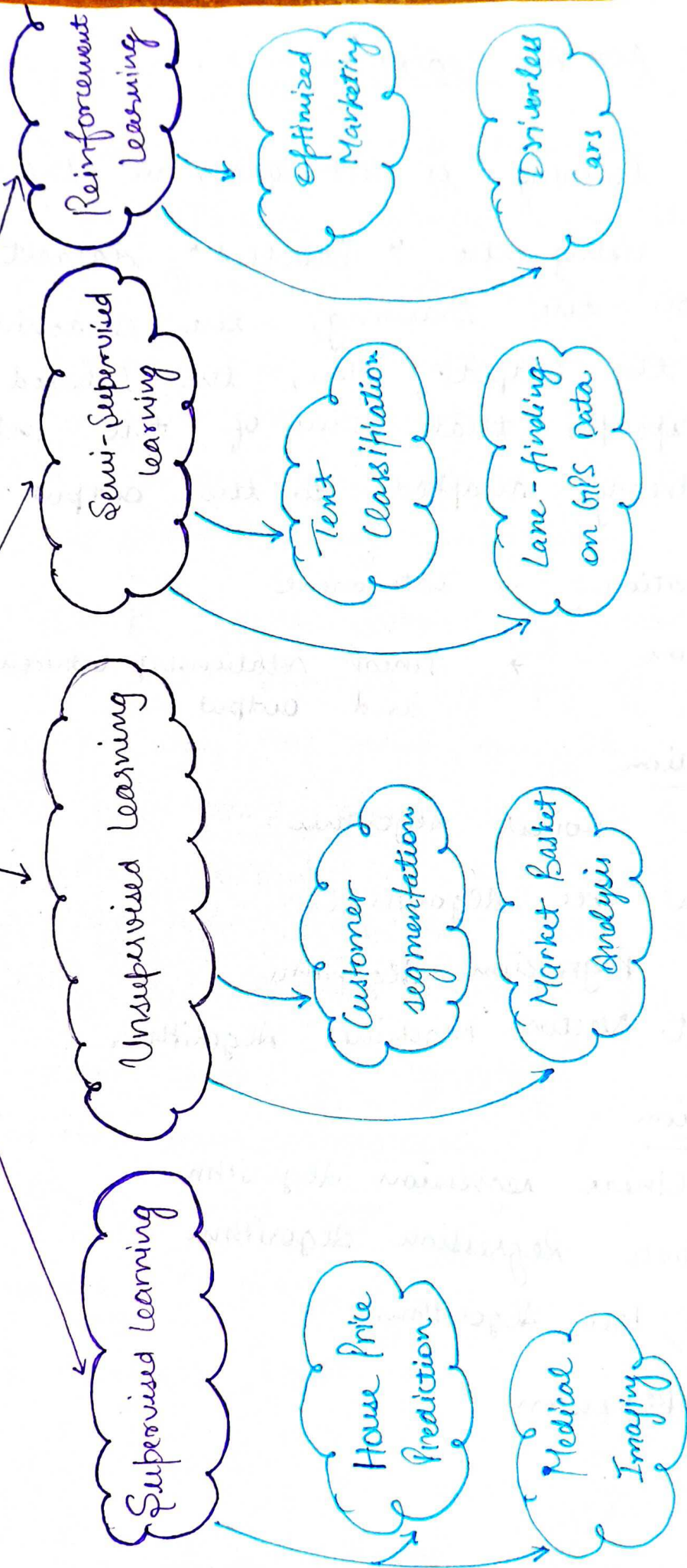


Machine Learning



I. Supervised Machine Learning

Supervised learning is technique, we train the machine using the "labelled" dataset, and based on the training, the machine predicts the output. Here, the labelled data specifies that some of the inputs are already mapped to the output.

- o Classification → categorical
- o Regression → linear relationship between input and output.

Classification

- (i) Random Forest Algorithm
- (ii) Decision Tree Algorithm
- (iii) Logistic Regression Algorithm
- (iv) Support Vector Machine Algorithm

Regression

- (i) Simple linear regression algorithm
- (ii) Multivariate Regression algorithm
- (iii) Decision Tree algorithm
- (iv) Lasso Regression.

2. Unsupervised Machine learning

Unsupervised learning is different from the Supervised learning technique, as its name suggests, there is no need for supervision.

It means, in unsupervised machine learning the machine is trained using the available dataset, and the machine predicts the output without any supervision.

o Clustering:- use when we want to find the inherent groups from the data.

It is a way to group the objects into a cluster such that objects with the most similarities remain in one group and have fewer or no similarities with the object groups. eg:- purchasing behaviour

→ k-mean clustering algorithm

→ Mean-shift algorithm

→ DBSCAN algorithm

→ Principal Component Analysis

→ Independent Component Analysis.

2) Association :-

Association rule learning is an unsupervised technique, which find interesting relationships among variable within a large dataset. The main aim of this learning algorithm is to find the dependency of one data item on another data item and map those variable accordingly so that it can generate maximum profit. eg:- Market Basket analysis, Basket analysis, web usage mining, continuous production etc.

