# ELNG 251: DC Machines and Transformers

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## Content

- Electromagnetism
- DC Machines
- DC Generators
- DC Motors
- Magnetic circuits
- Single-phase transformers
  - Ideal transformer
  - Actual transformer
- Three-phase transformers

## Assessment

- Continuous assessment 40 marks
  - Weekly quizzes and assignments 20 marks
  - Mid-semester examination 20 marks
- End of semester examination 60mks
  - Multiple choice examination 20 marks
  - Written examination 40 marks

## Further study

• Sahdev, S. K. (2017). Electrical machines. Cambridge University Press.

Click here for lecture materials

• Electromagnetism is the interaction or interrelation between electric charges and magnetic fields.

• In 1820 Danish physicist Hans Christian Ørsted discovered that an electric current creates a

magnetic field around it.

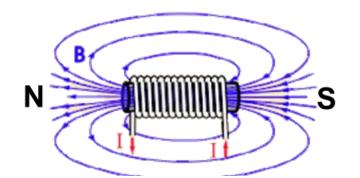
• The magnetic field lines encircle the current-carrying wire.

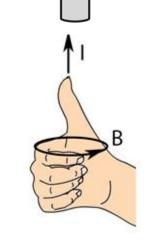
• The magnetic field lines lie in a plane perpendicular to the wire.

• If the direction of the current is reversed, the direction of the magnetic field reverses.

 The strength of the field is directly proportional to the magnitude of the current.

 The strength of the field at any point is inversely proportional to the distance of the point from the wire.





Conducting wire

### Right hand thumb rule

• Thumb points in the direction of electric current and fingers curl around the current indicating the direction of the magnetic field.

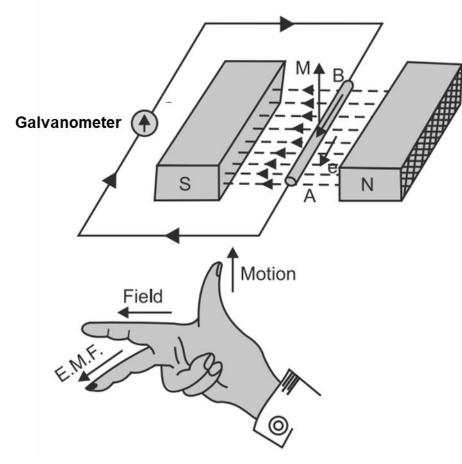
### Faraday's laws of electromagnetic induction

- 1<sup>st</sup> law: Whenever a conductor cuts across a magnetic field, an emf is induced in the conductor
- **OR** Whenever the magnetic flux linking with any circuit (or coil) changes, an emf is induced in the circuit.
- 2<sup>nd</sup> law: The magnitude of induced emf in a coil is directly proportional to the rate of change of flux linkages. N – Number of turns

dt – change in time

### Fleming's Right Hand Rule

 Stretch the 1<sup>st</sup> finger, middle finger and thumb of the right hand in mutually perpendicular manner such that the 1st finger points in the direction of the magnetic field and the thumb in the direction of the motion, the resulting induced emf is in the direction of the middle finger.



Direction of induced emf using the **RIGHT-HAND RULE** 

#### **Worked Example**

A coil of 500 turns is linked with a flux of 2 mWb. If this flux is reversed in 4 ms, calculate the average emf induced in the coil.

#### Solution

Induced emf, 
$$e = N \frac{d\phi}{dt}$$

$$N = 500 \text{ turns}$$

$$d\phi = 2\text{-}(-2) = 4 \text{ mWb} = 4 \text{ x } 10^{-3} \text{ Wb}$$

$$dt = 4 \text{ x } 10^{-3} \text{ s}$$

$$e = 500 \times \frac{4 \times 10^{-3}}{4 \times 10^{-3}} = 500 V$$

• A coil of 250 turns is wound on a magnetic circuit of reluctance 100,000 At/Wb. If a current of 2 A flowing in the coil is reversed in 5 ms, find the average emf induced in the coil.

#### Lenz's law

 states that the direction of the electric current induced in a conductor by a changing magnetic field is such that the magnetic field created by the induced current opposes changes in the initial magnetic field. It is named after physicist Heinrich Lenz, who formulated it in 1834.

### Fleming's Left Hand Rule

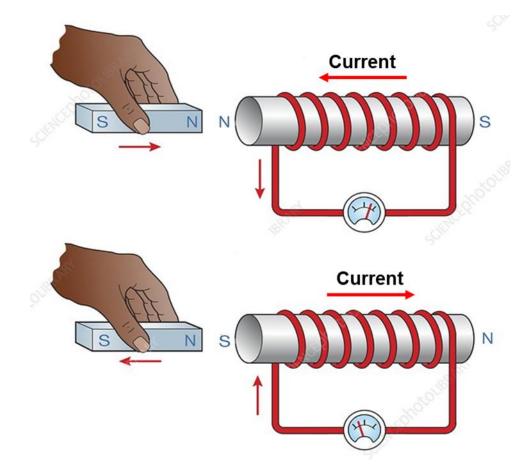
• Stretch the 1<sup>st</sup> finger, middle finger and thumb of the right hand in mutually perpendicular manner such that the 1<sup>st</sup> finger points in the direction of the magnetic field and the middle finger in the direction of the current, the thumb points in the direction of the force exerted on the conductor.

