

```

0 #
1 #
2 #
3 #
4 #
5 #
6 #
7 import zipfile
8 import os
9
10 fmux = zipfile.ZipFile("CSTR_CSTR_Opt2.fmux", 'r')
11 fmux.extract('modelDescription.xml', '.')
12 from casadi import *
13 ivp = DaeBuilder()
14 ivp.parse_fmi("modelDescription.xml")

```

Warning: Skipped TiXmlNode::TINYXML_DECLARATION

Error:

CasAdi warning: "opt:PointConstraints not supported, ignored" issued on line 327 of file "/home/travis/build/casadi/binaries/casadi/casadi/core/misc/dae_builder.cpp".
 CasAdi warning: "opt:PointConstraints not supported, ignored" issued on line 329 of file "/home/travis/build/casadi/binaries/casadi/casadi/core/misc/dae_builder.cpp".

Let us have a look at the flat optimal control problem:

```

18 print ivp

DAE(#s = 4, #x = 0, #z = 0, #q = 1, #y = 0, #p = 0, #d = 22, #u = 1)
Variables
{
  t = t
  s = [cstr.T, cstr.Tc, cstr.c, q]
  q = [lterm]
  d = [cstr.F0, cstr.c0, cstr.F, cstr.T0, cstr.r, cstr.k0, cstr.EdivR,
       cstr.U, cstr.rho, cstr.Cp, cstr.dH, cstr.V, cstr.c_init, cstr.T_init,
       c_ref, T_ref, Tc_ref, q_c, q_T, q_Tc, startTime, finalTime]
  u = [u]
}
Dependent parameters
cstr.F0 == 0.00166667
cstr.c0 == 1000
cstr.F == 0.00166667
cstr.T0 == 350
cstr.r == 0.219
cstr.k0 == 1200000000
cstr.EdivR == 8750
cstr.U == 915.6
cstr.rho == 1000
cstr.Cp == 239
cstr.dH == -50000
cstr.V == 100
cstr.c_init == 1000
cstr.T_init == 350
c_ref == 500
T_ref == 320
Tc_ref == 300
q_c == 1
q_T == 1

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q_Tc == 1
startTime == 0
finalTime == 150

Fully-implicit differential-algebraic equations
0 == MX((der_cstr.c-(((cstr.F0*(cstr.c0-cstr.c))/cstr.V)-((cstr.k0*cstr.c)
*exp((-cstr.EdivR/cstr.T))))))
0 == MX((der_cstr.T-(((cstr.F0*(cstr.T0-cstr.T))/cstr.V)-(((cstr.dH/(
cstr.rho*cstr.Cp))*cstr.k0*cstr.c)*exp((-cstr.EdivR/cstr.T))))))
+(((2.*cstr.U)/((cstr.r*cstr.rho)*cstr.Cp))*(cstr.Tc-cstr.T))))
0 == MX((u-cstr.Tc))
0 == MX((q-(2.*u)))

Quadrature equations
der_lterm == (0.0001*((q_c*sqr((c_ref-cstr.c)))+(q_T*sqr((T_ref-cstr.T)))
+(q_Tc*sqr((Tc_ref-cstr.Tc))))

```

```

Initial equations
0 == (cstr.c-cstr.c_init)
0 == (cstr.T-cstr.T_init)
ivp.make_explicit()

