

# Package ‘zernike’

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**Author** M.L. Peck <mpeck1@ix.netcom.com>

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**Description** Routines for Manipulation of Zernike polynomials and Interferogram fringe analysis

**Maintainer** M.L. Peck <mlpeck54@gmail.com>

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addfit	<i>Add zernike coefficients to a matrix.</i>
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### **Description**

Add zernike coefficients to a matrix.

### **Usage**

```
addfit(..., th = 0, zcm = NULL, theta = numeric(0))
```

**Arguments**

...	One or more fits as from <code>psifit</code> , etc.
th	Rotation angles, in degrees
zcm	The matrix to be added to (defaults to NULL)
theta	The vector of rotation angles to be added to

**Author(s)**

M.L. Peck

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aiapsi

---

*Iterative algorithms for PSI with unknown phase shifts*


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**Description**

Three iterative algorithms for PSI with unknown phase shifts.

**Usage**

```
aiapsi(im.mat, phases, ptol = 0.001, maxiter=20, trace=1)
aiapsiC(im.mat, phases_init, ptol, maxiter, trace)
hkpsi(im.mat, phases, maxiter = 20, ptol = 0.001,
      trace = 1, plotprogress = TRUE)
tiltpsi(im.mat, phases, coords, ptol = 0.01, maxiter = 20, trace = 1)
tiltpsiC(im.mat, phases, coords, ptol, maxiter, trace)
```

**Arguments**

im.mat	a <i>matrix</i> of interferogram values
phases	Starting guess for phase shifts
ptol	Convergence criterion for phase shifts
maxiter	Maximum number of iterations
trace	Boolean: Print some summary data at each iteration.
plotprogress	Plot some summary data for each iteration? Also, for <code>tiltpsi</code> and <code>tiltpsiC</code>
coords	Low order Zernike polynomial matrix

**Details**

The “variable tilt” algorithm now allows an indefinite number of low order Zernike terms to be variable between phase steps. `coords` can be created with `zpm` setting `maxorder` to a small value, say 4, discarding the first (dc) column and retaining as many as desired. There must be at least two columns for tilts. The third will be defocus, the next two astigmatism, the next two primary coma, ...

`aiapsi` and `tiltpsi` are wrappers for the calls to the C++ code in `aiapsiC` and `tiltpsiC` with sensible defaults for `ptol`, `maxiter`, and `trace`.

**Value**

A list containing the following elements:

phi	The wrapped phase estimate. This is a vector as long as the number of rows in im.mat.
mod	Modulation estimate.
phases	Phase shift estimates.
iter	Number of iterations.
sse	Sum squared error at each iteration.

Also, for tiltpsi

zcs	Matrix of Zernike coefficients, with one row for each column in coords and number of columns = number of columns of im.mat.
-----	-----------------------------------------------------------------------------------------------------------------------------

**Author(s)**

M.L. Peck <mpeck1@ix.netcom.com>

**References**

Zhaoyang Wang and Bongtae Han, "Advanced iterative algorithm for phase extraction of randomly phase-shifted interferograms," *Opt. Lett.* 29, 1671-1673 (2004).

Han, G-S and Kim, S-W,, "Numerical correction of reference phases in phase-shifting interferometry by iterative least squares fitting," *Applied Optics* 33, 7321-7325 (1994),

Lin, B-J et al., "An iterative tilt-immune phase-shifting algorithm," OSA conference Optical Fabrication and Testing 2010.

**See Also**

[psifit](#)

---

astig.bath

*Zernike coefficients for astigmatism due to Bath astigmatism.*

---

**Description**

Calculates Bath astigmatism coefficients with optional rotation of phi degrees.

**Usage**

```
astig.bath(D, rc, s, lambda = 1e-06, phi = 0)
```

**Arguments**

D	Diameter
rc	Radius of curvature
s	separation of reference and test beams
lambda	Wavelength – defaults to 1 nm.
phi	angle of image horizontal relative to interferometer axis, in degrees

**Details**

D, rc, s, and lambda must have the same units.

**Value**

The Zernike coefficients for primary astigmatism terms.

**Author(s)**

M.L. Peck <mpeck1@ix.netcom.com>

---

brcutpuw

*Branch cut algorithm for phase unwrapping*


---

**Description**

Solves a modification of the assignment problem to minimize the total length of branch cuts.

**Usage**

```
brcutpuw(phase, pen = 0, details = FALSE)
```

**Arguments**

phase	Matrix containing the wrapped phase map
pen	Optional penalty value for connecting a residue to an edge
details	boolean: if TRUE return some extra details for diagnostics

**Value**

A matrix containing the unwrapped wavefront. If details==TRUE a named list starting with the unwrapped wavefront in puw.

**Author(s)**

M.L. Peck

**See Also**

[qpuw](#) [idiffpuw](#)

**Examples**

```
set.seed(1234)
PW <- wrap(matrix((0:100)*pi/10,101,101))
## need a border of NA's
PW <- cbind(rep(NA,101), PW, rep(NA,101))
PW <- rbind(rep(NA,103), PW, rep(NA,103))
PW <- PW + rnorm(103^2)
mtext(rmap(PW, plot=TRUE))
PU <- brcutpuw(PW, details=TRUE)
image(1:103, 1:103, PU$bcuts, col="blue", add=TRUE)
X11()
image(PU$puw, col=grey256, asp=1, useRaster=TRUE)
```

circle.hough

*Estimate parameters of a circle using Hough Circle Transform***Description**

Uses a portion of the canny algorithm to find candidate edge points and the direction of the gradient at those points, then uses Hough Circle Transform to estimate circle parameters.

**Usage**

```
circle.hough(
  im,
  fw = 2,
  qt = 0.995,
  excl = 5,
  rmin = min(dim(im))/4,
  rmax = min(dim(im))/2,
  rstep = 1,
  dtheta_max = 0.5,
  dtheta_step = 0.05,
  nn = 7,
  plots = TRUE,
  details = FALSE
)
```

**Arguments**

im	The image to find a circle in (a modulation estimate is best)
fw	Size of Gaussian blur to smooth image
qt	Threshold to accept strong edge candidate
excl	Number of pixels to exclude around edge of frame as candidates
rmin	Minimum circle radius
rmax	Maximum circle radius
rstep	step size in constructing lookup table
dtheta_max	maximum assumed error in gradient direction
dtheta_step	increment for dtheta
plots	plot?
details	Return extra details?
number	of nearest neighbors for alternate calculation

**Details**

The Hough transform section first creates a lookup table of candidate radii and center points, then for each candidate edge point calculates potential centers along a fan of rays near the gradient direction. An inner join then finds matches in the lookup table and increments an accumulator vector. Highest vote at the end wins.

**Value**

If details is FALSE a named list with the circle parameters

**Note**

This is experimental and can be very slow. A good guess for the radius is very helpful. Experimental feature: find the nn nearest neighbors of the selected trio of parameters and calculate a vote weighted mean. This is returned as rxy\_alt if details is TRUE.

**See Also**

`circle.pars()`, `pupil.pars()`

**Examples**

```
example("psifit", package="zernike", ask=FALSE)
X11()
cp2 <- circle.hough(tfit$mod, rmin=round(tfit$cp$rx)-10, rmax=round(tfit$cp$rx)+10)
```

---

circle.pars	<i>Pupil parameters</i>
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**Description**

Automatically determine the center and radius of a circular interferogram image.

**Usage**

```
circle.pars(im, fw=2, qt=0.995, excl=5,
  plots=TRUE, details=FALSE)
```

**Arguments**

im	A matrix containing an image of a circular disk
fw	Amount to smooth image
qt	Threshold to accept an edge point, expressed as a quantile
excl	number of pixels around border of frame to exclude
plots	Plot edge candidates and fit?
obstructed	Logical: is there a central obstruction?

**Details**

This routine partially implements the Canny algorithm for edge detection. After optionally smoothing the input image the gradient is calculated using a Sobel filter, and edge pixels are identified by locating local maxima in the magnitude of the gradient.

The edge pixels with qt percentile largest gradients are passed to nlsrob in package robustbase lqs in package MASS to determine robustly the best fit circle.

