

CS 403: Types and Classes

Stefan D. Bruda

Fall 2021



- Algorithms + data structures = programs
- Abstractions of data entities highly desirable
- Program semantics embedded in data types
- Data types enable semantic checking
- Data types can enhance design
- Data types can determine memory layout and allocation
- Issues:
 - Extent to which type information is represented in program
 - How types are constructed
 - ~~How types are checked (done)~~
 - ~~When types are checked (done)~~



- Algorithms + data structures = programs
- Abstractions of data entities highly desirable
- Program semantics embedded in data types
- Data types enable semantic checking
- Data types can enhance design
- Data types can determine memory layout and allocation
- Issues:
 - Extent to which type information is represented in program
 - How types are constructed
 - ~~How types are checked (done)~~
 - ~~When types are checked (done)~~
- Data type = set of values + operations on those values
 - A data type is an algebra
 - Set of values defined by enumeration, subrange, or mathematical construction
 - Set model with membership concept (\in)
 - Set model of types means language type constructor equivalents for the set operations \in , \subset , \cup , \times



- Determining types

- **Explicit typing** → type determined at declaration, usually invariant throughout execution (Pascal, C, C++, Java)
- **Implicit typing** → type determined by usage (Prolog, Lisp)
- **Mixed** → implicit typing by default, but allows explicit declarations (Miranda, Haskell, ML)



- Determining types

- **Explicit typing** → type determined at declaration, usually invariant throughout execution (Pascal, C, C++, Java)
- **Implicit typing** → type determined by usage (Prolog, Lisp)
- **Mixed** → implicit typing by default, but allows explicit declarations (Miranda, Haskell, ML)

- Simple types

- **Pre-defined** (int, bool, etc.)
- **Enumeration**

```
enum colour {red, green, blue};  
data Colour = Red | Green | Blue
```
- **Ordinal** (discrete order on elements i.e., not real)



- Determining types

- **Explicit typing** → type determined at declaration, usually invariant throughout execution (Pascal, C, C++, Java)
- **Implicit typing** → type determined by usage (Prolog, Lisp)
- **Mixed** → implicit typing by default, but allows explicit declarations (Miranda, Haskell, ML)

- Simple types

- **Pre-defined** (int, bool, etc.)
- **Enumeration**

```
enum colour {red, green, blue};  
data Colour = Red | Green | Blue
```
- **Ordinal** (discrete order on elements i.e., not real)

- Type constructors: cartesian product

- $U \times V = \{(u, v) : u \in U, v \in V\}; p_1 : U \times V \rightarrow U; p_2 : U \times V \rightarrow V$
- **Record implementation**

```
struct icr {int i; char c; double r;};
```
- **Tuple implementation**

```
type Icr = (Int, Char, Double)
```



- Type constructors: union

- **Undiscriminated unions** → uses names to distinguish components
`union intOrReal {int i; double r};`
- **Direct algebraic definition** `data Either a b = Left a | Right b`



DATA TYPES (CONT'D)

- Type constructors: union

- **Undiscriminated unions** → uses names to distinguish components
`union intOrReal {int i; double r};`
- **Direct algebraic definition** `data Either a b = Left a | Right b`

- Type constructors: function types $U \rightarrow V$

- **Array types** → `A[i]` is a mapping from `int` to the type of the array
- Issues regarding the type of the index:
 - Restrict to `int`? (e.g., C)
 - Restrict to subrange? (e.g., Pascal)
 - Allow any ordinal type? (e.g., Perl)
 - Is the index part of the type?

- **Function types**

```
typedef int (*fun) (int, int)
Int -> Int -> Int
```




- Type constructors: union

- **Undiscriminated unions** → uses names to distinguish components
 - `union intOrReal {int i; double r};`
- **Direct algebraic definition** `data Either a b = Left a | Right b`

- Type constructors: function types $U \rightarrow V$

- **Array types** → `A[i]` is a mapping from `int` to the type of the array
- Issues regarding the type of the index:
 - Restrict to `int`? (e.g., C)
 - Restrict to subrange? (e.g., Pascal)
 - Allow any ordinal type? (e.g., Perl)
 - Is the index part of the type?