Simple Linear Regression

Dataset:-

Linear Regression

Independent → dependent

Weight

Height

74

170

80

180

75

175.5

—

—

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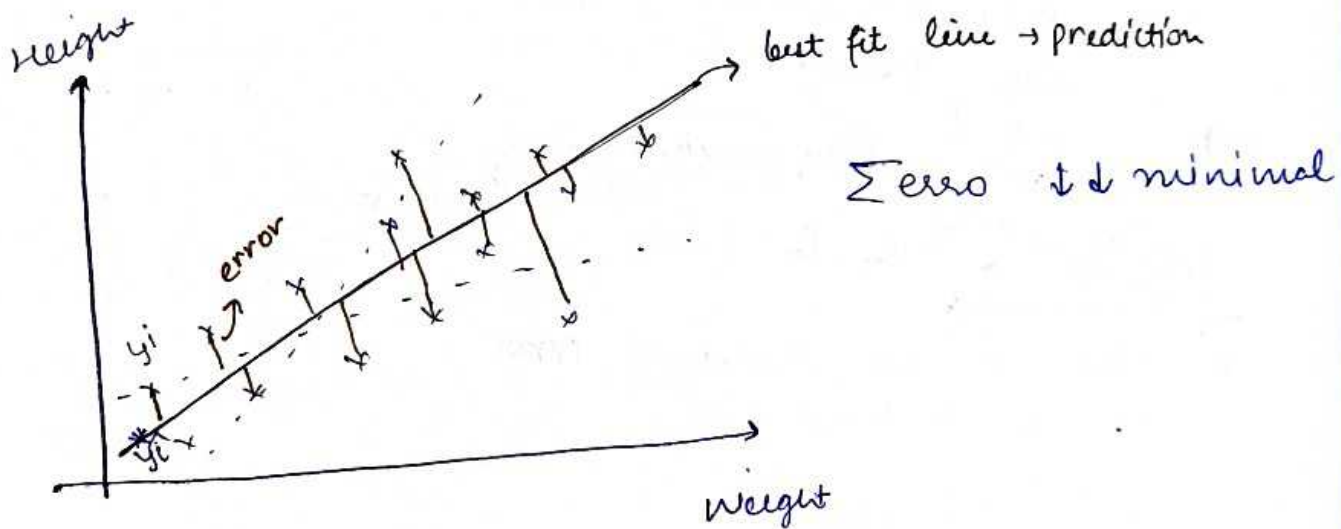
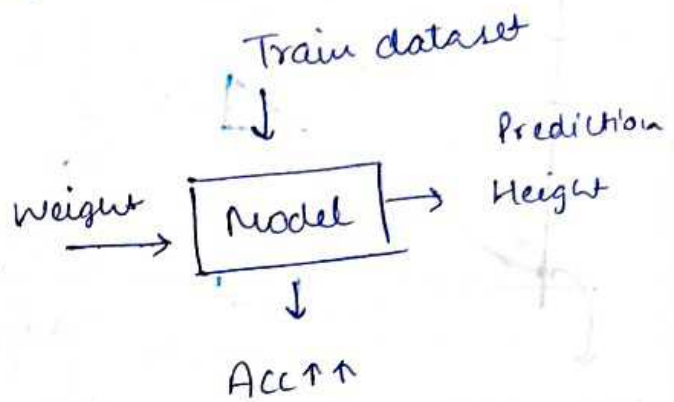
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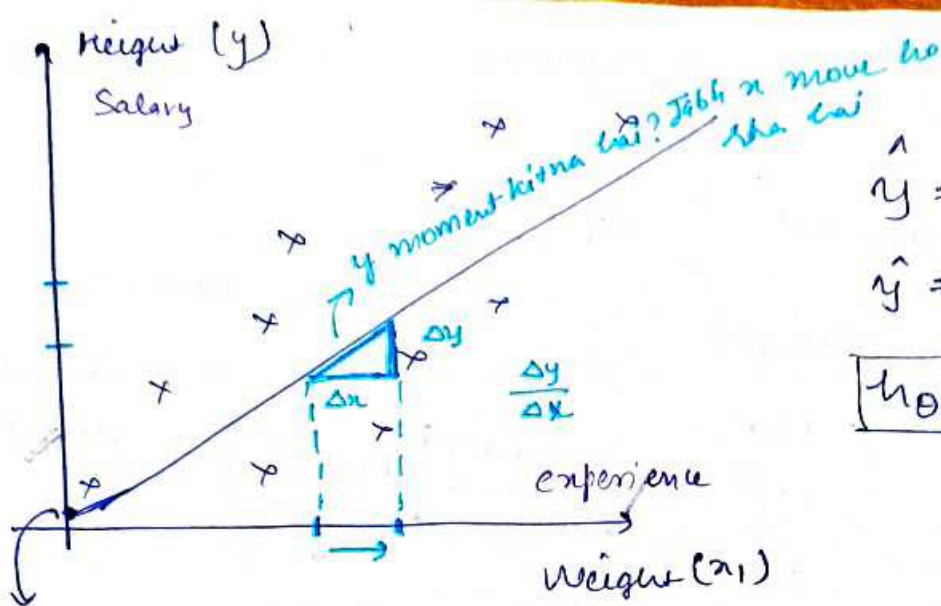
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Aim:- The main Aim of simple linear regression is to find best fit line in such a way when we do the ~~sum~~ summation (addition) of actual points and the predicted point or ~~sum~~ addition of the all point it should be minimal.



$$y = mx + c$$

$$\hat{y} = \beta_0 + \beta_1 x_1$$

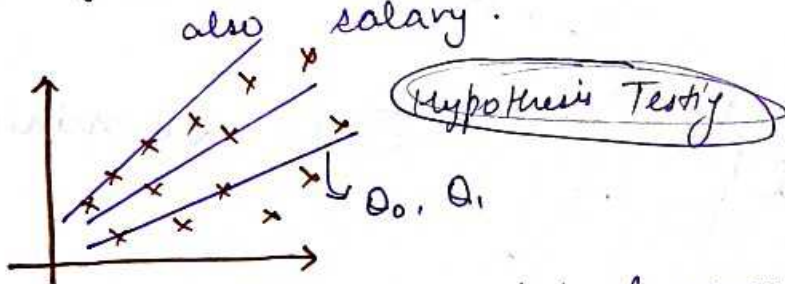
$$h_{\theta}(x) = \theta_0 + \theta_1 x_1$$

θ_0 = Intercept

θ_1 = Slope or Coefficient

Intercept :- when value of x is 0 then the line join the point is called Intercept.

eg:- where 0 experience person have also salary.



* which line has minimal error
 $\theta_0, \theta_1 \rightarrow$ Change
 Error $\downarrow \downarrow$

Cost function [Error]

$$J(\theta_0, \theta_1) = \frac{1}{n} \sum_{i=1}^n \left(\underset{\text{Actual}}{y_i} - \underset{\substack{\text{Predicted} \\ \downarrow \\ \hat{y}_i}}{h_{\theta}(x)_i} \right)^2 \quad \left[\begin{array}{l} \text{mean squared} \\ \text{error} \end{array} \right]$$

n = no. of data points

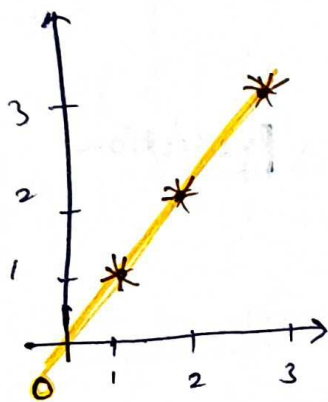
y_i = Actual value

$h_{\theta}(x)_i$ = predicted value

Final aim : [In order to get best fit line]

Minimize $J(\theta_0, \theta_1) = \frac{1}{n} \sum_{i=0}^n (y_i - h_{\theta}(x_i))^2$

