

hw6

● Graded

Student

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Total Points

29 / 40 pts

Question 1

pda formal description

14 / 15 pts

✓ - 0.5 pts Incomplete/incorrect table (minor infraction)

✓ - 0.5 pts CFG has minor error

💬 b and c never appear on stack, shouldn't be on table. Also, the string abcc can never be created with your implementation. Very close though.

Question 2

regular language is context-free

10 / 15 pts

✓ - 2 pts proof using NFA: incomplete / missing delta

✓ - 3 pts proof using DFA: conversion to PDA or CFG is not equivalent or is not general

Question 3

non-cfl

4 / 9 pts

✓ - 1 pt counterexample must be a specific string (e.g., cannot include something like "indent1")

✓ - 2 pts counterexample not in the language

✓ - 2 pts didnt explain why each possible splitting of counterexample cannot be pumped

💬 in counterexample, did you forget a p on indent3?

Question 4

readme

1 / 1 pt

✓ - 0 pts Correct

Question assigned to the following page: [1](#)

1. Formal Descriptions for PDA's

1.1)

A formal description of this PDA is a 6 tuple $(Q, \Sigma, \Gamma, \delta, q_0, F)$ specified below:

$Q = \{q_1, q_2, q_3, q_4, q_5, q_6, q_7\}$

$\Sigma = \{a, b, c\}$

$\Gamma = \{a, \$\}$

δ is given by the following table, where blank cells signify \emptyset .

| Input: | a | b | c | e |
|--------|----------------|----------------|----------------|--------------------------|
| Stack: | a b c \$ e | a b c \$ e | a b c \$ e | a b c \$ e |
| q_1 | | | | $\{(q_2, \$)\}$ |
| q_2 | $\{(q_2, a)\}$ | | | $\{(q_2, e), (q_3, e)\}$ |
| q_3 | | $\{(q_3, e)\}$ | | $\{(q_4, e)\}$ |
| q_4 | | | $\{(q_4, e)\}$ | |
| q_5 | | $\{(q_5, e)\}$ | | $\{(q_6, e)\}$ |
| q_6 | | | $\{(q_6, e)\}$ | $\{(q_7, e)\}$ |
| q_7 | | | | |

$q_0 = q_1$

$F = \{q_4, q_7\}$

Question assigned to the following page: [1](#)

1.2)

string 1: aabb

$(q_1, aabb, \epsilon) \vdash (q_2, aabb, \$)$
 $\vdash (q_2, abb, a\$)$
 $\vdash (q_2, bb, aa\$)$
 $\vdash (q_3, bb, aa\$)$
 $\vdash (q_3, b, a\$)$
 $\vdash (q_3, \epsilon, \$)$
 $\vdash (q_4, \epsilon, \epsilon)$

string 2: aabcc

$(q_1, aabcc, \epsilon) \vdash (q_2, aabcc, \$)$
 $\vdash (q_2, abcc, a\$)$
 $\vdash (q_2, bcc, aa\$)$
 $\vdash (q_5, bcc, aa\$)$
 $\vdash (q_5, cc, aa\$)$
 $\vdash (q_6, cc, aa\$)$
 $\vdash (q_6, c, a\$)$
 $\vdash (q_6, \epsilon, \$)$
 $\vdash (q_7, \epsilon, \epsilon)$

1.3)

string 1: aaa

$(q_1, baa, \epsilon) \vdash (q_2, aaa, \$)$
 $\vdash (q_2, aa, a\$)$
 $\vdash (q_2, a, aa\$)$
 $\vdash (q_2, \epsilon, aaa\$)$

→ can go no further than q_3 and q_6 , therefore it is not a string in the language

string 2: ccab

$(q_1, cbba, \epsilon) \vdash (q_2, cbba, \$)$

→ can reach accept states, but pda will not have finished reading the input, therefore it is not a string in the language

Question assigned to the following page: [1](#)

1.4)

$G \rightarrow aXc \mid cC \mid bB \mid aFb$

$X \rightarrow \varepsilon \mid b \mid bX \mid aXc$

$C \rightarrow \varepsilon \mid c \mid cC$

$B \rightarrow \varepsilon \mid b \mid bB$

$F \rightarrow \varepsilon \mid aFb$

Let P be the cfg that represents this pda.

P is a 4 tuple (V, Σ, R, S) , where:

$V = \{G, X, C, B, F\}$

$\Sigma = \{a, b, c, \varepsilon\}$

$R = \{$

$G \rightarrow aXc \mid cC \mid bB \mid aFb,$

$X \rightarrow \varepsilon \mid b \mid bX \mid aXc,$

$C \rightarrow \varepsilon \mid c \mid cC,$

$B \rightarrow \varepsilon \mid b \mid bB,$

$F \rightarrow \varepsilon \mid aFb$

$\}$

$S = G$

Question assigned to the following page: [2](#)

