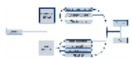
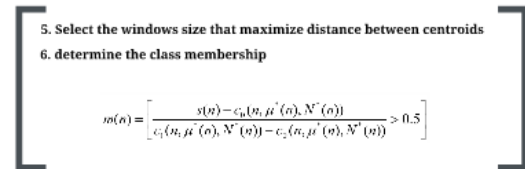
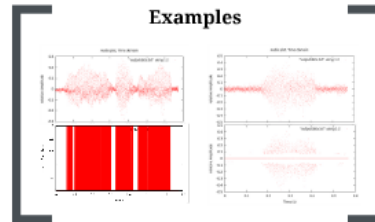
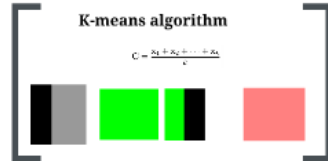
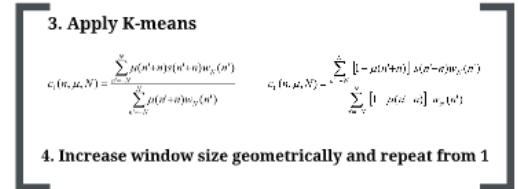
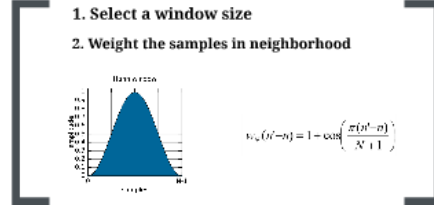




Digital signal processing is the mathematical manipulation of an information signal to modify or improve it in some way.



SHUKRANI




Antonio Agui e Claudio  
Cullerda Corrallo  
José Luis Rodríguez

# Nyoka Sound Library



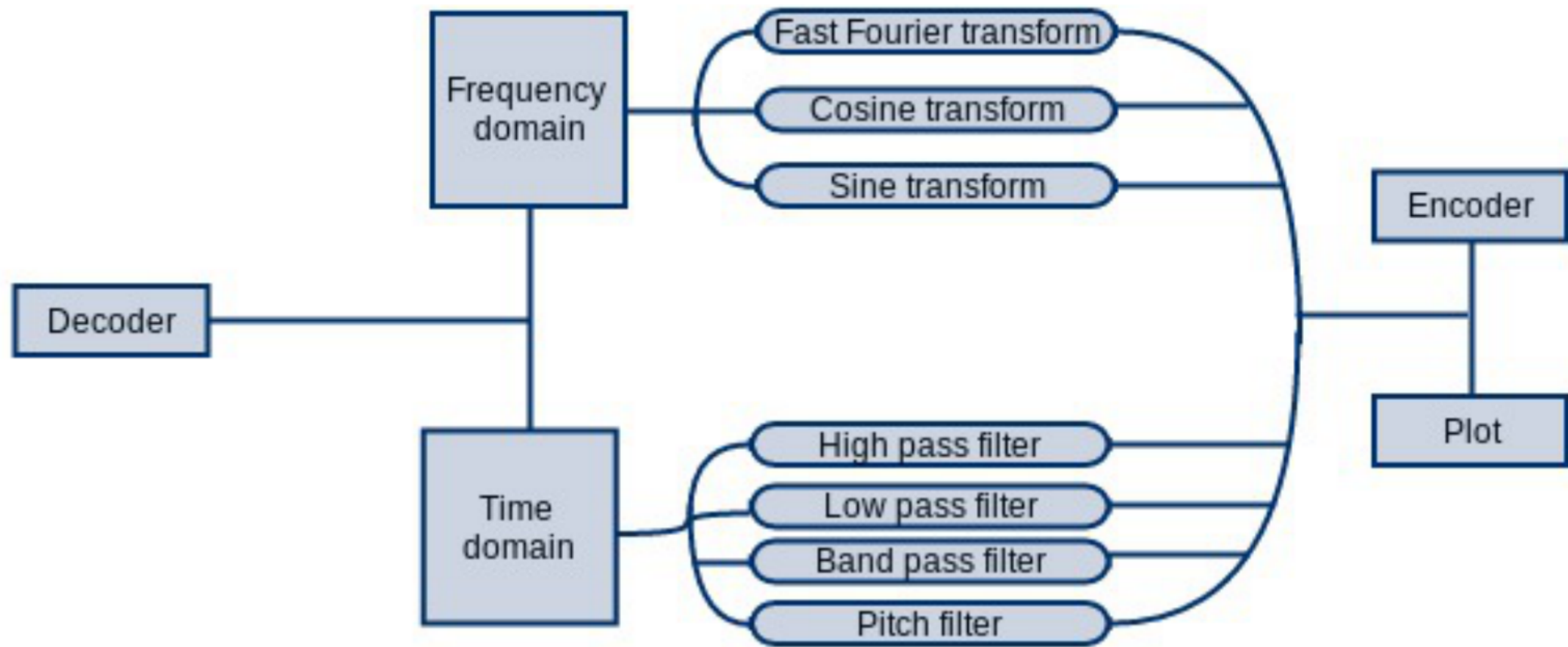
Arturo Apú Chinchilla  
Guillermo Cornejo Suárez  
José Johel Rodríguez Pineda



