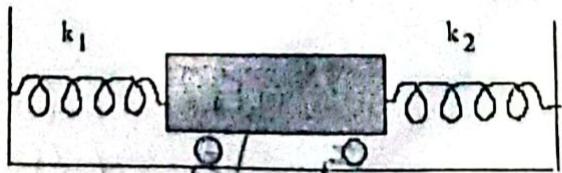


Section A (40 marks)

Answer all questions in this section

1. (a) Differentiate error from mistake. (2 marks)
 - (b) A new born baby was measured in four different ways and her mass was found to be 2000g, 2001g, 2003g and 1999g respectively. Determine
(i) Her actual mass. (2 marks)
(ii) Mean absolute error of the measurement. (2 marks)
 - (c) Name the physical quantities with the following dimensions (2 marks)
(i) $ML^{-1}T^{-2}$ (ii) ML^2T^{-1}
 - (d) Prove whether the following equation is dimensional correct or not (2 marks)
 $v = \sqrt{2gR}$, where g is acceleration due to gravity and R is the radius of the earth.
2. (a) (i) According to Newton's third law of motion, action and reaction are in opposite direction. Will they cancel each other on addition? (3 marks)
(ii) Differentiate the two types of collision in terms of their coefficient of restitution. (3 marks)
 - (b) Can a projectile motion be observed inside a free fall cube? Give reasons for your answer. (4 marks)
 3. (a) What cause a body whirled in a vertical circle not to have constant velocity? (2 marks)
 - (b) A particle of mass 50g is whirled in a vertical circle by a string of 40cm in length. Find what must be the minimum possible velocity of the particle to have tension equal to the weight of the particle at the top of a described vertical circle. (4 marks)
 - (c) A car moving round a circular path of radius of curvature 200m has a pendulum of mass 100g hangs from its ceiling. If the pendulum get inclined at 30° from the vertical as the car goes round the path, find the velocity of the car. (4 marks)
4. (a) Briefly explain the importance of inertia in simple harmonic motion. (2 marks)
(b) Prove that the following system will execute simple harmonic motion if slightly pushed parallel to the springs and get released (4 marks)



- (c) An object of mass 2kg executes simple harmonic motion with a frequency of 2Hz and amplitude of 2.5cm. Calculate its maximum velocity and maximum potential energy. (4 marks)

(4 marks)

SECTION B(30 MARKS)

Answer all questions in this section

5. (a) Why does a good absorber of radiant energy appear black? (03 marks)

(b) Two bodies A and B are kept in evacuated vessel maintained at a temperature of 27°C. The temperature of A is 527°C and that of B is 127°C. Compare the rates at which heat is lost from A and B. (03 marks)

*(c) When a block of metal of mass 0.11kg and specific heat capacity of 400J/kgK heated to 100°C and quickly transferred to a copper calorimeter of mass 0.1kg containing 0.2kg of liquid at 10°C the resulting temperature after stirring is 18°C. Calculate the specific heat capacity of liquid (04 marks)

6. (a) A person sitting on a bench on a calm hot summer day is aware of a cool breeze blowing from the sea. Briefly explain why there is a natural convection? (03 marks)

(b) Briefly explain why forced convection is necessary for excess temperate less than 20 K? (03 marks)

(c) A cup of tea kept in a room with temperature of 22°C cools from 66°C to 63°C in 1 minute. How long will the same cup of tea take to cool from the temperature of 43°C to 40°C under the same conditions? (04 marks)

7. (a) How does the average translational kinetic energy of a molecule of an ideal gas change if;

(i) The pressure is doubled while the volume is kept constant? (02 marks)

(ii) The volume is doubled while the pressure is kept constant? (02 marks)

(b) Based on the kinetic theory of gases determine;

(i) The average translational kinetic energy of air at a temperature of 290K. (02 marks)

(ii) The root mean square speed (r.m.s) of an air molecule at the same temperature (above). One mole of air has a mass of 29 g. (02 marks)

(c) Compare the law governing the conduction of heat and electricity by pointing out the corresponding quantities in each case. (02 marks)