- **Function types**

```
typedef int (*fun) (int, int)
Int -> Int -> Int
```

- Type constructors: recursive types

- **Least fixed point:** $\emptyset \cup \text{int} \cup \text{int} \times \text{int} \cup \text{int} \times \text{int} \times \text{int} \cup \dots$
- `struct intList {int key; intList next};` **not legal in C++** (infinite recursion with no base case)
 - Faked in C++: `struct intList {int key; intList *next};`
- `data IntList = Nil | Cons Int IntList`



- Advantages of implicit typing:
 - Smaller code
 - Can use explicit types if desired/needed
 - Construction of a **most general type** → **polymorphism**
- Polymorphic data structures require **explicit polymorphism**
- Example: To avoid separate definitions for `IntStack`, `CharStack`, `StringStack`, etc., introduce a mechanism to parameterise the data type declaration
 - **C++:**

```
template <typename T> struct StackNode {  
    T data;  
    StackNode<T> *next;  
};  
template <typename T> struct Stack {  
    StackNode<T> *theStack;  
};
```
 - **Haskell:**

```
data Stack a = EmptyStack | StackNode a (Stack a)
```



- Why data abstraction?
 - Easier to think about → hide what doesn't matter
 - Protection → prevent access to things you shouldn't see
 - Plug compatibility
 - Replacement of pieces often without recompilation, definitely without rewriting libraries
 - Division of labor in software projects
- An **abstract data type** specifies the allowed operations and consistency constraints for some type **without** specifying an actual implementation
- An abstract data type can be specified as an algebra of operations on entities
- An algebraic specification of a data type consists of signatures of available operations, and axioms defining behaviour
 - Algebraic types (implicitly) parameterized
 - Operations divided into constructors and inspectors
 - Axioms contain rules for each combination of constructor and inspector
 - Existence of error operations (or restrictions)



ADT *Stack*

type *Stack*(*Elm*)

Operators:

empty : $\emptyset \rightarrow \text{Stack}$

push : $\text{Elm} \times \text{Stack} \rightarrow \text{Stack}$

pop : $\text{Stack} \rightarrow \text{Stack}$

top : $\text{Stack} \rightarrow \text{Elm}$

isEmpty : $\text{Stack} \rightarrow \text{Bool}$

Axioms:

$\text{pop}(\text{push}(e, S)) = S$

$\text{top}(\text{push}(e, S)) = e$

$\text{isEmpty}(\text{empty}) = \text{true}$

$\text{isEmpty}(\text{push}(e, S)) = \text{false}$

Restrictions:

$\text{pop}(\text{empty})$

$\text{top}(\text{empty})$

Haskell implementation

```
-- Stack.hs
```

```
module Stack (Stack, empty, push, pop,
              top, isEmpty) where
```

```
data Stack a = Empty | Push a (Stack a)
              deriving Show
```

```
empty :: Stack a
```

```
push :: a -> Stack a -> Stack a
```

```
pop :: Stack a -> Stack a
```

```
top :: Stack a -> a
```

```
isEmpty :: Stack a -> Bool
```

```
empty = Empty
```

```
push a s = Push a s
```

```
pop (Push e s) = s
```

```
pop (Empty) = error "pop (empty)."
```

```
top (Push e s) = e
```

```
top (Empty) = error "top (empty)"
```

```
isEmpty (Push e s) = False
```

```
isEmpty Empty = True
```





```
-- main.hs
module Main where
import Stack

aStack = push 0 (push 1 (push 2 empty))
```

```
Main> aStack
Push 0 (Push 1 (Push 2 Empty))
Main> :type aStack
aStack :: Stack Integer
Main> isEmpty aStack
False
Main> pop aStack
Push 1 (Push 2 Empty)
Main> let aStack = push 0 empty in pop (pop aStack)
```

```
Program error: pop (empty)
```

```
Main>
```



```
-- Stack.hs
module Stack where
data Stack a = Empty |
    Push a (Stack a)
    deriving Show

pop :: Stack a -> Stack a
top :: Stack a -> a
isEmpty :: Stack a -> Bool

pop (Push e s) = s
pop (Empty) = error "pop (empty)."
top (Push e s) = e
top (Empty) = error "top (empty)"
isEmpty (Push e s) = False
isEmpty Empty = True
```

```
-- main.hs
module Main where
import Stack
```

```
Main> aStack
Push 0 (Push 1 (Push 2 Empty))
Main> :r
Main> aStack
Push 0 (Push 1 (Push 2 Empty))
Main> :type aStack
aStack :: Stack Integer
Main> isEmpty aStack
False
Main> pop aStack
Push 1 (Push 2 Empty)
Main> let aStack = Push 0 Empty
    in pop (pop aStack)

Program error: pop (empty).
```