Digital signal processing is the mathematical manipulation of an information signal to modify or improve it in some way.

# *Benefits*

- Exact reproduction
- Easy manipulation



# *Fast Fourier Transform*

$$H_n = \sum_{k=0}^{N-1} h_k e^{2\pi i k n / N}$$

## Danielson-Lanzczon lemma

$$\begin{aligned} F_k &= \sum_{j=0}^{N-1} e^{2\pi i j k / N} f_j \\ &= \sum_{j=0}^{N/2-1} e^{2\pi i k (2j) / N} f_{2j} + \sum_{j=0}^{N/2-1} e^{2\pi i k (2j+1) / N} f_{2j+1} \\ &= \sum_{j=0}^{N/2-1} e^{2\pi i k j / (N/2)} f_{2j} + W^k \sum_{j=0}^{N/2-1} e^{2\pi i k j / (N/2)} f_{2j+1} \\ &= F_k^e + W^k F_k^o \end{aligned}$$



Sample numbers  
in normal order

Decimal Binary

0	0000
1	0001
2	0010
3	0011
4	0100
5	0101
6	0110
7	0111
8	1000
9	1001
10	1010
11	1011
12	1100
13	1101
14	1110
15	1111



Sample numbers  
after bit reversal

Decimal Binary

0	0000
8	1000
4	0100
12	1100
2	0010
10	1010
6	0110
14	1110
1	0001
9	1001
5	0101
13	1101
3	0011
11	1011
7	0111
15	1111

1 signal of  
16 points

0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15
---	---	---	---	---	---	---	---	---	---	----	----	----	----	----	----

2 signals of  
8 points

0	2	4	6	8	10	12	14	1	3	5	7	9	11	13	15
---	---	---	---	---	----	----	----	---	---	---	---	---	----	----	----

4 signals of  
4 points

0	4	8	12	2	6	10	14	1	5	9	13	3	7	11	15
---	---	---	----	---	---	----	----	---	---	---	----	---	---	----	----