Motion (Force)

→ Motion

Current

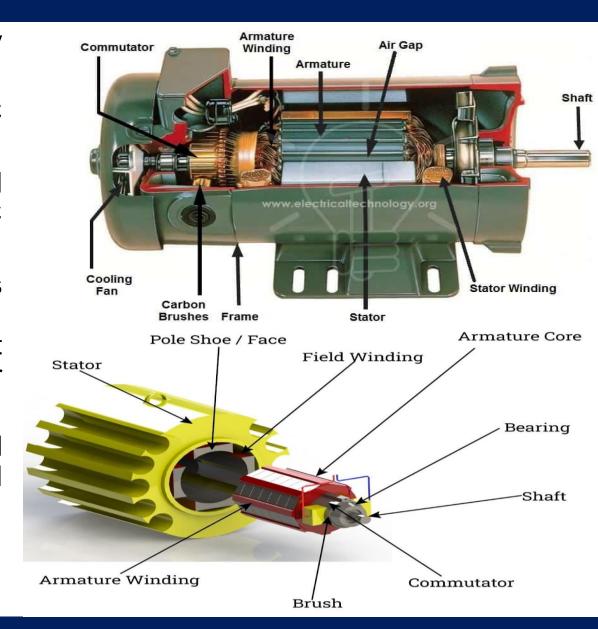
Click here for a video on Lenz's law



Induced current opposing magnetic field – **LENZ'S LAW** 

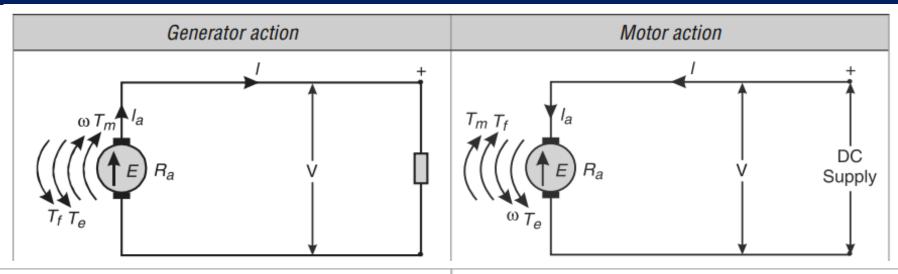
## DC machines

- A DC machine is an electro-mechanical energy conversion device.
- When it converts mechanical power into DC electrical power, it is known as a DC generator.
- On the other hand, when it converts DC electrical power into mechanical power it is known as a DC motor.
- Applications where large quantity of DC power is required are in chemical and metal extraction plants, for electroplating and electrolysis processes etc. At such places DC generators are used to deliver power.
- DC motors have several applications in industry and every day use; toys, windshield wipers, small appliances, power tools, electric vehicles, robotics, industrial automation, etc.



### DC machines

### **Comparing DC** generator and motor operation



- 1. In generating action, the rotation is due to mechanical torque, therefore,  $T_m$  and  $\omega$  are in the same direction.
- to rotation  $\omega$ .
- 3. Electromagnetic torque  $T_e$  acts in opposite direction to mechanical torque  $T_m$  so that  $\omega T_m = \omega T_e + \omega T_f$
- 4. In generating action, an emf is induced in the armature conductors which circulates current in the armature when load is connected to it. Hence, e and i both are in the same direction.
- 5. In generator action, E > V
- 6. In generating action, the torque angle  $\theta$  is leading.
- 7. In generating action, mechanical energy is converted into electrical energy.

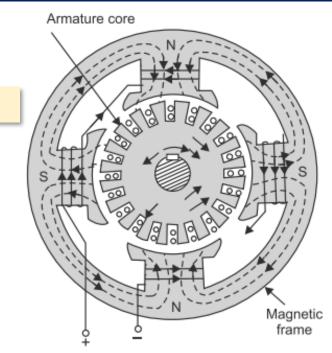
- 1. In motoring action, the rotation is due to electromagnetic torque, therefore,  $T_{\rho}$  and  $\omega$  are in the same direction.
- 2. The frictional torque  $T_f$  acts in opposite direction | 2. The frictional torque  $T_f$  acts in opposite direction to rotation  $\omega$ .
  - 3. Mechanical torque  $T_m$  acts in opposite direction to electromagnetic torque  $T_e$  so that  $\omega T_e = \omega T_m + \omega T_f$
  - 4. In motoring action, current is impressed to the armature against the induced emf (e), therefore current flows in opposite direction to that of induced emf.
  - 5. In motor action, E < V
  - 6. In motoring action, the torque angle  $\overline{\theta}$  is lagging.
  - 7. In motoring action, electrical energy is converted into mechanical energy.

## Armature winding of a dc machine

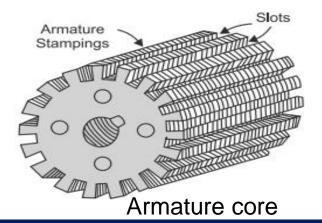
### **Armature winding**

- The armature winding are the insulated conductors housed in the armature slot. NB: DC motors and DC generators are collectively referred to as DC machine
- It is the place where one form of power is converted to the other form i.e., in case of generator, mechanical power is converted into electrical power and in case of motor, electrical power is converted into mechanical power.
- There are two types of armature windings:
- (i) Lap winding: In this winding, that the number of parallel paths (A) is equal to number of poles. In this case, the number of brushes is equal to the number parallel paths. Out of which half the brushes are positive and the remaining (half) are negative.
- (ii) Wave winding: In this winding, the parallel paths are only two irrespective of the number of poles. In this case, is equal to two i.e., number of parallel paths.

