MA2SO Assignment 4 8.0322 la.) Let di, dz >0 where $D = \begin{pmatrix} -d_1 & 0 \\ 0 & -d_2 \end{pmatrix} \in \mathbb{R}^{2\times 2}$ then trace (D) = -d1 - d2 and dc+ (D) = d1d2 > 0. Since trace (D) <0 and det (D) >0 the the system is stable and will converges to $\begin{pmatrix} 9!' \\ 92' \end{pmatrix} = \begin{pmatrix} -d_1 & 0 \\ 0 & -d_2 \end{pmatrix} \begin{pmatrix} 9_1 \\ 9_2 \end{pmatrix} = -d_1 t$ y'=-diy => y = Ae y2:-d2y2 => y2 = Be -d2E Therefore 11- 4 (0): (2,-3) T they

y(E) = { 2 e - d2 e } -3 e

2a.) If a is a stationary point then
$$V(a) = \{0\}$$

Thus

$$V_{5}\left(1+u_{1}^{2}\right)-\mu u_{1}=0$$

1 + U1 = MU1 U2 V6

Now, if U,2 = CX Uz then

$$\frac{1+1}{U_2}\left(\frac{XU_2}{Vb}\right) = \mu U_1$$

1 + 0 = 1001 Vb Vb

$$\frac{Vb}{M}\left(\begin{array}{c} 1+X\\ Vb \end{array}\right)=U_1$$

U, = Vb - X

$$U_2 = \frac{Vb}{X} \frac{Vb^2}{Vb} \left(\frac{1+x}{Vb} \right)^2$$

Now, where U= (U1, U2) is a stationing Qui (Vb (1+412) - 1441 = 241 - 14 Qu, V2 = 2 16 ly Ouz VI = - 412 Our V2 = - 0 Therefore 2 rb U1

$$B_{11} = 2V_b \propto \mu^2 \left(1 + \alpha \right)^{-1}$$

$$\mu V_b^3 \left(1 + \alpha \right)^{-1}$$

$$|3_{21} = 2v5^2 \left(1 + \alpha \right)$$

$$B_{12} = -v_{5}^{2} \alpha^{2} u^{4} (1 + \alpha)^{-2}$$
 $M^{2} v_{5}^{6} v_{5}^{6}$

$$B_{12} = -\alpha^2 \mu^2 \left(1 + \alpha \right)^{-2}$$

b.)

$$\frac{1}{\sqrt{2}} + \sqrt{2} = 2 \times \mu \times (1 + x \times 1)^{-1} - \alpha - \mu \times (1 + x \times 1)^{-1} - \alpha \times (1 + x \times 1)^{-1} \times (1$$

Take (X, Vb, M) = (1,1,1) They

trace B = 2 - 1 - 1

2

trace 13 = -

de+B = 2-2 +1

2_

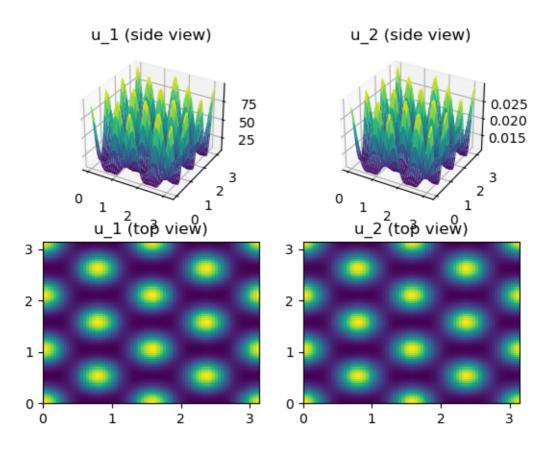
det 13 = 1

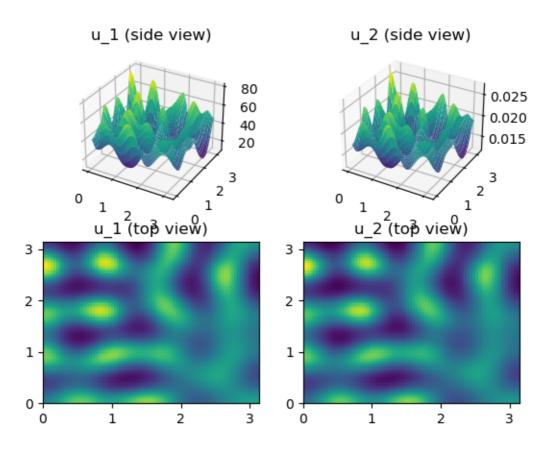
Since trace B < 0 and det B > 0 theretore the system is stable

$$\left(-\alpha - dz |u|^2\right)$$

$$det A = \begin{pmatrix} 2\alpha\mu & -\mu - \alpha_1 |\mu|^2 \\ \nu b (\nu b + \alpha) \end{pmatrix}$$

$$(-\alpha - \alpha_2 |u|^2)$$





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def react fct (uval):
    # problem dependent function for reaction terms
     ************* TODO ***********
   # implement the correct reaction function
    alpha = 1500 # Values from 3b
    rb = 0.015
    mu = 35
    u1 = uval[0]
    u2 = uval[1]
    x = rb*(1+(u1*u1)/u2) - mu*u1
    y = rb*u1*u1 - alpha*u2
    return x,y
```