**Value**

A list with the following components:

xc	X coordinate of the center of the pupil
yc	Y coordinate of the center of the pupil
rx	Horizontal radius of the pupil
ry	Vertical radius of the pupil = rx
obstruct	Obstruction fraction (always = 0)

**Note**

This routine is only effective on modulation estimates, and will almost certainly fail on interferogram images. Since data quality varies widely considerable experimentation may be needed on any given image. Increasing the smoothing parameter `fw` helps to suppress artifacts. Depending on how strong the actual edge is compared to artifacts `qt` may need to be either increased or decreased from the default value.

if `details==TRUE` several more pieces of data are returned. This is mostly for debugging purposes and may be eliminated in the future.

**Author(s)**

M.L. Peck <mpeck1@ix.netcom.com>

**See Also**

Many routines require the pupil parameters in the form returned by `circle.pars`. For example [psifit](#), [fftfit](#), [pupil](#), etc.

---

col3d

*OpenGL plot*


---

**Description**

Returns a vector of colors similar to `image()` display.

**Usage**

```
col3d(surf, surf.col=topo.colors(256), zlim = NULL, eqa=FALSE)
```

**Arguments**

surf	A matrix of surface values
surf.col	Color palette for surface
zlim	Range of values to display
eqa	Equal area per color?

**Value**

A vector of color values the same length as `surf`.



**Author(s)**

M.L. Peck <mpeck1@ix.netcom.com>

**References**

The **rgl** package is described at <http://rgl.neoscientists.org/about.shtml>, and available from CRAN.

**See Also**

[plot.pupil](#)

---

convolve2d	<i>2D convolution</i>
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---

**Description**

General 2D convolution using FFTs

**Usage**

```
convolve2d(im, kern)
```

**Arguments**

im	A matrix representing an image
kern	the convolution kernel

**Value**

The filtered matrix im.

**Author(s)**

M.L. Peck <mpeck1@ix.netcom.com>

**See Also**

[gblur](#). Called by [circle.pars](#).

---

crop	<i>Crop an array</i>
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**Description**

Crop a matrix or 3D array. Main application is to trim excess pixels from an image array, wavefront, etc.

**Usage**

```
crop(img, cp, npad = 20)
```

**Arguments**

img	Array to be cropped.
cp	A list describing the pupil boundary.
npad	Amount of padding to leave around the edge.

**Details**

cp is the list provided by [circle.pars](#).

**Value**

im	The cropped array
cp	Revised value of cp

**Author(s)**

M.L. Peck <mpeck1@ix.netcom.com>

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fftfrit	<i>Fourier transform interferogram analysis</i>
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**Description**

High level routines for FFT analysis of interferograms.

**Usage**

```
fftfrit(imagedata, cp = NULL,
        sl = c(1, 1), filter = NULL, taper = 2,
        options = psfit_options())
```

**Arguments**

imagedata	A matrix containing the interferogram
cp	A list describing the pupil boundary, as returned by <a href="#">pupil.pars</a>
sl	Position of sidelobe in the form c(x,y)
filter	Size of background filter around DC
taper	Size of taper applied to edge of half plane cut
options	a list of parameters passed to other functions. See <a href="#">psfit_options</a> .

**Details**

If `is.null(filter)` (the default), [pick.sidelobe](#) will be called to select a Fourier domain sidelobe and background filter size.

If `is.null(cp)` [circle.pars](#) is applied to the modulation to estimate the pupil parameters.

See [wf\\_net](#) for details of the process of creating net and smoothed wavefronts from raw unwrapped wavefront maps.

**Value**

A list with the following components:

phase	Wrapped phase map
mod	The estimated modulation
cp	A list describing the pupil boundary
cp.orig	The precropped value of cp
wf.net	Net unsmoothed wavefront; a matrix of class " <a href="#">pupil</a> "
wf.smooth	Net smoothed wavefront
wf.residual	Difference between net wavefront and polynomial fit
fit	Return value from <a href="#">fitzernikes</a>
zcoef.net	Net Zernike coefficients from fit

**Note**

These functions are based largely on the work of Roddier and Roddier (1987).

**Author(s)**

M.L. Peck <mpeck1@ix.netcom.com>

**References**

Roddier, C. and Roddier, F. 1987, **Interferogram analysis using Fourier transform techniques**, *Applied Optics*, vol. 26, pp. 1668-1673.

**See Also**

[wf\\_net](#), [pupil.pars](#), [pick.sidelobe](#).

**Description**

Miscellaneous utilities for working with 2D images in the Fourier domain.

**Usage**

```
wftophase(X, lambda=1)
padmatrix(X, npad, fill = mean(X, na.rm=TRUE))
submatrix(X, size = 255)
fftshift(X)
.up2(nr, nc=nr)
```

**Arguments**

X	A matrix
lambda	Value of the wavelength, in the same units as X
npad	Size of padded matrix
fill	Values to be assigned to padded matrix elements
size	Size of returned matrix
nr	A number
nc	A number

**Details**

wftophase computes the complex phase from wavefront values.

padmatrix pads a matrix to size npad x npad, placing the original matrix in the lower left hand corner of the padded matrix.

submatrix extracts a size x size matrix from the center of a larger matrix.

fftshift shuffles the quadrants of a matrix around to put the DC element (1,1) in the center of the transformed matrix, with spatial frequencies increasing to the right and up.

**Value**

A matrix transformation of the input matrix X.

.up2 returns the next higher power of 2 than max(nr, nc).

**Note**

These low level routines are used by several higher level functions that operate in the Fourier domain.

**Author(s)**

M.L. Peck <mpeck1@ix.netcom.com>

**See Also**

[startest](#), [fftfit](#).

---

fitzernikes*Least Squares fit to Zernike polynomials*

---

**Description**

Performs a least squares fit of a specified set of Zernike polynomials to a vector of wavefront measurements.

**Usage**

```
fitzernikes(wf, rho, theta, phi = 0, maxorder = 14, uselm = FALSE)
```

**Arguments**

wf	A vector of wavefront values
rho	A vector of radial coordinates.
theta	A vector of angular coordinates, in radians.
phi	Orientation of the image, in degrees
maxorder	Maximum Zernike polynomial order
uselm	Boolean: use <code>lm()</code> for least squares fit

**Details**

wf, rho, and theta must be the same length.

**Value**

The model fit as returned by `lm`, or the coefficients of the least squares fit if `uselm` is FALSE.

**Note**

The model fit is of the form  $wf \sim Z_0 + Z_1 + Z_2 + \dots$ . With the standard ordering of Zernikes  $Z_0$  is the piston term,  $Z_1$  and  $Z_2$  are x and y tilts,  $Z_3$  is defocus, etc.

**Author(s)**

M.L. Peck <mpeck1@ix.netcom.com>

**See Also**

[zpm](#), [psifit](#), [fftfit](#).

foucogram

*Simulate a Foucaultgram***Description**

Simulates the appearance of a wavefront under the Foucault test.

**Usage**

```
foucogram(wf, edgex = 0, phradius = 0, slit = FALSE,
          pad = 4, gamma = 1, map = FALSE, lev = 0.5)
```

**Arguments**

wf	An object of class <a href="#">pupil</a> containing wavefront values
edgex	lateral position of knife edge
phradius	radius of light source
slit	Logical: Is source a slit or pinhole?
pad	pad factor for FFT
gamma	Gamma value for graphics display
map	Logical: Overlay contours from wavefront map?
lev	Increment for contour levels, if used

**Details**

The default value of 0 for phradius simulates a monochromatic point source. Try values in the range 10-30 to suppress diffraction effects.

**Value**

A matrix of intensity levels in the simulated image.

**Note**

The key approximations here are treating the light source as monochromatic and spatially coherent, which is usually not the case for an extended source. Also, Fraunhofer diffraction theory is used.

**Author(s)**

M.L. Peck <mpeck1@ix.netcom.com>

**References**

See [http://home.netcom.com/~mpeck1/astro/foucault/ext\\_foucault.pdf](http://home.netcom.com/~mpeck1/astro/foucault/ext_foucault.pdf) for an outline of the mathematical treatment of an extended source.

**See Also**

[pupil](#)

---

`gblur`*Gaussian blur*

---

**Description**

Blur an image by fw pixels

**Usage**

```
gblur(X, fw=0, details=FALSE)
```

**Arguments**

X	A matrix representing an image
fw	Width of the Gaussian convolution kernel, in pixels
details	Return convolution kernel?

**Details**

fw is the standard deviation of the Gaussian.

**Value**

The filtered matrix X.