```

Let us extract variables for the states, the control and equations

```

21 x = vertcat(*ivp.x)
22 u = vertcat(*ivp.u)
23 f = vertcat(*ivp.ode)
24 L = vertcat(*ivp.quad)
25 l = vertcat(*ivp.init)
26 print 5*sin(f[0])

(5*sin((zeros(2x2, diagonal)[:2] += ones(2x1, dense))' [0]
\(((0.00166667*(1000-cstr.c))/100)-((1200000000*cstr.c)*exp((-8750/
cstr.T))))))

27 print jacobian(f,x)

@1=8750, @2=(@1/cstr.T), @3=exp((-@2)), @4=1200000000, @5=vertsplite(ones(2
x1, 1 nnz)){0}, @6=0.00166667, @7=vertsplite(ones(2x1, 1 nnz)){1}, @8=
zeros(2x2, diagonal)[:2] += ones(2x1, dense))', @9=horzsplit((@8[0]\
horzcat(((-(@3*(@4*@5)))-(0.01*(@6*@5))), -(4*cstr.c)*(@3*((@2/cstr
.T)*@7))))), @10=(@1/cstr.T), @11=exp((-@10)), @12=-2.51046e+08, @13
=horzsplit((@8[1]\horzcat((-@11*(@12*@5))), (((-(@12*cstr.c)*(@11*((
@10/cstr.T)*@7))))-(0.01*(@6*@7))-(0.034986*@7))))), zeros(2x2, dense
)[:4:2] = vertcat(@9[0], @13[0])[1:5:2] = vertcat(@9[1], @13[1]))'

28 print hessian(L,x)

(MX(@1=0.0001, @2=vertsplite(ones(2x1, dense)), @3=vertcat((-@1*(2.*(-@2
{0}))), (-@1*(2.*(-@2{1})))), zeros(2x2, diagonal)[:2] = @3[:2] =
@3)'), MX(@1=0.0001, vertcat((-@1*(2.*(500-cstr.c))), (-@1
*(2.*(320-cstr.T))))))

29 ubx = ivp.max(x)
30 lbx = ivp.min(x)
31 ubu = ivp.max(u)
32 lbu = ivp.min(u)
33 x0 = ivp.guess(x)

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34 u0 = ivp.guess(u)
35 tf = 150.
36 print "f = ", f, "\nI = ", I, "\nL = ", L

f = @1=0.00166667, @2=100, @3=8750, @4=zeros(2x2, diagonal)[:2] += ones(2
x1, dense))', vertcat((@4[0]\(((@1*(1000-cstr.c))/@2)-((1200000000*
cstr.c)*exp((-@3/cstr.T))))), (@4[1]\(((@1*(350-cstr.T))/@2
-((-2.51046e+08*cstr.c)*exp((-@3/cstr.T))))+(0.034986*(-1\(-u))-
cstr.T))))

I = vertcat((cstr.c-1000), (cstr.T-350))
L = (0.0001*((sq((500-cstr.c))+sq((320-cstr.T))+sq((300-(-1\(-u))))))

37 print "lbx = ", lbx, "ubx = ", ubx, "lbu = ", lbu, "ubu = ", ubu

lbx = [-inf, -inf] ubx = [inf, 350.0] lbu = [230.0] ubu = [370.0]

38 ode_fcn = Function('ode_fcn', [x,u],[f,L])
39 init_fcn = Function('init_fcn', [x],[I])
40 ode_fcn = ode_fcn.expand()
41 init_fcn = init_fcn.expand()
42 nk = 20
43 dt = tf/nk
44 nx = x.size1()
45 nu = u.size1()
46 nj = 10; h = dt/nj
47 xk = MX.sym("xk", nx)
48 uk = MX.sym("uk", nu)
49 xkj = xk; xkj_L = 0
50 for j in range(nj):
51     k1, k1_L = ode_fcn(xkj, uk)
52     k2, k2_L = ode_fcn(xkj + h/2*k1, uk)
53     k3, k3_L = ode_fcn(xkj + h/2*k2, uk)
54     k4, k4_L = ode_fcn(xkj + h*k3, uk)
55     xkj += h/6 * (k1 + 2*k2 + 2*k3 + k4)
56     xkj_L += h/6 * (k1_L + 2*k2_L + 2*k3_L + k4_L)
57 integrator = Function('integrator', [xk,uk],[xkj,xkj_L])
58 xk = [MX.sym("x" + str(k), nx) for k in range(nk+1)]
59 uk = [MX.sym("u" + str(k), nu) for k in range(nk)]
60 v = []; lbv = []; ubv = []; v0 = []
61 nv = 0
62 vind = {'x':[], 'u':[]}
63 def valloc(n, nv): return range(nv, nv+n), nv+n
64 for k in range(nk):
65     # $ States
66     ind, nv = valloc(nx, nv)
67     v.append(xk[k]); lbv.append(lbx); ubv.append(ubx); v0.append(x0); vind['x']
        ].append(ind)
68     # $ Control
69     ind, nv = valloc(nu, nv)
70     v.append(uk[k]); lbv.append(lbu); ubv.append(ubu); v0.append(u0); vind['u']
        ].append(ind)
71 ind, nv = valloc(nx, nv)
72 v.append(xk[-1]); lbv.append(lbx); ubv.append(ubx); v0.append(x0); vind['x'].
        append(ind)
73 v = vertcat(*v); lbv = vertcat(*lbv); ubv = vertcat(*ubv); v0 = vertcat(*v0)
74 J = 0; eq = []
75 eq0 = init_fcn(xk[0])

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76 eq.append(eq0)
77 for k in range(nk):
78     xk_end, Jk = integrator(xk[k], uk[k])
79     J += Jk
80     if k+1<nk: eq.append(xk_end - xk[k+1])
81 nlp = {'x':v, 'f':J, 'g':vertcat(*eq)}
82 solver = nlpsol("solver", "ipopt", nlp)
83 sol = solver(lbx=lbv, ubx=ubv, x0=v0, lbg=0, ubg=0)