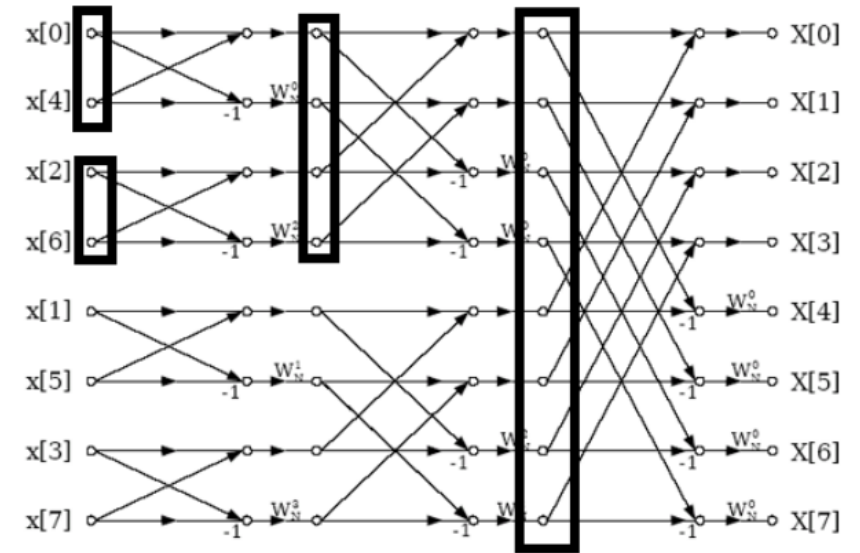
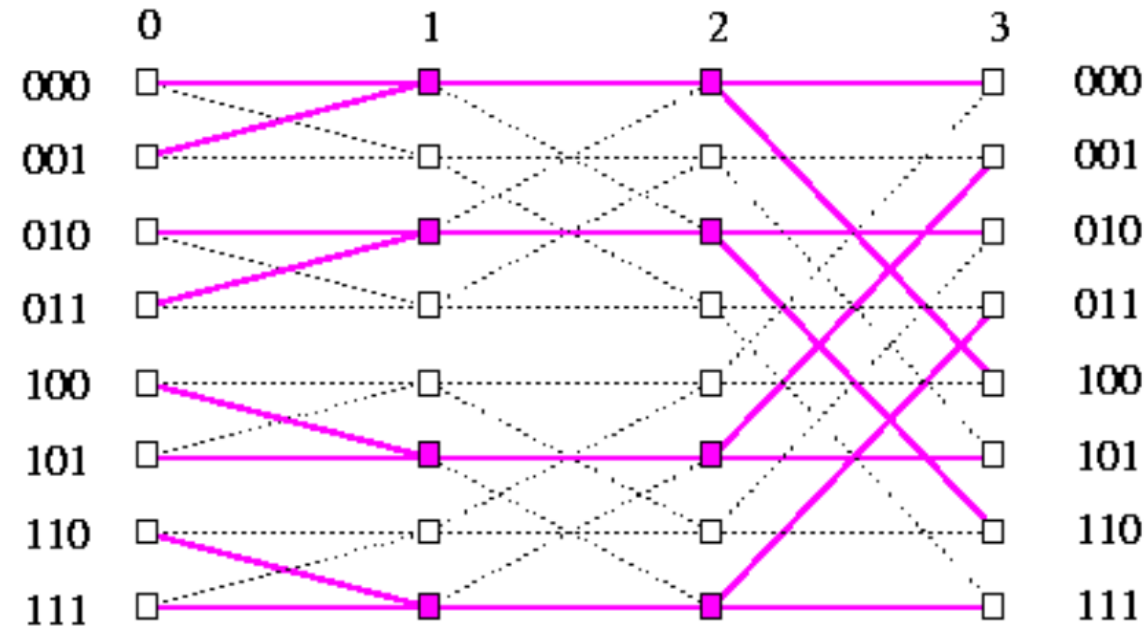
8 signals of  
2 points

0	8	4	12	2	10	6	14	1	9	5	13	3	11	7	15
---	---	---	----	---	----	---	----	---	---	---	----	---	----	---	----

16 signals of  
1 point

0	8	4	12	2	10	6	14	1	9	5	13	3	11	7	15
---	---	---	----	---	----	---	----	---	---	---	----	---	----	---	----