$f_0 = 10$
 $f_s = 4f_0$
 $f_d = 8f_0$
 $f_s = 2f_0$

SECTION C (30 MARKS)
Answer all questions in this section

8. (a) (i) Why doesn't the Doppler effect take place when the listener and the source are moving perpendicularly? (2.0 marks)
- (ii) Would the Doppler Effect in sound still happen if the source and the listener move in a circle? (2.0 marks)
- (b) (i) A bike rider approaching a vertical wall observes that the frequency of his bike horn changes from 440 Hz to 480 Hz when it gets reflected from the wall. Find the speed of the bike if the speed of sound is 330 m/s. (3.0 marks)
- (ii) Two trains A and B are moving toward each other at a speed of 432 km/h. If the frequency of the whistle emitted by A is 800 Hz, then what is the apparent frequency of the whistle heard by the passenger sitting in train B. (The velocity of sound in air is 360 m/s). (3.0 marks)
9. (a) (i) If the third harmonics of a closed organ pipe is equal to the fundamental frequency of an open organ pipe, compute the length of the open organ pipe if the length of the closed organ pipe is 30 cm. (2.0 marks)
- (ii) A student performed an experiment to determine the speed of sound in air using the resonance column method. The length of the air column that resonates in the fundamental mode with a tuning fork is 0.2 m. If the length is varied such that the same tuning fork resonates with the first overtone at 0.7 m. Calculate the end correction. (3.0 marks)
- (b) (i) A string has both ends kept fixed, produces a fundamental tone with a frequency of 420 Hz. Determine the third overtone. (2.0 marks)
- (ii) The wavelength of the first overtone of a string is 40 cm. If the speed of sound wave in air is 340 m/s, determine the third overtone. (3.0 marks)
10. (a) (i) When do we use the progressive wave equation as $y = A \sin(\omega t - kx)$ and when do we use $y = A \sin(kx - \omega t)$? (2.0 marks)
- (ii) Two vibrating tuning forks produce waves whose equation is given by

$y_1 = 5\sin(240\pi t)$ and $y_2 = 4\sin(244\pi t)$. Compute the number of beats per second.

$$2\pi f = 244\pi - 240\pi \\ f = 2\pi \times 4 = 8\text{ Hz}$$

(2.0 marks)

- (b) Two waves of the same frequency are out of phase by 30 degrees, and both waves have amplitude 6 m. Find the amplitude of the resultant wave when the waves combine. Round to two decimal places. (2.0 marks)
- (c) The transverse displacement of a string clamped at its two ends is given by

$$y(x, t) = 0.06\sin\frac{2\pi}{3}x\cos(120\pi t), \text{ where } x, y \text{ are in metres and } t \text{ is in seconds.}$$

The length of the string is 1.5m and its mass is $3 \times 10^{-2}\text{ kg}$

- (i) Does the function represent a travelling or a stationary wave? (1.0 mark)
- (ii) Interpret the wave as a superposition of two waves travelling in opposite directions. What are the wavelength, frequency and speed of propagation of each wave? (2.0 marks)
- (iii) Determine the tension in the string. (1.0 mark)

$$\sqrt{A_1^2 + A_2^2 + 2A_1A_2\cos\theta} \\ 2A_1\cos\left(\frac{\theta}{2}\right)$$

*****THE END*****

- 1 (a) Error
 Is the difference between the actual value and measured value while Mistake is the wrong way of doing measurement.
- (ii) Error can be accounted for but mistake cannot be accounted for.
- (iii) Error can be minimized while Mistake cannot be minimized.

$$1 \text{ b) } (i) = \frac{2000 \text{ g} + 2001 + 2003 + 1999}{4}$$

$$= 2000.75 \text{ g}$$

\therefore the actual mass is 2000.75 g .

$$\Delta x_{e1} = x - \bar{x}_e = 2000 - 2000.75 = -0.75$$

$$\Delta x_{e2} = x - \bar{x}_e = 2001 - 2000.75 = 0.25$$

$$\Delta x_{e3} = x - \bar{x}_e = 2003 - 2000.75 = 2.25$$

$$\Delta x_{e4} = x - \bar{x}_e = 1999 - 2000.75 = -1.75$$

but

$$\bar{x}_e = \frac{\Delta x_{e1} + \Delta x_{e2} + \Delta x_{e3} + \Delta x_{e4}}{4}$$

$$= \frac{-0.75 + 0.25 + 2.25 + 1.75}{4}$$

$$= \frac{5}{4}$$

$$= 1.25$$

\therefore The mean absolute error is 1.25 g

1 (c) (i) $M L^{-1} T^{-2}$ - Pressure ✓ (01)

~~$M L^2 T^{-4}$~~ - Power and Plants of turbines
of angular velocity & angular momentum