type *Queue*(*Elm*)

Operators:

create : $\emptyset \rightarrow \text{Queue}$

enqueue : $\text{Elm} \times \text{Queue} \rightarrow \text{Queue}$

dequeue : $\text{Queue} \rightarrow \text{Queue}$

front : $\text{Queue} \rightarrow \text{Elm}$

isEmpty : $\text{Queue} \rightarrow \text{Bool}$

Axioms:

front(*enqueue*(*e*, *Q*)) = if (*isEmpty*(*Q*)) then *e* else *front*(*Q*)

dequeue(*enqueue*(*e*, *Q*)) = if (*isEmpty*(*Q*)) then *Q*
else *enqueue*(*e*, *dequeue*(*Q*))

isEmpty(*create*) = *true*

isEmpty(*enqueue*(*e*, *Q*)) = *false*

Restrictions:

dequeue(*empty*)

front(*empty*)





type *Complex*

Operators:

create : $Real \times Real \rightarrow Complex$

real : $Complex \rightarrow Real$

imaginary : $Complex \rightarrow Real$

$+$: $Complex \times Complex \rightarrow Complex$

\times : $Complex \times Complex \rightarrow Complex$

...

Axioms:

$real(create(r, i)) = r$

$imaginary(create(r, i)) = i$

$real(x + y) = real(x) + real(y)$

$imaginary(x + y) = imaginary(x) + imaginary(y)$

$real(x \times y) = real(x) \times real(y) - imaginary(x) \times imaginary(y)$

$imaginary(x \times y) = imaginary(x) \times real(y) + real(x) \times imaginary(y)$

...





- ❶ Problem: Early binding of ADT interface to implementation
 - Can have only one implementation of any given ADT
 - Solution: dynamic binding
 - `stack.pop()` selects the right function at run time depending on the specific implementation being used
 - caller needs not know what implementation is used



❶ Problem: Early binding of ADT interface to implementation

- Can have only one implementation of any given ADT
- **Solution:** dynamic binding
 - `stack.pop()` selects the right function at run time depending on the specific implementation being used
 - caller needs not know what implementation is used

❷ Problem: Related ADTs are different ADTs

- Example: `draw()`, `moveTo(x,y)` applicable to several graphical object ADTs (Square, Circle, Line, etc.)
 - Cumbersome code for drawing a list of objects of different types

```
case obj.tag is
  when t_square => Square.draw(obj.s);
  when t_circle => Circle.draw(obj.s);
  when t_line   => Line.draw(obj.s);
end case;
```
 - Unmaintainable code (what if we later add the Rectangle ADT?)
- **Solution:** dynamic binding and subtyping
 - automatically select the right draw function for object depending on its type



- ③ Problem: Why reimplement every ADT from scratch
 - ADT are often related, with substantial overlapping in implementation
 - Solution: inheritance
 - Define an ADT as a variant of another ADT and specify only the differences: “FilledSquare is like Square, except . . .”
 - Differential programming



- ③ Problem: Why reimplement every ADT from scratch
 - ADT are often related, with substantial overlapping in implementation
 - Solution: inheritance
 - Define an ADT as a variant of another ADT and specify only the differences: "FilledSquare is like Square, except ..."
 - Differential programming
- ADT + Dynamic binding + inheritance = object-oriented programming (OOP)
 - OOP can be added to an existing language (C++ added over C, CLOS added over Lisp)
 - Languages can support OOP but have the same structure and appearance of imperative languages (Eiffel, Java)
 - OOP can be integral part of the language yet a subset of the complete language (type classes in Haskell)
 - Pure OOP languages (Smalltalk)



