

Is it a DAG?

2022-03-28

Contents

- 1 John's function 1
- 2 Georges' function 1
- 3 Random triangularizable matrix 2
- 4 Timing tests 2

Comparing different algorithms to find a permutation that, applied to both rows and columns of a square matrix with zeros on the diagonal, results in a lower triangular matrix.

1 John's function

```
isLowerTriangular <- function(X){
  all(0 == X[upper.tri(X)])
}

triangularize <- function(X){
  if (is.null(rownames(X))) rownames(X) <- 1:nrow(X)
  if (isLowerTriangular(X)) return(rownames(X))
  tri <- function(X){ # recursion helper function
    if (length(X) == 0) return()
    diag(X) <- 0
    roots <- which(rowSums(X) == 0)
    c(rownames(X)[roots], tri(X[-roots, -roots, drop=FALSE]))
  }
  perm <- tri(X)
  if (length(perm) != nrow(X)) stop("matrix cannot be triangularized")
  perm
}
```

2 Georges' function

```
to_dag <- function(mat){
  # check that mat has unique column and row names
  find_leaves <- function(m) { # wasteful because we only need for find one
                                # 'orphan', not all possible 'orphans'
    sumabs <- function(x) sum(abs(x))
    diag(m) <- 0 # in case they're used for epsilons
    which(apply(m,2,sumabs)==0)
  }
}
```

```

}
if(nrow(mat) != ncol(mat)) stop('matrix must be square')
if(any(sort(colnames(mat)) != sort(rownames(mat)))) stop('colnames not same as rownames')
if(length(unique(colnames(mat))) != length(colnames(mat))) stop('names not unique')
mat <- mat[colnames(mat), colnames(mat)]
if(sum(abs(mat[row(mat) < col(mat)])) == 0) {
  # matrix already lower diagonal
  class(mat) <- unique(c('dag', class(mat)))
  return(mat)
}
ret <- mat
dag_perm <- rep('', nrow(mat))
for(i in 1:nrow(ret)) {
  ll <- find_leaves(mat)
  if(length(ll) == 0) return(FALSE)
  dag_perm[i] <- names(ll[1])
  if(i < nrow(ret)) mat <- mat[-ll[1], -ll[1], drop = FALSE]
}
ret <- ret[rev(dag_perm), rev(dag_perm)]
class(ret) <- unique(c('dag', class(ret)))
ret
}

```

3 Random triangularizable matrix

```

rdag <- function(size) {
  x <- matrix(0, size, size)
  x[lower.tri(x)] <- rnorm(size*(size-1)/2)
  perm <- sample(size)
  x[perm, perm]
}

```

4 Timing tests

```

testn <- function(fun, size, reps = 1000) {
  system.time(
    lapply(seq_len(reps), function(i) fun(rdag(size)))
  )
}

```

```
testn(triangularize, 3)
```

```

      user  system elapsed
0.078   0.003   0.082

```

```
testn(to_dag, 3)

    user  system elapsed
    0.08   0.00   0.08

testn(triangularize, 5)

    user  system elapsed
    0.081  0.000   0.082

testn(to_dag, 5)

    user  system elapsed
    0.061  0.000   0.062

testn(triangularize, 20)

    user  system elapsed
    0.290  0.000   0.291

testn(to_dag, 20)

    user  system elapsed
    0.071  0.000   0.070

testn(triangularize, 100)

    user  system elapsed
    5.607  0.003   5.615

testn(to_dag, 100)

    user  system elapsed
    0.283  0.001   0.283
```