* Changing the value θ_0 , and θ_1 for minimize and get best fit line



$$h_{\theta}(x) = \theta_0 + \theta_1 x$$

lets consider $\theta_0 = 0$

$$h_{\theta}(x) = \theta_1 x$$

let $\theta_1 = 1$

Dataset

x	y	h _θ (x)
1	1	1
2	2	2
3	3	3

$x=1 \Rightarrow h_{\theta}(x) = 1(1) = \textcircled{1}$

$x=2 \Rightarrow h_{\theta}(x) = 1(2) = \textcircled{2}$

$x=3 \Rightarrow h_{\theta}(x) = 1(3) = \textcircled{3}$

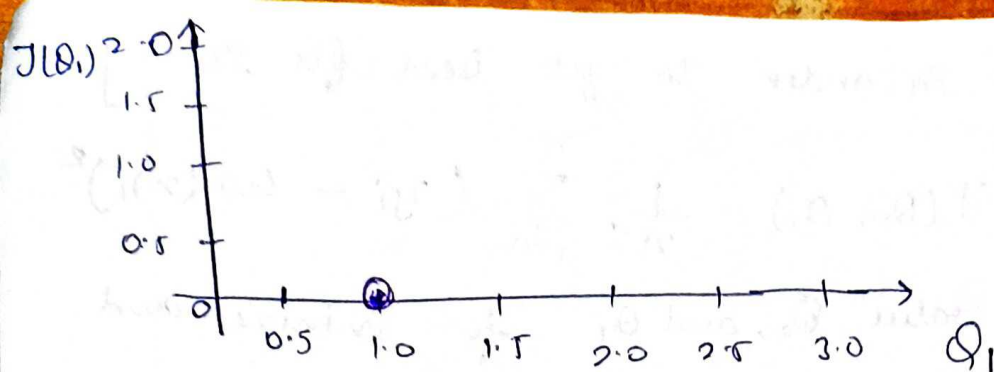
} Predicted

Cost function

$$J(\theta_1) = \frac{1}{n} \sum_{i=1}^n (y_i - h_{\theta}(x_i))^2$$

$$= \frac{1}{3} [(1-1)^2 + (2-2)^2 + (3-3)^2]$$

$$= 0$$



$$J(u) = 0$$

Let $\theta_1 = 0.5$ $n=1$

$$h(\theta_1) = 0.5$$

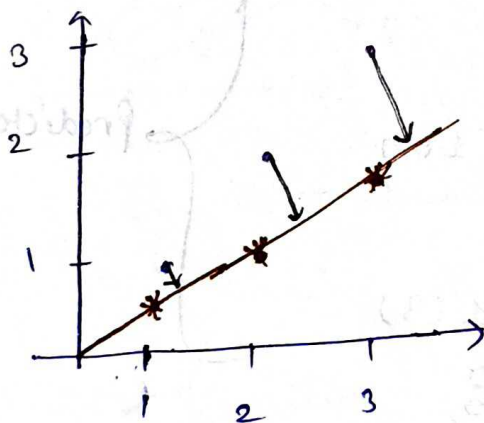
$$h(\theta_1) = 1.0$$

$$n=2$$

$$h(\theta_1) = 1.5$$

$$n=3$$

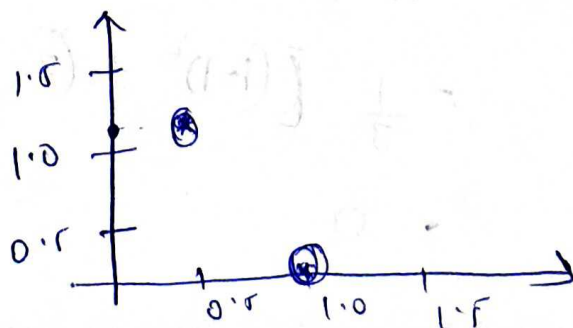
} Prediction



Cost fn

$$J(\theta_1) = \frac{1}{3} [(1 - 0.5)^2 + (2 - 1)^2 + (3 - 1.5)^2]$$

$$= 1.16$$



let $Q_1 = 0$

$h_0(x) = 0$

$x = 1$

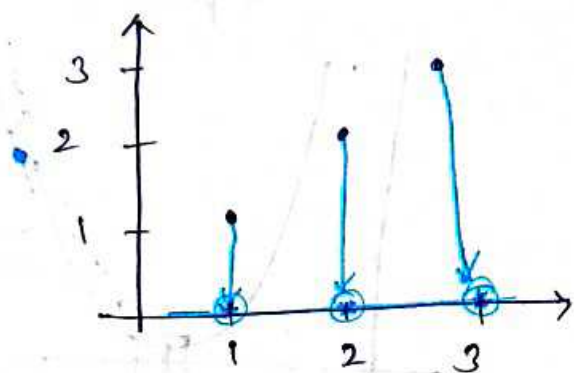
$h_0(x) = 0$

$x = 2$

$h_0(x) = 0$

$x = 3$

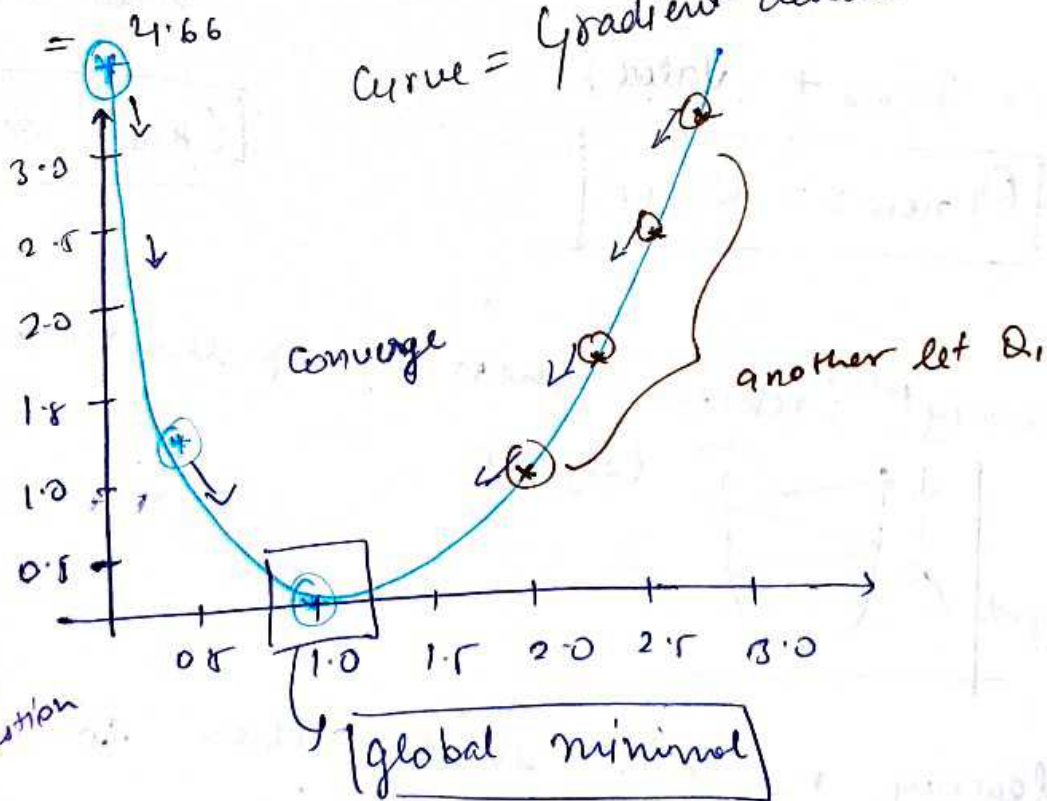
} Prediction



Cost function

$$J(Q_1) = \frac{1}{3} [(1-0)^2 + (2-0)^2 + (3-0)^2]$$

$= 4.66$



Interview question

