A repository is a collection of images indexed by content digest and by tag.

```
Repo cd : ContentDigest \mapsto Image
tag : Tag \mapsto Image
\forall d : dom cd \bullet d.alg (cd d) = d.hash
ran tag \subseteq ran cd
```

The content digests identify the corresponding images and there is only one content digest per image (since this is chosen when the image added to the repository, as we shall soon see). Each image identified by a tag is also identified by a content digest.

Initially, a repository is empty.

An image is added to a repository by *pushing* it. The operation takes any image and any tag and returns a content digest of the image.

```
RepoPush \_
\Delta Repo
i?: Image
t?: Tag
d!: ContentDigest
tag' = tag \oplus \{t? \mapsto i?\}
cd' = cd \oplus \{d! \mapsto i?\}
```

The tag may be omitted, in which case it defaults to *Latest*, although this is not modelled. Note that the invariant of *Repo'* ensures that the output digest identifies the input image. There is, in theory, some non-determinism in the choice of algorithm, but for OCI compliant implementations, SHA-256 is used everywhere.

An image is retrieved from a repository by *pulling* it.

We can pull an image using a content digest.

```
 \begin{array}{c} RepoPullByDigest \\ \hline \Xi Repo \\ d?: OptionalContentDigest \\ i!: Image \\ \hline d? \in \text{dom } Cd \\ i! = cd(Cd \ d?) \end{array}
```

The content digest is provided and is used to identify the output image.

Alternatively, we can pull and image using a tag.

The content digest is not provided. The tag is used to identify the output image.

A successful pull operation uses either a content digest or a tag.

```
RepoPullOk \triangleq RepoPullByDigest \lor RepoPullByTag
```

If a content digest is provided, the image is pulled by digest and the tag is ignored. Failure cases, such as "not found", are omitted from the model.

5 Registries

A registry is a collection of repositories indexed by path.

```
Registry \_
repo: Path \rightarrow Repo
```

An empty registry has no repositories.

```
EmptyRegistry = [Registry \mid repo = \varnothing]
```

Initially a registry has no repositories.

```
RegistryInit \triangleq EmptyRegistry'
```

An empty repository may be added at a given path.

```
Registry AddRepoOk \\ \triangle Registry \\ p?: Path \\ \hline p? \notin \text{dom } repo \\ \exists RepoInit \bullet repo' = repo \cup \{p? \mapsto \theta Repo'\}
```

Some registry implementations, such as Amazon's ECR, require a repository to be created before an image can be pushed to the repository. Other registry implementations such as Docker's registry and Google's GCR will create a repository automatically when the first image is pushed to it. We do not model automatic repository creation.

We define a promotion schema² which operates on a single repository in a registry.

```
Registry Promote \\ \Delta Registry \\ \Delta Repo \\ p?: Path \\ \hline p? \in \text{dom } repo \\ \theta Repo = repo \ p? \\ repo' = repo \oplus \{p? \mapsto \theta Repo'\}
```

The path must be valid and the registry is preserved except for the repository identified by the path which may be updated.

We then promote the repository push and pull operations to operate on a registry.

```
RegistryPush \ \widehat{=} \ \exists \ \Delta Repo \bullet RepoPush \land RegistryPromote
RegistryPullOk \ \widehat{=} \ \exists \ \Delta Repo \bullet RepoPullOk \land RegistryPromote
```

Registries are accessed remotely in a network via their hostnames.

```
Net \_\_
reg: Hostname \rightarrow Registry
```

Initially, there are no registries in the network.

We can add an empty registry to the network.

²Promotion schemas are used to turn operations on a particular type into operations on a collection of the type which operate on a single member of the collection and leave the rest unchanged.

We can also remove a registry from the network.

```
NetRemoveRegistryOk
\Delta Net
h?: Hostname
h? \in \text{dom } reg
reg' = \{h?\} \lessdot reg
```

We define a promotion schema which operates on a single registry in a network.

```
NetPromote \_
\Delta Net
\Delta Registry
h?: Hostname
h? \in \text{dom } reg
\theta Registry = reg \ h?
reg' = reg \oplus \{h? \mapsto \theta Registry'\}
```

The hostname must be valid and the network is preserved except for the registry identified by the hostname which may be updated.