**Note**

the details option is mostly for debugging purposes and may go away.

**Author(s)**

M.L. Peck <mpeck1@ix.netcom.com>

**See Also**

[convolve2d](#)

---

`gpcapsi`*Generalized Principal components algorithm for phase shifting interferometry*

---

**Description**

A generalized principal components algorithm for phase shifting interferometry developed by the author. This is the “low level” implementation.

**Usage**

```
gpcapsi(im.mat, ptol = 0.001, maxiter = 20, trace = 1)  
gpcapsiC(im.mat, ptol, maxiter, trace)
```

**Arguments**

<code>im.mat</code>	Matrix containing the unmasked pixels from a set of interferograms.
<code>ptol</code>	Convergence tolerance for phase shifts
<code>maxiter</code>	Maximum number of iterations
<code>trace</code>	Print progress of nonlinear solver every trace iterations. Use <code>trace=0</code> for silent operation.

**Details**

`gpcapsi` is a wrapper to the C++ call in `gpcapsiC`.

**Value**

A list with the following items:

<code>phi</code>	Estimated wrapped phase.
<code>mod</code>	Estimated modulation.
<code>phases</code>	Estimated phase shifts.
<code>snr</code>	An estimate of the S/N of the interferograms.
<code>eigen</code>	Eigenvalues of the crossproduct matrix

**Note**

This is the low level interface to the algorithm. The matrix `im.mat` should contain the unmasked pixel values from the input interferogram array. No checks are made for valid data. This should normally be called through the high level function [psifit](#).

**Author(s)**

M. L. Peck

**See Also**

[pcapsi](#) [psifit](#)

---

gray256

*8 bit Grayscale*

---

**Description**

A vector of gray scale levels

**Usage**

```
gray256
grey256
```

**Value**

Defined as `gray256 <- grey(seq(0,1,length=256))`



**Author(s)**

M.L. Peck <mpeck1@ix.netcom.com>.

---

hypot	<i>Hypotenuse</i>
-------	-------------------

---

**Description**

The Euclidean length of a vector

**Usage**

hypot(x)

**Arguments**

x                      a vector

**Value**

the length of the vector

**Author(s)**

M.L. Peck

**Examples**

hypot(c(1,2))

---

idiffpuw	<i>Phase unwrapping by Integrating DIFFerences</i>
----------	----------------------------------------------------

---

**Description**

Simple path following algorithm for two dimensional phase unwrapping.

**Usage**

idiffpuw(phase, mask = phase, ucall = TRUE, dx = NULL, dy = NULL)

**Arguments**

phase	A matrix of wrapped phase values
mask	Matrix the same size as phase indicating masked pixels
ucall	Boolean: User call?
dx	Matrix of x differences
dy	Matrix of y differences

**Details**

mask indicates pixels that shouldn't be unwrapped. In the simplest (default) case these are just pixels where phase is undefined.

**Value**

if(ucall), a matrix of class "[pupil](#)" with unwrapped wavefront values, otherwise a list with items:

puw	Unwrapped phase
uw	Matrix indicating pixels that have been unwrapped.

**Note**

[brcutpuw](#) calls [rmap](#) first to check for the presence of residues. If there are none [idiffpuw](#) is guaranteed to work and is called to do the phase unwrapping.

If there *are* residues [brcutpuw](#) creates a mask then calls [idiffpuw](#) to unwrap unmasked portions of the phase map.

This function is user callable as well; use a call of the form [idiffpuw](#)(phase).

**Author(s)**

M.L. Peck <mpeck1@ix.netcom.com>. Thanks to Steve Koehler for programming ideas to considerably speed up the algorithm.

**References**

Ghiglia, D.C., and Pritt, M.D., 1998, **Two-Dimensional Phase Unwrapping**, New York: Wiley & Sons, Inc., ISBN 0-471-24935-1.

**See Also**

[rmap](#), [brcutpuw](#)

---

id\_dxy\_uw

---

*Compiled code via Rcpp for Itoh's method of phase unwrapping*


---

**Description**

Called by [brcutpuw\(\)](#) for fast phase unwrapping

**Usage**

```
id_dxy_uw(nr, nc, phase, mask, dx, dy, uw)
```

**Arguments**

nr	number of rows in phase matrix
nc	number of columns in phase matrix
phase	phase matrix converted to vector
mask	matrix of mask values converted to vector
dx	wrapped phase differences in x direction
dy	wrapped phase differences in y direction

**Details**

This is called by `brcutpuw()` through `idiffpuw()` but is also user callable. Wrapped phase values and differences are divided by  $2\pi$  before input making the input values in the range  $[-1/2, 1/2)$ . In `brcutpuw()` the mask indicates areas outside the interferogram area and lines of branch cuts

**Value**

a vector with the unwrapped phase

**Author(s)**

M.L. Peck (mlpeck54 -at- gmail.com)

**See Also**

`brcutpuw()`, `idiffpuw()`

---

id\_uw

---

*Compiled code via Rcpp for Itoh's method of phase unwrapping*


---

**Description**

Called by `idiffpuw()` for fast phase unwrapping

**Usage**

```
id_uw(nr, nc, phase)
```

**Arguments**

nr	number of rows in phase matrix
nc	number of columns in phase matrix
phase	phase matrix converted to vector

**Details**

This is called by `idiffpuw()` but is also user callable. Wrapped phase values are divided by  $2\pi$  before input making the input values in the range  $[-1/2, 1/2)$ . In `brcutpuw()` the mask indicates areas outside the interferogram area and lines of branch cuts

**Value**

a vector with the unwrapped phase

**Author(s)**

M.L. Peck (mlpeck54 -at- gmail.com)

**See Also**

`brcutpuw()`, `idiffpuw()`

---

`load.images`*Read images*

---

**Description**

Loads image files in jpeg, tiff or raw format. `load.pgm` provides legacy support for reading files in pgm format.

**Usage**

```
load.images(files, channels=c(1,0,0), scale=1, FLIP=FALSE)
load.pgm(files, imdiff=NULL)
```

**Arguments**

<code>files</code>	A vector of character strings with file names
<code>channels</code>	channel weights
<code>scale</code>	scale factor for image resize
<code>FLIP</code>	flip image left for right?

**Details**

set `FLIP=TRUE` to reverse mirror imaged interferograms.

Any file extension other than jpg, jpeg, tif, tiff is assumed to be in RAW format. Supported raw formats are determined by libraw and may not be up to date

**Value**

An array containing the contents of the image files.

**Note**

`load.pgm` is the original `load.images` included for legacy support of greyscale portable anymap files.

**Author(s)**

M.L. Peck <mpeck1@ix.netcom.com>

---

lspsi	<i>Phase Shifting Interferometry</i>
-------	--------------------------------------

---

**Description**

Least squares fitting of phase shifted interferograms.

**Usage**

```
lspsi(images, phases, wt = rep(1, length(phases)))  
lspsiC(images, phases, wt)
```

**Arguments**

images	An array containing the interferogram images
phases	A vector of phase shifts
wt	A vector of weights

**Details**

images is a 3 dimensional array with dimensions nrow x ncol x length(phases), where nrow and ncol are the number of rows and columns in the individual interferogram images.

lspsi reshapes the image array into a matrix and calls lspsiC which in turn calls the compiled C++ routine.

**Value**

A list containing the following components:

phi	Estimated wrapped wavefront phase.
mod	Estimated modulation

**Author(s)**

M.L. Peck <mpeck1@ix.netcom.com>

**See Also**

[psifit](#)

---

mpinv

*Moore-Penrose generalized inverse*


---

**Description**

Computes the Moore-Penrose generalized inverse of a matrix using singular value decomposition.

**Usage**

```
mpinv(X)
```

**Arguments**

X                      A matrix

**Value**

Matrix containing the generalized inverse. If X is an n x m matrix the return will have dimension m x n.

**Note**

The threshold for determining if a matrix is rank deficient is `eps <- .Machine$double.eps * max(dim(X)) * S$d[1]`

**Author(s)**

M. L. Peck

**Examples**

```
X <- matrix(rnorm(18), 6, 3) ## this should be full rank almost always
mpinv(X) %*% X

X <- matrix(1:18, 6, 3) ## this is not
mpinv(X) %*% X
```

---

pcapsi

*Vargas et al.'s Principal Components method for PSI*


---

**Description**

Compute the phase using the Principal components algorithm.