* Convergence Algorithm :- {Optimise the change of Q_0 to Q_1 to global minimum}

Repeat until Convergence

\mathcal{L}

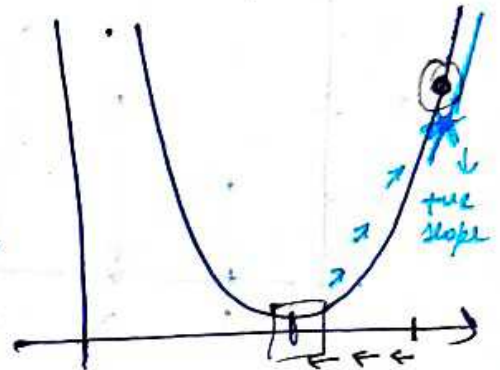
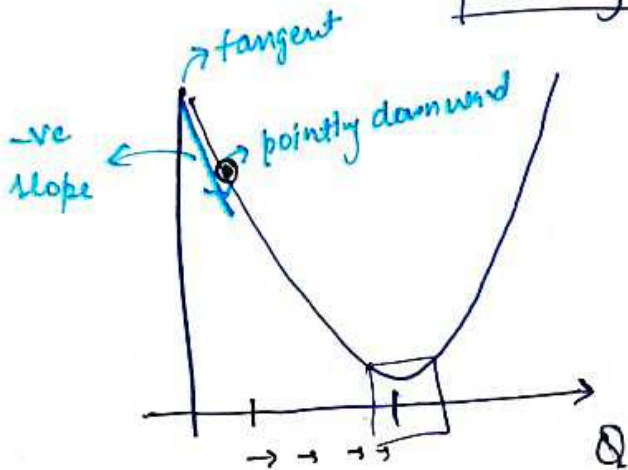
$$\Theta_j : \Theta_j - \mathcal{L} \left[\frac{\partial J(\Theta_j)}{\partial \Theta_j} \right]$$

\Rightarrow Derivative

\Downarrow
slope of a point

usually Learning rate = 0.01

Learning rate



$$\Theta_1 = \Theta_1 - \mathcal{L}(-ve)$$

$$\Theta_{1\text{ new}} = \Theta_{1\text{ old}} + (\text{value})$$

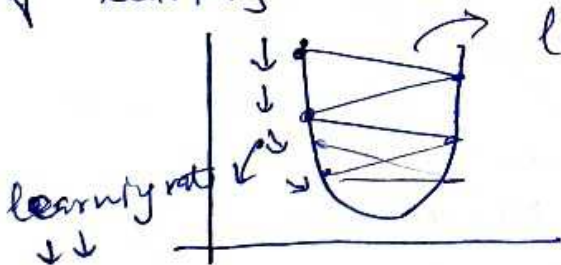
$$\Theta_{1\text{ new}} > \Theta_{1\text{ old}}$$

$$\Theta_{1\text{ new}} = \Theta_{1\text{ old}} - \mathcal{L}(\text{+ve})$$

$$\Theta_{1\text{ new}} = \Theta_{1\text{ old}} - (\text{value})$$

$$\Theta_{1\text{ new}} < \Theta_{1\text{ old}}$$

if learning rate $\uparrow\uparrow$ increase then jump the value



if learning rate $\downarrow\downarrow$ is small then converge the value is slow.

Learning rate \Rightarrow Speed of Convergence

Conclusion:- Repeat the step until convergence
 ξ

$$\theta_j := \theta_j - \xi \frac{\partial}{\partial \theta_j} J(\theta_0, \theta_1)$$

ξ

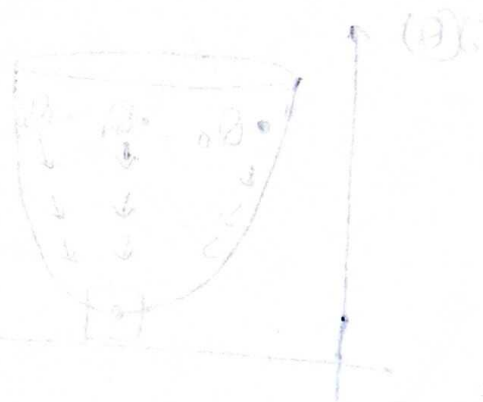
$$J(\theta_0, \theta_1) = \frac{1}{n} \sum_{i=1}^n (y_i - h_{\theta}(x_i))^2$$

