Magnetism: quantities, units and relationships

If you occasionally need to design a wound component, but do not deal with the science of magnetic fields on a daily basis, then you may become confused about what the many terms used in the data sheet for the core represent, how they are related and how you can use them to produce a practical inductor.

About your browser: if this character 'x' does not look like a multiplication sign, or you see lots of question marks '?' or symbols like ' \square ' or sequences like '&cannot;' then please accept my apologies.

See also ...

[↑ Producing wound components] [Air coils] [Power loss in wound components] [The force produced by a magnetic field] [Faraday's law] [The magnetic properties of materials] [Unit Systems]

Index to magnetic terms & units in the SI

This set of web pages uses the system of units known as the SI (Système International). For more information on the SI, and how it compares with other systems, see Unit Systems in Electromagnetism.

Quantity name	Quantity symbol	Quantity name	Quantity symbol
coercivity	Нс	core factor	ΣΙ/Α
current	I	effective area	Ae
effective length	le	effective permeability	μе
flux linkage	λ	induced voltage	u
inductance	L	inductance factor	AI
initial permeability	μί	intensity of magnetization	I
magnetic field strength	Н	magnetic flux	Ф
magnetic flux density	В	magnetic mass susceptibility	χρ
magnetic moment	m	magnetic polarization	J
magnetic susceptibility	χ	magnetization	М
magnetomotive force	Fm	permeability	μ
permeability of vacuum	μ0	relative permeability	μr
reluctance	Rm	remnance	Br

Magnetic quantities in the SI

An Example Toroid Core

As a concrete example for the calculations throughout this page we consider the

'recommended' toroid, or *ring core*, used in this Faculty. Manufacturers use toroids to derive material characteristics because there is no gap, even a residual one. Such tests are done using fully wound cores rather than just the two turns here; but, providing the permeability is high, then the error will be small.

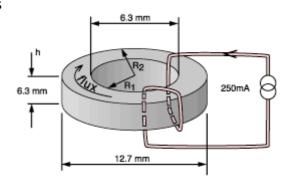


Fig. TDE: An example toroid.

Parameter	Symbol	Value
Effective magnetic path length	le	27.6×10 ⁻³ m
Effective core area	Ae	19.4×10 ⁻⁶ m ₂
Relative permeability	μr	2490
Inductance factor	AI	2200 nH
saturation flux density	Bsat	360 mT

Data for approved toroid

Let's take a worked example to find the inductance for the winding shown with just two turns (N=2).

$$\Sigma$$
I/A = le / Ae = 27.6×10⁻³ / 19.4×10⁻⁶ = 1420 m⁻¹ μ =
μ0 × μr = 1.257×10⁻⁶ × 2490 = 3.13×10⁻³ Hm⁻¹
Rm = (ΣI/A) / μ = 1420 / 3.13×10⁻³ = 4.55×10⁵ A-t Wb⁻¹
AI = 10⁹ / Rm = 10⁹ / 4.55×10⁵ = 2200 nH per turn²
L = AI × N² = 2200 × 10⁻⁹ × 2² = 8.8 μH



Core Factor

Ouantity name	core factor or geometric
	core constant

Quantity symbol	ΣΙ/Α
Unit name	per metre
Unit symbols	m-1

Core Factor in the SI

The idea of core factor is, apart from adding to the jargon :-(, to encapsulate in one figure the contribution to core reluctance made by the size and shape of the core. It is usually quoted in the data sheet but it is calculated as $\Sigma I/A = Ie/Ae$ m⁻¹

So for our example toroid we find -

$$\Sigma I/A = 27.6 \times 10^{-3} / 19.4 \times 10^{-6} = 1420 \text{ m}^{-1}$$

Core factors are often specified in millimetres⁻¹. You should then multiply by 1000 before using them in the formula for reluctance.

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Effective Area

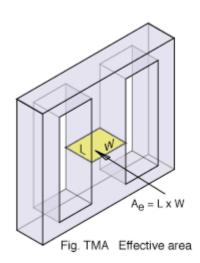
Quantity name	effective Area
Quantity symbol	Ae
Unit name	square metre
Unit symbols	m2

Effective Area in the SI

The 'effective area' of a core represents the cross sectional area of one of its limbs. Usually this corresponds closely to the physical dimensions of the core but because flux may not be distributed completely evenly the manufacturer will specify a value for Ae which reflects this.