3. (d) $V = \sqrt{2gR}$

Dimensions of $R \cdot H \cdot S$ ✓ (02)

$$[V] \checkmark [g]^{\frac{1}{2}} [R]^{\frac{1}{2}}$$

$$[M^0 L T^{-1}] \checkmark [M^0 L T^{-2}]^{\frac{1}{2}} [M^0 L T^0]^{\frac{1}{2}}$$

$$[M^0 L T^{-1}] \checkmark [M^0 L^{\frac{1}{2}} T^{-\frac{1}{2}}] [M^0 L^{\frac{1}{2}} T^0]$$

$$[M^0 L T^{-1}] \checkmark [M^0 L T^{-1}]$$

$$L \cdot H \cdot S = R \cdot H \cdot S$$

Hence Proved ✓ (01) (d)

✓ (01)

25.0000 + 25.0000 + 25.0000 + 25.0000 = 100.0000

$$25.0 = 25.0000 - 0000 = 25X - X = 24X \quad (0)$$

$$25.0 = 25.0000 - 0000 = 25X - X = 24X$$

$$25.0 = 25.0000 - 0000 = 25X - X = 24X$$

$$25.0 = 25.0000 - 0001 = 25X - X = 24X$$

Ans

$$24X + 24X + 24X + 24X = 96X$$

4

$$\underline{25.0 + 25.0 + 25.0 + 25.0} =$$

4

$$\begin{array}{r} 2 \\ 2 \\ 5 \\ + 2 \\ \hline 50 \end{array}$$

25.0 is standard answer

(9)

2 (b) (i) Action and reaction do not cancel each other even though they act in opposite direction due to the fact that they act on two different bodies

✓ (03)

2 (b) (ii) Elastic collision is the type of collision whose coefficient of restitution is equal to 1 ($e=1$)

WHILE

(1/2)

Inelastic collision is the type of collision where coefficient of restitution is less than 1 ($e < 1$)

(1/2)

2 (b) No, projectile motion cannot be observed in a free fall cube because
One of the assumptions of projectile motion is acceleration due to gravity is constant but in free fall motion acceleration due to gravity is zero

(a)

$$V = \sqrt{20.0 + 9.81t} = \sqrt{10.0}$$

$$v_{0x} = \sqrt{20}$$

$$v_{0y} = \frac{9.81}{2} t$$

$$v_{0x} = \sqrt{20}$$

$$v_0 = \sqrt{20}$$

$$F_{0x} = 20$$

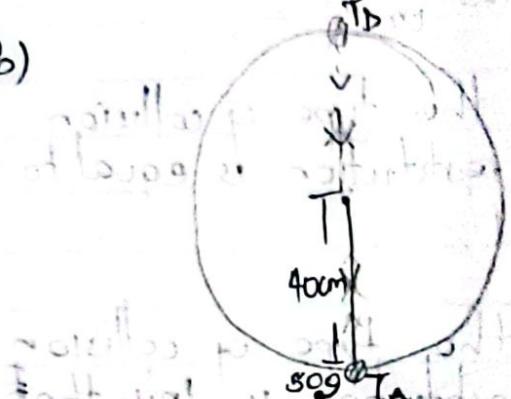
$$v_{0x} = 20$$

thus it is a right angled motion w.r.t.

(10)

- Direction of the body will be changing with direction.
- 3 (a) The vertical circle can not have constant velocity since the tension of the string acts differently at different positions. 103

(b)



$$T_D = T + mg \quad (1)$$

$$T_D = mg + ma \quad (2)$$

$$mg + ma = \frac{mv^2}{r}$$

$$v = \sqrt{gr} = \sqrt{0.8} = 0.98 \text{ m/s}$$

$$T_D = mg \Rightarrow F = mg$$

for this to occur, $T_D = 0$,
then,

$$PE_A + KE_A = PE_B + KE_B$$

$$\frac{1}{2}mv_A^2 = mgh + \frac{1}{2}mv_B^2$$

$$\frac{1}{2} \times 0.05 \text{ kg} \times V_A^2 = 0.05 \times 9.8 \times 0.8 + \frac{1}{2} \times 0.05 \times V_B^2$$