- A **class** is an ADT defining
 - Format of object (instance variables = "fields")
 - Operations on objects (methods = functions)
 - Operations for creating new objects
- **Objects** are instances of a class
- A class may **inherit** all operations of another class, needs to override only those that it wants to change
 - In the simplest case, a class inherits all of the entities of its parents
- A class that inherits is a **derived class** or **subclass**
- The class from which another class inherits is the **parent class** or **superclass**
- Subprograms that define operations on objects are called **methods** or **member functions**
- The entire collection of methods of an object is called its **message protocol** or **message interface**
- Messages have two parts - a method name and the destination object (often called **receiver**)
- **Dynamic dispatch**: call specifies operation name (not implementation), system selects appropriate implementation (function) at runtime



```
class GraphicalObject {
    private int x, y;
    public void draw() { ... }
    public void moveTo(int x, int y) { ... }
}

class line extends GraphicalObject {
    public void draw() { ... }
}
```

```
GraphicalObject obj;
Line line;
... // initialization, etc.
```

```
obj.draw();           // dynamic dispatch
line.draw();          // dynamic dispatch
line.moveTo(0, 0);    // inheritance
obj = line;           // ok
line = obj;           // not ok -- why?
```



- OO implements **subtype polymorphism**
 - **Static type** of obj: GraphicalObject
 - **Dynamic type** of obj: the static type of any subtype (**actual type**)
- A **polymorphic variable** references objects of the class as declared as well as objects of any of its descendants
 - When a class hierarchy includes classes that override methods and such methods are called through a polymorphic variable, the binding to the correct method must be dynamic
 - This polymorphism simplifies the addition of new methods
- More polymorphic mechanisms:
 - A **virtual** or **abstract method** does not include a definition (only defines a protocol)
 - A **virtual** or **abstract class** is one that includes at least one virtual method
 - A virtual or abstract class cannot be instantiated
 - Extreme virtual classes: interfaces (Java), pure virtual classes (C++)



- Single and multiple inheritance
- Allocation and deallocation of objects
- Dynamic and static binding
- Multiple levels of hiding
- The exclusivity of objects
- Are subclasses subtypes?
- Implementation and interface inheritance



Multiple inheritance inherits from more than one class

Creates problems

- Conflicting definitions (e.g., two or more superclasses define a print method)
- **Repeated inheritance**: same class inherited more than once
 - If A is multiply inherited, should A's instance variables be repeated or not?
 - It depends: not allowed, can choose per field (Eiffel), can choose per class (C++)
 - Usefulness of multiple inheritance is not universally accepted
 - Smalltalk, Beta: single inheritance only
 - Java: single inheritance of classes but multiple inheritance of interfaces
 - C++, Eiffel: multiple inheritance



- Where are objects allocated?
 - Normal allocation for the language (stack + heap) or heap only
 - If they all live on the heap then references to them are uniform
- Is deallocation explicit or implicit?
 - Implicit: overhead (about 10%) and nondeterminism in running time
 - Explicit: no overhead, deterministic
 - Errors (as much as 40% of debugging time)
 - Whose responsibility to deallocate?



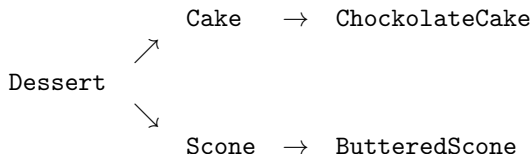
- Should all binding of messages to methods be dynamic?
- If dynamic binding is not allowed then one loses the advantages of dynamic binding
- If all are then the code is inefficient
 - C++ default is static but can use virtual functions to get dynamic binding
 - Java and Eiffel default is dynamic binding (except for final methods in Java)