**Usage**

```
pcapsi(im.mat, bgsub = TRUE, group_diag = "v")
```

**Arguments**

im.mat	A <i>matrix</i> of interferogram values
bgsub	Boolean - subtract the pixelwise mean as background estimate?
group_diag	controls treatment of singular values of the data matrix

**Details**

Images are input into an array by [load.images](#). This must be reshaped into a matrix for this function. Also, a mask should be applied if available prior to the call.

**Value**

A list containing the following elements:

phi	The wrapped phase estimate. This is a vector as long as the number of rows in im.mat.
mod	Modulation estimate.
phases	Phase shift estimates.
snr	An estimate of the signal to noise ratio in the input data.
eigen	Singular values of the crossproduct matrix.

**Author(s)**

M.L. Peck <mpeck1@ix.netcom.com>

**References**

J. Vargas, J. Antonio Quiroga, and T. Belenguer, "Phase-shifting interferometry based on principal component analysis," *Opt. Lett.* **36**, 1326-1328 (2011) <http://www.opticsinfobase.org/ol/abstract.cfm?URI=ol-36-8-1326>

J. Vargas, J. Antonio Quiroga, and T. Belenguer, "Analysis of the principal component algorithm in phase-shifting interferometry," *Opt. Lett.* **36**, 2215-2217 (2011) <http://www.opticsinfobase.org/ol/abstract.cfm?URI=ol-36-12-2215>

**See Also**

[psifit](#),

---

pick.sidelobe	<i>Select an interferogram sidelobe in the Fourier domain</i>
---------------	---------------------------------------------------------------

---

**Description**

Interactively locate the center of a first order sidelobe in the FFT of an interferogram, and mark the width of the background filter.

**Usage**

```
pick.sidelobe(imagedata, logm=FALSE, gamma=3)
```

**Arguments**

imagedata	A matrix containing an interferogram image
logm	Logical: pass fn="logMod" to <a href="#">plot.cmat</a> ?
gamma	gamma value for display

**Details**

Uses the basic graphics utility [locator](#).

**Value**

A list with the following components:

sl	The coordinates c(x,y) of the selected sidelobe
filter	Estimated size of background filter

**Note**

The high level FFT interferogram analysis routine [fftfit](#) requires the approximate location of the intended first order interferogram sidelobe to be specified.

**Author(s)**

M.L. Peck <mpeck1@ix.netcom.com>

**See Also**

[fftfit](#),

---

plot.cmat

*Plot a complex matrix*

---

**Description**

Plot a real valued function of a complex matrix

**Usage**

```
plot.cmat(X, fn = "Mod", col = grey256,
cp=NULL, zoom=1, gamma=1, ...)
```

**Arguments**

X	A complex valued matrix
fn	A function returning a real value
col	Color palette for graph
cp	pupil parameters as returned by <a href="#">pupil.pars</a>
zoom	zoom factor for display
gamma	gamma value for display
...	Other parameters to pass to <a href="#">image.default</a>



**Details**

In addition to the functions described in [complex](#) fn can be assigned the values "logMod", which will call an internally defined function returning the value  $\log(1+\text{Mod}(X))$ , "Mod2" to plot the power spectrum, and "logMod2" to plot the logarithm of the power spectrum.

If the parameter cp is passed axes will display spatial frequencies in cycles per pupil radius.

**Value**

none

**Note**

This is used primarily for displaying FFT's of interferograms. In the case of an interferogram in which the background has not been removed use fn="logMod" to make the first order sidelobes visible.

**Author(s)**

M.L. Peck <mpeck1@ix.netcom.com>

**See Also**

[pick.sidelobe](#), [fftfit](#).

---

plot.pupil

*Pupils and wavefronts*


---

**Description**

Plot and summary methods for objects of class "pupil".

**Usage**

```
plot.pupil(wf, cp=NULL, col = topo.colors(256), addContours = TRUE, cscale = FALSE,
           eqa=FALSE, zlim=NULL, ...)
summary.pupil(wf)
```

**Arguments**

wf	An object of class "pupil"
cp	Pupil parameters; a list as returned by <a href="#">pupil.pars</a>
col	Color palette for plot
addContours	Logical: add contour lines?
cscale	Add a color scale legend?
eqa	Perform an "equal area" plot?
zlim	z limits to pass to image
...	Additional parameters to pass to <a href="#">image.default</a>

**Details**

These give simple plot and summary methods for objects of class [pupil](#).

If eqa is TRUE, each color in the palette will be used for an equal number of pixels (as opposed to representing an equal interval). Note: the color scale (when cscale == TRUE) may be inaccurate if a very small number of colors are used.

**Value**

none

**Author(s)**

M.L. Peck <mpeck1@ix.netcom.com>

**See Also**

[pupil](#), [pupilrms](#), [pupilpv](#), [strehlratio](#), [pupil.pars](#).

---

plotn	<i>Wavefront comparison plots</i>
-------	-----------------------------------

---

**Description**

Plot an arbitrary number of wavefronts and all differences.

**Usage**

```
plotn(..., labels = NULL, addContours=FALSE, wftype = "net",
col = rygcb(400), qt = c(0.01, 0.99))
```

**Arguments**

...	List of wavefront estimates as returned by <a href="#">wf_net</a> .
labels	Labels to identify the wavefronts.
addContours	Boolean to add contours to top row plots
wftype	If the inputs are from wf_net, one of "net", "smooth", "residual".
col	Color palette for top row of plot
qt	Quantiles of differences to plot in comparisons.

**Details**

... can be any number of objects containing wavefront estimates as returned for example by [wf\\_net](#).

Wavefronts are displayed on the top row, and differences of all pairs on subsequent rows. Grayscale is used to render the difference plots, and the color palette given in col is used for the wavefronts.

**Value**

none

**Author(s)**

M.L. Peck <mpeck1@ix.netcom.com>

**See Also**

[plot.pupil wf\\_net](#)

---

plotxs

*Plot cross-sections (profiles) through a wavefront map.*

---

**Description**

Plots an arbitrary number of cross-sections through a wavefront map, with one highlighted.

**Usage**

```
plotxs(wf, cp, theta0 = 0, ylim = NULL, N = 4, n = 101,
col0 = "black", col = "gray", lty = 2)
```

**Arguments**

wf	A matrix of wavefront values.
cp	List of pupil parameters as returned by <a href="#">pupil.pars</a> .
theta0	Angle of highlighted profile, in degrees.
ylim	range of heights to plot.
N	Number of cross sections.
n	Number of points for each cross section.
col0	Highlight color.
col	Cross section color.
lty	Line type for plots.

**Details**

The cross sections are equally spaced in angle from 0 to  $\pi*(N-1)/N$ . Any angle can be specified for the highlighted profile at theta0.

**Value**

none

**Author(s)**

M.L. Peck <mpeck1@ix.netcom.com>

**See Also**

[plot.pupil](#) is the main wavefront plotting routine.

psfit\_options

*Options for PSI and FFT based fitting routines***Description**

Get and optionally set parameters controlling various aspects of PSI algorithms, Zernike polynomial fitting, and data display

**Usage**

```
psfit_options(...)
```

**Arguments**

colors	topo.colors(256)
refine	TRUE
puw_alg	"qual"
fringescale	1
wt	NULL
bgsub	TRUE
maxiter	20
ptol	1e-04
trace	1
nzcs	2
zc0	c(1, 2, 3, 6, 7)
satarget	c(0, 0)
astig.bath	c(0, 0)
maxorder	14
uselm	FALSE
sgs	1
nthreads	parallel::detectCores()/2
plots	TRUE
crop	FALSE

**Details**

Calling `psfit_options` with an empty argument list returns the default values of the options used in `psifit` and `wf_net` as itemized above. The list can be modified directly or by passing argument value pairs to the function call.

Parameters you might want to change include:

`satarget` sets the target SA for “numerical nulling.” This is a vector of length 2 setting the target values of primary and 5th order SA.

`ptol` sets convergence tolerances for iterative PSI algorithms. These have different definitions and different values may be suitable for different algorithms. A value around 0.01 is appropriate for `tiltpsi`.

The number of variable Zernike terms in the algorithm `tiltpsi` is controlled by `nzcs`. Set it to 3 to include defocus, 5 to include primary astigmatism, 7 to include coma.

