

LogiCORE IP Complex Multiplier v5.0

DS793 March 1, 2011 Product Specification

Overview

The Xilinx[®] LogiCORE™ IP Complex Multiplier implements AXI4-Stream compliant, high-performance, optimized complex multipliers based on user-specified options.

The two multiplicand inputs and optional rounding bit are input on independent AXI4-Stream channels as slave interfaces and the resulting product output via an AXI4-Stream master interface.

Within each channel, operands and the results are represented in signed two's complement format. The operand widths and the result width are parameterizable.

Features

- Drop-in module for Virtex[®]-7, KintexTM-7, Virtex[®]-6 and Spartan[®]-6 FPGAs
- AXI4-Stream-compliant interfaces
- 8-bit to 63-bit input precision and up to 127-bit output precision
- Supports truncation or unbiased rounding
- Configurable minimum latency
- Three or four real multiplier implementation options
- Option to use LUTs or XtremeDSPTM slices
- Resource estimation in the Xilinx[®] CORE
 GeneratorTM graphical user interface (GUI)
- For use with Xilinx CORE Generator tool and Xilinx System Generator for DSP 13.1

| LogiCORE IP Facts | | |
|---|--|--|
| Core Specifics | | |
| Supported Device Family ⁽¹⁾ | Kintex-7, Virtex-7 Virtex-6, Spartan-6 | |
| Supported User Interfaces | AXI4-Stream | |
| Configuration | See Table 6 to Table 7 | |
| | Provided with Core | |
| Documentation | Product Specification | |
| Design Files | Netlist | |
| Example Design | Not Provided | |
| Test Bench | VHDL | |
| Constraints File | N/A | |
| Simulation Model | VHDL and Verilog | |
| | Tested Design Tools | |
| Design Entry Tools | CORE Generator 13.1 System Generator for DSP 13.1 | |
| Simulation | Mentor Graphics ModelSim 6.6d Cadence Incisive Enterprise Simulator (IES) 10.2 Synopsys VCS and VCS MX 2010.06 ISIM13.1 | |
| Synthesis Tools | XST 13.1 | |
| Support | | |
| Provided by Xilinx, Inc. | | |

For the complete list of supported devices, see the <u>release</u> notes for this core.



Functional Description

There are two basic architectures to implement complex multiplication, given two operands: $a = a_r + ja_i$ and $b = b_r + jb_i$, yielding an output $p = ab = p_r + jp_i$.

Direct implementation requires four real multiplications:

$$p_r = a_r b_r - a_i b_i$$
 Equation 1
$$p_i = a_r b_i + a_i b_r$$
 Equation 2

By exploiting that

$$p_r = a_r b_r - a_i b_i = a_r (b_r + b_i) - (a_r + a_i) b_i$$
 Equation 3
 $p_i = a_r b_i + a_i b_r = a_r (b_r + b_i) + (a_i - a_r) b_r$ Equation 4

a three real multiplier solution can be devised, which trades off one multiplier for three pre-combining adders and increased multiplier wordlength.

Pinout

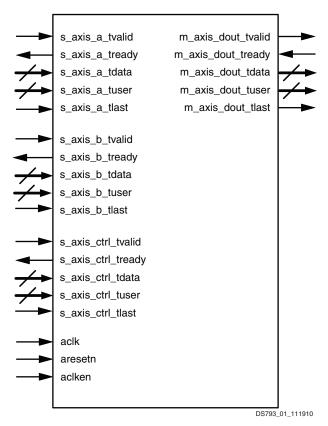


Figure 1: Core Schematic Symbol



This section describes the Complex Multiplier core ports as shown in Figure 1 and described in Table 1.

Table 1: Core Signal Pinout

| Name | Direction | Optional | Description | |
|--------------------------|-----------|----------|--|--|
| aclk | Input | yes | Rising-edge clock. aclk is optional. It is not present when FlowControl is NonBlocking and MinimumLatency = 0. | |
| aclken | Input | yes | Active-high clock enable (optional) | |
| aresetn | Input | yes | Active-low synchronous clear (optional, always take priority over aclken) | |
| | | | Note: aresetn should be asserted or deasserted for not less than two aclk cycles. | |
| s_axis_a_tvalid | Input | no | TVALID for channel A | |
| s_axis_a_tready | Output | yes | TREADY for channel A | |
| s_axis_a_tuser[A-1:0] | Input | yes | TUSER for channel A. Width selectable from 1 to 256 bits | |
| s_axis_a_tdata[B-1:0] | Input | no | TDATA for channel A. See TDATA Packing for internal structure and width. | |
| s_axis_a_tlast | Input | yes | TLAST for channel A. | |
| s_axis_b_tvalid | Input | no | TVALID for channel B | |
| s_axis_b_tready | Output | yes | TREADY for channel B | |
| s_axis_b_tuser[C-1:0] | Input | yes | TUSER for channel B. Width selectable from 1 to 256 bits | |
| s_axis_b_tdata[D-1:0] | Input | no | TDATA for channel B. See TDATA Packing for internal structure and width. | |
| s_axis_b_tlast | Input | yes | TLAST for channel B. | |
| s_axis_ctrl_tvalid | Input | yes | TVALID for channel CTRL | |
| s_axis_ctrl_tready | Output | yes | TREADY for channel CTRL | |
| s_axis_ctrl_tuser[E-1:0] | Input | yes | TUSER for channel CTRL. Width selectable from 1 to 256 bits | |
| s_axis_ctrl_tdata[7:0] | Input | yes | TDATA for channel CTRL. See TDATA Packing for internal structure and width. | |
| s_axis_ctrl_tlast | Input | yes | TLAST for channel CTRL. | |
| m_axis_dout_tvalid | Output | no | TVALID for channel DOUT | |
| m_axis_dout_tready | Input | yes | TREADY for channel DOUT | |
| m_axis_dout_tuser[G-1:0] | Output | yes | TUSER for channel DOUT. Width is the sum of the enabled TUSER fields on input channels. | |
| m_axis_dout_tdata[H-1:0] | Output | no | TDATA for channel DOUT. See TDATA Packing internal structure. | |
| m_axis_dout_tlast | Output | yes | TLAST for channel DOUT. | |

Notes:

- 1. All AXI4-Stream port names are lower case but for ease of visualization, upper case is used in this document when referring to port name suffixes, such as TDATA or TLAST.
- 2. Width constants A to H are arbitrary variables, determined by GUI or XCO parameters.