The need for the core area arises when you want to relate the flux density in the core (limited by the material type) to the total flux it carries $Ae = \Phi / B$

In the example toroid the area could be determined approximately as the product of the core height and the difference between the major and minor radii $Ae = 6.3 \times ((12.7 - 6.3) / 2) = 20.2 \text{ mm}^2$



However, because the flux concentrates where the path length is shorter it is better to use the value stated by the manufacturer - 19.4 mm². For the simple toroidal shape Ae is calculated (Snelling) as

$$Ae = h \times ln^2(R_2/R_1) / (1/R_1 - 1/R_2) m^2$$

This assumes square edges to the toroid; real ones are often rounded.

There is a slight twist to the question of area: the manufacturer's value for Ae will give give the correct results when used to compute the core reluctance but it may not be perfect for computing the saturation flux (which depends upon the narrowest part of the core or Amin). In a well designed core Amin won't be very different from Ae, but keep it in mind.

⚠ Effective area is usually quoted in millimetres squared. Many formulae in data books implicitly assume that a numerical value in mm² be used. Other books, and these notes, assume metres squared. [↑ Top of page]

Effective Length

Quantity name	effective length
Quantity symbol	le
Unit name	metre
Unit symbols	m

Effective Length in the SI

The 'effective length' of a core is a measure of the distance which flux lines travel in making a complete circuit of it. Usually this corresponds closely to the physical dimensions of the core but because flux has a tendency to concentrate on the inside corners of the path the manufacturer will specify a value for le which reflects this.

In the toroid example the path length could be determined approximately as $le = \pi \times I$

$$(12.7 + 6.3) / 2 = 29.8 \text{ mm}$$

However, because the flux concentrates where the path length is shorter it is better to use the value stated by the manufacturer - 27.6 mm. For a simple toroidal shape le is calculated as le = $2\pi \times \ln(R_2/R_1)/(1/R_1-1/R_2)$

Another common core type, the EE, is shown in Fig: EEE. The red line represents the shortest path which a flux line could take to go round the core. The green line is the longest. Shown in blue is a path

whose length is that of the short path plus four sectors whose radius is sufficient to take the path midway down the limbs.

This is all a bit approximate; but bear in mind that since manufacturing tolerances on permeability are often 25% there isn't much point in being more exact.

 \triangle Effective length is usually quoted in millimetres. Many formulae in data books implicitly assume that a numerical value in mm be used. Other books, and these notes, assume metres. $l_e = 2(3.8 + 1.2)$

 $+\pi((2.63 - 1.2) / 2)$ Equation TMB = 12.25 mm

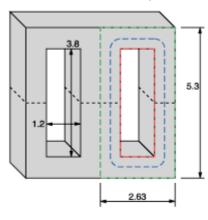
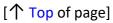


Fig. EEE: An example EE core.



Magnetomotive Force

Quantity name Quantity symbol	magnetomotive force, alias magnetic potential Fm, η or \Im
Unit name	ampere
Unit symbol	A

Magnetomotive Force in the SI

Duality with the Electric World

QuantityUnitFormulaMagnetomotive force amperes $Fm = H \times Ie$

V = E (Electric field strength)
× I (distance)

Electromotive force volts

MMF can be thought of as the

magnetic equivalent of electromotive force. You can calculate it as -

 $Fm = I \times N$ ampere turns

Equation TMM

The units of MMF are often stated as ampere turns (A-t) because of this. In the example toroid core-

$$Fm = 0.25 \times 2 = 0.5$$
 ampere turns

Equation TMC

Don't confuse magnetomotive force with magnetic field strength (magnetizing force). As an analogy think of the plates of a capacitor with a certain *electromotive* force (EMF) between them. How high the electric field strength is will depend on the distance between the plates. Similarly, the magnetic field strength in a transformer core depends not just on the MMF but also on the distance that the flux must travel round it.