\Downarrow

mean squared error



$$h_{\theta}(x) = \theta_0 + \theta_1 x$$



Multiple Linear Regression

House Pricing Dataset

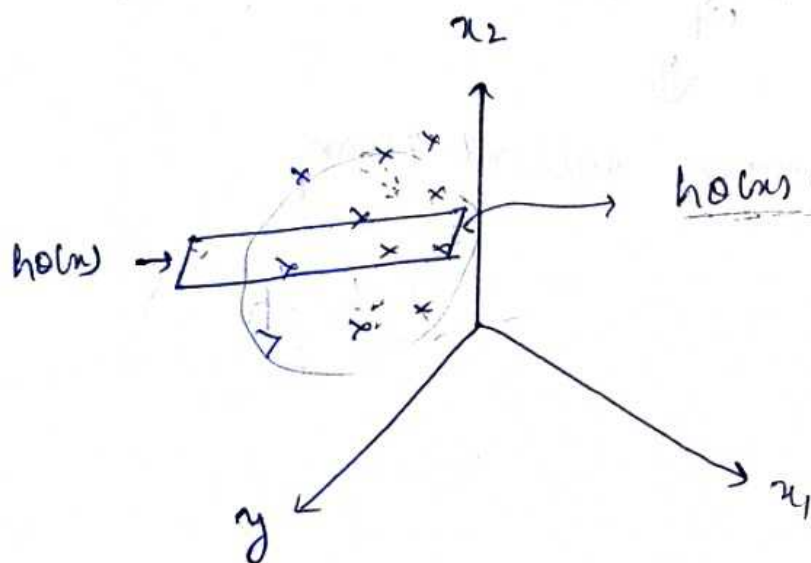
Independent
House Pricing Dataset

No. of Rooms x_1 Size of rooms x_2

Dependent

Price y

Price $y = 10$



$$h_0(x) = \theta_0 + \theta_1 x_1 + \theta_2 x_2$$

$\theta_1, \theta_2 \Rightarrow$ slope of coefficient

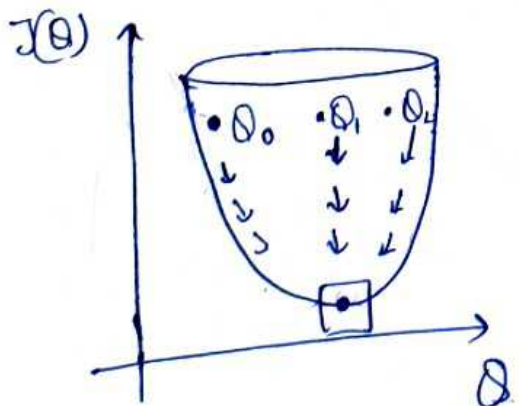
$\theta_0 \Rightarrow$ Intercept

Generic Equation Multiple regression :-

$$h_0(x) = \theta_0 + \theta_1 x_1 + \theta_2 x_2 + \theta_3 x_3 + \dots + \theta_n x_n$$

Sample linear regression

$$h_0(x) = \theta_0 + \theta_1 x_1$$

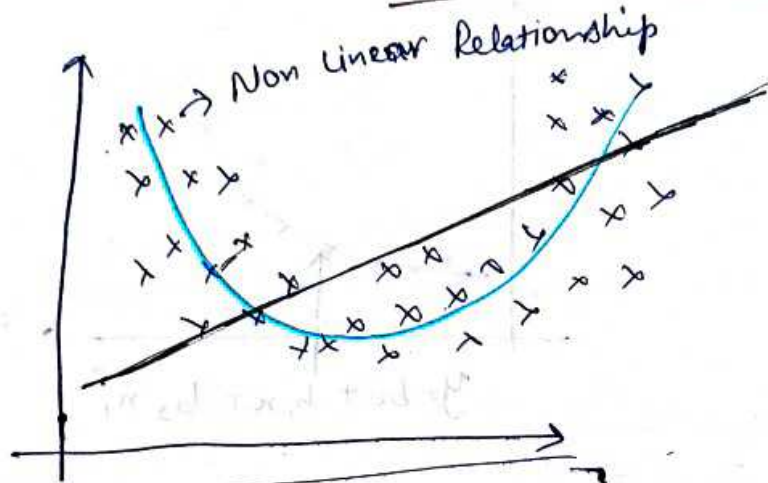


Polynomial Regression

Simple Linear Regression

$$h_0(x) = \theta_0 + \theta_1 x_1$$

error ↑



Polynomial Regression

Polynomial degrees

Simple polynomial Regression

Polynomial degree = 0

$$h_0(x) = \theta_0 x_1^0 = \theta_0 x_1^0 = \theta_0$$

⇒ Constant

Polynomial degree = 1

$$h_0(x) = \theta_0 x_1^0 + \theta_1 x_1^1$$

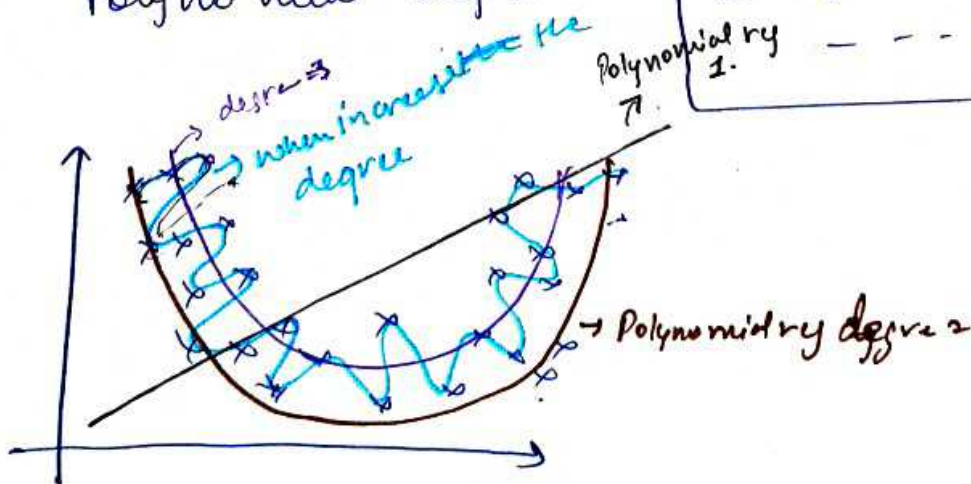
Simple Linear Regress

Polynomial degree = 2

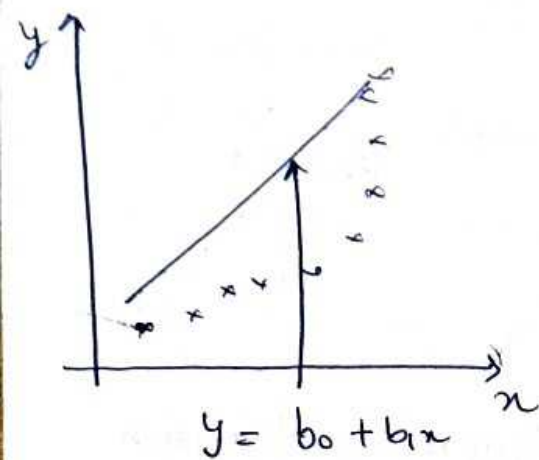
$$h_0(x) = \theta_0 x_1^0 + \theta_1 x_1^1 + \theta_2 x_1^2$$