CORE Generator Graphical User Interface

The Complex Multiplier core GUI has a number of fields to set parameter values for the particular instantiation required. This section provides a description of each GUI field.

Component Name: The name of the core component to be instantiated. The name must begin with a letter and be composed of the following characters: a to z, A to Z, D to D and D and D and D and D and D and D are D and D and D are D are D and D are D are D and D are D and D are D

Channel A Options:

- AR/AI Operand Width: Select the first operand width. The width applies to both the real and imaginary components of the complex operand. See TDATA Structure for A, B and DOUT Channels to see how the operand components map into TDATA for this channel.
- **Has TLAST:** Select whether the channel has TLAST. To ease system design, the core passes any TLAST and TUSER to the output with latency equal to the TDATA field. See TLAST and TUSER Handling.
- **Has TUSER:** Select whether the channel has TUSER. To ease system design, the core passes any TLAST and TUSER to the output with latency equal to the TDATA field. See TLAST and TUSER Handling.
- TUSER Width: Select the width, in bits, of the TUSER field for this channel.

Channel B Options:

- **BR/BI Operand Width**: Select the second operand width. The width applies to both the real and imaginary components of the complex operand. See TDATA Structure for A, B and DOUT Channels to see how the operand components map into TDATA for this channel.
- **Has TLAST:** Select whether the channel has TLAST. To ease system design, the core passes any TLAST and TUSER to the output with latency equal to the TDATA field. See TLAST and TUSER Handling.
- **Has TUSER:** Select whether the channel has TUSER. To ease system design, the core passes any TLAST and TUSER to the output with latency equal to the TDATA field. See TLAST and TUSER Handling.
- TUSER Width: Select the width, in bits, of the TUSER field for this channel.

Multiplier Construction Options: Allows the choice of using LUTs (slice logic) to construct the complex multiplier, or using XtremeDSP slices.

Optimization Goal: Selects between Resource and Performance optimization.

- This selection affects both the internal architectural decisions and the performance/resource trade-offs in the AXI4-Stream interfaces.
- For Multiplier-based implementations, Resource optimization generally uses the three real multiplier structure. The core uses the four real multiplier structure when the three real multiplier structure uses more multiplier resources. Performance optimization always uses the four real multiplier structure to allow the best clock frequency performance to be achieved.

Flow Control Options: Selects between Blocking and NonBlocking behavior for the AXI4-Stream Interfaces. See NonBlocking Mode and Blocking Mode for greater detail.

Output Product Range

• Output Width: Selects the width of the output product real and imaginary components. The values are automatically initialized to provide the full-precision product when the A and B operand widths are set. The natural width of a complex multiplication is the sum of the input widths plus one. If Output Width is set to be less than this natural width, the least significant bits are truncated or rounded, as selected by the next GUI field.



Output Rounding: If the full-precision product (output width equals natural width) is selected, no rounding options are available. Otherwise either Truncation or Random Rounding can be selected. When Random Rounding is selected, the CTRL channel is enabled. Bit 0 of the TDATA field of this channel determines the particular type of rounding for the operation in question. See the Rounding section for further details.

Channel CTRL Options: The control channel exists to supply the bit which determines the rounding type. However, it also provides an opportunity to pass TUSER or TLAST information which has no association with either of the input operands via the core.

- Has TLAST: Select whether the channel has TLAST. To ease system design, the core passes any TLAST and TUSER to the output with latency equal to the TDATA field. See TLAST and TUSER Handling.
- **Has TUSER:** Select whether the channel has TUSER. To ease system design, the core passes any TLAST and TUSER to the output with latency equal to the TDATA field. See TLAST and TUSER Handling.
- TUSER Width: Select the width, in bits, of the TUSER field for this channel.

Output TLAST Behavior

- TLAST Behavior: Determines which of the input channels' TLAST or which combination of input channel TLASTs is conveyed to the output channel TLAST. Available options are to pass any one of the input channels' TLAST or to pass the logical OR of all available input TLASTs or to pass the logical AND of all available input TLASTs. See TLAST and TUSER Handling.
- **Core Latency**: Select the desired latency for the core.

Latency Configuration: Selects between Automatic and Manual. When Automatic, latency is set such that the core is fully pipelined for maximum performance. Manual allows user-selectable minimum latency. Performance drops when the value set is less than the fully pipelined latency. When the value set is larger than fully pipelined, the core delays the output via an SRL. With Blocking Flow Control selected, the core latency is not fixed, so only minimum latency can be specified.

Minimum Latency: The value for Manual Latency Configuration.

Control Signals: Selects which control signals should be present on the core. These options are disabled when the core has a minimum latency of zero.

- ACLKEN: Enables the clock enable (aclken) pin on the core. All registers in the core are enabled by this signal.
- **ARESETn:** Enables the active low synchronous clear (aresetn) pin on the core. All registers in the core are reset by this signal. This can increase resource use and degrade performance, as the number of SRL-based shift registers that can be used is reduced. aresetn always take priority over aclken.

Resource Estimation Tab: Click the tab below the GUI symbol to display an estimate of the XtremeDSP slice resources used for a particular complex multiplier configuration. This value updates instantaneously with changes in the GUI, allowing trade-offs in implementation to be evaluated immediately.



Using the Complex Multiplier IP Core

The CORE Generator GUI performs error-checking on all input parameters. Resource estimation and latency information are also available.

Several files are produced when a core is generated, and customized instantiation templates for Verilog and VHDL design flows are provided in the .veo and .vho files, respectively. For detailed instructions, see the CORE Generator software documentation.

Simulation Models

The core has a number of options for simulation models:

- VHDL behavioral model in the xilinxcorelib library
- VHDL UniSim structural model
- Verilog UniSim structural model

The models required can be selected in the CORE Generator tool project options.

Xilinx recommends that simulations utilizing UniSim-based structural models are run using a resolution of 1 ps. Some Xilinx library components require a 1 ps resolution to work properly in either functional or timing simulation. The UniSim-based structural models might produce incorrect results if simulation with a resolution other than 1 ps. See the "Register Transfer Level (RTL) Simulation Using Xilinx Libraries" section in *Synthesis and Simulation Design Guide* for more information. This document is part of the ISE® Software Manuals set available at www.xilinx.com/support/documentation/dt_ise.htm.



XCO Parameters

Table 2 defines valid entries for the XCO parameters. Parameters are not case sensitive. Default values are displayed in bold.

