## MACM 201 Homework 1 - Solutions

1. List all strings of size 3 over the alphabet  $\{A, B\}$ .

Solution: AAA, AAB, ABA, ABB, BAA, BAB, BBA, BBB

2. Find all permutations of  $\{X, Y, Z\}$ .

Solution: XYZ, XZY, YXZ, YZX, ZXY, ZYX

3. Find all strings of length 4 over the alphabet  $\{0, 1, 2\}$  with the property that there are no 10, 21, or 20 substrings.

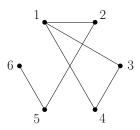
Solution: Observe that a string satisfying these properties is a non-decreasing sequence. It will consist of a string of 0's then a string of 1's, then a string of 2's (any one of which might be empty). Therefore, the valid strings are:

0000,0001,0002,0011,0012,0111,0112,0122,0222,1111,1112,1122,1222,2222

4. Draw the graph G = (V, E) given by

$$V = \{1, 2, 3, 4, 5, 6\} \qquad \text{and} \qquad E = \{\{1, 2\}, \{1, 3\}, \{1, 4\}, \{2, 5\}, \{3, 4\}, \{5, 6\}\}.$$

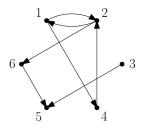
Solution:



5. Draw the directed graph G = (V, E) given by

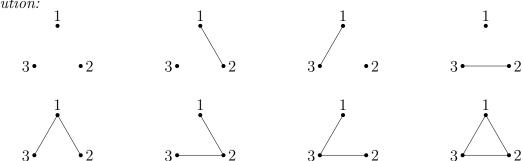
$$V = \{1, 2, 3, 4, 5, 6\}$$
 and  $E = \{(1, 2), (2, 1), (1, 4), (2, 6), (4, 2), (3, 5), (6, 5)\}.$ 

Solution:



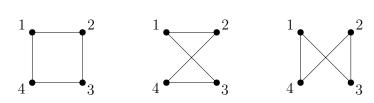
6. Find all 8 graphs with vertex set  $V = \{1, 2, 3\}$ .

Solution:



7. Find all graphs with vertex set  $V = \{1, 2, 3, 4\}$  that are cycles.

Solution:



8. Draw a rooted tree with 9 vertices and no vertex of level 3.

Solution: There are many correct answers to this, below are two possibilities.