Click here for further study on armature windings



Magnetic circuit of a DC machine



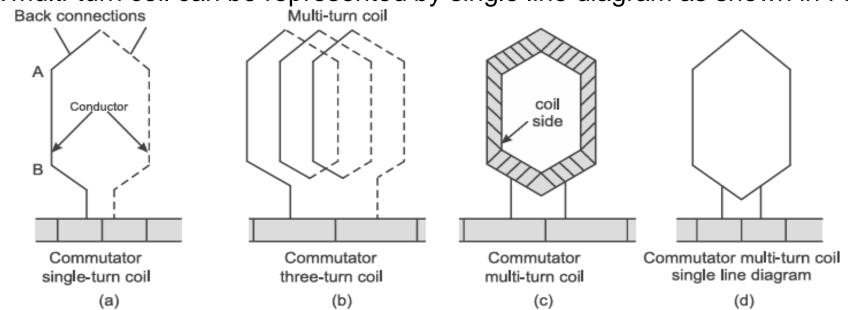
## Armature winding of a dc machine

**Conductor:** The length of wire embedded in armature core and lying within the magnetic field. Number of conductor is represented by Z.

**Turn:** Two conductors lying in a magnetic field connected in series at the back.

$$Z = number of turns \times 2$$

**Coil:** A coil may be a single-turn coil having only two conductors, as shown in Fig (a), or it may be a multi-turn coil having more than two conductors as shown in Fig (b). In Fig. 4.17(b), a three-turn coil is shown. The bunch of three conductors may be wrapped by the cotton tape, as shown in Fig (c), before placing it in the armature slot. A multi-turn coil can be represented by single line diagram as shown in Fig (d).



## Emf and torque equation of a DC machine

### **Emf equation**

P = number of poles

 $\emptyset$  = Flux per pole

Z = Number of conductors

A = Number of parallel paths

N = speed in rpm

Total flux cut by one conductor

$$= P\emptyset$$

Time in seconds taken in one revolution

$$=\frac{60}{N}$$

• Per Faraday's law, induced emf per conductor 
$$e = \frac{\emptyset}{t} = \frac{P\emptyset}{60/N} = \frac{P\emptyset N}{60}$$

Total emf for all conductors

$$E = \frac{P\emptyset N}{60} \times \frac{Z}{A}$$

### Torque equation

 $I_a$  = Armature current

$$\omega$$
 = speed in rad/s =  $\frac{2\pi}{60}N$ 

- The torque generated in a dc machine is due to electromagnet effect, hence it's called electromagnetic torque, T<sub>e</sub>.
- The electrical power in the armature is equal to the electromagnetic torque, hence

$$EI_{a} = T\omega$$

$$\frac{P\emptyset NZ}{60A} \times I_a = T \times \frac{2\pi}{60}N$$

$$T = \frac{P\emptyset ZI_a}{2\pi A}$$

 $E = \frac{P\emptyset N}{60} \times \frac{Z}{A}$  Where  $\frac{Z}{A}$  is the number of conductors per parallel path

- A DC generator is an **electro-mechanical** energy conversion device (electrical machine) that converts mechanical energy or power (ωT) into DC electrical energy or power (EI).
- There are some applications where large quantity of DC power is required (such as in chemical and metal extraction plants, for electroplating and electrolysis processes etc.), at such places DC generators are used to deliver power.
- DC generators share the same internal composition and design with DC motors. The difference lies in the peripheral systems that support them.
- Motors often require control circuits for speed regulation, while generators require protection circuits for overvoltage and overcurrent.

### Working principle

- The basic principle of a DC generator is electro-magnetic induction i.e., "When a conductor cuts across the magnetic field, an emf is induced in it."
- The direction of the induced emf is determined by the Fleming's Right Hand Rule.

- In a DC generator, maximum emf is induced when the conductor cuts the magnetic field lines at 90°, any deviation from this decreases the emf.
- Since the conductor rotates, it only cuts the magnetic field at 90° twice in its revolution, and 0° twice when its perfectly parallel with the field.
- At 0°, no emf is induced.
- Hence, the emf is said to be dynamically induced as seen in Figure (a), where  $e = Blv \sin \theta$

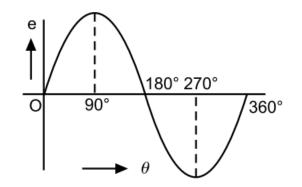
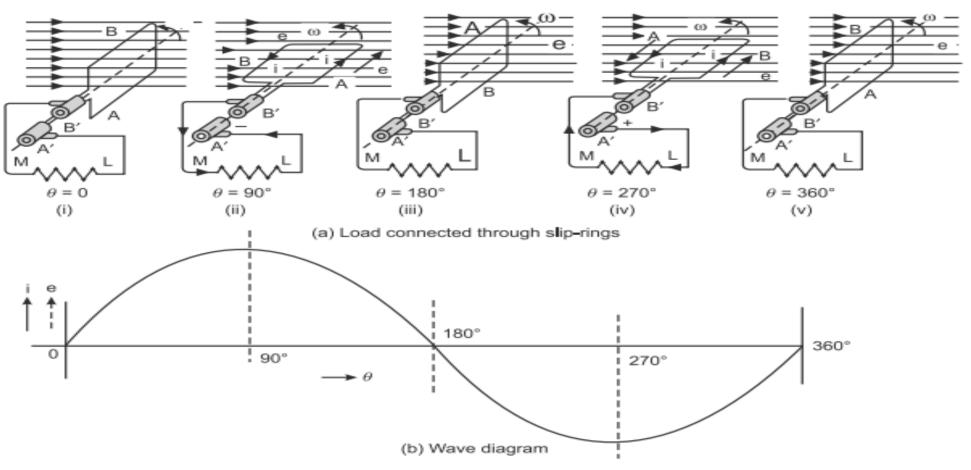