$$0.025V_A^2 = 0.392 + 0.025V_B^2 \rightarrow V_B$$

Then

from

$$\frac{mV_B^2}{r} = mg$$

$$\frac{V_B^2}{r} = mg \quad \times$$

$$V_B^2 = rg$$

$$V_B^2 = r g$$

$$V_B = \sqrt{rg}$$

$$V_B = 1.98 \text{ m/s}$$

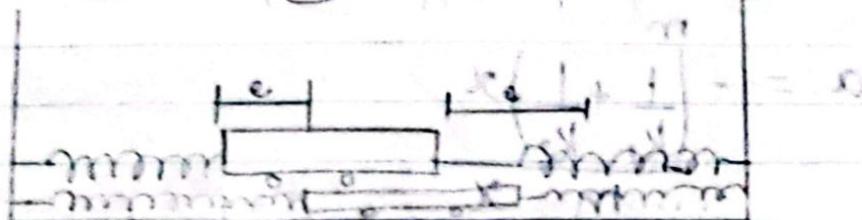
\therefore The minimum velocity of the ball is 1.98 m/s

(4)

4 (a) Inertia helps to bring back the body back into its mean position and conserve its Kinetic energy and Potential energy.

→ Reducing damping effect of oscillation

(b)



$$E_T = E_1 + E_2$$

$$\frac{F}{K_T} = \frac{F_1}{K_1} + \frac{F_2}{K_2}$$

Harmonic motion along
the axis of oscillation

$$\frac{F}{K_T} = \frac{1}{k} + \frac{1}{K_2}$$

imp(2)

then

$$-F_r = -F_c \quad F_c = -F_r$$

$$\frac{mv^2}{r} = -\mu N$$

$$\frac{mv^2}{r} = -Kx$$

$$\frac{v^2}{r} = -\frac{Kx}{m}$$

$$\frac{v^2}{r} = -\frac{Kx}{m}$$

$$a_c = -\frac{Kx}{m}$$

$$a_c = \left(\frac{1}{K_1} + \frac{1}{K_2} \right) x$$

$$(m \omega^2 x) \times (m \omega^2 x) \times 2 \pi f + 1 =$$

$$a_c = -\omega^2 y$$

then,

Since $a_c = -\omega^2 y$

P.T.O. → ~~SCHEDE~~

(20)

4(b) Then what will be the equation of motion?

$$F_C = -k_1 x \quad \checkmark \text{ (01)}$$

$$ma = -k_1 x$$

$$a = -\frac{k_1}{m} x \quad \checkmark \text{ (01)}$$

$$a = -\frac{\left(\frac{1}{k_1} + \frac{1}{k_2}\right)}{m} x \quad a = -\frac{(k_1 + k_2)}{m} x$$

$$a = -\omega^2 y \quad \times$$

Since acceleration is directly proportional to displacement then it executes S.H.M.

4(c) from

$$y = A \sin \omega t$$

$$v = A \omega \cos \omega t$$

from

$$V_{max} = A \omega \quad \checkmark \text{ (01)}$$

$$V_{max} = A \times 2\pi f$$

$$V_{max} = 0.025 \text{ m} \times 2 \times \pi \times 2$$

$$V_{max} = 0.314 \text{ m/s}$$

\therefore The maximum velocity is 0.314 m/s

Max potential energy

$$P.E_{max} = \frac{1}{2} m \omega^2 A^2 \quad \checkmark \text{ (01)}$$

$$= \frac{1}{2} \times 2 \text{ kg} \times (2 \times \pi \times 2)^2 \times (0.025 \text{ m})$$

$$= 1 \times 157.7536 \times 0.025$$

$$= 3.944 \text{ J} \quad \checkmark \text{ (01)}$$

\therefore The maximum potential energy is 3.944 J .

(11)

5 (a) A good absorber of radiant energy appears black because as the radiations are received by the body, the body absorbs all radiations and reflects none hence appearing black.

(b) Case 01

$$P_1 = \sigma A (T_1^4 - T_s^4)$$

$$P_2 = \sigma A (T_2^4 - T_s^4)$$

Taking ratio of the two equations.

$$\frac{P_1}{P_2} = \frac{\sigma A (T_1^4 - T_s^4)}{\sigma A (T_2^4 - T_s^4)}$$

$$\frac{P_1}{P_2} =$$

*5 (b) Case 01

$$\left(\frac{d\theta}{dt} \right)_1 = K (\theta_1 - \theta_s) \quad \rightarrow$$

Case 02

$$\left(\frac{d\theta}{dt} \right)_2 = K (\theta_2 - \theta_s) \quad \rightarrow$$