A magnetic field represents stored energy and

$$F_m = 2 W / \Phi$$
 Equation TMF

where W is the energy in joules. You can also relate MMF to the total flux going through part of a magnetic circuit whose reluctance you know.

$$Fm = \Phi \times Rm$$
 Rowland's Law

There is a clear analogy here with an electric circuit and Ohm's Law, $V = I \times R$. The analogy with electric potential (voltage) leads to the alternate name *magnetic potential*. There is, however, then a risk of confusion with *magnetic vector potential* - which has quite different units. A specific MMF is required to sustain a given field strength along a known path length -

$$F_m = H \times I_e$$
 Equation TMP

Practical coil windings are made from copper wire which has a current carrying capacity limited mainly by its cross-section. There is therefore a limit to the MMF of a coil in continuous operation of about 3.5×10^6 ampere-turns per square metre of aperture.

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Magnetic Field Strength

Quantity name	magnetic field strength alias magnetic field intensity alias the auxiliary field alias the H-field alias magnetizing force
Quantity symbol	Н
Unit name	ampere per metre

Unit symbols	A m ⁻¹	
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Magnetic Field Strength in the SI

Whenever current flows it is always accompanied by a magnetic field. Scientists talk of the field as

being due to 'moving electric charges' - a reasonable description of electrons flowing along a wire. The strength, or intensity, of this field surrounding a straight wire is given by

$$H = I / (2 \pi r)$$

Equation TML

where r, the distance from the wire, is small in comparison with the length of the wire. The situation for short wires is described by the Biot-Savart equation.

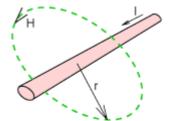


Fig. TMD The H-field near a long wire

By the way, don't confuse the speed of the charges (such as electrons) with the speed of a signal travelling down the wire they are in. Think of the signal as being the boundary between those electrons that have started to move and those that have

yet to get going. The boundary might move close to the speed of light $(3x10^8 \text{ m s}^{-1})$ whilst the electrons themselves drift (on average) something near to 0.1 mm s⁻¹. The electrons would be outpaced by a snail - even if it wasn't in a hurry.

You may object that magnetic fields are also produced by permanent magnets (like compass needles, door catches and fridge note holders) where no current flow is evident. It turns out that even here it is electrons moving in orbit around nuclei or spinning on their own axis which are responsible for the magnetic field.

Duality with the Electric World

Quantity Unit Formula

Magnetic field strength amperes per metre $H = F_m/le$

Electric field strength volts per metre $\varepsilon = e/d$

Magnetic field strength is analogous to

electric field strength. Where an electric field is set up between two plates separated by a distance, d, and having an electromotive force, e, between

them the electric field is given by -

$$\epsilon$$
 = e / d V m⁻¹ Equation TMG

Similarly, magnetic field strength is -

$$H = Fm / le$$
 Equation TMH

In the example the field strength is then -

$$H = 0.5 / 27.6 \times 10^{-3} = 18.1 \text{ A m}^{-1}$$

The analogy with electric field strength is mathematical and not physical. An electric field has a clearly defined physical meaning: simply the force exerted on a 'test charge' divided by the amount of charge.

Magnetic field strength cannot be measured in the same way because there is no 'magnetic monopole' equivalent to a test charge.

Do not confuse magnetic field strength with flux density, B. This is closely related to field strength but depends also on the material within the field. The strict definition of H is H = B / μ 0

- M

Sommerfeld Field Equation

This formula applies generally, even if the materials within the field have non-uniform permeability or a permanent magnetic moment. It is rarely used in coil design because it is usually possible to simplify the calculation by assuming that within the field the permeability can be regarded as uniform. With that assumption we say instead that $H = B / \mu$

Flux also emerges from a permanent magnet even when there are no wires to impose a field.

Equation TMU about

A field strength of about 2000 A m^{-1} is about the limit for cores made from iron powder. [\uparrow Top

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Magnetic Flux

Quantity name	magnetic flux
Quantity symbol	Φ
Unit name	weber
Unit symbol	Wb
Base units	kg m2 s-2 A-1

Magnetic Flux in the SI

We talk of magnetism in terms of lines of force or flow or *flux*. Although the Latin *fluxus*, means 'flow' the English word is older and unrelated. Flux, then, is a measure of the number of these lines - the total amount of magnetism.