Figure (a): Wave shape of induced emf



• For simplicity, consider only one coil AB placed in the strong magnetic field. The two ends of the coil are joined to slip rings A' and B' respectively. Two brushes rest on these slip rings as shown in Figure

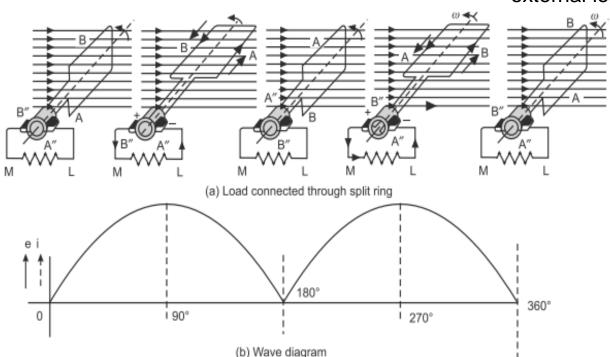
(a).



Generated emf for external circuit connected through slip rings

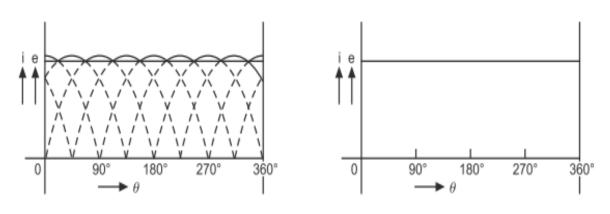
#### **Function of commutator**

 The commutator is to converts the alternating current produced in the armature into direct current in the external circuit.



#### **Commutator action**

- Now, consider that the two ends of the coil are connected to only one slip ring split into two parts (segment) i.e., A" and B". Each part is insulated from the other by a mica layer. Two brushes rest on these parts of the ring as shown in the figure below.
- The magnitude of emf induced in the coil at various instants will remain the same as shown in the previous slide, however, the flow of current in the external load will become unidirectional as been below



(a) Wave shape of output delivered by number of coils (b) True wave shape of output delivered by a dc generator

Wave shape of output delivered by a DC generator

#### Generated emf for external circuit connected through split ring

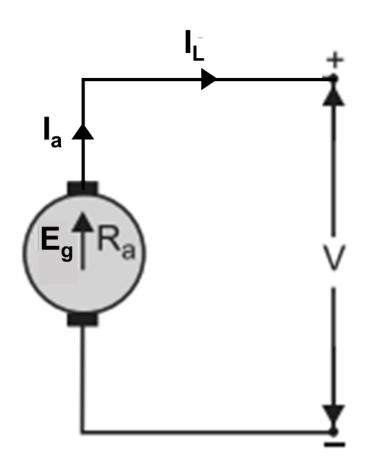
DC Machines and Transformers - G. Mensa.

### **Equivalent circuit of a DC generator**

$$E_g = V + I_a R_a$$

$$I_a = I_L$$

- Where  $E_g$  is the generated voltage
- $I_a$  is the armature current
- $I_L$  is the load current
- *V* is the terminal voltage
- $R_a$  is the armature resistance



#### **Problems**

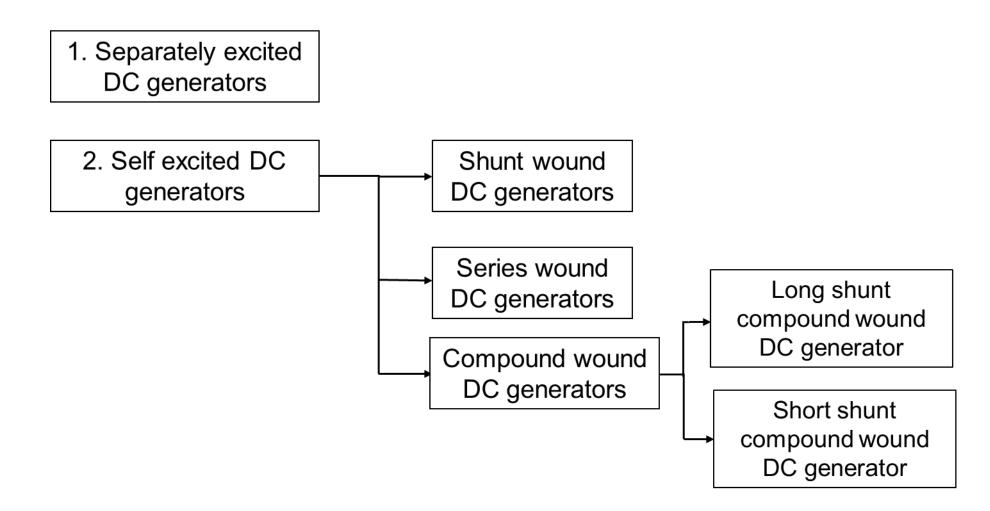
- 1. A 12 kW, six-pole DC generator develops an emf of 240 at 1500 rpm. The armature has a lap connected winding. The average flux density over the pole pitch is 1.0 T. The length and diameter of the armature is 30 cm and 25 cm respectively. Calculate flux per pole, total number of active armature conductors. Power generated in the armature and torque developed when the machine is delivering 50 A current to the load.
- 2. The useful flux of a four-pole, lap wound DC generator is 0.07 Wb. Its armature carries 220 turns and each turn has 0.004  $\Omega$  resistance, if its armature current is 50 A, running at a speed of 900 rpm, determine its terminal voltage.
- 3. A DC generator is connected to a 220 V DC mains. The current delivered by the generator to the mains is 100A. The armature resistance is 0.1  $\Omega$ . The generator is driven at a speed of 500 rpm Calculate (i) the induced emf (ii) the electromagnetic torque (iii) the mechanical power input to the armature neglecting iron, winding and friction losses, (iv) Electrical power output from the armature, (v) armature copper loss.