Xilinx strongly suggests that XCO parameters are not manually edited in the XCO file; instead, use the CORE Generator GUI to configure the core and perform range and parameter value checking.

Table 2: XCO Parameters

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|------------------------|---|
| XCO Parameter | Valid Values |
| component_name | ASCII text using characters: a to z, A to Z, 0 to 9 and '_'; starting with a letter |
| APortWidth | 8 - 63 (default value is 16) |
| HasATLAST | false, true |
| HasATUSER | false, true |
| ATUSERWidth | 1 to 256 |
| BPortWidth | 8 - 63 (default value is 16) |
| HasBTLAST | false, true |
| HasBTUSER | false, true |
| BTUSERWidth | 1 to 256 |
| MultType | Use_LUTs, Use_Mults |
| OptimizeGoal | Resources, Performance |
| FlowControl | Blocking, NonBlocking |
| OutputWidth | APortWidth+BPortWidth (default value is 32) |
| RoundMode | Truncate, Random_Rounding |
| HasCTRLTLAST | false, true |
| HasCTRLTUSER | false, true |
| CTRLTUSERWidth | 1 to 256 |
| OutTLASTBehv | Null, Pass_A_TLAST, Pass_B_TLAST, Pass_CTRL_TLAST, OR_all_TLASTs, AND_all_TLASTs |
| LatencyConfig | Automatic, Manual |
| MinimumLatency | 0 to 59 (default value and range depend on configuration of other XCO parameters) |
| ACLKEN | false, true |
| ARESETn | false, true |
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Demonstration Test Bench

When the core is generated using CORE Generator, a demonstration test bench is created. This is a simple VHDL test bench that exercises the core.

The demonstration test bench source code is one VHDL file: demo_tb/tb_<component_name>.vhd in the CORE Generator output directory. The source code is comprehensively commented.

Using the Demonstration Test Bench

The demonstration test bench instantiates the generated Complex Multiplier core. Either the behavioral model or the netlist can be simulated within the demonstration test bench.

- Behavioral model: Ensure that the CORE Generator project options are set to generate a behavioral model. After generation, this creates a behavioral model wrapper named <component_name>.vhd. Compile this file into the work library (see your simulator documentation for information on how to do this).
- Netlist: If the CORE Generator project options were set to generate a structural model, a VHDL or Verilog netlist named <component_name>.vhd or <component_name>.v was generated. If this option was not set, generate a netlist using the netgen program, for example:

```
netgen -sim -ofmt vhdl <component_name>.ngc <component_name>_netlist.vhd Compile the netlist into the work library (see your simulator documentation for more information on how to do this).
```

Compile the demonstration test bench into the work library. Then simulate the demonstration test bench. View the test bench's signals in your simulator's waveform viewer to see the operations of the test bench.

The Demonstration Test Bench in Detail

The demonstration test bench performs the following tasks:

- Instantiate the core
- Generate two input data tables containing complex sinusoids of different frequencies
- Generate a clock signal
- Drive the core's clock enable and reset input signals (if present)
- Drive the core's input signals to demonstrate core features (see below for details)
- Checks that the core's output signals obey AXI protocol rules (data values are not checked in order to keep the test bench simple)
- Provide signals showing the separate fields of AXI TDATA and TUSER signals

The demonstration test bench drives the core's input signals to demonstrate the features and modes of operation of the core. The Complex Multiplier is treated as a mixer that is combining two complex sinusoids with different but similar frequencies, but opposite sign and different amplitude. The output of the core is therefore a complex sinusoid with a frequency equal to the difference in frequencies of the inputs, that is, a much slower frequency. The input data is pre-generated and stored in data tables, and the test bench drives the core's data inputs with the sinusoid data throughout the operation of the test bench.



The demonstration test bench drives the AXI handshaking signals in different ways, split into three phases. The operations depend on whether Blocking Mode or NonBlocking Mode is selected:

- Blocking Mode:
 - Phase 1: full throughput, all TVALID and TREADY signals are tied high
 - Phase 2: apply increasing amounts of backpressure by deasserting the master channel's TREADY signal
 - Phase 3: deprive slave channel A of valid transactions at an increasing rate by deasserting its TVALID signal
- NonBlocking Mode:
 - Phase 1: full throughput, all TVALID and TREADY signals are tied high
 - Phase 2: deprive slave channel A of valid transactions at an increasing rate by deasserting its TVALID signal
 - Phase 3: deprive all slave channels of valid transactions at different rates by deasserting each of their TVALID signals

Customizing the Demonstration Test Bench

It is possible to modify the demonstration test bench to drive the core's inputs with different data or to perform different operations.

Input data is pre-generated in the create_ip_a_table and create_ip_b_table functions and stored in the IP_A_DATA and IP_B_DATA constants. New input data frames can be added by defining new functions and constants. Make sure that each input data frame is of an appropriate type, similar to the T_IP_A_TABLE and T_IP_B_TABLE array types.

All operations performed by the demonstration test bench to drive the core's inputs are done in the stimuli process. This process is comprehensively commented, to explain clearly what is being done. New input data or different ways of driving AXI handshaking signals can be added by modifying sections of this process.

The total run time of the test can be modified by changing the TEST_CYCLES constant: this controls the number of clock cycles before the simulation is stopped.

The clock frequency of the core can be modified by changing the CLOCK_PERIOD constant.



System Generator for DSP Graphical User Interface

This section describes each tab of the System Generator for DSP GUI and details the parameters that differ from the CORE Generator GUI. The Complex Multiplier core can be found in the Xilinx Blockset in the Math section. The block is called "Complex Multiplier 5.0." See the System Generator for DSP Help page for the "Complex Multiplier 5.0." block for more information on parameters not mentioned here.

Page 1

Page 1 is used to specify the complex multiplier construction, optimization options and output width in a similar way to the CORE Generator GUI. See CORE Generator Graphical User Interface.

Page 2

Page 2 is used to specify latency, output product rounding options and block control signals.

As with page 1, all controls have the same effect as controls in the CORE Generator GUI. See CORE Generator Graphical User Interface.

Implementation

This page is used only for System Generator for DSP FPGA area estimation, and has no equivalent parameters on the CORE Generator GUI.

Rounding

In a DSP system, especially if the system contains feedback, the wordlength growth through the multiplier should be offset by quantizing the results. Quantization, or reduction in wordlength, results in error, introduces quantization noise, and can introduce bias. For best results it is favorable to select a quantization method that introduces zero mean noise and minimizes noise variance. Figure 2 illustrates the quantization method used for truncation.