```

This program contains Ipopt, a library for large-scale nonlinear optimization.
Ipopt is released as open source code under the Eclipse Public License (EPL).

For more information visit <http://projects.coin-or.org/Ipopt>

This is Ipopt version 3.12.3, running with linear solver ma57.

Number of nonzeros in equality constraint Jacobian...	154
Number of nonzeros in inequality constraint Jacobian..	0
Number of nonzeros in Lagrangian Hessian.....	120

Total number of variables.....	62
variables with only lower bounds:	0
variables with lower and upper bounds:	20
variables with only upper bounds:	21
Total number of equality constraints.....	40
Total number of inequality constraints.....	0
inequality constraints with only lower bounds:	0
inequality constraints with lower and upper bounds:	0
inequality constraints with only upper bounds:	0

iter	objective	inf_pr	inf_du	lg(mu)	d	lg(rg)	alpha_du
	alpha_pr	ls					
0	6.4299292e+02	7.00e+02	1.00e+00	-1.0	0.00e+00	-	0.00e+00 0.00e
	+00 0						
1	5.9103062e+02	7.00e+02	1.47e+00	-1.0	7.00e+02	-4.0	3.61e-21 3.39e
	-21F 1						
2	5.2897122e+02	6.03e+02	8.24e+00	-1.0	7.00e+02	-4.5	7.81e-01 1.39e
	-01f 1						
3	3.2549076e+02	4.41e+02	2.97e+01	-1.0	6.03e+02	-5.0	2.50e-01 2.68e
	-01f 1						
4	1.7251112e+02	4.30e+02	2.27e+01	-1.0	5.58e+03	-5.4	5.17e-03 2.55e
	-02f 1						
5	1.2226738e+02	4.22e+02	3.28e+01	-1.0	4.35e+03	-5.9	1.69e-03 1.82e
	-02f 1						
6	1.2206550e+02	4.22e+02	2.70e+01	-1.0	1.30e+03	-6.4	3.04e-03 1.32e
	-03h 1						
7	1.2432796e+02	4.04e+02	2.90e+01	-1.0	5.57e+02	-6.9	1.97e-03 4.18e
	-02h 1						
8	2.1892488e+02	3.23e+02	1.87e+02	-1.0	4.36e+02	-7.3	1.61e-02 1.99e
	-01h 1						

```

 9  2.2145519e+02  3.21e+02  1.82e+02  -1.0  3.23e+02  -7.8  1.78e-02  8.40e
    -03h  1
iter   objective    inf_pr   inf_du lg(mu)  ||d|| lg(rg) alpha_du
alpha_pr ls
10  4.9597972e+02  1.73e+02  8.76e+01  -1.0  4.02e+02  -8.3  1.21e-03  4.60e
    -01h  1
11  5.1249276e+02  1.65e+02  8.37e+01  -1.0  1.73e+02  -8.8  2.87e-01  4.52e
    -02h  1
12  8.0199667e+02  4.23e+01  4.60e+01  -1.0  1.65e+02  -9.2  2.36e-01  7.44e
    -01h  1
13  6.2728789e+02  6.10e+01  1.75e+01  -1.0  9.00e+01  -9.7  5.98e-02  9.85e
    -01f  1
14  5.5225226e+02  2.91e+01  7.29e+00  -1.0  6.61e+01  -1.9  9.20e-02  9.90e
    -01f  1
15  4.5828993e+02  1.05e+01  5.44e+01  -1.0  6.82e+01  -2.4  4.24e-01  6.83e
    -01f  1
16  4.1540595e+02  9.90e+00  2.40e+01  -1.0  1.10e+02  -2.8  2.73e-01  2.47e
    -01f  1
17  4.0202390e+02  9.44e+00  1.07e+02  -1.0  1.31e+02  -3.3  2.22e-01  7.19e
    -02f  1
18  3.6766946e+02  4.82e+00  3.14e+02  -1.0  5.72e+01  -3.8  9.12e-02  4.90e
    -01f  1
19  3.1887985e+02  2.12e+01  6.62e+02  -1.0  1.82e+02  -4.3  6.66e-02  3.23e
    -01f  1
iter   objective    inf_pr   inf_du lg(mu)  ||d|| lg(rg) alpha_du
alpha_pr ls
20  3.0753849e+02  1.32e+01  9.19e+01  -1.0  5.18e+01  -4.7  5.84e-01  3.85e
    -01f  1
21  2.9636430e+02  2.76e+00  7.30e+02  -1.0  3.05e+01  -5.2  8.00e-01  1.00e
    +00f  1
22  2.9687769e+02  3.30e-01  2.10e-03  -1.0  5.15e+01  -5.7  1.00e+00  1.00e
    +00h  1
23  2.9673719e+02  1.28e-02  2.42e-04  -1.7  1.08e+02  -6.2  1.00e+00  1.00e
    +00h  1
24  2.9665238e+02  7.54e-04  3.13e+00  -3.8  1.22e+00  -6.7  9.99e-01  1.00e
    +00h  1
25  2.9665135e+02  6.71e-07  6.43e-07  -3.8  8.65e+00  -7.1  1.00e+00  1.00e
    +00h  1
26  2.9665075e+02  2.65e-08  6.98e-09  -5.7  2.81e-01  -7.6  1.00e+00  1.00e
    +00h  1
27  2.9665075e+02  3.98e-12  1.05e-11  -8.6  1.27e-03  -8.1  1.00e+00  1.00e
    +00h  1