On taking ratio

$$\frac{\left(\frac{d\theta}{dt} \right)_1}{\left(\frac{d\theta}{dt} \right)_2} = \frac{K (\theta_1 - \theta_s)}{K (\theta_2 - \theta_s)}$$

$$\frac{\left(\frac{d\theta}{dt} \right)_1}{\left(\frac{d\theta}{dt} \right)_2} = \frac{\theta_1 - \theta_s}{\theta_2 - \theta_s}$$

$$\frac{\left(\frac{d\theta}{dt} \right)_1}{\left(\frac{d\theta}{dt} \right)_2} = \frac{527^\circ C - 27^\circ C}{127^\circ C - 21^\circ C}$$

$$\frac{\left(\frac{d\theta}{dt} \right)_1}{\left(\frac{d\theta}{dt} \right)_2} = \frac{300}{100} = 3$$

\therefore The rate of heat loss by A is 3 times
rate of heat loss by body B.

Q2

5 (c) Heat lost by metal = Heat gained by liquid and copper calorimeter

$$m c \Delta \theta_1 = m c \Delta \theta_2$$

$$0.11 \times 400 \times 100 = (0.3 + 0.2 \text{ kg}) \times c \times (8)$$

$$1640 = 0.3 \times 8c$$

$$4400 = 2.4c$$

$$c = 1833.3 \text{ J kg}^{-1} \text{ K}^{-1}$$

\therefore The specific heat capacity of liquid is 1833.3 J/kgK

$$0.11 \times 400 \times (100 - 18) = 0.3 \times 8c$$

$$(100 - 18) \times 100 = 8c$$

$$82 \times 100 = 8c$$

$$\frac{82 \times 100}{8} = c$$

$$1025 = c$$

Ans. A and b are both correct
Q. What is the final temperature?

6 (a) There is natural convection because of the differences in temperature between the land and sea. As in, during the day, the land absorbs energy, hence it is warm correspondingly the sea loses heat during the day, thus the warm air of the land rises as cool air from the sea moves to the land. ~~Because there is no cooling agent~~



Q3

6 (b) Forced convection is ~~not~~ necessary for excess temperature less than $20K$, because the validity of the law under ~~forced~~^{natural} convection is $20K \leq \theta - \theta_s \leq 500K$; hence the application of other factors like forced convection are needed for body to cool.

~~To allow movement of air around the object~~

Q3

6 (c) from

$$\theta_F = \theta_s + (\theta_1 - \theta_s) e^{-\lambda t}$$

$$63 = 22 + (66 - 63) e^{-\lambda t}$$

$$41 = 3 e^{-\lambda t} \text{ and then taking log both sides}$$

$$\frac{41}{3} = e^{-\lambda t}$$

(3)

$$\lambda = \ln(41/3)/-1$$

$$\lambda = -2.615$$

then ~~now consider various parts~~ ~~both ends ad~~

$$\theta_F = \theta_s + (\theta_1 - \theta_s) e^{-\lambda t}$$

$$40 = 22 + (43 - 40) e^{+2.615t}$$

$$18 = 3 e^{+2.615t}$$

$$6 = e^{+2.615t}$$

$$t = \frac{\ln 6}{2.615} = 0.68 \text{ minutes.}$$

\therefore It will take the cup 0.68 minutes

7 (a) From:

$$P = \frac{2}{3} N \bar{K} E_1 \rightarrow$$

$$2P = \frac{2}{3} N \bar{K} E_2 \rightarrow$$

On taking ratio in eqn ν to eqn ν ,

$$\frac{2P}{P_1} = \frac{2/3 N (\bar{K} E_1)}{2/3 N (\bar{K} E_2)}$$

$$2 = \frac{\bar{K} E_1}{\bar{K} E_2}$$

$$\bar{K} E_1 = 2 \bar{K} E_2$$

$$\bar{K} E_2 = \frac{1}{2} \bar{K} E_1$$

\therefore The average translational energy will be halved.

(ii) Since from Boyle's Law

$$P \propto \frac{1}{V}$$

Hence, when the volume is doubled, the pressure becomes halved, thus the kinetic energy will be doubled.

$$\frac{\bar{K} E_1}{\bar{K} E_2} = \frac{1}{2}$$

$$\bar{K} E_2 = 2 \bar{K} E_1$$

\therefore the average translational energy will be doubled.