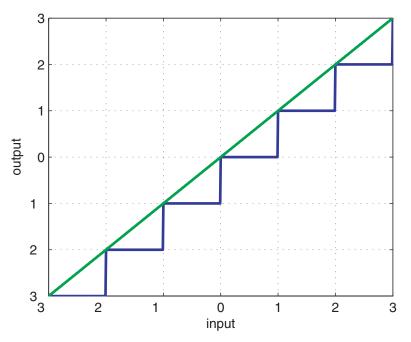


Figure 2: Truncation

For truncation the probability density function (PDF) of the noise is:

$$p(e) = \begin{cases} \frac{1}{\Delta} - \Delta < e < 0 \\ 0 & otherwise \end{cases}$$

Equation 5

therefore the mean and the variance of the error introduced are:

$$m_e = \int_{-\Delta}^{0} ep(e)de = \frac{1}{\Delta} \int_{-\Delta}^{0} ede = -\frac{\Delta}{2}$$

Equation 6

$$\sigma_e^2 = \int_0^\Delta e^2 p(e) de = \frac{1}{\Delta} \int_0^\Delta e^2 de = \frac{\Delta^2}{3}$$

Equation 7

Implementing truncation has no cost in hardware; the fractional bits are simply trimmed.

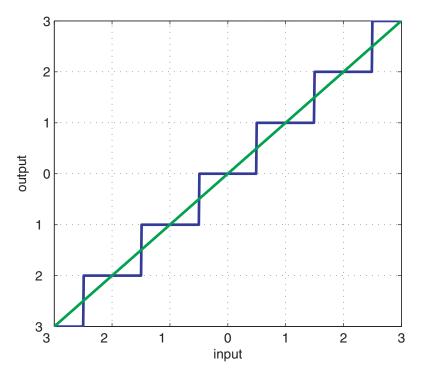


Figure 3: Rounding

For rounding the PDF of the noise is:

$$p(e) = \begin{cases} \frac{1}{\Delta} - \Delta / & 2 < e < \Delta / & 2 \\ 0 & otherwise \end{cases}$$
 Equation 8

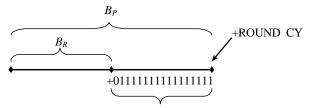
the mean and the variance of the error introduced are:

$$m_{e} = \int_{-\Delta/2}^{\Delta/2} ep(e)de = \frac{1}{\Delta} \int_{-\Delta/2}^{\Delta/2} ede = 0$$
 Equation 9

$$\sigma_{e}^{2} = \int_{-\Delta/2}^{\Delta/2} e^{2} p(e) de = \frac{1}{\Delta} \int_{-\Delta/2}^{\Delta/2} e^{2} de = \frac{\Delta^{2}}{12}$$
 Equation 10

Therefore, the ideal rounder introduces no DC bias to the signal flow. If the full product word (for example, a_rb_r - a_ib_i) is represented with B_P bits, and the actual result of the core (for example, p_r) is represented with B_R bits, then bits B_P -1... B_P - B_R are the integer part, and B_P - B_R -1..0 are the fractional part of the result.





Rounding constant (provided by the core)

Figure 4: Rounding to B_r Bits from B_p Bits

To implement the rounding function shown in Figure 3, 0.5 (represented in B_PB_P - B_R format) has to be added to the full product word, then the lower B_P - B_R bits need to be truncated. However, if the fractional part is exactly 0.5, this method always rounds up, which introduces positive bias to the computation. Also, if the rounding constant is -1 (Figure 4), 0.5 would be always rounded down, introducing negative bias.

If 0.5 is rounded using a static rule, the resulting quantization always introduces bias. To avoid bias, rounding has to be randomized. Therefore, the core adds a rounding constant, and an extra 1 should be added with ½ probability, thus dithering the exact rounding threshold. Typical round carry sources being used extensively as control signals are listed in Table 3.

Table 3: Unbiased Rounding Sources

| 0.5 Rounding Rule | Round Carry Source | |
|----------------------------|--------------------|--|
| Round towards 0 | -MSB(P) | |
| Round towards +/- infinity | MSB(P) | |
| Round towards nearest even | LSB(P) | |

Rounding of the results is not trivial when multiple, cascaded XtremeDSP slices are involved in the process, such as evaluation of Equation 9 or Equation 10. The sign of the output (MSB_0) cannot be predicted from the operands before the actual multiplications and additions take place, and would incur additional latency or resource to implement outside the XtremeDSP slices. Therefore an external signal should be used to feed the round carry input, through the $ROUND_CY$ pin.

A good candidate for a source can be a clock-dividing flip-flop, or any 50% duty cycle random signal, which is not correlated with the fractional part of the results. For predictable behavior (as for bit-true modeling) the *ROUND_CY* signal might need to be connected to a CLK independent source in the user design, such as an LSB of one of the complex multiplier inputs.

Nevertheless, even when a static rule is used (such as tying $ROUND_CY = '0'$), bias and quantization error are reduced compared to using truncation.

In many cases, for XtremeDSP slice implementation, the addition of the rounding constant is 'free', as the C port and carry-in input may be utilized. In devices without XtremeDSP slices, the addition of rounding typically requires an extra slice-based adder and an additional cycle of latency.



Hardware Implementation

Three Real Multiplier Solution

The three real multiplier implementation maps well to devices that have a pre-adder as part of the XtremeDSP slice (such as Spartan-6 and Virtex-6 FPGAs), saving slice resources.

In general, the three multiplier solution uses more slice resources (LUTs/flipflops) and have a lower maximum achievable clock frequency than the four multiplier solution.

Four Real Multiplier Solution

The four real multiplier solution makes maximum use of XtremeDSP slice resources, and has higher clock frequency performance than the three real multiplier solution, in many cases reaching the maximum clock frequency of the FPGA device.

It still consumes slice resources for pipeline balancing, but this slice cost is always less than that required by the equivalent three real multiplier solution.

LUT-based Solution

The core offers the option to build the complex multiplier using LUTs only. While this option uses a significant number of slices, achieves a lower maximum clock frequency and uses more power than XtremeDSP slice implementations, it might be suitable for applications where XtremeDSP slices are in limited supply, or where lower clock rates are in use.

The three real multiplier configuration is used exclusively when LUT implementation is selected.