```

Number of iterations.....: 27

	(scaled)	(unscaled)
Objective.....:	2.9665074612381767e+02	2.9665074612381767e+02
Dual infeasibility.....:	1.0469387648521393e-11	1.0469387648521393e-11
Constraint violation.....:	3.9790393202565610e-12	3.9790393202565610e-12
Complementarity.....:	2.5116299426194594e-09	2.5116299426194594e-09
Overall NLP error.....:	2.5116299426194594e-09	2.5116299426194594e-09

```

Number of objective function evaluations = 28
Number of objective gradient evaluations = 28
Number of equality constraint evaluations = 29
Number of inequality constraint evaluations = 0
Number of equality constraint Jacobian evaluations = 28
Number of inequality constraint Jacobian evaluations = 0
Number of Lagrangian Hessian evaluations = 27
Total CPU secs in IPOPT (w/o function evaluations) = 0.028
Total CPU secs in NLP function evaluations = 1.138

```

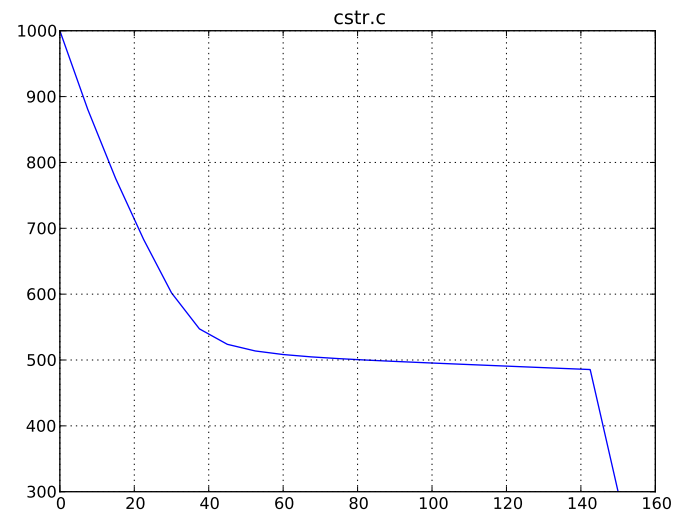
EXIT: Optimal Solution Found.