- **Everything is an object**
 - Advantage: elegance, purity, least surprise (everything works in the same way)
 - Disadvantage: potential slow operations on simple objects (e.g., float)
 - However all modern languages where everything is an object have implementation tricks that minimize the overhead
 - Notable examples: C++, Haskell
- Include an **imperative-style typing system for primitive types**, but make everything else objects
 - Advantage: fast operations on simple objects, relatively small typing system
 - Disadvantage: confusion caused by the existence of two separate type systems
 - Can also have class wrappers for primitive types (such as Integer, Float, Character, etc. in Java)
 - Single mainstream example: Java



- Does an **is-a** relationship hold between a parent class object and an object of the subclass?
 - If so, then a variable of the derived type could appear anywhere that a variable of the parent type is requested
- Characteristics of a subclass that guarantees it is a subtype:
 - Can only add variables and methods, or redefine existing methods in a compatible way
- If the subclass hides some of the parent's variables and functions or modifies them in an incompatible way, then it does not create a subtype
- So what is a compatible way?
 - By imposing some restrictions on the use of inheritance, the language can ensure substitutability
 - **Type extension**: If the subclass is allowed to only extend the parent class, then substitutability is guaranteed (we have subtypes)
 - The subclass does not modify and does not hide any method
 - **Overriding Methods**: The redefined method(s)
 - must have the same number of parameters
 - must not enforce any more requirements on the input parameters
 - may require stronger requirements on the result

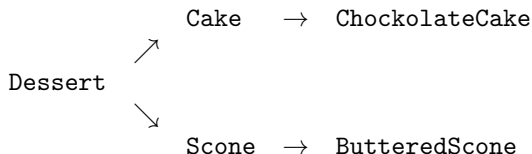


Definitions

- 1 `Feast(Dessert d, Scone s) { ... }`
- 2 `Feast(Cake c, Dessert d) { ... }`
- 3 `Feast(ChockolateCake cc, Scone s) { ... }`

Usage

- `Feast(dessertref, sconeref)`
- `Feast(chockolatecakeref, dessertref)`
- `Feast(chockolatecakeref, butteredsconeref)`



Definitions

- 1 `Feast(Dessert d, Scone s) { ... }`
- 2 `Feast(Cake c, Dessert d) { ... }`
- 3 `Feast(ChockolateCake cc, Scone s) { ... }`

Usage

- `Feast(dessertref, sconeref) → uses definition 1`
- `Feast(chockolatecakeref, dessertref) → uses definition 2`
- `Feast(chockolatecakeref, butteredsconeref) → uses definition 3`



- **Contravariance** for input parameters: the input parameters of the subclass method must be supertypes of the corresponding parameters of the overridden method
- **Covariance** on the result: the result of the redefined method must be a subtype of the result of the overridden method
- Very few languages enforce both rules
 - C++, Java, Object Pascal and Modula-3 require exact identity of the two methods
 - Eiffel and Ada require covariance of both the input and result parameters



- **Subclass** = inheritance
 - Code reuse
 - Relationship between implementations
- **Subtype** = polymorphic code
 - Organization of related concepts
 - Relationship between types/interfaces
- Two different concepts but many languages unify them
 - Notable exception: **Java**
 - Class hierarchy (single inheritance, class B extends class A)
 - Interface hierarchy (multiple subtyping)
- **Abstract (deferred) classes** = classes with incomplete implementation
 - Cannot be instantiated
 - Provide partial implementation with “holes” that are filled in by subclasses
 - Pure virtual functions in C++
- Polymorphism may require dynamic type checking
 - Dynamic type checking is costly and delays error detection
 - But, if overriding methods are restricted to having the same type then the type checking can be static (provided there is no change in visibility in subclasses)
 - Example: C++ public inheritance



```
class Printable {  
    void print() { /* default implementation */ } }  
class Person extends Printable {  
    void print() { /* overriding method */ } }
```

```
interface Printable { void print() }  
class Person implements Printable {  
    void print() { /* body of method */ }}
```

- With Printable as a class:
 - Actual parameter must be a subclass
 - Must inherit the implementation of Printable
 - Specify both interface and implementation
- With Printable as an interface:
 - Actual parameter must be an instance of a class that implements the Printable interface
 - Specifies only interface
 - Fewer constraints (more reusable)