(b) (ii) from ~~the law of equipartition~~

$$\overline{KE} = \frac{3}{2} k_B T$$

$$KE = \frac{3}{2} \times 1.38 \times 10^{-23} \times 290$$

$$KE = 6.003 \times 10^{-21} J$$

\therefore The average translational Kinetic energy
is $6.003 \times 10^{-21} J$

(iii) from

$$KE = \frac{1}{2} m \bar{u}^2$$

$$\bar{u}^2 = \frac{2KE}{m}$$

$$\bar{u} = \sqrt{\frac{2KE}{m}}$$

$$\bar{u} = \sqrt{\frac{2 \times 6.003 \times 10^{-21}}{m(6.67 \times 10^{-3})}}$$

$$\bar{u} = 6.43 \times 10^{-10} \text{ m/s.}$$

$$290 \rightarrow 6.02 \times 10^{23}$$

$$x \Rightarrow 1.$$

$$x = 4.817 \times 10^{-26}$$

\therefore The root mean square speed is $6.43 \times 10^{-10} \text{ m/s.}$

(v) Conduction of heat

$$\left(\frac{dQ}{dt} \right) = K \cdot A \cdot \frac{\Delta Q}{L}$$

Conduction of electricity

$$\frac{dQ}{dt} = I = \frac{V}{R} = \frac{VA}{\delta L}$$

$$\frac{dQ}{dt} = \frac{V}{\delta L} \cdot A \cdot \frac{dv}{dt}$$

7 (c) On comparing eqn. v and w

$$KA \frac{\Delta\theta}{L} = \frac{1}{3} \cdot A \cdot \frac{\Delta v}{d}$$

the corresponding quantities

$$k = \frac{1}{S}$$

$$A = A$$

$$\frac{\Delta\theta}{L} = \frac{v}{L}$$

Gold wall

Friction

is balanced by friction

friction

is balanced by friction

but is rebuked by

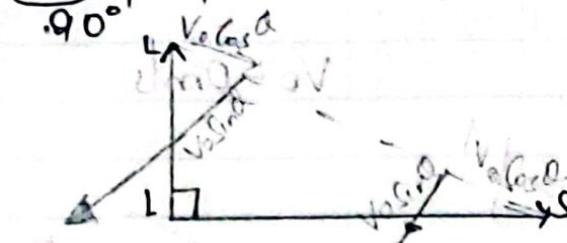
$$\left(\frac{2A}{3} \cdot \frac{A}{3} \right)$$

rebuked by

$$\frac{Av}{L} \cdot v \cdot L = \frac{Av^2}{L}$$

$v =$ rebuked by

8 (a) (i) Because when the source and listener are moving perpendicularly, the angle between them is 90°



A.

then

$$f' = \left(\frac{V \pm V_s \cos \theta}{V + V_s \sin \theta} \right) f$$

$$f' = \left(\frac{V \pm V_s \cos 90^\circ}{V \pm V_s \sin 90^\circ} \right) f$$

$$f' = \left(\frac{V \pm 0}{V \pm 0} \right) f$$

$$f' =$$

\therefore No doppler effect can occur since $\cos 90^\circ$ is 0.

(b) (ii) No, doppler effect in sound would not happen if the source and listener are moving in a circle because one of the major conditions for doppler effect to occur is that the source and observer by a straight line.

A:

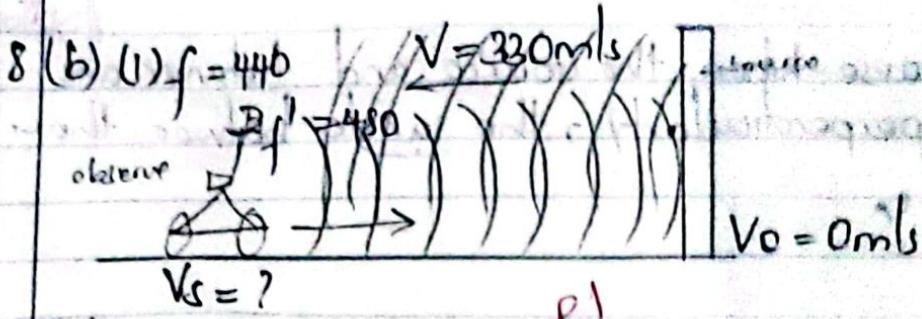
$$f' = \left(\frac{V + V}{V - V} \right) f$$

