

## Spring 2023 Algebra &amp; Number Theory



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*Reductive subgroup schemes of a parahoric group scheme*

Let  $G$  be a reductive algebraic group over  $K$  where  $K$  is the field of fractions of a complete discrete valuation ring  $A$ . The parahoric group schemes attached to  $G$  are certain smooth group schemes  $P$  over  $A$  for which the group  $P_K$  obtained by base-change coincides with  $G$ .

Write  $k$  for the residue field of  $A$ . In general, the special fiber  $P_k$  of a parahoric group scheme is not reductive. When  $G$  splits over an unramified extension of  $K$ , we proved in a relatively recent paper that for any parahoric group scheme  $P$  attached to  $G$  that there is a closed  $A$ -subgroup scheme  $M$  of  $P$  for which the special fiber  $M_k$  is a Levi factor of the group  $P_k$ , and the generic fiber  $M_K$  is a maximal rank reductive subgroup of  $P_K = G$ .

The talk will aim to describe this result and some background material: among other things, it will describe the notion of a Levi factor, of a parahoric group scheme, and of a maximal rank reductive subgroup.



*Come join us!*

"Tea"  
(informal  
meet-and-  
greet)  
before talk

**FRIDAY**  
**May 5**

**11 am PST**

**IN PERSON !**  
**McHenry 4130**

Refreshments  
in the tea room (Mch 4161)  
~30m beforehand

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