`maxorder` sets the maximum Zernike polynomial order for wavefront fitting. It must be even and at least 6. The default generally produces a good wavefront representation but you may want to experiment with higher order fits.

A new and somewhat experimental feature from version 3.6.0 of the package is threaded computation of Zernike polynomial matrices. The number of threads used is set with the option `nthreads`. The default is to use half the number of cores detected because on CPUs that support multi- or hyperthreading the number of cores reported by `detectCores()` is double the number of physical cores. Setting `nthreads = 1` will turn off threading. Different C++ routines are used for the matrix fill in the unthreaded (`zpmC`) and threaded (`zpmCP`) cases. Speed improvements, if any, may vary.

If you don't like the default color palette there are many other choices. If you like rainbows `rygcb` defined in this package produces a relatively perceptually uniform version that's well suited for display on an RGB monitor.

### Value

A named list with the current values of the arguments.

### Author(s)

M.L. Peck <mlpeck54@gmail.com>

---

psifit

*Phase Shifting Interferometry*

---

### Description

High level function for Least squares analysis of phase shifted interferograms.

### Usage

```
psifit(images, phases, cp = NULL, satarget = NULL, psialg = "ls", options = psifit_options())
```

### Arguments

<code>images</code>	An array containing the interferogram images
<code>phases</code>	A vector of phase shifts
<code>cp</code>	A list describing the pupil boundary, as returned by <code>pupil.pars</code>
<code>satarget</code>	Target 4th and 6th order SA coefficients in non-null tests of aspheres
<code>psialg</code>	String identifying the PSI algorithm to use
<code>options</code>	a list of options

## Details

`images` is a 3 dimensional array with dimensions `nrow` x `ncol` x `length(phases)`, where `nrow` and `ncol` are the number of rows and columns in the individual interferogram images.

The current values recognized for `psialg` are

**ls** least squares with known phase shifts

**aia** the “advanced iterative algorithm“ [aiapsi](#)

**pc1** pca with `group_diag = "v"`

**pc2** pca with `group_diag = "u"`

**gpc** my generalized PC algorithm in [gpcapsi](#)

**gpcthentilt** first [gpcapsi](#) the [tiltpsi](#)

**tilt** [tiltpsi](#)

## Value

A list with the following components

<code>phi</code>	wrapped phase estimate
<code>mod</code>	modulation estimate
<code>phases</code>	phase shifts
<code>cp</code>	the interferogram boundary
<code>wf.net</code>	net, unfiltered wavefront (see <a href="#">wf_net</a> )
<code>wf.smooth</code>	Zernike fit wavefront
<code>wf.residual</code>	the difference
<code>fit</code>	Coefficients of Zernike fit to wavefront
<code>zcoef.net</code>	Net Zernike coefficients
<code>extras</code>	any extra data returned by low level functions

## Author(s)

M.L. Peck <[mlpeck54@gmail.com](mailto:mlpeck54@gmail.com)>

## See Also

[lspsi](#), [aiapsi](#), [tiltpsi](#), [gpcapsi](#), [pcapsi](#)

## Examples

```
## reuse the files from the demo for an example of two stage fitting
## using gpca then tiltpsi
require(zernike)
fpath <- file.path(find.package(package="zernike"), "psidata")
files <- scan(file.path(fpath, "files.txt"), what="character")
for (i in 1:length(files)) files[i] <- file.path(fpath, files[i])

# load the images into an array

images <- load.images(files)
```

```

# parameters for this run

source(file.path(fpath, "parameters.txt"))

# phase shifts

phases <- wrap((0:(dim(images)[3]-1))/frames.per.cycle*2*pi)
phases <- switch(ps.dir, ccw = -phases, cw = phases, phases)

# target SA coefficients for numerical null.

sa.t <- sconic(diam,roc,lambda=wavelength)
zopt <- psfit_options()
zopt$satarget <- sa.t
zopt$ptol <- 0.01
tfit <- psifit(images, phases, psialg="gpcthentilt", options=zopt)

```

pupil

*Pupils and wavefronts*

## Description

Create a pupil object and optionally fill it with a wavefront. For our purposes a “pupil” is defined to be a matrix representation of a circular or annular aperture. Simple plot and summary methods are also provided.

## Usage

```

pupil(zcoef=NULL, zlist=makezlist(), phi=0, piston=0,
      nrow=512, ncol=nrow, cp=list(xc=256,yc=256,rx=255,ry=255,obstruct=0))
pupil.arb(zcoef=NULL, zlist=makezlist(), phi=0, piston=0,
          nrow=512, ncol=nrow, cp=list(xc=256,yc=256,rx=255,ry=255,obstruct=0))

```

## Arguments

<code>zcoef</code>	A vector of Zernike coefficients
<code>zlist</code>	List of indexes the same length as <code>zcoef</code>
<code>phi</code>	Amount to rotate image, in degrees
<code>piston</code>	Constant to add to wavefront values
<code>nrow</code>	Number of rows in output matrix
<code>ncol</code>	Number of columns in output matrix
<code>cp</code>	A list with items <code>xc</code> - x coordinate of central pixel, <code>yc</code> - y coordinate of central pixel, <code>rx</code> - x radius in pixels, <code>ry</code> - y radius in pixels, <code>obstruct</code> - central obstruction fraction.

## Details

[plot.pupil](#) and [summary.pupil](#) provide simple plot and summary methods for objects of class “pupil”.

`pupil.arb` will accept an arbitrary list of Zernikes.

`pupil` requires a complete set of Zernikes as returned by [makezlist](#).

**Value**

A matrix of size nrow x ncol. The matrix is assigned to the class "pupil". NA's are used to fill the matrix outside the defined area of the pupil.

**Note**

The parameter cp is used to define the dimensions of the pupil. See [pupil.pars](#) for details.

**Author(s)**

M.L. Peck <mpeck1@ix.netcom.com>

**See Also**

[Zernike](#), [makezlist](#), [pupilrms](#), [pupilpv](#), [strehlratio](#), [pupil.pars](#), [circle.pars](#).

**Examples**

```
wf <- pupil(zcoef=rnorm(length(makezlist())$n), 0, 0.01))
plot(wf, addContours=FALSE)
summary(wf)
```

---

pupil.pars	<i>Pupil parameters</i>
------------	-------------------------

---

**Description**

Interactively determine the center, radius, and obstruction fraction of a circular or annular interferogram image.

**Usage**

```
pupil.pars(im = NULL, obstructed = FALSE)
```

**Arguments**

im	A matrix containing an interferogram image
obstructed	Logical: is there a central obstruction?

**Details**

In `pupil.pars`, if the image has already been plotted `im` can be `NULL`, which is the default.

**Value**

A list with the following components:

xc	X coordinate of the center of the pupil
yc	Y coordinate of the center of the pupil
rx	Horizontal radius of the pupil
ry	Vertical radius of the pupil
obstruct	Obstruction fraction



**Note**

pupil.pars uses the basic graphics library routine [locator](#) to interactively mark the edge of the pupil, and optionally the edge of the obstruction. After right clicking to terminate locator() a least squares fit is performed to the marked points to determine the center and radius of the pupil.

Note that all routines that make use of Zernikes implicitly assume a circular pupil, or an annular one with small obstruction. We allow  $r_x \neq r_y$  for imaging sensors with non-square aspect ratios.

**Author(s)**

M.L. Peck <mpeck1@ix.netcom.com>

**See Also**

Many routines require the pupil parameters in the form returned by pupil.pars. For example [psifit](#), [fftfit](#), [pupil](#), etc.

---

pupil.rhotheta	<i>Polar coordinates</i>
----------------	--------------------------

---

**Description**

Calculate matrixes of polar coordinates for [pupil](#)'s.

**Usage**

```
pupil.rhotheta(nrow, ncol, cp)
```

**Arguments**

nrow	Number of rows in interferogram images
ncol	Number of columns in interferogram images
cp	A list describing the pupil boundary, as returned by <a href="#">pupil.pars</a>

**Value**

A list with the following components:

rho	A matrix of radial coordinates
theta	A matrix of angular coordinates

**Note**

My Zernike polynomial routines work in polar coordinates, which this function provides. Also, NA's are used to fill the matrix outside the pupil boundary, making the returned values convenient for selecting pixels inside interferograms.