# Bit reverse & Butterfly



$$F_k = \frac{1}{2}(f_0 + (-1)^k f_N) + \sum_{j=1}^{N-1} f_j \cos(\pi j k / N)$$

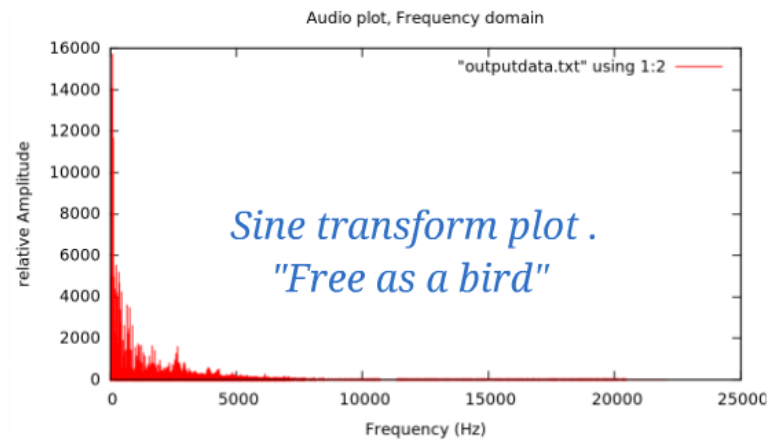
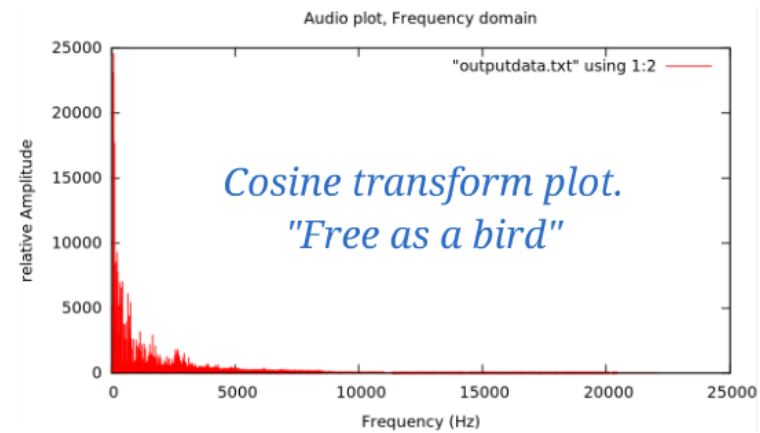
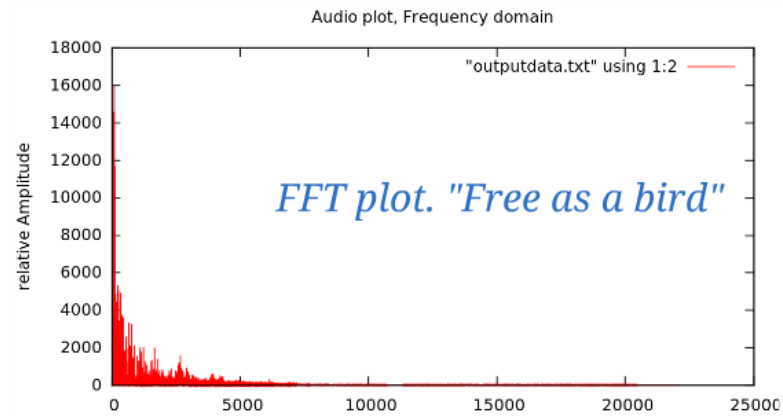
## *Cosine transform*

$$F_{2k} = R_k \quad F_{2k+1} = F_{2k-1} + I_k$$

$$F_k = \sum_{j=0}^{2N-1} f_j e^{2\pi i j k / 2N} = 2i \sum_{j=1}^{N-1} f_j \sin(\pi j k / N)$$