AXI4-Stream Considerations

The conversion to AXI4-Stream interfaces brings standardization and enhances interoperability of Xilinx IP LogiCORE solutions. Other than general control signals such as aclk, aclken and aresetn, all inputs and outputs to the Complex Multiplier are conveyed via AXI4-Stream channels. A channel consists of TVALID and TDATA always, plus several optional ports and fields. In the Complex Multiplier, the optional ports supported are TREADY, TLAST and TUSER. Together, TVALID and TREADY perform a handshake to transfer a message, where the payload is TDATA, TUSER and TLAST. The Complex Multiplier operates on the operands contained in the TDATA fields and outputs the result in the TDATA field of the output channel. The Complex Multiplier does not use TUSER and TLAST as such, but the core provides the facility to convey these fields with the same latency as for TDATA. This facility is intended to ease use of the Complex Multiplier in a system. For example, the complex multiplier can be used as a mixer or phase shift operating on streaming packetized data. In this example, the core could be configured pass the TLAST of the packetized data channel saving the system designer the effort of constructing a bypass path for this information.

For further details on AXI4-Stream Interfaces see the Xilinx AXI Design Reference Guide (UG761) and the AMBA 4 AXI4-Stream Protocol Version: 1.0 Specification.



Basic Handshake

Figure 5 shows the transfer of data in an AXI4-Stream channel. TVALID is driven by the source (master) side of the channel and TREADY is driven by the receiver (slave). TVALID indicates that the value in the payload fields (TDATA, TUSER and TLAST) is valid. TREADY indicates that the slave is ready to receive data. When both TVALID and TREADY are true in a cycle, a transfer occurs. The master and slave set TVALID and TREADY respectively for the next transfer appropriately.

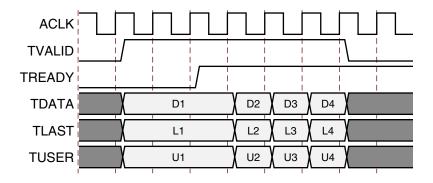


Figure 5: Data Transfer in an AXI-Stream Channel

NonBlocking Mode

The term NonBlocking means that lack of data on one input channel does not block the execution of an operation if data is received on another input channel. The full flow control of AXI4-Stream is not always required. Blocking or NonBlocking behavior is selected via the FlowControl parameter or GUI field. The Complex Multiplier core supports a NonBlocking mode in which the AXI4-Stream channels do not have TREADY, that is, they do not support back pressure. The choice of Blocking or NonBlocking applies to the whole core, not each channel individually. Channels still have the non-optional TVALID signal, which is analogous to the New Data (ND) signal on many cores prior to the adoption of AXI4-Stream. Without the facility to block dataflow, the internal implementation is much simplified, so fewer resources are required for this mode. This mode is recommended for users wishing to move to this version from a pre-AXI version with minimal change.

When all of the present input channels receive an active TVALID, an operation is validated and the output TVALID (suitably delayed by the latency of the core) is asserted to qualify the result. Operations occur on every enabled clock cycle and data is presented on the output channel payload fields regardless of TVALID. This is to allow a minimal migration from v3.1. Figure 6 shows the NonBlocking behavior for a case with latency of one cycle.

Warning: For performance, ARESETn is registered internally, which delays its action by a clock cycle. The effect of this is that any transaction input in the cycle following the de-assertion of ARESETn is reset by the action of ARESETn, resulting in an output data value of zero. TVALID is also inactive on the output channel for this cycle

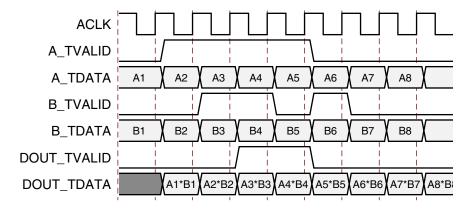


Figure 6: NonBlocking Mode

Blocking Mode

The term Blocking means that operation execution does not occur until fresh data is available on all input channels. The full flow control of AXI4-Stream aids system design because the flow of data is self-regulating. Blocking or NonBlocking behavior is selected via the FlowControl parameter or GUI field. Data loss is prevented by the presence of back-pressure (TREADY), so that data is only propagated when the downstream datapath is ready to process the data.

The Complex Multiplier has two or three input channels and one output channel. When all input channels have validated data available, an operation occurs and the result becomes available on the output. If the output is prevented from off-loading data because TREADY is low then data accumulates in the output buffer internal to the core. When this output buffer is nearly full the core stops further operations. This prevents the input buffers from off-loading data for new operations so the input buffers fills as new data is input. When the input buffers fill, their respective TREADYs are deasserted to prevent further input. This is the normal action of backpressure.

The three inputs are tied in the sense that each must receive validated data before an operation is prompted. Therefore, there is an additional Blocking mechanism, where at least one input channel does not receive validated data while others do. In this case, the validated data is stored in the input buffer of the channel. After a few cycles of this scenario, the buffer of the channel receiving data fills and TREADY for that channel is de-asserted until the starved channel receives some data. Figure 7 shows both Blocking behavior and back-pressure. The first data on channel A is paired with the first data on channel B, the second with the second and so on. This demonstrates the Blocking concept. The diagram further shows how data output is delayed not only by latency, but also by the handshake signal DOUT_TREADY. This is back-pressure' Sustained back-pressure on the output along with data availability on the inputs eventually lead to a saturation of the core's buffers, leading the core to signal that it can no longer accept further input by de-asserting the input channel TREADY signals. The minimum latency in this example is two cycles, but it should be noted that in Blocking operation latency is not a useful concept. Instead, as the diagram shows, the important idea is that each channel acts as a queue, ensuring that the first, second, third data samples on each channel are paired with the corresponding samples on the other channels for each operation.

Also note that the core buffers have a greater capacity than implied by the diagram.

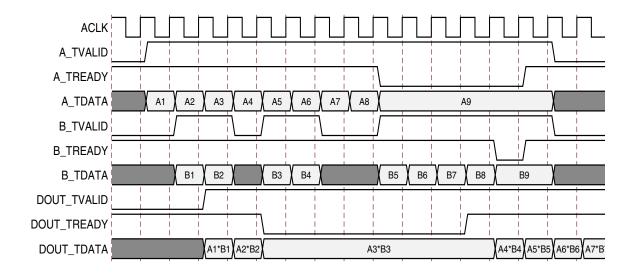


Figure 7: Blocking Mode

Note: This diagram is for illustration of the Blocking behavior and handshake protocol. Latencies implied by the diagram might not be accurate.