### **Assignment 1 – (Deadline Mon, Jan 20, 2025, 23:59)**

- 1. A four-pole, lap wound DC machine is having 500 conductors on its armature and running at 1000 rpm. The flux per pole is 30 m Wb Calculate the voltage induced in the armature winding. What will be induced emf if the armature is rewound for wave winding?
- 2. A 4-pole machine has an armature with 90 slots and 8 conductors per slot, the flux per pole is 0.05 Wb and runs at 1200 rpm. Determine induced emf if winding is (i) lap connected (ii) wave connected.
- 3. A wave wound armature of a six-pole generator has 51 slots. Each slot contains 20 conductors. The voltage required to be generated is 250 V. What would be the speed of coupled prime mover if flux per pole is 0.07 Wb. If the armature is rewound as lap wound machine and run by same prime mover, what will be the generated voltage.
- 4. The armature of a four-pole 200 V, lap wound generator has 400 conductors and rms of 300 rpm. Determine the useful flux per pole. If the number of turns in each field coil is 900, what is the average induced emf in each field coil on breaking its connection if the magnetic flux set-up by it dies away completely in 0.1 second?

## Types of DC generators

DC generators are classified based on the method of exciting their field winding.



# Applications of the different types of DC generators

 The various types of DC generators have different applications due to their various characteristics.

## **Separately excited DC generators:**

- These generators are more costly than self excited generators as they require a separate source for their field excitation.
- However, their response to changes in field resistance is quicker and more precise.
- Hence, they are employed where quick and definite response to control is important such as the Ward-Leonard System of speed control.

## **Shunt-wound DC generators:**

- As they provide constant terminal voltage, they are best suited for battery charging.
- Along with field regulators, they are also used for light and power supply purposes.

# Applications of the different types of DC generators

## **Series-wound DC generators:**

- These generators have very few (i) applications. Their best application is in the DC locomotives, where they supply field current for regenerative braking.
- They are also employed in series arc lighting.
- Another application of these generators is as series boosters for increasing DC voltage across the feeders.

## **Compound-wound DC generators**

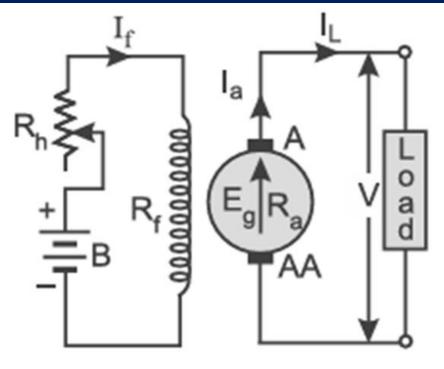
- (i) Over-compounded type: These are more suited for lighting and power services, as they compensate for the voltage drop in the lines and voltage at the terminals of the load remains constant.
- (ii) Differential-compounded type: They are usefully employed as are welding sets. In such cases, the generator is practically short-circuited every time the electrode touches the metal plates to be welded.

## Separately excited DC generators

- In a separately excited DC generator, the field winding is excited with current from an **external DC source**.
- $I_a = I_L$  where  $I_a$  is the armature current and  $I_L$  is the line current.
- Terminal voltage,  $V = E_g I_a R_a$
- If contact brush drop per brush (v<sub>b</sub>) is known,

$$V = E_g - I_a R_a - 2v_b$$

- Power developed =  $E_g I_a$ ;
- Power output =  $VI_L = VI_a$



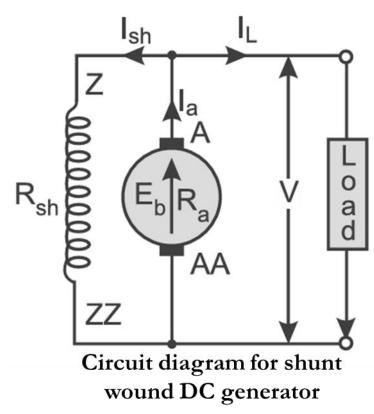
Circuit diagram for separately excited DC generators

# Self excited DC generators

- In a self excited DC generator, the field winding is excited with current from the generator itself.
- The field coils may be connected in parallel with the armature, in series with the armature or partly in series and partly in parallel with the armature winding.
- They may be classified as
  - (i) Shunt wound DC generators
  - (ii) Series wound DC generators
  - (iii) Compound wound DC generators.