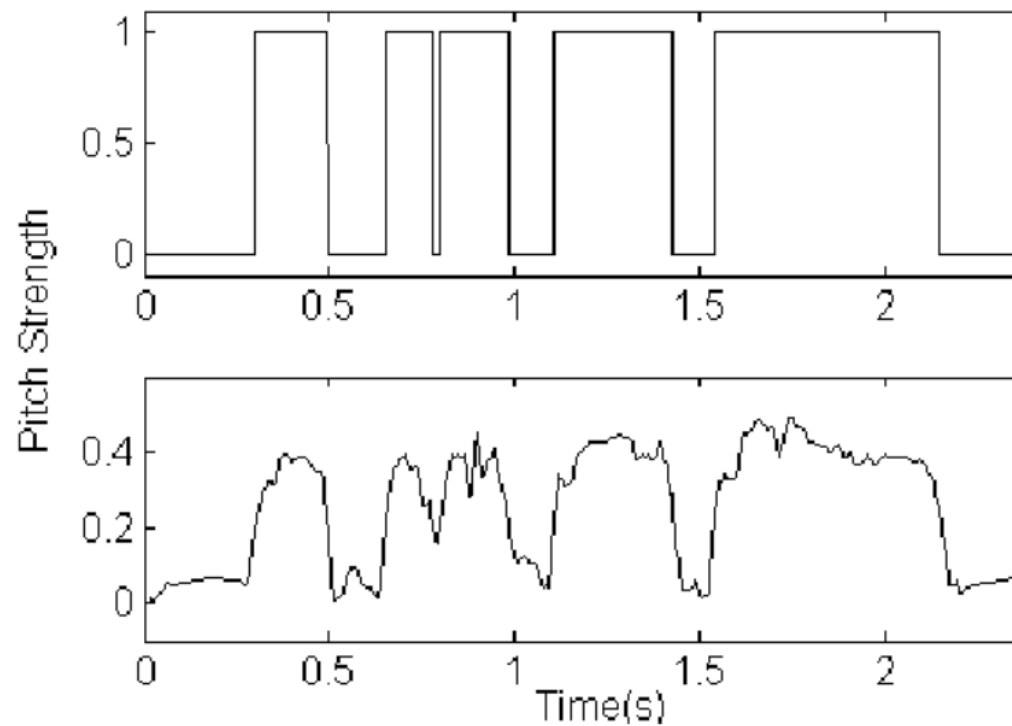
## *Sine transform*

$$F_{2k} = I_k \quad F_{2k+1} = F_{2k-1} + R_k$$



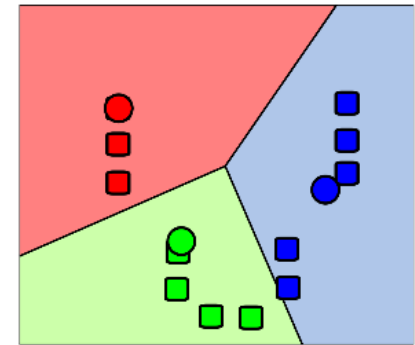
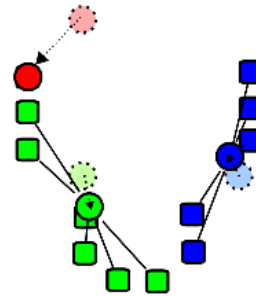
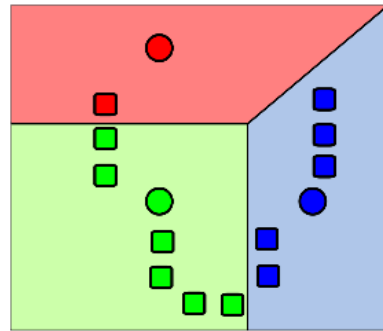
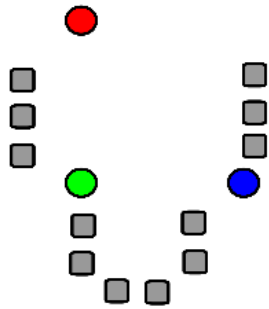
# Pitch filter

Developed by Prof. Arturo Camacho. Ph.D



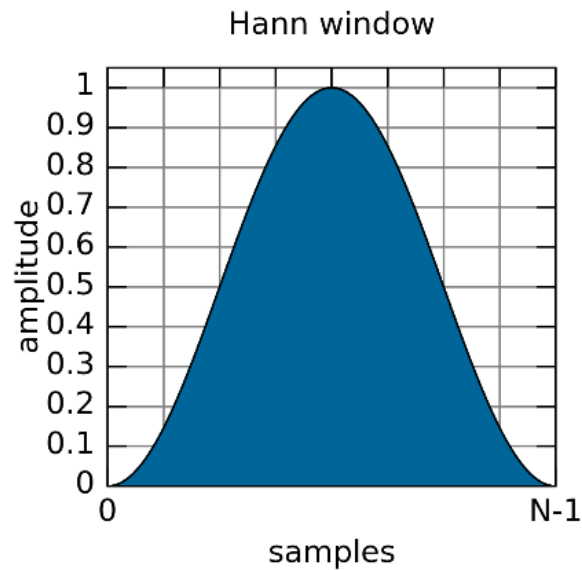
# K-means algorithm

$$C = \frac{x_1 + x_2 + \dots + x_k}{k}$$



**1. Select a window size**

**2. Weight the samples in neighborhood**



$$w_N(n'-n) = 1 + \cos\left(\frac{\pi(n'-n)}{N+1}\right)$$



### 3. Apply K-means

$$c_1(n, \mu, N) = \frac{\sum_{n'=-N}^N \mu(n'+n) s(n'+n) w_N(n')}{\sum_{n'=-N}^N \mu(n'+n) w_N(n')}$$

$$c_0(n, \mu, N) = \frac{\sum_{n'=-N}^N [1 - \mu(n'+n)] s(n'+n) w_N(n')}{\sum_{n'=-N}^N [1 - \mu(n'+n)] w_N(n')}$$