2) A Regular Language is a Context-Free

proof using dfa

| step | statement | justification |
|------|---|-------------------------------------|
| 1 | Every regular language is a context free language | given statement to prove |
| 2 | A language is regular if it can be recognized by a dfa | definition of a regular language |
| 3 | A context free language can be described by a context free grammar | definition of context free language |
| 4 | A dfa $M = (Q, \Sigma, \delta, q_0, F)$ recognizes the regular language L | (2) |
| 5 | <p>M can be converted into a CFG named $X = (V, \Sigma, R, S)$ where:</p> <p>$V = Q$ $\Sigma = \Sigma$ $R = \delta_q$, where δ_q is the alphabet from the transition to the next state and q is the next state $S = q_0$, where q_0 now has a ϵ as a terminal as well as its R rule.</p> | computation |
| 6 | The regular language L can be described by X , therefore it is a context free language | (5) and (3) |

proof using nfa

| step | statement | justification |
|------|---|-------------------------------------|
| 1 | Every regular language is a context free language | given statement to prove |
| 2 | A language is regular if it can be recognized by a nfa | definition of a regular language |
| 3 | A context free language can be described by a pda | definition of context free language |
| 4 | A nfa $N = (Q, \Sigma, \delta, q_0, F)$ recognizes the language L | (2) |

Question assigned to the following page: [2](#)

| | | |
|---|---|---------------------|
| 5 | N can be converted into a pda named X : $Q = Q$ $\Sigma = \Sigma$ $\Gamma = \epsilon$ $\delta = Q \times \Sigma \times \Gamma \rightarrow P(Q \times \Gamma)$ $q_0 = q_0$ $F = F$ | computation and (4) |
| 6 | The regular language L can be described by X , therefore it is a context free language | (5) and (3) |

proof using regular expression

| step | statement | justification |
|------|---|---|
| 1 | Every regular language is a context free language | given statement to prove |
| 2 | A language is regular if it can be recognized by a regular expression | definition of a regular language |
| 3 | A regular expression can be converted into an equivalent nfa | theorem (backwards part): a lang is reg iff some regex describes it |
| 4 | A context free language can be described by a pda | definition of context free language |
| 5 | A regular expression R recognizes the language L | (2) |
| 6 | R can be converted into an nfa $N = (Q, \Sigma, \delta, q_0, F)$ | (3) |
| 7 | N can be converted into a pda named X : $Q = Q$ $\Sigma = \Sigma$ $\Gamma = \epsilon$ $\delta = Q \times \Sigma \times \Gamma \rightarrow P(Q \times \Gamma)$ $q_0 = q_0$ $F = F$ | computation |
| 8 | The regular language L can be described by X , therefore it is a context free language | (4) and (7) |

Question assigned to the following page: [3](#)

3) Non-CFL Whitespace Checking

| step | statement | justification |
|------|--|-------------------------------------|
| 1 | <p>prove that W is not a CFL</p> <p>W = $\{w \mid$ $w = \text{if_}b_1: \text{indent}_1 n_1 \text{ elif_}$ $b_2: \text{indent}_2 n_2 \text{ else: indent}_3 n_3\}$ where: 1. b_1, b_2 is in $\{\text{true}, \text{false}\}$ 2. n_1, n_2, n_3 are in $\{0, 1, \dots, 9\}$ 3. $\text{indent}_1, \text{indent}_2, \text{indent}_3$ are in $_ _^*$ 4. $\text{indent}_1 = \text{indent}_2 = \text{indent}_3$</p> | given statement to prove |
| 2 | proof by contradiction on W | method of proof |
| 3 | assume that W is a CFL | (2) |
| 4 | <p>The pumping lemma for CFL says that for a CFL there is a pumping length where any string in the language of length at least p, then that string may be divided into five pieces satisfying three conditions.</p> <p>s = string p = pumping length $s = uvxyz \rightarrow 5 \text{ pieces}$ conditions: 1. for $i \geq 0$, $uv^i xy^i z$ in A, 2. $vy > 0$, and 3. $vxy \leq p$</p> | definition of pumping lemma for CFL |
| 5 | <p>counterexample for assumption: $\text{if_}b_1: \text{indent}_1^p n_1 \text{ elif_}b_2: \text{indent}_2^p n_2 \text{ else: indent}_3 n_3$</p> | (4) |
| 6 | <p>pumping the first two indents will always cause the condition of W, $\text{indent}_1 = \text{indent}_2 = \text{indent}_3$ to be false. This means that no matter how you split it the string will not be in the language, therefore the pumping lemma does not work on W</p> <p>$u = \text{if_}b_1:$ $v = \text{indent}_1^p$</p> | (1), (4) and (5) |

Question assigned to the following page: [3](#)

| | | |
|---|--|------------------|
| | $x = n_1 \text{ elif } b_2:$ $y = \text{indent}_2^p$ $z = n_2 \text{ else: indent}_3 n_3$ | |
| 7 | W is not pumpable, which means it is not a CFL | (6) |
| 8 | statement 7 and 3 contradict, therefore W is not a CFL due to the contrapositive of the CFL pumping lemma. | (3), (4) and (7) |



Question assigned to the following page: [4](#)

README

other students: none

websites/books: class slides, lecture,

<https://www.youtube.com/watch?v=pMvvvTHeHE&t=184s> for #2 using dfa proof, trying to convert dfa transition function to R for CFG.

hours spent: 5 hours