	proc	time	wall time	num	mean
				evals	proc time
nlp_f	0.070 [s]	0.065 [s]	28	2.50 [ms]	
nlp_g	0.080 [s]	0.068 [s]	29	2.76 [ms]	
nlp_grad_f	0.180 [s]	0.211 [s]	29	6.21 [ms]	
nlp_jac_g	0.280 [s]	0.289 [s]	29	9.66 [ms]	
nlp_hess_l	0.530 [s]	0.525 [s]	27	19.63 [ms]	
all previous	1.140 [s]	1.158 [s]			
callback_prep	0.000 [s]	0.000 [s]	28	0.00 [ms]	
solver	0.020 [s]	0.013 [s]			
mainloop	1.160 [s]	1.171 [s]			

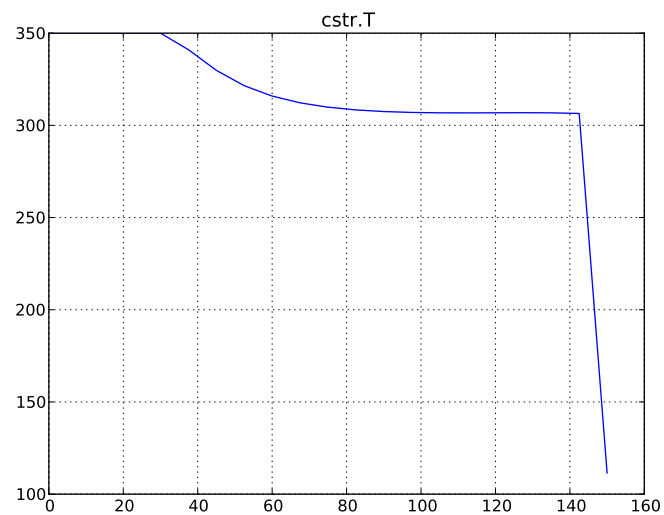
```

84 v_opt = sol["x"]
85 x0_opt = v_opt[[vind['x']][k][0] for k in range(nk+1)]
86 x1_opt = v_opt[[vind['x']][k][1] for k in range(nk+1)]
87 u_opt = v_opt[[vind['u']][k][0] for k in range(nk)]
88 from pylab import *
89 from numpy import *
90 tgrid = linspace(0,tf,nk+1)
91 figure(1)
92 plot(tgrid,x0_opt)
93 title(str(x[0]))
94 grid()
95 show()

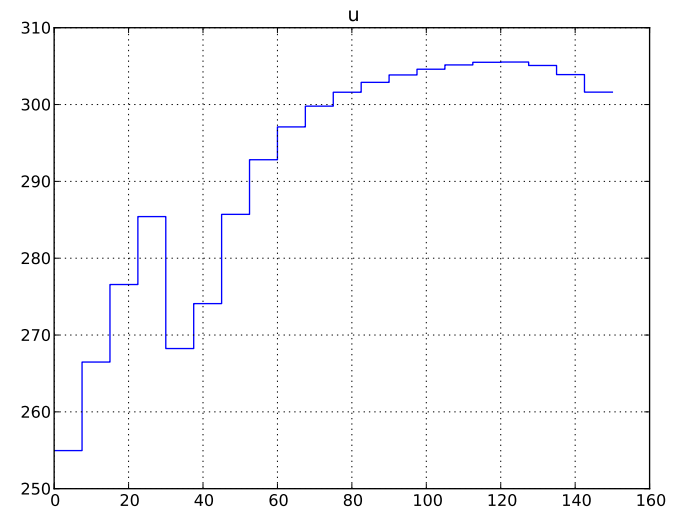
```



```
96 figure (2)
97 plot (tgrid , x1_opt)
98 title (str (x[1]))
99 grid ()
100 show ()
```



```
102 step (tgrid , vertcat (u_opt[0], u_opt))
103 title (str (u))
104 grid ()
105 show ()
```



```
101 figure (3)
```