TDATA Packing

Fields within an AXI4-Stream interface follow a specific naming nomenclature. See Figure 8. Normally, information pertinent to the application, complex multiplication in this case, is carried in the TDATA field. In this core the complex operand components, real and imaginary, are both passed to or from the core via the channel's TDATA port, with the real component in the least significant position. To ease interoperability with byte-oriented protocols, each subfield within TDATA which could be used independently is first extended, if necessary, to fit a bit field which is a multiple of 8 bits. For example, say the complex multiplier is configured to have an A operand width of 11 bits. Each of the real and imaginary components of A are 11 bits wide. The real component would occupy bits 10 down to 0. Bits 15 down to 11 would be ignored. Bits 26 down to 16 would hold the imaginary component and bits 31 down to 27 would likewise be ignored. For the output DOUT channel, result fields are sign extended to the byte boundary. The bits added by byte orientation are ignored by the core and do not result in additional resource use.

TDATA Structure for A, B and DOUT Channels

Input ports A, B and output port DOUT carry complex data in their TDATA field. For each, the real component occupies the least significant bits. The imaginary component occupies a bit field which starts on the next byte-boundary above the real component as shown in the previous section. See Figure 8.

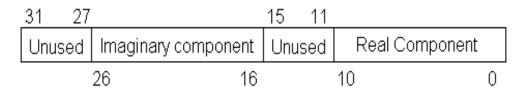


Figure 8: TDATA Structure for A, B and DOUT Channels



TDATA Structure for CTRL Channel

The CTRL channel exists only when Rounding has been selected and exists to convey only the rounding bit. This bit occupies bit 0 of TDATA for this channel. However, due to the byte-oriented nature of TDATA, this means that TDATA has a width of 8 bits.

TLAST and TUSER Handling

TLAST in AXI4-Stream is used to denote the last transfer of a block of data. TUSER is for ancillary information which qualifies or augments the primary data in TDATA. The complex multiplier operates on a per-sample basis where each operation is independent of any before or after. Because of this, there is no need for TLAST on a complex multiplier, nor is there any need for TUSER. The TLAST and TUSER signals are supported on each channel purely as an optional aid to system design for the scenario in which the data stream being passed through the complex multiplier does indeed have some packetization or ancillary field, but which is not relevant to the complex multiplier. The facility to pass TLAST and/or TUSER removes the burden of matching latency to the TDATA path, which can be variable, through the complex multiplier.

TLAST Options

TLAST for each input channel is optional. Each, when present, can be passed via the complex multiplier, or, when more than one channel has TLAST enabled, can pass a logical AND or logical OR of the TLASTs input. When no TLASTs are present on any input channel, the output channel does not have TLAST either.

TUSER Options

TUSER for each input channel is optional. Each has user-selectable width. These fields are concatenated, without any byte-orientation or padding, to form the output channel TUSER field. The TUSER field from channel A forms the least significant portion of the concatenation, then TUSER from channel B, then TUSER from channel CTRL.

Examples:

If channels A and CTRL both have TUSER with widths of 5 and 8 bits respectively, the output TUSER is a suitably delayed concatenation of A and CTRL TUSER fields, 13 bits wide, with A in the least significant 5 bit positions (4 down to 0).

If B and CTRL have TUSER widths of 4 and 10 respectively, but A has no TUSER, DOUT TUSER (m_axis_dout_tuser) has the bits of B_TUSER (s_axis_b_tuser) suitably delayed in positions 3 down to 0 with CTRL_TUSER (s_axis_ctrl_tuser) bits, suitably delayed, in positions 13 down to 4.



Migrating to Complex Multiplier v5.0 from Earlier Versions

XCO Parameter Changes

The CORE Generator core update functionality can be used to update an existing XCO file from v3.1 or v4.0 to Complex Multiplier v5.0, but it should be noted that the update mechanism alone does not create a core compatible with v3.1. See Instructions for Minimum Change Migration (v3.1 to v5.0).

While there are no parameter changes from v4.0 to v5.0 there are two changes of note. The first is that the behavior of the NonBlocking mode has changed. The second is that the minimum latency for Blocking modes has been reduced by 6 cycles. This means that for a given performance, less latency is required. Retaining the same value of manual latency as v4.0 might result in a resource increase.

Table 4 shows the changes to XCO parameters from version 3.1 to version 5.0.

Table 4: XCO Parameter Changes from v3.1 to v5.0

| Version 5.0 | Notes |
|----------------|---|
| APortWidth | Unchanged, but the parameter no longer directly indicates the width of the port carrying the A operand |
| BPortWidth | Unchanged, but the parameter no longer directly indicates the width of the port carrying the B operand |
| MultType | Unchanged |
| OptimizeGoal | Unchanged |
| OutputWidth | Note 1 |
| | |
| RoundMode | Unchanged |
| LatencyConfig | Latency = -1 is now LatencyConfig = Automatic. All other values map to LatencyConfig = Manual |
| MinimumLatency | This field allows the input of Latency when LatencyConfig=Manual, or reflects the actual value of MinimumLatency when LatencyConfig=Automatic |
| ACLKEN | Renamed only |
| ARESETn | Renamed only. Note that while the sense of the aresetn signal has changed, this XCO determined whether or not the signal exists and has not changed. Note also that a minimum length of 2 cycles is recommended when aresetn is asserted. |
| | Deprecated. aresetn always overrides aclken in accordance with AXI4-Stream protocol. |
| HasATLAST | Introduced in version 4.0 |
| HasATUSER | Introduced in version 4.0 |
| ATUSERWidth | Introduced in version 4.0 |
| HasBTLAST | Introduced in version 4.0 |
| HasBTUSER | Introduced in version 4.0 |
| BTUSERWidth | Introduced in version 4.0 |
| HasCTRLTLAST | Introduced in version 4.0 |
| HasCTRLTUSER | Introduced in version 4.0 |
| CTRLTUSERWidth | Introduced in version 4.0 |
| FlowControl | Introduced in version 4.0 |
| | APortWidth BPortWidth MultType OptimizeGoal OutputWidth RoundMode LatencyConfig MinimumLatency ACLKEN ARESETn HasATLAST HasATUSER ATUSERWidth HasBTLAST HasBTUSER BTUSERWidth HasCTRLTLAST HasCTRLTUSER CTRLTUSERWidth |



Table 4: XCO Parameter Changes from v3.1 to v5.0

| Version 3.1 | Version 5.0 | Notes |
|-------------|--------------|---------------------------|
| | OutTLASTBehv | Introduced in version 4.0 |

Notes

For more information on this upgrade feature, see the CORE Generator software documentation.