$$0.83 \left(\frac{8V + V}{8V - V} \right) f$$

$$0.83 \left(\frac{9V}{7V} \right) f = 1.14 f$$

02

AM



After reflection

~~$$f'' = \left(\frac{V + V_s}{V} \right) f_0$$~~

~~$$480 = \left(\frac{330 + V_s}{330} \right) 440$$~~

~~$$480 = \frac{440(330 + V_s)}{330}$$~~

$$158400 = 145200 + 440V_s$$

$$13200 = 440V_s$$

$$V_s = 30 \text{ m/s}$$

\therefore The speed of the bike is 30 m/s ~~X~~

~~$$(b)(ii) - A - f = 800 \text{ Hz} \quad V = 360 \text{ m/s}$$~~

~~$$V = 432 \text{ km/h} = 120 \text{ m/s}$$~~

The Relative velocity of A and B

$$RV = V_A \mp V_B$$

$$120 = V_A - V_B, \quad V_B = V_A - 120$$

then

$$f'' = \left(\frac{V + V_0}{V - V_s} \right) f$$

$$f'' = \left(\frac{V + V_B}{V - V_A} \right) 800$$

$$f'' = \left(\frac{360 + (V_A - 120)}{360 - V_A} \right) 800$$

$$f'' = \left(\frac{360 + V_A - 120}{360 - V_A} \right) 800$$

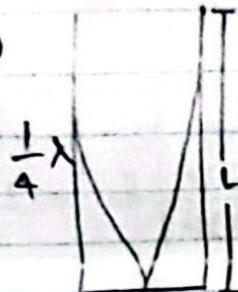
$$f'' = \left(\frac{240 + V_A}{360 - V_A} \right) 800$$

$$f'' = \frac{192000 + 800 V_A}{360 - V_A}$$

$$\cancel{f'' = V_A \left(\frac{192000}{V_A} \right)}$$

∴ The apparent frequency is $\frac{192000 + 800 V_A}{360 - V_A}$

2) (i)



$$x = 4L$$

The

$$V = \lambda f_0$$

$$f_0 = \frac{V}{\lambda}$$

$$f_0 = \frac{V}{4L}$$

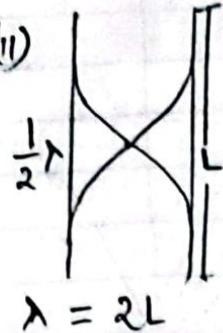
Then

$$f_3 = (2n+1)f_0$$

$$= (2 \times 3 + 1)f_0$$

$$7 \left(\frac{V}{4L} \right)$$

9(a)(ii)



$$\lambda = 2L$$

the

$$v = \lambda f_0$$

$$f_0 = \frac{v}{2L}$$

so

$$f_3 = f_0$$

$$7\left(\frac{v}{4L}\right) = \frac{v}{2L} \quad \cancel{\times}$$

$$\frac{7}{4L} = \frac{1}{2L}$$

$$\frac{7}{4 \times 30} = \frac{1}{2L}$$

$$14L = 120$$

$$L = 8.57 \text{ cm}$$

$$\frac{3v}{4L} = \frac{v}{2L}$$

$$\frac{3}{4L} = \frac{1}{2L}$$

$$\frac{3}{4 \times 30} = \frac{1}{2L}$$

$$\frac{6L}{6} = \frac{120}{4}$$

$$6L = 120$$

$$L = 20$$

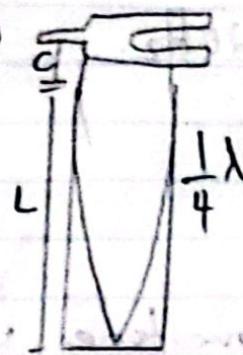
∴ The length of open pipe is 8.57 cm.

$$c(f_1 + 2f_0) = 8.57$$

$$c(f_1 + 8x3) =$$

$$\frac{V}{f_1}$$

9 (a)(i)



$$f_0; \quad \frac{4}{4(c+L)} = \lambda$$

the expression obtained is similar to 1(a)

$$f_0 = \frac{V}{4(c+L)}$$

$$I = \frac{V}{c}$$

In the first overtone

$$f_1 = 3 \left(\frac{V}{4(c+L)} \right)$$

$$f_1 = \frac{3V}{4(c+L)}$$

then

$$\frac{f_0}{4(c+0.2)} = \frac{3V}{4(c+0.7)}$$

$$\frac{1}{4c+0.8} = \frac{3}{4c+2.8}$$

$$4c+2.8 = 12c+2.4$$

$$\frac{0.4}{8} = \frac{8c}{8}$$

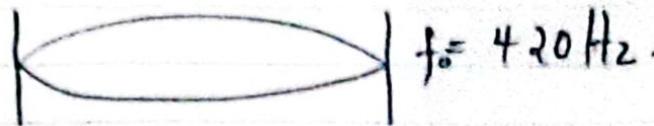
$$c = 0.05 \text{ m} \text{ (by inspection)}$$

\therefore The length of the end correction is 0.05 m.