## Shunt wound DC generators

- In a shunt wound DC generator, the field winding is connected across the armature winding forming, a parallel or shunt circuit.
- Therefore, full terminal voltage is applied across the field winding.
- A very small current  $I_{sh}$  flows through it because this winding has many turns of fine wire having very high resistance  $R_{sh}$  (of the order of 100  $\Omega$ .
- Shunt field current,  $I_{sh} = \frac{V}{R_{sh}}$
- Where R<sub>sh</sub> is the shunt field winding resistance. The field current I<sub>sh</sub> is practically constant at all loads, therefore, the DC shunt machine is considered a **constant flux machine**.
- Armature current,  $I_a = I_{sh} + I_L$
- Terminal voltage,  $V = E_g I_a R_a$
- Including brush contact drop,  $V = E_g I_a R_a 2 v_b$
- Power developed =  $E_g I_a$ ; Power output =  $VI_L$



## Shunt wound DC generators

#### **Problems**

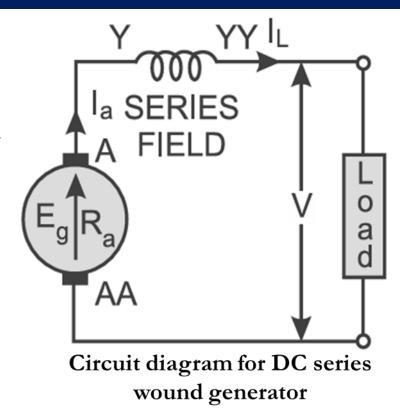
- 1. A 12-pole DC shunt generator has 50 slots on its armature with 12 conductors per slot with wave winding. The armature and field winding resistance is 0.5  $\Omega$  and 60  $\Omega$  respectively. The generator is supplying a resistive load of 15  $\Omega$  at terminal voltage of 300 V when running at a speed of 625 rpm. Find the armature current, the generated emf and the flux per pole.
- 2. A four-pole shunt generator with lap connected armature has field and armature resistance of 50 and 0.1 respectively. The generator is supplying a load of 2.4 kW at 100 V. Calculate the armature current, current in each conductor and generated emf.
- 3. A four-pole DC shunt generator with a wave wound armature having 390 conductors has to supply a load of 500 lamps each of 100 W at 250 V. Allowing 10 V for the voltage drop in the connecting leads between the generator and the load and brush drop of 2 V. Calculate the speed at which the generator should be driven. The flux per pole is 30 m Wb and the value of  $R_a = 0.05 \Omega$  and  $R_{sh} = 65 \Omega$ .

## Series wound DC generators

- In a DC series wound generator, the field winding is connected in series with the armature winding forming a series circuit.
- Therefore, full line current I<sub>L</sub> or armature current I<sub>a</sub> flows through it.
   Since the series field winding carries full load current, it has a few turns of thick wire having low resistance (usually of the order of less than one ohm).
- Series current,  $I_{se} = I_a = I_L$
- Terminal voltage,  $V = E_g I_a R_a I_{se} R_{se}$

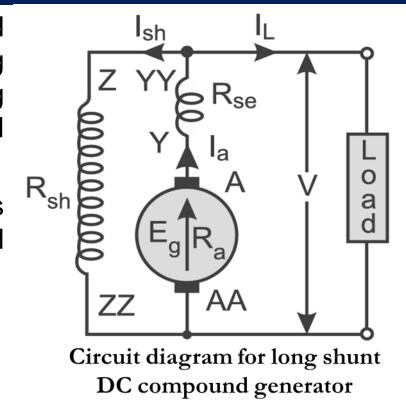
$$V = E_g - I_a R_a - I_a R_{se} = E_g - I_a (R_a + R_{se})$$

- Including brush contact drop,  $V = E_g I_a(R_a + R_{se}) 2v_b$
- Power developed =  $E_g I_a$
- Power output =  $VI_L = VI_a$



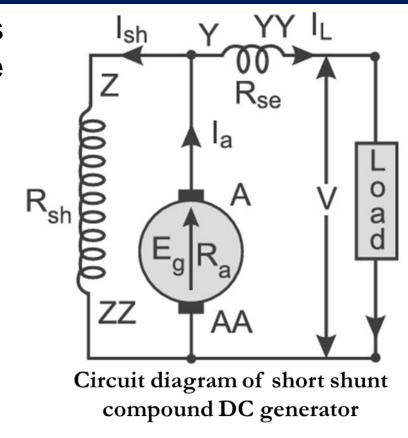
## Compound wound DC generators

- In a compound wound DC generator, there are two sets of field windings on each pole. One of them is connected in series (having few turns of thick wire) and the other is connected in parallel (having many turns of fine wire) with armature. A compound wound generator may be;
- (a) Long shunt: In this generator, the shunt field winding is connected in parallel with the combination of both armature and series field winding.
- Shunt field current,  $I_{sh} = \frac{V}{R_{sh}}$
- Series field current,  $I_{se} = I_a = I_L + I_{sh}$
- Terminal voltage,  $V = E_g I_a R_a I_{se} R_{se} = E_g I_a (R_a + R_{se})$
- Including brush contact drop,  $V = E_g I_a(R_a + R_{se}) 2v_b$
- Power developed =  $E_g I_a$ ; Power output =  $VI_L$