**Author(s)**

M.L. Peck <mpeck1@ix.netcom.com>

**See Also**

[Zernike](#), [pupil](#).

pupilrms

*Wavefront statistics***Description**

Compute basic statistics of wavefronts stored in "pupil" objects.

**Usage**

```
pupilrms(pupil)
pupilpv(pupil)
strehlratio(rms)
```

**Arguments**

pupil	A matrix of class "pupil"
rms	An rms wavefront error

**Value**

Estimates of the RMS and P-V wavefront errors. `strehlratio` calculates Mahajan's approximation to the Strehl ratio.

**Note**

`pupilrms` simply calculates the standard deviation of finite values in the matrix `pupil`. This is a crude, but usually accurate enough estimate of the true RMS wavefront error.

[summary.pupil](#) calls these functions.

**Author(s)**

M.L. Peck <mpeck1@ix.netcom.com>

**References**

Schroeder, D.J. 2000, *Astronomical Optics, 2nd Edition*, Academic Press, chapter 10.

**See Also**

[summary.pupil](#).

**Examples**

```
zcoef <- rnorm(length(makezlist())$n, 0, 0.01)
wf <- pupil(zcoef=zcoef)
plot(wf)
summary(wf)
sqrt(crossprod(zcoef)) # A more accurate estimate of RMS
```

---

qpuw

*Quality guided algorithm for phase unwrapping*


---

**Description**

Quality guided algorithm for two dimensional phase unwrapping.

**Usage**

```
qpuw(phase, qual)
```

**Arguments**

phase	A matrix of wrapped phase values
qual	A matrix of quality values the same size as phase.

**Value**

puw	A matrix of class " <a href="#">pupil</a> " with the unwrapped wavefront.
-----	---------------------------------------------------------------------------

**Note**

This is a straightforward implementation of the quality guided algorithm of G&P.

**Author(s)**

M.L. Peck <mpeck1@ix.netcom.com>

**References**

Ghiglia, D.C., and Pritt, M.D., 1998, **Two-Dimensional Phase Unwrapping**, New York: Wiley & Sons, Inc., ISBN 0-471-24935-1.

**See Also**

[idiffpuw](#), [brcutpuw](#)

---

q\_uw

*Compiled code via Rcpp for quality guided phase unwrapping*


---

**Description**

Called by [qpuw\(\)](#) for fast quality guided phase unwrapping

**Usage**

```
q_uw(nr, nc, phase, qual)
```

**Arguments**

nr	number of rows in phase matrix
nc	number of columns in phase matrix
phase	phase matrix converted to vector
qual	quality matrix converted to vector

**Details**

This is called by `qpaw()` but is also user callable. Wrapped phase values are divided by  $2\pi$  before input making the input values in the range  $[-1/2, 1/2)$ .

**Value**

a vector with the unwrapped phase

**Author(s)**

M.L. Peck (mlpeck54 -at- gmail.com) with valuable programming advice from Steve Koehler

**See Also**

`qpaw()`, `idiffpw()`

---

readjpeg

*Read a jpeg or tiff file*


---

**Description**

Reads a jpeg or tiff file and combines the channels to produce a monochrome image in a matrix.

**Usage**

```
readjpeg(filename, channels)
readtiff(filename, channels)
```

**Arguments**

filename	File name
channels	A vector of length 3 with the channel weights

**Details**

Values in channels should be non-negative, but need not add to one.

**Value**

A double precision matrix with the image data.

**Note**

The matrix must have rows reversed and transposed to display properly with `image()`.

**Author(s)**

M.L. Peck <mpeck1@ix.netcom.com>

---

rescale

*Rescale an image.*

---

**Description**

Rescale a matrix containing a bitmapped image using bilinear interpolation.

**Usage**

```
rescale(im, scale)
```

**Arguments**

im	A matrix with image data.
scale	Scale factor.

**Details**

A value <1 will shrink the image.

**Value**

A matrix containing the rescaled image data.

**Note**

NA's are OK.

**Author(s)**

M.L. Peck <mpeck1@ix.netcom.com>

**See Also**

Called by [load.images](#) if necessary.

---

`rmap`*Utilities for phase unwrapping*

---

**Description**

Utility functions for use in 2D phase unwrapping.

**Usage**

```
rmap(phase, dx = NULL, dy = NULL, plot = FALSE, ...)  
wrap(phase)
```

**Arguments**

<code>phase</code>	Matrix of wrapped phase values
<code>dx</code>	Matrix of x differences
<code>dy</code>	Matrix of y differences
<code>plot</code>	Boolean: plot residue positions?
<code>...</code>	additional arguments for image

**Details**

`dx` and `dy` must have the same dimension as `phase`.

**Value**

In `rmap` if `plot == TRUE`

<code>nr</code>	the number of residues identified in the map
-----------------	----------------------------------------------

otherwise

<code>phase</code>	wrapped phase returned by <code>wrap</code>
--------------------	---------------------------------------------

<code>residues</code>	Matrix the same size as <code>phase</code> with residues marked as + or - 1.
-----------------------	------------------------------------------------------------------------------

**Note**

These are primarily intended for internal use but can be used interactively. Calling `rmap(phase, plot=TRUE)` will plot the positions of residues and return nothing. If (`plot==FALSE`) in the call to `rmap` a matrix the same size as `phase` is returned with residues identified with values of +1 or -1.

**Author(s)**

M.L. Peck <mpeck1@ix.netcom.com>. Steve Koehler is responsible for the efficient implementation of the `wrap` function.

**References**

Ghiglia, D.C., and Pritt, M.D., 1998, **Two-Dimensional Phase Unwrapping**, New York: Wiley & Sons, Inc., ISBN 0-471-24935-1.

**See Also**

Called by [brcutpuw](#).

---

rygcb	<i>A better rainbow.</i>
-------	--------------------------

---

**Description**

Produces a rainbow color palette with colors ranging from "red" to "blue" or "magenta". Perceptual uniformity should be superior to R's rainbow.

**Usage**

```
rygcb(n)
rygcbm(n)
```

**Arguments**

n                      Number of color levels

**Details**

The palette is created using colorRampPalette.

**Value**

A vector of colors.

**Note**

The call to colorRampPalette sets space="Lab" and interpolate="spline" with the intent of creating a more perceptually uniform rainbow.

**Author(s)**

M.L. Peck

**See Also**

[grey256](#)

**Examples**

```
plotsp <- function(spectrum) {
  sl <- length(spectrum)
  rgbv <- col2rgb(spectrum)
  plot((0:(sl-1))+0.5, rgbv[1,], type="l", col="red", xlim=c(0,sl),ylim=c(0,300),xlab="Index",ylab="Channel va
  points((0:(sl-1))+0.5, rgbv[2,], type="l", col="green")
  points((0:(sl-1))+0.5, rgbv[3,], type="l", col="blue")
  grid()
  rect(0:(sl-1), 260, 1:sl, 300, col=spectrum, density=NA)
}
plotsp(rygcb(400))
```

```
X11()  
plotsp(rygcbm(500))
```

---

sconic	<i>Sconic</i>
--------	---------------

---

## Description

twice the radial height difference between a sphere and conic surface

## Usage

```
sconic(D, rc, b = -1, lambda = 632.8, nmax = 6)
```

## Arguments

D	Diameter (mm)
rc	Radius of curvature (mm)
b	conic constant
lambda	source or test wavelength (nm)
nmax	maximum polynomial order

## Value

Zernike polynomial coefficients

## Note

This estimates twice the radial distance between a sphere and conic surface with same paraxial radius of curvature, and returns Zernike coefficients of polynomial expansion. Intended for “numerical nulling” when testing an asphere at center of curvature, and should be more accurate than the vertical height difference calculated by [zconic](#) for that purpose.

## Author(s)

M.L. Peck

## See Also

[zconic](#)

## Examples

```
2.*zconic(1000,5000)  
sconic(1000,5000)
```



---

separate.wf	<i>Separate wavefronts</i>
-------------	----------------------------

---

**Description**

Separate “polished in” from “instrumental” aberrations if possible

**Usage**

```
separate.wf(zcm, theta, maxorder = 14)
```

**Arguments**

zcm	Matrix of observed Zernike coefficients
theta	Vector of rotation angles (in radians)
maxorder	Maximum Zernike order to extract

**Value**

zcb	Table of extracted coefficients and standard errors
-----	-----------------------------------------------------

**Author(s)**

M.L. Peck

---

startest	<i>Star test simulator</i>
----------	----------------------------

---

**Description**

Simulates a star test.

