week09-00

March 24, 2025

1 Sorting...

```
[1]: import numpy as np
     L = np.random.rand(20)
     L
[1]: array([0.15496462, 0.43771374, 0.7691895, 0.07377782, 0.79910591,
            0.56433127, 0.73494644, 0.13545665, 0.66473965, 0.19518556,
            0.21220215, 0.33412276, 0.94886737, 0.4219934, 0.98005206,
            0.42314489, 0.67667685, 0.610882 , 0.28401761, 0.12808084])
[2]: L.sort()
     L
[2]: array([0.07377782, 0.12808084, 0.13545665, 0.15496462, 0.19518556,
            0.21220215, 0.28401761, 0.33412276, 0.4219934, 0.42314489,
            0.43771374, 0.56433127, 0.610882 , 0.66473965, 0.67667685,
            0.73494644, 0.7691895, 0.79910591, 0.94886737, 0.98005206])
[3]: np.flip(L)
[3]: array([0.98005206, 0.94886737, 0.79910591, 0.7691895, 0.73494644,
            0.67667685, 0.66473965, 0.610882 , 0.56433127, 0.43771374,
            0.42314489, 0.4219934, 0.33412276, 0.28401761, 0.21220215,
           0.19518556, 0.15496462, 0.13545665, 0.12808084, 0.07377782])
[5]: rng = np.random.default_rng()
     import pprint
     float_formatter = "{:.5f}".format
     np.set_printoptions(formatter={'float_kind':float_formatter})
     colors = [ "Gainsboro",
                "Gamboge",
                "Glossy grape",
                "Gold (metallic)",
                "Gold (Crayola)",
```

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"Golden poppy",
                "Golden yellow",
                "Goldenrod",
                "Gotham green",
                "Granite gray",
                "Granny Smith apple",
                "Gray (web)",
                "Gray (X11 gray)",
                "Green",
                "Green (Crayola)",
                "Green (web)",
                "Green (Munsell)",
                "Green (pigment)",
                "Green-blue",
                "Green Lizard"
                ٦
     vals = rng.random(20)
     { colors[i]:float(vals[i]) for i in range(20) }
[5]: {'Gainsboro': 0.06757705361621236,
      'Gamboge': 0.6814114044289292,
      'Glossy grape': 0.7277477398996349,
      'Gold (metallic)': 0.2668064570821498,
      'Gold (Crayola)': 0.7745500036614242,
      'Golden poppy': 0.19907674132921627,
      'Golden yellow': 0.3086028613701629,
      'Goldenrod': 0.43478402025095453,
      'Gotham green': 0.30007057477468146,
      'Granite gray': 0.9523168993121307,
      'Granny Smith apple': 0.1460670657546972,
      'Gray (web)': 0.7686009347303981,
      'Gray (X11 gray)': 0.0034087779127690565,
      'Green': 0.25618679306680814,
      'Green (Crayola)': 0.5852818538285638,
      'Green (web)': 0.7002443464296474,
      'Green (Munsell)': 0.24841718303543836,
      'Green (pigment)': 0.026560789524888828,
      'Green-blue': 0.3865936880142321,
      'Green Lizard': 0.6988164796183741}
[7]: vals
[7]: array([0.06758, 0.68141, 0.72775, 0.26681, 0.77455, 0.19908, 0.30860,
            0.43478, 0.30007, 0.95232, 0.14607, 0.76860, 0.00341, 0.25619,
            0.58528, 0.70024, 0.24842, 0.02656, 0.38659, 0.69882
```

2 Example: financial markets, again briefly

Recall our model:

	bull	bear	recession
followed by bull	0.90	0.15	0.25
followed by bear	0.075	0.00	0.25
followed by recession	0.025	0.05	0.50

```
[14]: vals, vecs = npl.eig(A)
vals
```

[14]: array([1.00000, 0.74142, 0.45858])

Now, recall that the long term behavior of the market is predicted by the normalized 1-eigenvector.

```
[15]: w = vecs[:,0]

# not normalized!
(w, sum(w))
```

[15]: (array([0.89087, 0.44544, 0.08909]), np.float64(1.4253932901995967))

```
[16]: # normalized
      nw = 1/sum(w) * w
      (nw,sum(nw))
[16]: (array([0.62500, 0.31250, 0.06250]), np.float64(1.0))
     Now we can display the market states in descending order of their long-term probabilities:
[18]: { states[i] : float(nw[i]) for i in np.argsort(nw) }
[18]: {'recession': 0.0625, 'bear': 0.3125, 'bull': 0.625}
[20]: def market_probabilities(A):
          vals, vecs = npl.eig(A)
          # get the 1-eigenvectors, as a list (which should be of length 1)
          oe = [ vecs[:,i] for i in range(len(vals)) if vals[i] - 1 < 1E-5 ]</pre>
          w = oe[0]
          nw = 1/sum(w) * w
          return { states[i] : float(nw[i]) for i in np.argsort(-nw) }
[21]: market_probabilities(A)
[21]: {'bull': 0.625, 'bear': 0.3125, 'recession': 0.0625}
[22]: B = np.array([0.80, 0.15, 0.25],
                    [0.075, 0.80, 0.25],
                    [0.035, 0.05, 0.50]
[23]: market_probabilities(B)
[23]: {'bull': 0.5228037465286232,
       'bear': 0.3933745222671231,
       'recession': 0.0838217312042538}
 []:
```