# Compound wound DC generators

- (b) Short shunt: In this generator, the shunt field winding is connected in parallel with only the armature winding and the series field winding in series with the load.
- Series field current,  $I_{se} = I_L = I_a I_{sh}$
- Shunt field current,  $I_{Sh} = \frac{V + I_L R_{Se}}{R_{Sh}}$
- Terminal voltage,  $V = E_g I_a R_a I_L R_{se}$
- Including brush contact drop,  $V = E_g I_a R_a I_L R_{se} 2v_b$
- Power developed =  $E_g I_a$ ; Power output =  $VI_L$



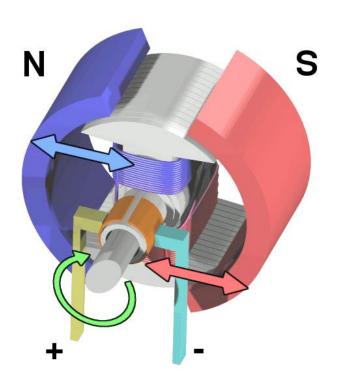
## Compound wound DC generators

#### **Problems**

- A load of 7.5 kW at 230V is supplied by a short-shunt cumulatively compound DC generator. If the armature, series and shunt field resistances are 0.4, 0.3 and 100  $\Omega$  respectively. Calculate the induced emf and the load resistance. Calculate the emf is this was a long shunt generator.
- A load of 20 kW at 230 V is supplied by a compound DC generator. If the series, shunt field and armature resistances are 0.05, 115 and 0.1  $\Omega$  respectively. Calculate the generated emf when the generator is connected as (i) long shunt (ii) short shunt.

- A DC motor is an **electro-mechanical** energy conversion device (electrical machine) that converts DC electrical energy or power (EI) into mechanical energy or power (ωT).
- DC motors have extensive applications in industrial automation, transportation, robotics, aerospace, home appliances, medical devices, etc.

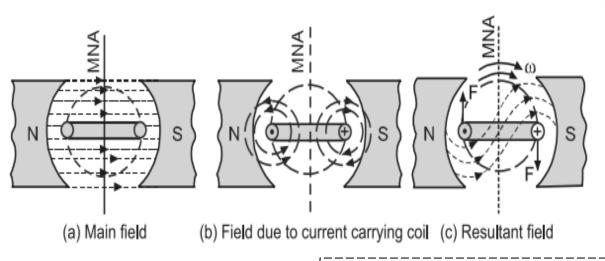


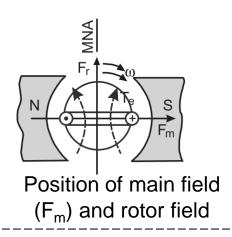


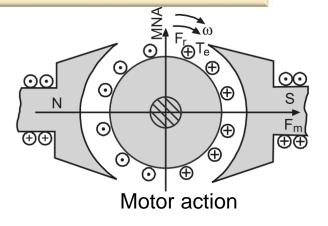
### Working principle

- The operation of a DC motor is based on the principle that when a current carrying conductor is placed in a magnetic field, a mechanical force is experienced by it.
- The direction of this force is determined by **Fleming's Left Hand Rule** and its magnitude is given by the relation: F = B i l (newton)

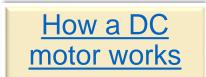
Where, B is the magnetic flux density in Tesla (T), i is the current in the conductor and l is the length of the conductor







the direction of flow of current in each conductor or coil side must be reversed when it passes through the magnetic neutral axis (MNA). A commutator is used to achieve this.



#### **Function of a Commutator**

• The function of a commutator in DC motors is to reverse the direction of flow of current in each armature conductor when it passes through the M.N.A. to obtain continuous torque.

#### **Back EMF**

- Due to the armature conductors (coil) cutting across the magnetic field of the main poles, a back emf is induced. "Back" because **the direction of this emf is opposite that of the applied voltage** in the coils.
- The back EMF plays a crucial role in DC motor operation.
  - Speed regulation: The back EMF helps regulate the motor's speed by opposing the applied voltage.
  - **Current limitation:** The back EMF reduces the current flowing through the coil, preventing excessive currents and potential damage.
  - Efficiency: The back EMF contributes to the motor's efficiency, as it reduces energy losses due to excessive currents.

- Shaft torque: This is the actual torque seen at the output of the motor after windage and frictional losses. Hence  $T_{sh} \omega = Pe P_{losses}$ , where  $P_e$  is the electrical power, and  $P_{losses}$  is the power losses.
- Brake horse power (BHP): In the case of motors, the mechanical power (H.P.) available at the shaft is known as brake horsepower.

$$BHP = \frac{T_{sh} \,\omega}{745.7}$$

• Hence, BHP is shaft power (P<sub>sh</sub>) converted to units of horse power.

$$E_b = \frac{P\Phi NZ}{60~A}$$
 
$$E_b \propto \Phi N \qquad \text{since } \frac{PZ}{60~A} \text{ are constants}$$

The supply voltage (V) is always greater than the induced or back emf ( $E_b$ ) (i.e.,  $V > E_b$ ). Therefore, current is always supplied to the motor from the mains and the relation among the various quantities will be;  $E_b = V - I_a R_a$ .