You can calculate flux from the time integral of the voltage V on a winding -

$$\Phi = (1/N) V.dt$$
 webers

Equation TMX

This is one form of Faraday's law. If a constant voltage is applied for a time T then this boils down to -

$$\Phi = V \times T / N$$
 Wb

How much simpler can the maths get? Because of this relationship flux is sometimes specified as *volt seconds*.

Duality with the Electric World

QuantityUnitFormulaMagnetic flux Φ volt second= V × TElectric charge amp second (= coulomb) Q = I × T

Although as shown above flux corresponds in physical terms most closely to electric charge, you may find it easiest to envisage flux flowing round a core in the way that current flows round a circuit. When a given voltage is applied across a component with a known resistance then a specific current will flow. Similarly, application of a given magnetomotive force across a ferromagnetic component with a known reluctance results in a specific amount of magnetic flux -

$$\Phi = Fm / Rm$$
 Rowland's Law

There's a clear analogy here with Ohm's Law. You can also calculate flux as $\Phi = I \times L$

/ N

Flux can also be derived by knowing both the magnetic flux density and the area over which it applies:

$$\Phi = Ae \times B$$
 Equation TMS

A magnetic field represents energy stored within the space occupied by the field. So

$$\Phi = 2W/F_m$$
 Equation TMW

where W is the field energy in joules. Or, equivalently,

$$\Phi = \sqrt{2W/R_m}$$
 Equation TMZ

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Magnetic Flux Density

Quantity name	Magnetic flux density, alias Magnetic induction alias The B-field	
Quantity symbol	В	
Unit name	tesla	
Unit symbol	Т	
Base units	kg s-2 A-1	

Magnetic Flux Density in the SI

Duality with the Electric World

QuantityUnitFormulaMagnetic flux densityB $webers per metre^2$ = Φ /Area

Electric flux density $coulombs per metre^2 D = C/Area$

Flux density is simply the total flux divided by the cross sectional area of the part through which it flows -

$$B = \Phi / Ae$$
 teslas

Thus 1 weber per square metre = 1 tesla. Flux density is related to field strength via the permeability

$$B = \mu \times H$$
 Equation TMD

So for the example core -

$$B = 3.13 \times 10^{-3} \times 18.1 = 0.0567$$
 teslas

Equation TMD suggests that the 'B field' is simply an effect of which the 'H field' is the cause. Can we visualize any qualitative distinction between them? Certainly from the point of view of practical coil design there is rarely a need to go beyond equation TMD. However, the presence of magnetized materials modifies formula TMD B = μ 0 (M + H)

If the B field pattern around a bar magnet is compared with the H Sommerfeld field equation field then the lines of B form continuous loops without beginning or end whereas the lines of H may either originate or terminate at the *poles* of the magnet. A mathematical Maxwell's Equation for B statement of this general rule is div **B** = 0

You could argue that B indicates better the strength of a magnetic field than does the 'magnetic field strength' H! This is one reason why modern authors tend not to use these names and stick instead with 'B field' and 'H field'. The *definition of B* is in terms of its ability to produce a force F on a wire, length L, carrying current, I, -

$$B = F / (I \times L \times sin\theta)$$
 The Motor Equation

where θ is the angle between the wire and the field direction. So it seems that H describes the way magnetism is **generated** by moving electric charge (which is what a current is), while B is to do with the ability to be **detected** by moving charges.

In the end, both B and H are just abstractions which the maths can use to model magnetic effects. Looking for more solid explanations isn't easy.

A feel for typical magnitudes of B helps. One metre away in air from a long straight wire carrying one ampere B is exactly 200 nanoteslas. The earth's field has a value of roughly 60 microteslas (but varies from place to place). A largish permanant magnet will give 1 T, iron saturates at about 1.6 T and a super conducting electromagnet might achieve 15 T. [\(\bar{\tau}\) Top of page]

Flux Linkage

Quantity name	flux linkage
Quantity symbol	λ
Unit name	weber-turn
Unit symbol	Wb-t
Base units	kg m2 s-2 A-1

Flux Linkage in the SI

In an ideal inductor the flux generated by one of its turns would encircle all the other other turns. Real coils come close to this ideal when the cross sectional dimensions of the winding are small compared with its diameter, or if a high permeability core guides the flux right the way round. In longer air-core coils the situation is likely to be nearer to that shown in Fig.TFK: Here we see that the flux density decreases towards the ends of the coil as some flux takes a 'short cut' bypassing the outer turns. Let's assume that the current into the coil is 5 amperes and that each flux line represents 7 mWb.