Port Changes

Table 5 details the changes to port naming, additional or deprecated ports and polarity changes from v3.1 to v5.0 There are no changes from v4.0 to 5.0.

Table 5: Port Changes from Version 3.1 to Version 5.0

| Version 5.0 | Notes | | |
|--|---|--|--|
| aclk | Rename only | | |
| aclken | Rename only | | |
| aresetn | Rename and change of sense (now active low). Note recommendation that aresetn should be asserted for a minimum of 2 cycles. | | |
| s_axis_a_tdata(N-1:0) | Both AR and AI map to s_axis_a_tdata | | |
| s_axis_a_tdata(N-1+byte(N):byte(N)) | byte(N) is to round N up to the next multiple of 8. | | |
| s_axis_b_tdata(M-1:0) | Both BR and BI map to s_axis_b_tdata | | |
| s_axis_b_tdata(M-1+byte(M):byte(M)) | byte(M) is to round M up to the next multiple of 8. | | |
| s_axis_ctrl_tdata(0) | | | |
| m_axis_dout_tdata(S-1:0) | Both PR and PI map to m_axis_dout_tdata | | |
| m_axis_dout_tdata(S-1+byte(S):byte(S)) | byte(S) is to round S up to the next multiple of 8. | | |
| | | | |
| s_axis_a_tvalid | TVALID (AXI4-Stream channel handshake signal) for each | | |
| s_axis_b_tvalid | channel | | |
| s_axis_ctrl_tvalid | | | |
| m_axis_dout_tvalid | | | |
| s_axis_a_tready | TREADY (AXI4-Stream channel handshake signal) for each | | |
| s_axis_b_tready | channel. | | |
| s_axis_ctrl_tready | | | |
| m_axis_dout_tready | | | |
| s_axis_a_tlast | TLAST (AXI4-Stream packet signal indicating the last transfer | | |
| s_axis_b_tlast | of a data structure) for each channel. The complex multiplier does not use TLAST, but provides the facility to pass TLAST | | |
| s_axis_ctrl_tlast | with the same latency as TDATA. | | |
| m_axis_dout_tlast | | | |
| | aclk aclken aresetn s_axis_a_tdata(N-1:0) s_axis_a_tdata(N-1+byte(N):byte(N)) s_axis_b_tdata(M-1:0) s_axis_b_tdata(M-1+byte(M):byte(M)) s_axis_b_tdata(O) m_axis_dout_tdata(S-1:0) m_axis_dout_tdata(S-1+byte(S):byte(S)) s_axis_a_tvalid s_axis_b_tvalid s_axis_ctrl_tvalid m_axis_dout_tvalid s_axis_a_tready s_axis_a_tready s_axis_b_tready m_axis_dout_tready m_axis_dout_tready s_axis_b_tlast s_axis_b_tlast s_axis_ctrl_tlast | | |

^{1.} The natural output width of a complex multiplication is APortWidth+BPortWidth+1. When OutputWidth is set to be less than this, the most significant bits of the result are those output. The remaining bits are either truncated or rounded according to RoundMode. In other words OutputWidthHigh has been deprecated and is now fixed at (APortWidth +BPortWidth).



Table 5: Port Changes from Version 3.1 to Version 5.0 (Cont'd)

| Version 3.1 | Version 5.0 | Notes |
|-------------|---|--|
| | s_axis_a_tuser(E-1:0) ⁽⁴⁾ | TUSER (AXI4-Stream ancillary field for application-specific |
| | s_axis_b_tuser(F-1:0) ⁽⁵⁾ | information) for each channel. The complex multiplier does not use TUSER, but provides the facility to pass TUSER with the |
| | s_axis_ctrl_tuser(G-1:0) ⁽⁶⁾ | same latency as TDATA. |
| | m_axis_dout_tuser(H-1:0) ⁽⁷⁾ | |

Notes:

- N is APortWidth
 M is BPortWidth
 S is OutputWidth
 E is ATUSERWidth
 F is BTUSERWidth
 G is CTRLTUSERWidth
- H is calculated from the input channel TUSERWidth and HASTUSER parameters.



Latency Changes

The latency of Complex Multiplier v5.0 is different compared to v3.1 for AXI Blocking mode. The update process cannot account for this and guarantee equivalent performance. Latency is the same as v3.1 in v5.0 for AXI NonBlocking mode.

The latency of AXI NonBlocking mode is reduced by 1 from v4.0 going to v5.0 except for the case of zero latency which is still zero in v5.0. The latency of AXI Blocking mode from v4.0 to v5.0 is reduced by 6 cycles.

Importantly, when in Blocking Mode, the latency of the core is variable, so only the minimum possible latency can be determined.

Instructions for Minimum Change Migration (v3.1 to v5.0)

To configure the Complex Multiplier v5.0 to most closely mimic the behavior of v3.1 the translation is as follows:

Parameters - Set FlowControl to NonBlocking and OutputWidth to APortWidth+BPortWidth+1-OutputWidthLow. All other new parameters default to false and can be ignored. If OutputWidthHigh was previously set to other than APortWidth+BPortWidth then translation is not directly possible, but the (APortWidth+BPortWidth-OutputWidthHigh) most significant bits of the output can be ignored.

Ports - Rename and map signals as detailed in Port Changes previously. Tie all TVALID signals on input channels (A, B, CTRL) to '1'.

Performance and resource use are mostly unchanged versus v3.1 other than small changes due to the use of a different version of ISE tools.

Instructions for Minimum Change Migration (v4.0 to v5.0)

For AXI Blocking Mode minimum latency is reduced by 6 cycles. The resource cost of Blocking mode is also reduced versus v4.0. This saving is proportional to the total number of input bits. NonBlocking behaviour has also been changed relative to v4.0 to further reduce the resource cost of moving to AXI from pre-axi versions such as v3.1. Latency in v5.0 is one cycle less than for v4.0 in NonBlocking mode except for the zero latency case, which is still zero.

Performance and Resource Usage

Table 6 through Table 7 provide performance and resource usage information for a number of different core configurations.

The maximum clock frequency results were obtained by double-registering input and output ports to reduce dependence on I/O placement. The inner level of registers used a separate clock signal to measure the path from the input registers to the first output register through the core.