Polynomial degree = n

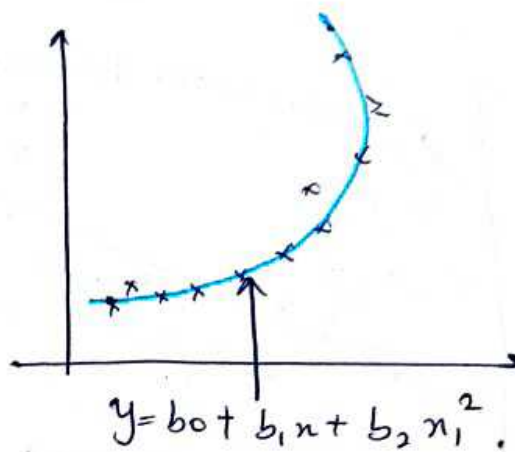
$$h_0(x) = \theta_0 x_1^0 + \theta_1 x_1^1 + \theta_2 x_1^2 + \dots + \theta_n x_1^n$$



Simple linear reg



Polynomial model



Multiple polynomial Regression

$$h_0(x) = \theta_0 + \theta_1 x_1 + \theta_2 x_2 + \theta_3 x_3 \quad \left\{ \begin{array}{l} \text{multiple linear} \\ \text{regression} \end{array} \right\}$$

Polynomial degree = 2

$$h_0(x) = \theta_0 + \theta_1 x_1 + \theta_2 x_2 + \theta_3 x_3 + \theta_4 x_1^2 + \theta_5 x_2^2 + \theta_6 x_3^2$$

Performance Metrics Used in Regression

① R squared

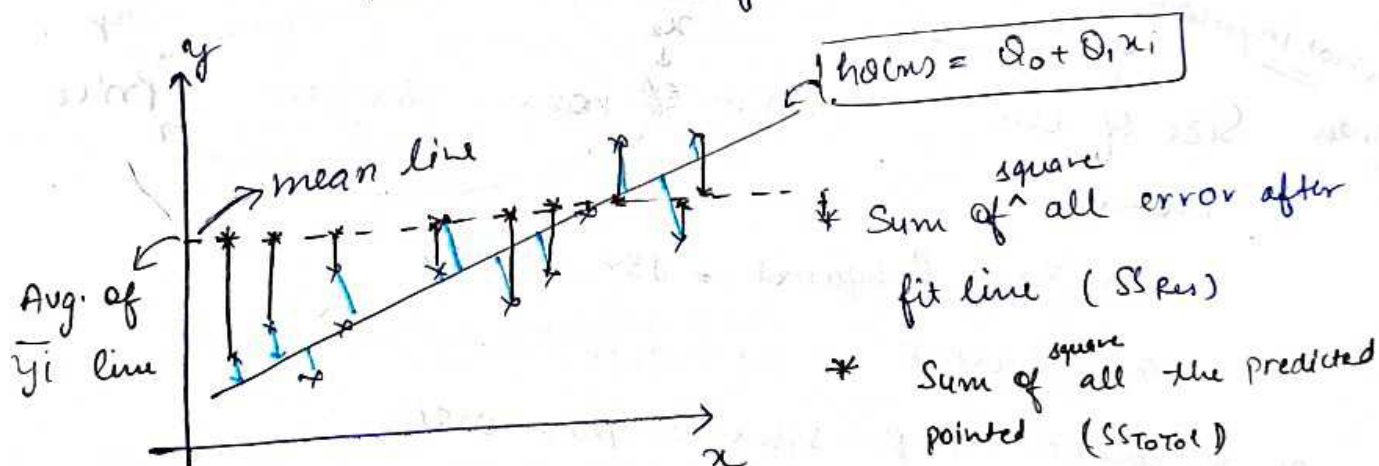
② Adjusted R squared

R squared

$$R_{\text{squared}} = 1 - \frac{SS_{\text{Res}}}{SS_{\text{Total}} \text{ (Average of } \bar{y}_i \text{ line)}}$$

SS_{Res} = Sum of square Residual (Error)

SS_{Total} = Sum of ^{square} \hat{y}_{Total}



$$R_{\text{squared}} = 1 - \frac{\sum_{i=1}^n (y_i - \hat{y}_i)^2}{\sum_{i=1}^n (y_i - \bar{y}_i)^2}$$

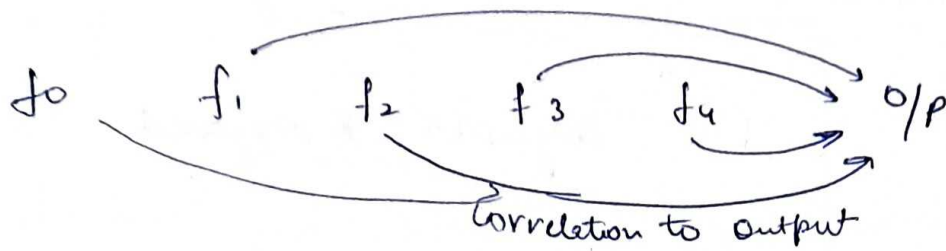
\hat{y}_i is $h_0(n)$

SS_{Res} \Rightarrow small value

\Rightarrow large value

$$R_{\text{squared}} = 1 - \frac{\sum_{i=1}^n (y_i - \hat{y}_i)^2}{\sum_{i=1}^n (y_i - \bar{y})^2}$$