The central three turns all 'link' four lines of flux: 28 mWb. The two outer turns link just two lines of flux: 14 mWb.

We can calculate the total 'flux linkage' for the coil as:

$$\lambda = 3 \times 28 + 2 \times 14 = 112$$
 mWb-t

The usefulness of this result is that it enables us to calculate the total self inductance of the coil, L: L = λ / I = 112/5 = 22.4 mH

In general, where an ideal coil is assumed, you see expressions involving N× Φ or N×d Φ /dt. For greater accuracy you substitute λ or d λ /dt.

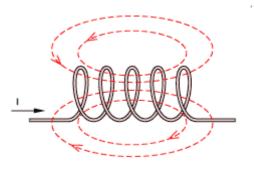


Fig. TFK: Flux Linkage



Inductance

Quantity name	Inductance
Quantity symbol	L
Unit name	henry
Unit symbol	Н
Base units	kg m2 s-2 A-2

Inductance in the SI

Duality with the Electric World

Quantity	Unit	Formula
Inductance		
Capacitance	webers per amp	L = Φ/I
volt $C = Q/V$		

Any length of wire has inductance. Inductance is a measure of a coil's ability to store energy in the form of a magnetic field. It is defined as the rate of change of flux with current $L = N \times d \Phi / d I$

If the core material's permeability is considered constant then the relation between flux and current is linear and so: $L = N \times \Phi / I$

By Substitution of Equation TMM and Rowland's Law -

Equation TMI

 $L = N^2 / R_m$ Equation TMA

You can relate inductance directly to the energy represented by the surrounding magnetic field

$$L = 2 W / I^2$$
 Equation TME

Where W is the field energy in joules.

In practice, where a high permeability core is used, inductance is usually determined from the AI value specified by the manufacturer for the core -

$$L = 10^{-9} \text{ Al} \times \text{N}^2$$
 Equation TMK

Inductance for the toroid example is then:

$$L = 2200 \times 10^{-9} \times 2^2 = 8.8 \mu H$$

If there is no ferromagnetic core so μr is 1.0 (the coil is 'air cored') then a variety of formulae are available to estimate the inductance. The correct one to use depends upon

- Whether the coil has more than one layer of turns.
- The ratio of coil length to coil diameter.
- The shape of the cross section of a multi-layer winding.
- Whether the coil is wound on a circular, polygonal or rectangular former.
- Whether the coil is open ended, or bent round into a toroid.
- Whether the cross section of the wire is round or rectangular, tubular or solid.
- The permeability of the wire.
- The frequency of operation.

The phase of the moon, direction of the wind etc..

Most of these variants are described in early editions of Terman or successor publications. There are too many formulae to reproduce here. You can find them all in Grover.



Inductance Factor

Quantity name	inductance factor
Quantity symbol	Aı
Unit name	nanohenry
Unit symbol	nH
Base units	kg m2 s-2 A-2

Inductance Factor

At is usually called the *inductance factor*, defined

$$AI = L \times 10^9 / N^2$$
 Equation TMT

If you know the inductance factor then you can multiply by the square of the number of turns to find the inductance in nano henries. In our example core AI = 2200, so the inductance is -

$$L = 2200 \times 10^{-9} \times 2^2 = 8800 \text{ nH} = 8.8 \mu\text{H}$$
 Equation TMV

The core manufacturer may directly specify an AI value, but frequently you must derive it via the reluctance, Rm. The advantage of this is that only one set of data need be provided to cover a range of cores having identical dimensions but fabricated using materials having different permeabilities.

$$AI = 10^9 / R_m$$
 Equation TMY

So, for our example toroid core -

$$AI = 10^9 / 4.55 \times 10^5 = 2200$$
 Equation TSA

The inductance factor may sometimes be expressed as "millihenries per 1000 turns". This is synonymous with nanohenries per turn and takes the same numerical value.

If you have no data on the core at all then wind ten turns of wire onto it and measure the inductance (in henrys) using an inductance meter. The AI value will be 10⁷ times this reading.

