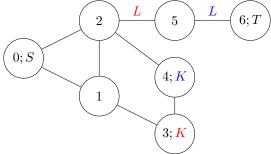
# CS 571 Programming Assignment 4

### Due Friday, April 5 at 11:59pm

#### 1 Search Problem

15 points

In this problem you will consider an agent whose goal is to get to some treasure. At each time step, the agent can move between rooms using doors arranged according to an undirected graph. However, some of the doors are locked, and the agent must acquire the appropriate key in order to pass through a locked door. For example, consider the scenario depicted in the following graph:



In this scenario, the agent starts in room 0, as indicated by the S annotation. The treasure is located in room 6, but the door from room 5 to 6 is locked with a red lock – as indicated by a red L – and the door from room 4 to 5 is locked with a blue lock – as indicated by a blue L. Thus in order to reach the treasure, the agent must first acquire both the red key – located in room 3 as indicated by the red K – and the blue key – located in room 4 as indicated by the blue K. Thus, the shortest path the agent can travel to reach the treasure in this scenario is through the rooms 0,1,3,4,2,5,6. This scenario is modeled in Prolog in the file search/scenario1.pl.

Your task in this question is to, given a specification of a problem such as the one in search/scenario1.pl, write a search procedure in Prolog to find the shortest path for the agent to reach the treasure. You should write — in the file search/search.pl — a predicate called search(X) that binds X to the shortest sequence of moves to lead the agent to the treasure. Examples of the output format are in search/test1.pl and search/test2.pl.

#### 2 Peano Arithmetic

5 points

In this question, you will write a Prolog predicate to perform integer division in using a formalization of Peano arithmetic. Your predicate — div(X,Y,Z,R) — should be true if and only if X divided by Y is equal to Z with remainder R. You should use the Peano arithmetic formalization in peano/peano.pl and write your solution in the same file.

### 3 Binary Search Trees

5 points

The file binary/binary.pl contains a formalization of a binary search tree in Prolog. Your task in this question is to write predicates rotateLeft(In,Out) and rotateRight(In,Out) that respectively perform

a left or right binary search tree rotation<sup>1</sup> on the input binary search tree In to produce the output binary search tree Out. You should write your predicate in binary/binary.pl, which also has examples of the expected output.

## 4 Parsing in Prolog

10 points

Write a parsing algorithm in Prolog for the following grammar, assuming the start nonterminal is Lines.

$$\begin{split} \mathit{Lines} & \rightarrow \mathit{Line} \; ; \; \mathit{Lines} \; | \; \mathit{Line} \\ & \mathit{Line} \rightarrow \mathit{Num} \; , \; \mathit{Line} \; | \; \mathit{Num} \\ & \mathit{Num} \rightarrow \mathit{Digit} \; | \; \mathit{Num} \\ & \mathit{Digit} \rightarrow 0 \; | \; 1 \; | \; 2 \; | \; 3 \; | \; 4 \; | \; 5 \; | \; 6 \; | \; 7 \; | \; 8 \; | \; 9 \end{split}$$

Please write your parser as the predicate parse(X) that is true if andd only if the input list X of tokens is in the language specified by the grammar. Write this in hte file parsing/parse.pl, which also contains examples.

<sup>&</sup>lt;sup>1</sup>https://en.wikipedia.org/wiki/Tree\_rotation