R squared ranges between 0 to 1



$$R \text{ squared} = 75\% = 0.75$$

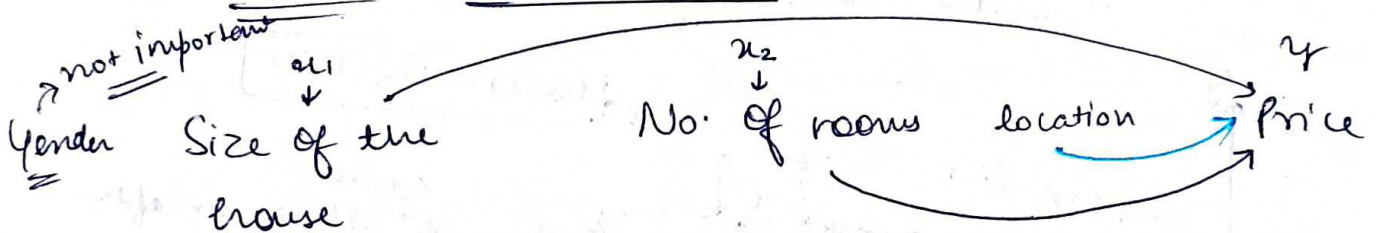
$$R \text{ squared} = 80\%$$

No. of feature $\uparrow \rightarrow$ Output
Correlation

$$R \text{ squared} = 90\% \uparrow \uparrow$$

* add any feature
r squared value increase Accuracy also $\uparrow \uparrow$

② Adjusted R squared



$$n_1, n_2 \rightarrow R \text{ squared} = 85\% = 0.85$$

$$n_1, n_2, \text{location} \rightarrow R \text{ squared} = 90\% = 0.90$$

$$n_1, n_2, \text{location}, \text{Gender} \rightarrow R \text{ squared} = 91\% = 0.91$$

$$\text{Adjusted} = 1 - \frac{(1 - R^2)(N - 1)}{N - P - 1}$$

N = No. of datapoints

R^2 = R squared

P = No. of Independent feature

Adjusted R squared $<$ R squared

$$R^2 = 80\%$$

$$\text{Adjusted} = 75\%$$

$p=3$

$$R^2 = 85\%$$

$$\text{Adjusted} = 78\%$$

$p=4$

$$R^2 = 87\%$$

$$\text{Adjusted} = 76\%$$

↓

↓

* Independent feature is not that important

* Use both R^2 and Adjusted R^2

MAE, MSE, RMSE [loss function]

- ① Mean Squared Error (MSE)
- ② Mean Absolute Error (MAE)
- ③ Root Mean Squared Error (RMSE)

① Mean Squared Error (MSE)

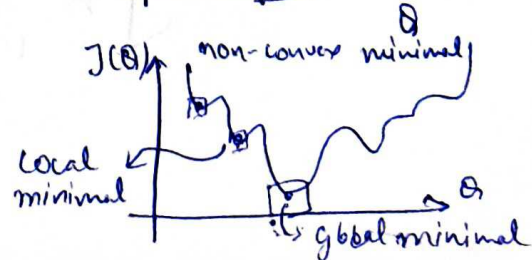
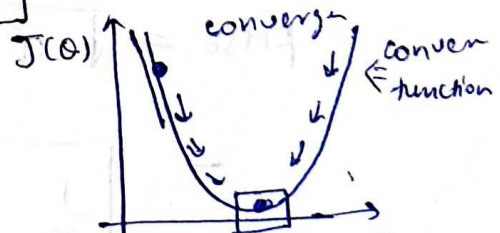
$$MSE = \frac{1}{n} \sum_{i=1}^n (y_i - h_0(x)_i)^2$$

$$MSE = \frac{1}{n} \sum_{i=1}^n (y_i - \hat{y}_i)^2$$

→ Quadratic equation

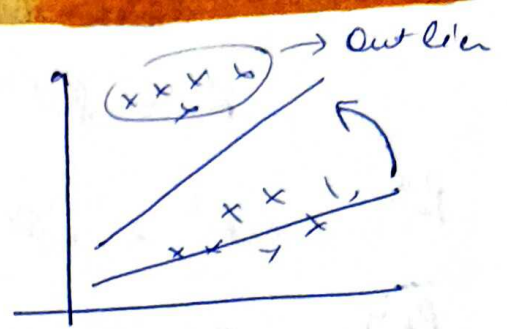
Advantage

- (1) This equation is differentiable
- (2) It has only one local or global minima



Disadvantage

- ① Not Robust to outlier.
- ② It is not in the same unit.



② Mean Absolute Error (MAE)

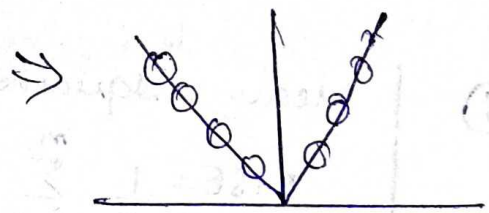
$$\boxed{MAE = \frac{1}{n} \sum_{i=1}^n |y - \hat{y}|}$$

Advantage

- ① Robust to outlier.
- ② It is the same unit.

Disadvantage

- ① Convergence usually takes more time



③ Root means squared error (RMSE)

$$RMSE = \sqrt{MSE}$$

$$= \sqrt{\frac{1}{n} \sum_{i=1}^n (y_i - \hat{y}_i)^2}$$

Advantage

- ① Same Unit
- ② Differentiable

disadvantage

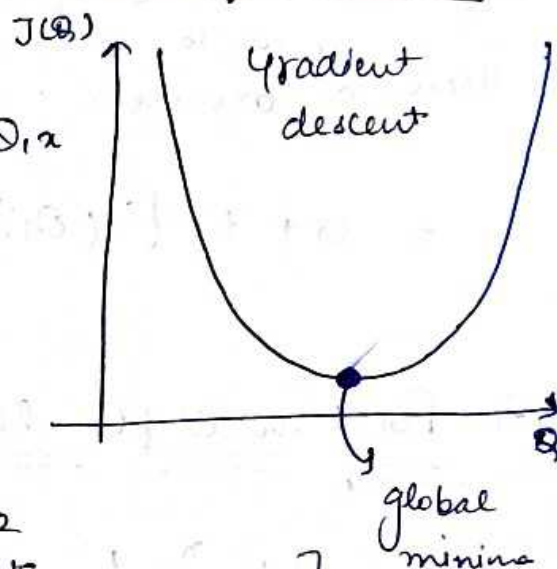
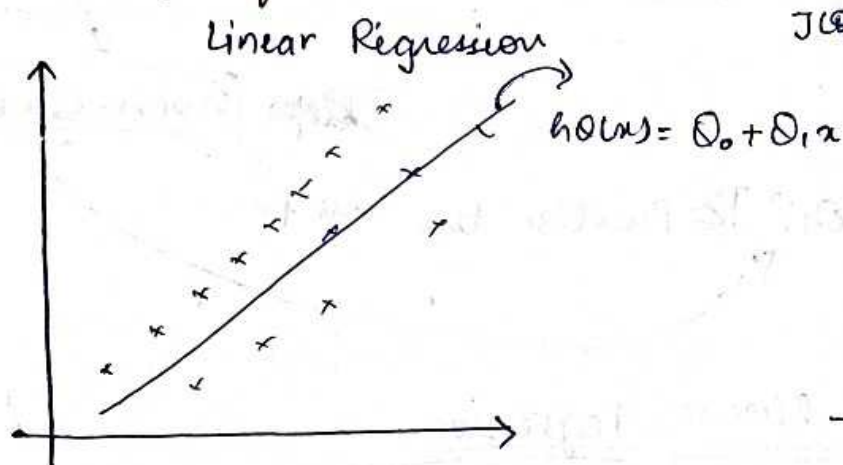
- ① Not Robust to outliers