At values are, like permeability, a non-linear function of flux. The quoted values are usually measured at low (<0.1 mT) flux.



Reluctance

Quantity name	reluctance
Quantity symbol	Rm or R
Unit name	per henry or ampere-
Offic flame	turns per weber
Unit symbols	H-1
Base units	A2 s2 kg-1 m-2

Reluctance in the SI

Reluctance is the ratio of MMF to flux -

$$Rm = Fm / \Phi$$
 Rowland's Law

In a magnetic circuit this corresponds to Ohm's Law and resistance in an electric circuit. Compare

$$Re = V / I$$

Reluctance is also proportional to the core factor, $\Sigma I/A$, but inversely proportional to permeability -

$$Rm = (\Sigma I/A) / \mu$$
 Equation TMQ

Again, compare

Re = ($\Sigma I/A$) / σ where σ is the electrical conductivity of a conductor of given length and cross-sectional area.

Take care to use the absolute rather than the relative permeability here. So for the toroid example reluctance is then:

$$Rm = 1420 / 3.13 \times 10^{-3} = 4.55 \times 10^{5}$$
 A-t Wb⁻¹

A magnetic field represents stored energy and

$$Rm = 2 \text{ W} / \Phi^2$$
 Equation TMR where W is the energy in joules.

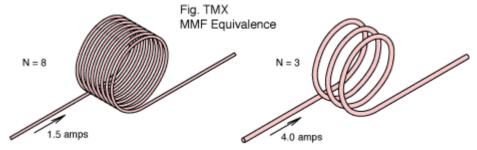
Although it can be a useful concept when analyzing series or parallel combinations of magnetic components reluctance is, like permeability, non-linear and must be used carefully. [\tau Top of page]

Current

Quantity name	current
Quantity symbol	l, i
Unit name	ampere
Unit symbol	А

Current in the SI

You might be forgiven for thinking that there would be no need to spell out what current is. That's obvious surely? Your mistake is to forget how



hard all writers on electromagnetism strive to obfuscate an already difficult subject. Here's the problem.

Figure TMX shows two coils with different numbers of turns but the

same magneto-motive force.

When considering the MMF it makes no difference whether you have twelve turns of wire carrying one amp, or

three turns carrying four amps, or two turns with six amps. As far as the MMF goes it's all just 'twelve ampere-turns'. You will get just the same magnetic field in each case. I = Fm / N

Reasoning that detail about the number of turns and the number of amps doesn't Equation TSD matter, only the **product of the two**, some writers decide to say that the current **is** twelve amps. They write I = 12 A and leave it to you to decide which scenario brought about that 'current'. This insidious practice carries over to formulae as well.

Which is fine as long as it's consistent and clear to the reader what's happening. If the current changes then, by Faraday's Law we have an induced voltage. You then have to remember that the induced voltage is **per turn** and not the total coil voltage. Ambiguity starts to creep in.

It depends, perhaps, on whether you're more interested in physics or engineering. These pages take the latter view and distinguish current from MMF. Current here, then, is what an ordinary ammeter reads, and the number of coil turns, N, is written explicitly.

The physicists get their way in the end because, although you might just speak of reluctance as 'ampere-turns per weber', inductance as 'weber-turns per ampere' is getting a little contrived - even if it does reflect the concept of flux linkage rather nicely. But permeability as 'weberturns per amperemetre'?

These pages are being converted to use upper case I both for direct current and for a current given as an RMS quantity; whilst the lower case I will stand for instantaneous values of time varying current.

Trivia point: why is the symbol I used for current? Allegedly, it stands for 'electric *intensity*', as opposed to 'total amount of electricity' (charge). Maxwell, though, used the symbol C for current and used electric intensity to refer to the E-field: what most people today know as electric field strength. So it goes.