The resource usage results do not include the preceding "characterization" registers and represent the true logic used by the core to implement a single Complex Multiplier. LUT counts include SRL32s and LUTs used as route-throughs.

The map options used were: "map -ol high"

The par options used were: "par -ol high"

Clock frequency does not take clock jitter into account and should be derated by an amount appropriate to the clock source jitter specification.

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The Virtex-6 FPGA test cases in Table 6 used an XC6VLX75T-FF784 (-1 speed grade) device and ISE software speed file version "PRODUCTION 1.11d 2010-11-17."

Table 6: Virtex-6 FPGA Performance and Resource Usage

| Complex Multiplier Configuration | Maximum Clock Frequency (MHz) | LUT/FF Pairs | LUT6s | FFs | XtremeDSP Slices |
|---|-------------------------------------|--------------|-------|------|---------------------|
| 16x16 Use Mults Resources, NonBlocking | 452 | 66 | 50 | 114 | 3 |
| 16x16 Use Mults Resources, Blocking | 452 | 219 | 131 | 320 | 3 |
| 16x16 Use Mults Resources, Blocking, with 32 bit TUSER and TLAST | 452 | 355 | 227 | 485 | 3 |
| 16x16 Use Mults Resources, NonBlocking, Truncated | 452 | 62 | 54 | 114 | 3 |
| 16x16 Use Mults Resources, NonBlocking, Rounded (has CTRL channel) | 452 | 67 | 51 | 116 | 3 |
| 16x16 Use Mults Performance | 452 | 2 | 2 | 2 | 4 |
| 16x16 Use LUTs Resources | 388 | 1089 | 1043 | 1080 | 0 |
| 32x16 Use Mults Resources | 452 | 300 | 214 | 477 | 6 |
| 32x16 Use Mults Performance | 452 | 79 | 55 | 132 | 8 |
| 32x16 Use LUTs Resources | 353 | 2068 | 2011 | 2093 | 0 |
| 32x32 Use Mults Resources | 339 | 867 | 636 | 1197 | 12 |
| 32x32 Use Mults Performance | 452 | 430 | 344 | 772 | 16 |
| 32x32 Use LUTs Resources | 318 | 3780 | 3724 | 3694 | 0 |



The Spartan-6 FPGA test cases in Table 7 used an XC6SLX45T-FGG484 (-2 speed grade) device and ISE software speed file version "PRODUCTION 1.13b 2010-11-17."

Table 7: Spartan-6 FPGA Performance and Resource Usage

| Complex Multiplier Configuration | Maximum Clock Frequency (MHz) | LUT/FF Pairs | LUT6s | FFs | XtremeDSP Slices |
|--|-------------------------------------|--------------|-------|------|---------------------|
| 16x16 Use Mults Resources, NonBlocking | 251 | 66 | 66 | 130 | 3 |
| 16x16 Use Mults Resources, Blocking | 244 | 211 | 155 | 336 | 3 |
| 16x16 Use Mults Resources, Blocking, with 32 bit TUSER and TLAST | 228 | 331 | 201 | 501 | 3 |
| 16x16 Use Mults Performance | 251 | 2 | 2 | 2 | 4 |
| 16x16 Use LUTs Resources | 212 | 1085 | 1034 | 1066 | 0 |
| 32x16 Use Mults Resources | 180 | 405 | 309 | 657 | 6 |
| 32x16 Use Mults Performance | 251 | 146 | 98 | 242 | 8 |
| 32x16 Use LUTs Resources | 188 | 2062 | 1970 | 2125 | 0 |
| 32x32 Use Mults Resources | 188 | 1131 | 931 | 1836 | 12 |
| 32x32 Use Mults Performance | 251 | 603 | 431 | 1032 | 16 |
| 32x32 Use LUTs Resources | 156 | 3942 | 3695 | 3927 | 0 |



Support

Xilinx provides technical support for this LogiCORE IP product when used as described in the product documentation. Xilinx cannot guarantee timing, functionality, or support of product if implemented in devices that are not defined in the documentation, if customized beyond that allowed in the product documentation, or if changes are made to any section of the design labeled *DO NOT MODIFY*.

See the IP Release Notes Guide (XTP025) for further information on this core.

For each core, there is a master Answer Record that contains the Release Notes and Known Issues list for the core being used. The following information is listed for each version of the core:

- New Features
- Bug Fixes
- Known Issues

Ordering Information

This LogiCORE IP module is included at no additional cost with the Xilinx ISE Design Suite software and is provided under the terms of the Xilinx End User License Agreement. Use the CORE Generator software included with the ISE Design Suite to generate the core. For more information, see the core page.

Contact your local Xilinx <u>sales representative</u> for pricing and availability of additional Xilinx LogiCORE modules and software. Information about additional Xilinx LogiCORE modules is available on the Xilinx <u>IP Center</u>.

References

- 1. IP Release Notes Guide (XTP025)
- Xilinx AXI Reference Guide (UG761) available at www.xilinx.com/support/ip_documentation/ug761_axi_reference_guide.pdf.
- 3. AMBA 4 AXI4-Stream Protocol Version: 1.0 Specification
- 4. Synthesis and Simulation Design Guide



List of Acronyms

| Acronym | Spelled Out |
|---------|---|
| AXI | Advanced eXtensible Interface |
| DC | Direct Current |
| DSP | Digital Signal Processing |
| FF | Flip-Flop |
| FPGA | Field Programmable Gate Array |
| GUI | Graphical User Interface |
| I/O | Input/Output |
| IP | Intellectual Property |
| ISE | Integrated Software Environment |
| LUT | Lookup Table |
| MHz | Mega Hertz |
| ND | New Data |
| PDF | Probability Density Function |
| RTL | Register Transfer Level |
| SRL | Shift Register LUT |
| VHDL | VHSIC Hardware Description Language (VHSIC an acronym for Very High-Speed Integrated Circuits) |
| XCO | Xilinx CORE Generator core source file |
| XST | Xilinx Synthesis Technology |

Revision History

| Date | Version | Description of Revisions | |
|----------|---------|--|--|
| 09/21/10 | 1.0 | First release of the core with AXI interface support. The previous release of this document was ds291. | |
| 03/01/11 | 2.0 | Second release of core with revisited AXI support. Support added for Virtex-7 and Kintex-7. ISE Design Suite 13.1. | |

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