Note:- Linear Regression

Performance metrics:- R^2 and Adjusted R^2 \rightarrow Acc. of model

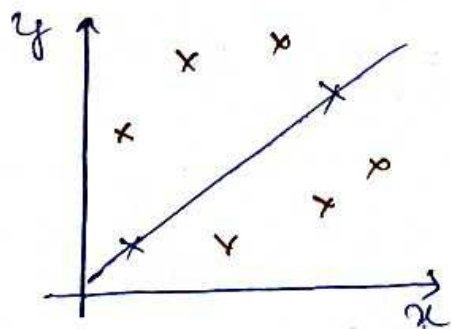
Cost function \rightarrow Error \rightarrow MSE, MAE, RMSE

Ridge, Lasso, Elastic Regression



$$\text{cost fn} = \frac{1}{n} \sum_{i=1}^n (y_i - h_0(x)_i)^2 \quad [\text{mean squared error}]$$

① Ridge Regression (L_2 Regularization) \rightarrow Reducing Overfitting



Error = 0 (Train Data)

Error = $\uparrow\uparrow$ (Test Data)

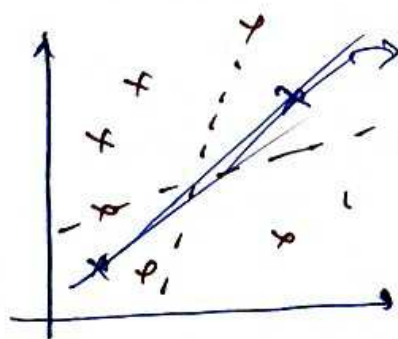
Data
Train Test

Overfitting

Train \rightarrow Acc $\uparrow\uparrow \rightarrow R^2$

Test \rightarrow Acc $\downarrow\downarrow \rightarrow R^2$

* In Ridge Regression, Error is not 0. Error is zero nhi hone dena. [need little bit error]



Error = 0

Ridge Regression Error $\neq 0$

if (zero error) then add \uparrow

$$\text{Cost fn} = \frac{1}{n} \sum_{i=1}^n (y_i - \hat{y}_i)^2 + \lambda \sum_{i=1}^n (\text{slope})^2$$

$\lambda \rightarrow$ Hyper parameter

Let error is 0, and $\lambda = 1$

then ^{according to} formula

slope = linear regression

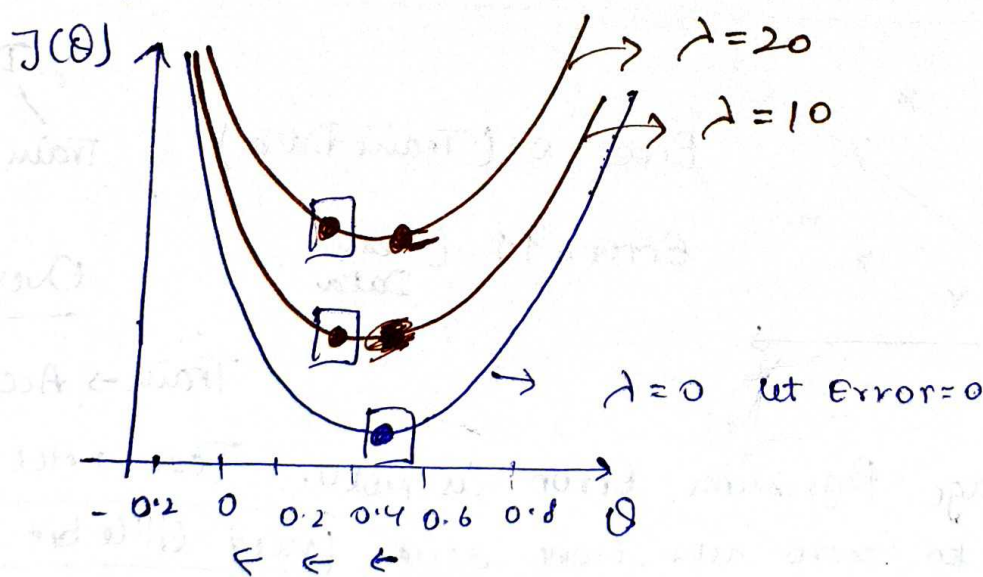
~~slope~~ $\boxed{h_0(x) = \theta_0 + \theta_1 x}$

$$= 0 + 1 [(\theta_1)^2] \leftarrow \text{penalize the cost fn.}$$

* For multiple linear regression

$$\text{cost fn} = \frac{1}{n} \sum_{i=1}^n (y_i - \hat{y}_i)^2 + \lambda [(\theta_1)^2 + (\theta_2)^2 + (\theta_3)^2]$$

* relation of slope and λ



② Lasso Regression (λ , Regularization) \rightarrow Feature Selection

$$\text{Cost fn: } \frac{1}{n} \sum_{i=1}^n (y_i - \hat{y}_i)^2 + \boxed{\lambda \sum_{i=1}^n |\text{slope}|}$$

$$h_0(x) = \theta_0 + \theta_1 x_1 + \theta_2 x_2 + \theta_3 x_3$$

$$= 0.52 + 0.65x_1 + 1.5x_2 + \boxed{0.2x_3}$$

feature removal \rightarrow cancel \rightarrow decrease and become zero

$x_2 \rightarrow 1 \text{ unit}$
 $y \rightarrow 1.5x_2$
 $x_3 \rightarrow 1 \text{ unit}$
 $y = 0.2x_3$

Predict with two features \rightarrow feature selection

$$\text{Cost fn} = \frac{1}{n} \sum_{i=1}^n (y_i - \hat{y}_i)^2 + \boxed{\lambda \sum_{i=1}^n |\text{slope}|} \quad \lambda = 1$$

$$= \text{Error} + \frac{1}{2} [\theta_1 + \theta_2 + \theta_3]$$