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Current density

Quantity name	current density
Quantity symbol	J
Unit name	amperes per square metre
Unit symbol	A m ⁻²

Current density in the SI

Current density is simply the total electric current divided by the area over which it is flowing. Example: if a wire 0.7 millimetres diameter carries a current of 0.5 amperes then the current density is

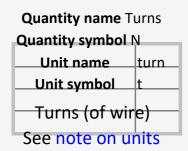
$$J = 0.5 / (\pi \ 0.0007^2 / 4) = 1.30 \times 10^6 \ A \ m^{-2}$$

Equation TMJ

Or 1.3 amps per millimetre². A reasonable limit for most small transformers is 3.5×10^6 A m⁻². [\uparrow Top

of page]

The number of turns



By tradition, coil calculations use the capital letter N to represent the total number of turns in the coil. Solenoid coils are sometimes described using the lower case letter n to represent the number of turns per unit length. So

 $N = n \times I_a$ Equation TMN

Where la is the axial length of the coil.

Naturally, for most designs, the number of turns required is the \$64,000 question. The answer comes in a bewildering variety of forms. For the most common case, such as the example toroid core, where the manufacturer has specified AI -

 $N = \sqrt{(10^9 L/AI)}$

Equation TSB

So, if you needed 330 microhenries then

 $N = \sqrt{(10^9 \times 330 \times 10^{-6} / 2200)} = 12 \text{ turns}$

Equation TSC

[Top of page]

Relationships between magnetic quantities

Flux, field strength, permeability, reluctance it's easy to go into jargon overload. Snelling lists over 360 different symbol uses connected with ferromagnetics. There isn't even agreement about what to call some properties (I say remnance, you say remanence, he says retentivity). You will cope better if you can form a mental picture of the party that these names throw when they get together inside your transformer.

Analogy with electric quantities:

You may find it easier to obtain an intuitive grasp of the relationships between magnetic quantities by thinking in terms of 'magnetic circuits' with flux flowing round a core in a fashion analogous to current flowing round an electric circuit.

Magnetic Electric quantity quantity

magnetomotive force	electromotive force (voltage)	
magnetic field strength	electric field strength	
permeability	conductivity	
magnetic flux	current	
magnetic flux density	current density	
reluctance	resistance	e then imagine that the core and the

Electric analogues

wing through both reluctance

r example, if you have a transformer with a gapped cor gap m a series magnetic circuit with the same flux mponents in an analogous fashion to a series electric circuitough two resistors -

$$F_m = \Phi \times (R_{m_gap} + R_{m_core})$$
 ampere-turns compare $V = I \times (R1 + R2)$ volts

ere's an entire family of formulae which take similar forms

falls rather quickly if you realise that flux flowing through a reluctance

analogies break down when pushed too far. rent flowing through a resistor dissipates energy while es not. In fact you can ask whether flux is a real physical efectron flow is).

quence of operation

the windings.

ansformer (or other wound

transformer design you would normally like to deal in termy cares about is the **current** in the wever, the key to understanding what happens in a mponent) is to realise that what the windings; and that erything follows on from that.

The current in a winding produces magneto-motive

$$Fm = I \times N$$
 ampere-turns

The magneto-motive force produces magnetic fiel

$$H = Fm / le$$
 ampere-turns per metre

• The field produces magnetic flux density -

$$B = \mu \times H$$
 tesla total flux -

Summed over the cross-sectional area of the core

$$\Phi = B \times Ae$$
 webers

The time-varying flux produces induced voltage
 e = N × dΦ/dt volts

If you can follow this five step sequence then building a mental image of a magnetic component becomes simpler. Remember, you put in a current and get back an induced voltage. In fact, if you can treat the permeability as being linear, then the constants N, le, μ and Ae can be lumped together into one constant for the winding which is called (surprise!) Inductance, L -

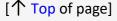
$$L = \mu \times Ae \times N^2 / le$$
 henrys

I give the base units for all the quantities in this equation; enabling thrill-seekers to make a dimensional analysis verifying that it is consistent. Right, so then our five step relationship between current and EMF boils down to:

$$e = L \times dI/dt$$
 volts

You may be about to complain that you know the EMF on your winding but don't know the current in it. The answer is that the process then works in reverse - the current will build up until the induced voltage is sufficient to oppose the applied voltage. You can find out more by looking at Faraday's law.

How do you take into account the presence of the secondary windings in a transformer? One way is to take the first four steps of the sequence above and apply them separately to each winding (whether primary or secondary). The arithmetic sum over all windings gives total core flux. From the time rate of change of flux you then have the induced voltage in each winding (since you also know the number of turns for each). There are less tedious methods of analyzing transformer operation which you would probably do better using. But they are another story.



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