**Usage**

```
startest(wf=NULL, zcoef=NULL, zlist=makezlist(), phi=0,
lambda = 1, defocus=5,
nrow = 255, ncol = nrow,
cp = list(xc=128,yc=128,rx=127,ry=127,obstruct=0),
obstruct=NULL, npad = 4,
gamma=2, psfmag=2, displaymtf=TRUE, displaywf=FALSE)
```

**Arguments**

wf	A matrix of class pupil containing wavefront values
zcoef	Vector of Zernike coefficients
zlist	Indexes of Zernike coefficients
phi	Angle to rotate wavefront
lambda	Wavelength, in same units as coefficients

defocus	Amount of defocus in waves
nrow	# rows in pupil matrix
ncol	# columns in pupil matrix
cp	pupil parameters
obstruct	Obstruction fraction
npad	Pad factor for FFT
gamma	Gamma value for graphics display
psfmag	Magnification factor for in focus PSF display
displaymtf	Logical: Display MTF?
displaywf	Logical: Display calculated wavefront?

### Details

If wf is NULL the wavefront is calculated from the the Zernike coefficients (which should be non-NULL).

### Value

A list with the following components:

psf	The in focus point spread function.
otf	The complex optical transfer function, a complex matrix of size pupilsize.
mtf	The modulation transfer function, a real matrix of size pupilsize.

### Author(s)

M.L. Peck <mpeck1@ix.netcom.com>

### References

Born, M. and Wolf, E. 1999, *Principles of Optics, 7th Edition*, Cambridge University Press.  
 Suiter, H. R., 1994, *Star Testing Astronomical Telescopes*, Willman-Bell, Inc.

### See Also

[Zernike](#), [pupil](#).

### Examples

```
# a random, but probably almost diffraction limited, wavefront

temp <- startest(zcoef=rnorm(length(makezlist())$n), mean=0, sd=0.01), zlist=makezlist(), displaywf=TRUE)
```

---

synth.interferogram	<i>Synthetic interferogram</i>
---------------------	--------------------------------

---

## Description

Compute and display a synthetic interferogram.

## Usage

```
synth.interferogram(wf = NULL, zcoef = NULL, zlist = NULL,  
  nr = nrow(wf), nc = ncol(wf), cp = NULL,  
  phi = 0, addzc = rep(0, 4), fringescale = 1, plots = TRUE)
```

## Arguments

wf	A matrix of wavefront values
zcoef	A vector of Zernike coefficients
zlist	A list of Zernike indexes
nr	Number of rows in the output matrix
nc	Number of columns in the output matrix
cp	A list describing the pupil boundaries, as created by <a href="#">pupil.pars</a>
phi	Amount to rotate the wavefront, in degrees
addzc	A 4-vector with piston, tilt, and defocus terms to be added
fringescale	Fringe scale. Should be 1 for single pass, 0.5 for double, etc.
plots	Logical: Plot the interferogram?

## Details

Either wf or zcoef should be non-null, but not both. If zcoef is specified zlist must be as well.

Additional piston, tilt, and defocus terms can be added to the calculated wavefront using addzc.

## Value

A matrix of intensity levels in the calculated interferogram, assigned class "[pupil](#)".

## Author(s)

M.L. Peck <mpeck1@ix.netcom.com>

## See Also

[pupil.](#)

**Examples**

```
# create a list of zernikes
zcoef <- rnorm(length(zlist.fr$n), mean=0, sd=0.01)

iwf <- synth.interferogram(zcoef=zcoef, zlist=zlist.fr)

X11()

# show again with some tilt
iwf <- synth.interferogram(zcoef=zcoef, zlist=zlist.fr, addzc=c(0,5,5,0))
```

turbwf

*Kolmogorov Turbulence***Description**

Simulates the optical effects of atmospheric turbulence using Noll's (1976) calculation of the covariance matrix of Zernike polynomials under Kolmogorov turbulence.

**Usage**

```
turbwf(friedratio = 1, zlist = makezlist(2, 40), reps = 1)
```

**Arguments**

friedratio	Ratio of pupil diameter to Fried parameter
zlist	A list of Zernikes, as returned for example by <a href="#">makezlist</a>
reps	Number of draws to simulate

**Details**

The default value of zlist has 440 elements, which may be more than necessary for a reasonable representation of an “atmospheric” wavefront.

**Value**

A list with the following components:

zcoef.turb	A reps x length(zlist\$n) matrix of simulated draws of Zernike coefficients.
V	Covariance matrix of the indexed Zernikes.

**Note**

Typos in the original source material have been corrected in the code. Note that scintillation is not modelled.

**Author(s)**

M.L. Peck <mpeck1@ix.netcom.com>

## References

Noll, R.J. 1976, **Zernike polynomials and atmospheric turbulence**, *J. Opt. Soc. Am.*, Vol. 66, No. 3, p. 207.

## See Also

[Zernike, pupil](#).

## Examples

```
# Simulate a single draw from a turbulent atmosphere
zcoef.turb <- turbwf(friedratio=5, zlist=makezlist(2,30), reps=1)$zcoef.turb
# Warning: this can take a while
wf <- pupil(zcoef=zcoef.turb, zlist=makezlist(2,30))
plot(wf)
summary(wf)
```

---

vortexfit

*Vortex transform.*


---

## Description

Fringe analysis by Vortex aka Spiral Quadrature transform.

## Usage

```
vortexfit(
  imagedata,
  cp = NULL,
  filter = NULL,
  fw.o = 5,
  options = psfit_options()
)
```

## Arguments

imagedata	matrix containing the interferogram data
cp	list with circle parameters describing interferogram location. Defaults to NULL
filter	size of filter to remove background
fw.o	size of gaussian blur to smooth orientation estimate
options	A list with general fitting and display options. See <a href="#">psfit_options()</a> .

## Details

Implements the Vortex or spiral phase quadrature transform method of Larkin et al. (2001) <https://doi.org/10.1364/JOSA> including the fringe orientation estimation approach in Larkin (2005) <https://doi.org/10.1364/OPEX.13.008097>. Thanks to Steve Koehler for ideas on implementation details.

## Value

a list with wavefront estimates, wrapped phase, modulation, etc.

**Warning**

This routine is offered as is with no license, as it may be in violation of one or more US and international patents.

**See Also**

This is one of two routines provided for analysis of single interferograms, along with `fftfit()`. This *may* be suitable for interferograms with closed fringes.

**Examples**

```
require(zernike)
fpath <- file.path(find.package(package="zernike"), "psidata")
fname <- "Image197.jpg"
img <- load.images(file.path(fpath, fname))

# parameters for this run

source(file.path(fpath, "parameters.txt"))

# target SA coefficients for numerical null.

sa.t <- sconic(diam,roc,lambda=wavelength)
zopt <- psfit_options()
zopt$satarget <- sa.t

# display an interferogram

if (tolower(.Platform$OS.type) == "windows") windows() else x11()
image(1:nrow(img), 1:ncol(img), img, col=grey256, asp=1,
      xlab="X", ylab="Y", useRaster=TRUE)
mtext("Sample Interferogram")

if (tolower(.Platform$OS.type) == "windows") windows() else x11()
vfit <- vortexfit(img, filter=15, fw.o=10, options=zopt)
```

---

wf3d.pupil

*OpenGL wavefront plot*


---

**Description**

Interactive plot of a wavefront using the OpenGL package **rgl**. This is a 3D plotting method for objects of class "`pupil`".

**Usage**

```
wf3d.pupil(wf, cp=NULL, zoom.wf = 1, surf.col = topo.colors(256), bg.col = "black",
           eqa=FALSE)
```

**Arguments**

wf	A matrix of wavefront values
cp	A list describing the pupil boundary
zoom.wf	Zoom factor for heights
surf.col	Color palette for surface
bg.col	Background color
eqa	Equal area per color?

**Details**

The default color palette will match the colors in the default version of [plot.pupil](#).

**Value**

none

**Author(s)**

M.L. Peck <mpeck1@ix.netcom.com>

**References**

The **rgl** package is described at <http://rgl.neoscientists.org/about.shtml>, and available from CRAN.