✓ D1

ok

9(b) (i)



$$f_0 = 420 \text{ Hz}$$

$$\begin{aligned} f_3 &= 3f_0 \\ &= 3 \times 420 \\ &= 1260 \text{ Hz} \end{aligned}$$

∴ The frequency of third overtone is
1260 Hz

(ii) First overtone - fundamental frequency

from

$$\frac{1}{2}\lambda = L$$

$$\lambda = 2L$$

then

$$f_0 = \frac{V}{\lambda}$$

$$f_0 = \frac{V}{2L}$$

$$f_0 = \frac{V}{40 \text{ cm}} = \frac{340 \text{ m/s}}{0.4 \text{ m}}$$

$$f_0 = 850 \text{ Hz}$$

then

$$f_3 = 3f_0$$

$$\begin{aligned} f_3 &= 3 \times 850 \\ &= 2550 \text{ Hz} \end{aligned}$$

∴ The frequency of the third overtone is
2550 Hz.

10(i) We know $y = A \sin(\omega t - kx)$ when a wave is progressing towards the positive x -direction and $y = A \sin(kx - \omega t)$ when the wave is progressing towards the negative x -direction.

(ii) (i) $y = 5 \sin(240\pi t)$ $y = 4 \sin(244\pi t)$

form Case 01

$$2\pi f = 240\pi$$

$$f = 120$$

$$f_1 = 120 \text{ Hz}$$

Case 02: It is now time to calculate f_2 .

$$2\pi f_1 = 244\pi$$

$$f_2 = 122$$

$$f_2 = 122 \text{ Hz}$$

then

$$f_B = |f_1 - f_2|$$

$$f_B = |120 - 122|$$

$$f_B = 2 \text{ Hz}$$

∴ The number of beats heard per second is $2\pi f_B$. $\therefore 2\pi f_B = 2\pi \times 2 = 4\pi$.

(b) Resultant amplitude

$$A = \sqrt{A_1^2 + A_2^2 + 2A_1 A_2 \cos \phi}$$

$$A = \sqrt{6^2 + 6^2 + 2(6)(6) \cos 30^\circ}$$

$$A = 11.59 \text{ m}$$

∴ The resultant amplitude is 11.59 m .

10 (c) (i) The function represents a stationary wave since it does not vary in the direction of wave propagation.

10 (c) (ii) $\frac{1}{2} A$

$$10 (c) (i) \cdot y = 0.06 \sin \frac{2\pi}{3}x \cos (120\pi t)$$

Amplitude,

$$2A = 0.06$$

$$A = 0.03 \text{ m}$$

∴ The amplitude of each wave is 0.03 m.

Wavelength

$$\frac{2\pi}{\lambda} = \frac{2\pi}{3}$$

$$\frac{2}{\lambda} = \frac{2}{3}$$

$$2\lambda = 6$$

$$\lambda = 3 \text{ m}$$

∴ The wavelength of each wave is 3 m.

Frequency

$$2\pi f = 120\pi$$

$$f = 60 \text{ Hz}$$

∴ The frequency of the waves is 60 Hz.

Then

$$v = \lambda f$$

$$v = 3 \times 60$$

$$v = 180 \text{ m/s}$$

∴ The speed of propagation of each wave is 180 m/s.

10 (c) (ii) Tension

$$V = \sqrt{\frac{TL}{m}}$$

$$V^2 = \frac{TL}{m}$$

$$T = \frac{V^2 L}{m} \quad T = \frac{V^2 m}{L}$$

$$T = \frac{(180)^2 \times 3 \times 10^{-3} \text{ kg}}{1.5 \text{ M}}$$

$$T = 648 \text{ N}$$

∴ The tension in the string is 648 N.

✓ 001
2

✓ 001
2