Finally, we promote the push and pull operations to work on a network.

```
NetPushOk \cong \exists \Delta Registry \bullet RegistryPush \land NetPromote
NetPullOk \cong \exists \Delta Registry \bullet RegistryPullOk \land NetPromote
```

Pushing and pulling fail if there is no registry with the input hostname.

6 Image References

An image reference identifies an image in a registry. Let's remind ourselves what image references look like.

An image reference consists of a hostname (with optional port) and a path. The image reference may also contain a tag and/or a digest. The hostname determines the network location of a registry. The path consists of one or more components separated by forward slashes. The first component is sometimes, by convention for certain registries, a user name providing access control to the image.

Let's look at some examples:

- The image name docker.io/istio/proxyv2 refers to an image with user name istio residing in the docker hub registry at docker.io.
- The image name projectriff/builder:v1 is short-hand for docker.io/projectriff/builder:v1 which refers to an image with user name projectriff also residing at docker.io. The image has tag v1.
- The image name gcr.io/cf-elafros/knative-releases/github.com/knative/serving/cmd/autoscaler@sha256:deadbeefd

For the purposes of our model, an image reference consists of a hostname, a path, a tag, and an optional content digest.

host: Hostname
path: Path

dig: Optional Content Digest

A tag is always logically present, but if it is omitted from the textual representation of an image reference, it defaults to *Latest*. A content digest may be part of an image reference or may be omitted.

So far the push and pull operations have accumulated several input parameters.

```
PushParms
h?: Hostname
p?: Path
t?: Tag

PullParms
h?: Hostname
p?: Path
t?: Tag
d?: OptionalContentDigest
```

An image reference is related to push input parameters as follows.

```
RefPushParms
r?: Ref
PushParms
h? = r?.host
p? = r?.path
t? = r?.tag
r?.dig = None
```

Pushing is not allowed if the image reference has a content digest.

An image reference is related to pull input parameters as follows.

```
RefPullParms
r?: Ref
PullParms

h? = r?.host
p? = r?.path
t? = r?.tag
d? = r?.dig
```

Push and pull can then be reframed to take an image reference instead of the corresponding input parameters.

```
RefPushOk \cong \exists PushParms \bullet NetPushOk \land RefPushParms
RefPullOk \cong \exists PullParms \bullet NetPullOk \land RefPullParms
```

A Bibliography

[1] Various authors, *Docker Inc.*, https://www.docker.com/.

- [2] Various authors, *Open Container Initiative*, https://www.opencontainers.org/.
- [3] Mike Spivey, *The Z Manual*, https://www.cs.umd.edu/mvz/handouts/z-manual.pdf.
- [4] Mike Spivey, The fuzz type-checker for Z, https://bitbucket.org/Spivey/fuzz.

B Z Notation

Numbers:							
\mathbb{N} Natural numbers $\{0,1,\ldots\}$							
Propositional logic and the schema calculus:							
∧ ∨ ∀ • ∃ • \ \ = =	And Or Implies For all There exists Hiding Schema definition Abbreviation Free type definition	$\langle\langle \dots \rangle\rangle$ $[\dots]$ $\langle ,?,!,0\dots 9$ $\dots \vdash \dots$ $\partial \dots$ $\partial \dots$ $\partial \dots$ $\partial \dots$ $\partial \dots$ $\partial \dots$	Free type injection Given sets Schema decorations theorem Binding formation Function definition Mu-expression State change Invariant state change				
Sets and sequences:							
{} { •} P Ø × ∈ ∉ ∪	Set Set comprehension Set of subsets of Empty set Cartesian product Set membership Set non-membership Union Intersection		Set difference Distributed union Cardinality Subset Proper subset Set partition Sequences Sequence Disjoint sequence of sets				
Functions and relations:							
$\begin{array}{cccc} \dots & & \dots & & \dots \\ \dots & & & \dots & & \dots \\ \dots & & & &$	Relation Partial function Total function Partial injection Injection Domain Range maplet Relational inverse	*()⊕	Reflexive-transitive closure Relational image Functional overriding Domain restriction Range restriction Domain subtraction Range subtraction				
Axiomatic descriptions:							
Declarations Predicates							
Schema definitions:							
SchemaName Declaration Predicates							
Decorations:							

Input parameter Output parameter