**See Also**

[plot.pupil](#)

**Examples**

```
# create a random wavefront

wf <- pupil(zcoef=rnorm(length(makezlist())$n), mean=0, sd=0.01))
# the default method

plot(wf)

#this is more fun

wf3d(wf)
```

---

wf_net	<i>Wavefront smoothing</i>
--------	----------------------------

---

### Description

Calculate net and smoothed wavefronts from a raw wavefront containing low order nuisance aberrations.

### Usage

```
wf_net(wf.raw, cp, options)
```

### Arguments

wf.raw	Raw wavefront to be processed
cp	a list describing the pupil boundary
options	a list of options. See <a href="#">psfit_options</a>

### Details

Called by [psifit](#)

### Value

A list with the following components:

wf.net	Net unsmoothed wavefront; a matrix of class " <a href="#">pupil</a> "
wf.smooth	Net smoothed wavefront
wf.residual	Difference between net wavefront and polynomial fit
fit	Return value from <a href="#">fitzernikes</a>
zcoef.net	Net Zernike coefficients from fit

### Author(s)

M.L. Peck <mpeck1@ix.netcom.com>

---

zconic	<i>Zernike coefficients for a conic surface</i>
--------	-------------------------------------------------

---

### Description

Calculates the radially symmetric Zernike coefficient values up to order nmax for a conic surface relative to a sphere of the same paraxial radius of curvature.

### Usage

```
zconic(D, rc, b = -1, lambda = 1e-06, nmax = 6)
```



**Arguments**

D	Diameter
rc	Radius of curvature
b	Conic constant
lambda	Wavelength – defaults to 1 nm.
nmax	Maximum radial polynomial order

**Details**

D, rc, and lambda must have the same units.

**Value**

A vector of length  $n_{\max}/2-1$  of coefficient values, in increasing radial order,  $n=c(4,6, \dots)$ .

**Author(s)**

M.L. Peck <mpeck1@ix.netcom.com>

**See Also**

[Zernike](#)

**Examples**

```
zconic(200,2000)
zconic(10, 20, b=-1.05, lambda=632.8E-9, nmax=12)
```

---

Zernike

*Zernike Polynomials*


---

**Description**

Routines for creating and manipulating Zernike polynomials.

**Usage**

```
Zernike(rho, theta, n, m, t)
DZernike(rho, theta, n, m, t)
DTZernike(rho, theta, n, m, t)
rzernike(rho, n, m)
drzernike(rho, n, m)
```

**Arguments**

rho	normalized radius, $0 \leq \rho \leq 1$
theta	angular coordinate
n	radial polynomial order
m	azimuthal order
t	character for trig function: one of c("n", "c", "s")

**Note**

These functions return Zernikes scaled such that they form an orthonormal basis set for the space of functions defined on the unit circle. Note that this is not the most commonly used definition (as given e.g. in *Born and Wolf*). The definition I use is often associated with *Noll (1976)*.

The function `zmult` can be used to convert between normalized and conventionally defined vectors of Zernike coefficients.

The basic low level functions `rzernike` and `drzernike` use numerically stable recurrence relationships for the radial Zernikes.

**Author(s)**

M.L. Peck <mpeck1@ix.netcom.com>

**References**

Born, M. and Wolf, E. 1999, *Principles of Optics, 7th Edition*, Cambridge University Press, chapter 9 and appendix VII.

Noll, R.J. 1976, **Zernike polynomials and atmospheric turbulence**, *J. Opt. Soc. Am.*, Vol. 66, No. 3, p. 207.

<http://wyant.opt-sci.arizona.edu/zernikes/zernikes.htm>

<http://mathworld.wolfram.com/ZernikePolynomial.html>

**See Also**

`makezlist`, `zlist.fr`, `zmult`, `zpm`, `pupil`, `pupilrms`, `pupilpv`, `strehlratio`.

**Examples**

```
Zernike(1, 0, 4, 0, "n") # == sqrt(5)

# A slightly more complex example

rho <- seq(0, 1, length = 101)
theta <- rep(0, 101)

plot(rho, Zernike(rho, theta, 6, 0, "n"), type="l",
     ylim=c(-3.5,3.5), main="Some 6th order Zernike Polynomials")
lines(rho, Zernike(rho, theta, 5, 1, "c"), lty=2)
lines(rho, Zernike(rho, theta, 4, 2, "c"), lty=3)
lines(rho, Zernike(rho, theta, 3, 3, "c"), lty=4)
```

---

zlist

---

*Lists of Zernike polynomial indexes*


---

**Description**

Ordered lists of Zernike polynomial indexes.

## Usage

```
makezlist(minorder = 2, maxorder = 14)
zlist.fr
zmult(zlist = makezlist())
```

## Arguments

minorder	minimum value of $n+m$
maxorder	maximum value of $n+m$
zlist	a list of the form returned by <code>makezlist</code>

## Details

Zernike polynomials are indexed by a radial index  $n$ , an azimuthal index  $m$ , and include cosine, sine, and radial terms. These routines return lists of indexes using a popular ordering scheme for Zernike polynomials.

## Value

`makezlist` and `zlist.fr` return lists with the following components:

$n$	radial order
$m$	azimuthal order
$t$	one of <code>c("c", "s", "n")</code>

`zmult` returns a vector the same length as the components of `zlist`.

## Note

`zlist.fr` is an augmented “Fringe” set of Zernike polynomials equivalent to `makezlist(2,12)`.

`makezlist` returns a complete list of indexes for all orders from `minorder` through `maxorder`, where “order” is the value of  $n+m$ .

## Author(s)

M.L. Peck <mpeck1@ix.netcom.com>

## See Also

Virtually all high level functions that work with Zernike polynomials use these lists. See for example [pupil](#), [psifit](#), [fftfit](#).

## Examples

```
zlist <- makezlist(2,12)
zcoef <- rnorm(length(zlist))
zcoef # a vector of normalized Zernike coefficients
zcoef*zmult(zlist) # Coefficients in conventional representation
sqrt(crossprod(zcoef)) # This is the RMS error of the wavefront
# constructed from these Zernikes
```

---

zmoments	<i>Zernike moments</i>
----------	------------------------

---

**Description**

Calculate Zernike moments from a vector of coefficients

**Usage**

```
zmoments(zcoef, maxorder = 14)
```

**Arguments**

zcoef	Zernike coefficients
maxorder	Maximum order to return

**Value**

A table of the moments along with radial and azimuthal orders

**References**

M.L. Peck

---

zpm	<i>Matrixes of Zernike polynomials</i>
-----	----------------------------------------

---

**Description**

Create a matrix of Zernike polynomial values, or their derivatives or gradient.

**Usage**

```
zpm(rho, theta, phi = 0, maxorder = 14, nthreads=parallel::detectCores()/2)
zpmC(rho, theta, maxorder)
zpmCP(rho, theta, maxorder)
zpm.arb(rho, theta, phi = 0, zlist = makezlist())
filldzm(rho, theta, phi = 0, zlist = makezlist())
fillgradientzm(rho, theta, phi = 0, zlist = makezlist())
```

**Arguments**

rho	A vector of radial coordinates.
theta	A vector of angular coordinates, in radians.
phi	Orientation of the image, in degrees
zlist	A list of indexes, as returned by <a href="#">makezlist</a>
maxorder	The maximum Zernike polynomial order
nthreads	Number of threads for threaded function call

**Details**

rho and theta must be the same length.

**Value**

zpm.arb and filldzm return a matrix of size `length(rho) x length(zlist$n)` with values of Zernike polynomials or their radial derivatives evaluated at the polar coordinates (rho, theta-pi\*phi/180).

zpm, zpmC, and zpmCP return a matrix of size `length(rho) x (maxorder/2+1)^2` of Zernike polynomial values including a piston term.

fillgradientzm returns the gradient, in polar coordinates, of Zernikes in a `2*length(rho) x length(zlist$n)` matrix. Rows `1:length(rho)` contain the radial derivative, followed by `1/rho` times the tangential derivative.

**Note**

These are used by various routines to make least squares fits of sets of Zernike polynomials to measured wavefront values.

zpmC is the C++ routine that does the computations for zpm. No column names are returned.

Threaded computation of the matrix is now available using zpmCP.

**Author(s)**

M.L. Peck <mpeck1@ix.netcom.com>

**See Also**

[Zernike](#), [makezlist](#), [zlist.fr](#), [fitzernikes](#)

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