

Maximin (A)

if $|A| = 2$

return ($\max(A[1], A[2])$, $\min(A[1], A[2])$) $O(1)$

else

Dividir A en dos subarreglos A_1 y A_2
iguales (cada uno con mitad de elementos)

$$(\max_1, \min_1) = \text{Maximin}(A_1) \quad O(n/2)$$

$$(\max_2, \min_2) = \text{Maximin}(A_2) \quad O(n/2)$$

return ($\max(\max_1, \max_2)$, $\min(\min_1, \min_2)$) $O(1)$

$$T(n) = \begin{cases} 2T(n/2) + 1, & n \geq 2 \\ 1 & ; n = 2 \end{cases}$$

$$1. \ f(n) = O(n^{\log_b a - \varepsilon}), \ \varepsilon > 0$$

$$1 = O(n^{\lg 2 - \varepsilon}), \ \varepsilon > 0$$

$$1 = O(n^{1-\varepsilon}) \checkmark, \ \varepsilon = 0.1$$

$$T(n) = \tilde{O}(n^{\log_2 \varepsilon})$$

$$\boxed{\tilde{O}(n)}$$

FMCS (A, low, mid, high)

left-sum = -∞ $O(1)$

sum = 0 $O(1)$

for $i = \frac{mid}{2}$ down to low $O(n/2)$

sum += A[i] $O(1)$

if sum > left-sum $O(1)$

left-sum = sum $O(1)$

max-left = i $O(1)$

right-sum = -∞ $O(1)$

sum = 0 $O(1)$

for $j = mid+1$ to high $O(n/2)$

sum += A[j] $O(1)$

if sum > right-sum $O(1)$

right-sum = sum $O(1)$

max-right = j $O(1)$

return (max-left, max-right, left-sum + right-sum)

$O(n/2) \approx [O(n)]$

FMS(A, low, high)

Find Max Subarray (A, low, high) : ~~Inducted~~

if $\text{high} == \text{low}$

 return (low , high , $A[\text{low}]$)

else

$\text{mid} = \lfloor (\text{low} + \text{high})/2 \rfloor$

$O(1)$

$O(1)$

$O(1)$

$(\text{ll}, \text{lh}, \text{ls}) = \text{FMS}(A, \text{low}, \text{mid})$ $O(\frac{n}{2})$

$(\text{rl}, \text{rh}, \text{rs}) = \text{FMS}(A, \text{mid}+1, \text{high})$ $O(\frac{n}{2})$

$(\text{cl}, \text{ch}, \text{cs}) = \text{FMCS}(A, \text{low}, \text{mid}, \text{high})$ $O(n)$

if $\text{ls} \geq \text{rs}$ and $\text{ls} \geq \text{cs}$

 return ($\text{ll}, \text{lh}, \text{ls}$)

$O(1)$

elseif $\text{rs} \geq \text{ls}$ and $\text{rs} \geq \text{cs}$

$O(1)$

 return ($\text{rl}, \text{rh}, \text{rs}$)

$O(1)$

else

 return ($\text{cl}, \text{ch}, \text{cs}$)

$O(1)$

$$T(n) = \begin{cases} 2T(\frac{n}{2}) + O(n), & n > 1 \\ 1, & n = 1 \end{cases}$$

caso 2: $f(n) = \Theta(n^{\log_b a})$

$$O(n) = \Theta(n^{\log_2 e})$$

$$O(n) = \Theta(n^a)$$

$$\Theta(n^{\log_b a} \log n)$$

$$\boxed{\Theta(n \log n)}$$