Hence the armature current is:  $I_a = \frac{V - E_b}{R_a}$ 

When mechanical load applied on the motor increases, its speed decreases which reduces the value of E<sub>b</sub>. As a result the value (V – E<sub>b</sub>) increases which consequently increases I<sub>a</sub>. Hence, motor draws extra current from the mains. Thus, the back emf regulates the input power as per the extra load.

#### Work example

A 50 HP, 400 V, 4 pole, 1000 rpm, DC motor has flux per pole equal to 0.027 Wb. The armature having 1600 conductors is wave connected. Calculate the gross torque when the motor takes 70 ampere.

#### Solution

Torque developed, 
$$T = \frac{P\emptyset ZI_a}{2\pi A}$$

Where, P = 4 poles;  $\emptyset = 0.027$  Wb;  $I_a = 70A$ ; A = 2 (wave connected)

$$T = \frac{4 \times 0.027 \times 1600 \times 70}{2\pi \times 2} = 963 Nm$$

### **Assignment**

- The induced emf in a DC machine is 200 V at a speed of 1200 rpm. Calculate the electromagnetic torque developed at an armature current of 15 A.
- A four-pole DC motor has a wave-wound armature with 594 conductors. The armature current is 40 A and flux per pole is 7.5 m Wb. Calculate H.P. of the motor when running at 1440 rpm.
- A DC motor has 6-poles with lap wound armature.
   What will be its brake horse power when it draws a current of 340 A and rotates at 400 rpm. The flux per pole is 0.05 Wb and the armature carries 864 turns, Neglect mechanical losses.

## Types of DC motors

 The construction of the various types of DC motors is the same as their corresponding types in DC generators. The only difference is that, in DC motors, the flow of current is from the terminal to the armature.

### **Separately excited DC motor**

- $E_b = V I_a R_a$
- $E_b = V I_a R_a 2v_b$  when voltage drops at brushes is considered.  $v_b$  is the voltage drop per brush

**Self excited DC motors:** These motors can be further classified as;

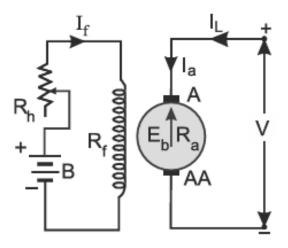
• (i) Shunt motors:

• 
$$I_{sh} = \frac{V}{R_{sh}}$$

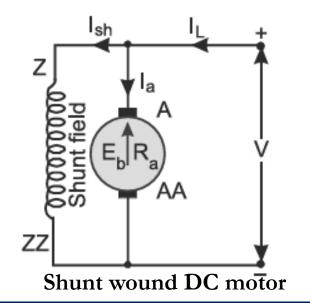
• 
$$I_a = I_L - I_{sh}$$

• 
$$E_b = V - I_a R_a$$

• 
$$E_b = V - I_a R_a - 2v_b$$



Separately excited DC motor



# Types of DC motors

### • (ii) Series motors:

• 
$$I_a = I_L = I_{se}$$

• 
$$E_b = V - I_a R_a - I_L R_{se}$$

• 
$$E_b = V - I_a(R_a + R_{se})$$

• 
$$E_b = V - I_a(R_a + R_{se}) - 2v_b$$

### • (ii) Compound motors:

• 
$$I_{sh} = \frac{V}{R_{sh}}$$

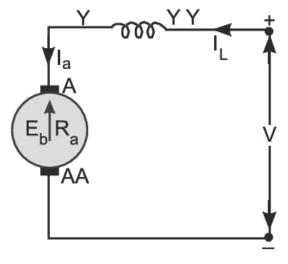
• 
$$I_{se} = I_a$$

• 
$$I_a = I_L - I_{sh}$$

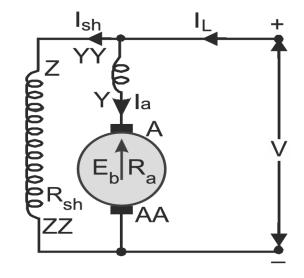
• 
$$E_b = V - I_a R_a - I_L R_{se}$$

• 
$$E_b = V - I_a(R_a + R_{se})$$

• 
$$E_b = V - I_a(R_a + R_{se}) - 2v_b$$



Series wound DC motor



Compound DC motor

## Types of DC motors

### **Examples**

- The armature resistance of a DC shunt motor is 0.5  $\Omega$ , it draws 20 A from 220 V mains and is running at a speed of 80 radian per second. Determine (i) Induced emf (ii) Electromagnetic torque (iii) Speed in rpm.
- A 400 V DC motor takes an armature current of 100 A when its speed is 1000 rpm If the armature resistance is 0.25  $\Omega$ , calculate the torque produced in Nm.
- The armature and series field winding resistance of a 220 V, four-pole DC series motor is 0.75  $\Omega$ . It has 782 wave wound armature conductors. If it draws 40 A from the supply mains and has a flux of 25 mWb, determine its speed and gross torque developed.
- The armature and shunt field resistance of a four-pole, lap wound DC shunt motor is 0.05  $\Omega$  and 25  $\Omega$  respectively. If its armature contains 500 conductors, find the speed of the motor when it take 120 A from a DC mains of 100 V supply. Flux per pole is 2 × 10–2 Wb.
- A 6-pole, 440 V DC motor has 936 wave wound armature conductors. The useful flux per pole is 25 m Wb. The torque developed is 45-5 kg-m. Calculate the following, if armature resistance is 0-5 Ω; (i) Armature current (ii) Speed