A Diophantine equation

Problem

Find the smallest positive integers a, b and c such that

$$a^2 = 2b^3 = 3c^5.$$

What can you say about other solutions to this equation?

Relevance

NA3   What are highest common factors and why do they matter?