### 4. Increase window size geometrically and repeat from 1

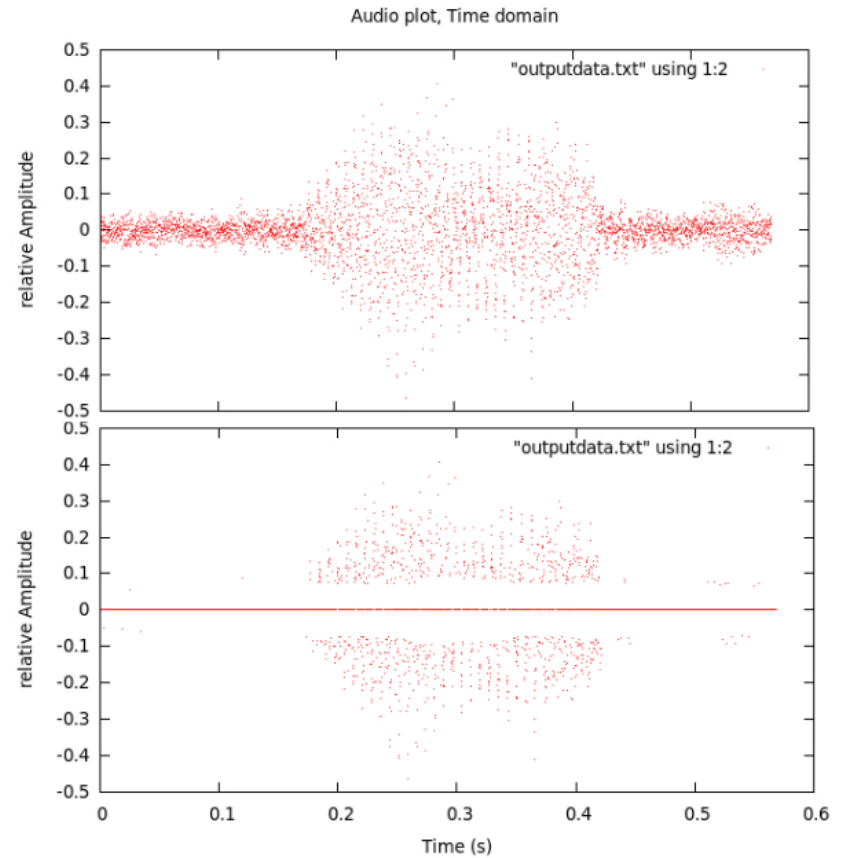
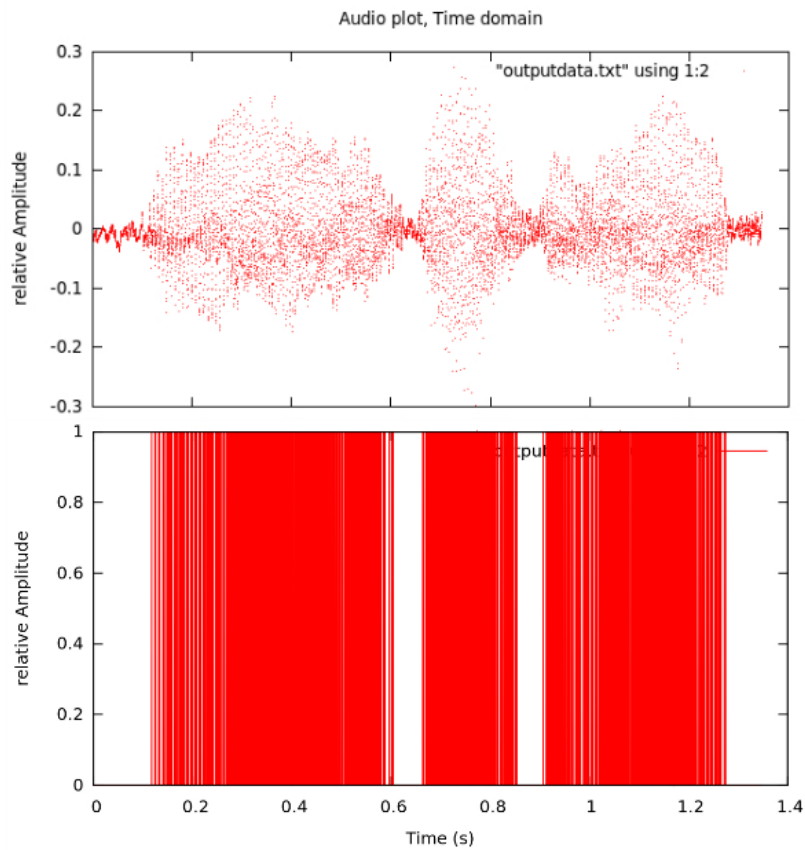
**4. Increase window size geometrically and repeat from 1**

**5. Select the windows size that maximize distance between centroids**

**6. determine the class membership**

$$m(n) = \left[ \frac{s(n) - c_0(n, \mu^*(n), N^*(n))}{c_1(n, \mu^*(n), N^*(n)) - c_0(n, \mu^*(n), N^*(n))} > 0.5 \right]$$

# Examples



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