Dynamic programming

70. Climbing Stairs

- 1. You are climbing a staircase. It takes n steps to reach the top.
- 2. Each time you can either climb 1 or 2 steps. In how many distinct ways can you climb to the top?

Solution:

```
class Solution {
   public int climbStairs(int n) {
      int[] res = new int[n+1];
      res[0]=0;
      res[1] = 1;
      res[2] = 2;
      for (int i = 3; i < n+1;i++) {
            res[i] = res[i-1] + res[i-2];
      }
      return res[n];
   }
}</pre>
```

322. Coin Change

You are given an integer array coins representing coins of different denominations and an integer amount representing a total amount of money. Return *the fewest number of coins that you need to make up that amount*. If that amount of money cannot be made up by any combination of the coins, return -1.

```
public int coinChange(int[] coins, int amount) {// Create an array to store the
fewest number of coins needed to make up each amount
```

```
int[] dp = new int[amount + 1];
       Arrays.fill(dp, amount + 1);
       dp[0] = 0; // Base case: 0 coins needed to make up 0 amount
       // Iterate through each amount from 1 to the target amount
       for (int i = 1; i <= amount; i++) {
           // Try each coin denomination
           for (int coin : coins) {
               if (coin <= i)
// If using this coin results in a smaller number of coins needed, update dp[i]
                   dp[i] = Math.min(dp[i], dp[i - coin] + 1);
       }
       // If dp[amount] is still amount + 1, it means the amount cannot be made
up by any combination of coins
       return dp[amount] > amount ? -1 : dp[amount];
```

300. Longest Increasing Subsequence

Solved

Medium

TopicsCompanies

Given an integer array nums, return the length of the longest strictly increasing

subsequence

Example 1:

Input: nums = [10,9,2,5,3,7,101,18]

Output: 4

Explanation: The longest increasing subsequence is [2,3,7,101], therefore the length is 4.

```
class Solution {
  public int lengthOfLIS(int[] nums) {
       if (nums == null || nums.length == 0) {
           return 0;
       }
       int[] dp = new int[nums.length];
       Arrays.fill(dp, 1);
       int maxLength = 1;
       for (int i = 1; i < nums.length; i++) {
           for (int j = 0; j < i; j++) {
               if (nums[i] > nums[j]) {
                   dp[i] = Math.max(dp[i], dp[j] + 1);
                   maxLength = Math.max(maxLength, dp[i]);
               }
       }
       return maxLength;
   }
}
```

139. Word Break

Solved

Medium

TopicsCompanies

Given a string s and a dictionary of strings wordDict, return true if s can be segmented into a space-separated sequence of one or more dictionary words.

Note that the same word in the dictionary may be reused multiple times in the segmentation.

```
public class Solution {
       public boolean wordBreak(String s, List<String> wordDict) {
           // Convert wordDict to a set for faster lookup
           Set<String> wordSet = new HashSet<>(wordDict);
           // Create a boolean array to track if a substring can be segmented
           boolean[] dp = new boolean[s.length() + 1];
           dp[0] = true;
           // Iterate through the string
           for (int i = 1; i <= s.length(); i++) {</pre>
               // Check if the substring from index 0 to i can be segmented
               for (int j = 0; j < i; j++) {
                   if (dp[j] && wordSet.contains(s.substring(j, i))) {
                       dp[i] = true;
                       break;
                   }
               }
           return dp[s.length()];
   }
}
```

64. Minimum Path Sum

Given a m x n grid filled with non-negative numbers, find a path from top left to bottom right, which minimizes the sum of all numbers along its path.

Note: You can only move either down or right at any point in time.

```
public class Solution {
  public int minPathSum(int[][] grid) {
     int m = grid.length; // Number of rows
     int n = grid[0].length; // Number of columns
     // Initialize a 2D array to store the minimum sum to reach each cell
     int[][] dp = new int[m][n];
     // Base case: Initialize the first cell with the value from the grid
     dp[0][0] = grid[0][0];
     // Initialize the first row: sum of values to reach each cell
     for (int j = 1; j < n; j++) {
        dp[0][j] = dp[0][j - 1] + grid[0][j];
     }
     // Initialize the first column: sum of values to reach each cell
     for (int i = 1; i < m; i++) {
        dp[i][0] = dp[i - 1][0] + grid[i][0];
     }
     // Compute the minimum sum to reach each cell
     for (int i = 1; i < m; i++) {
        for (int j = 1; j < n; j++) {
           // Minimum sum to reach the current cell is the sum of the value in the current cell
          // and the minimum of the values to reach the cell above and the cell to the left
          dp[i][j] = grid[i][j] + Math.min(dp[i - 1][j], dp[i][j - 1]);
        }
     }
     // Return the minimum sum to reach the bottom-right cell
     return dp[m - 1][n - 1];
}
```

63. Unique Paths II

Solved

Medium

TopicsCompanies

Hint

You are given an m x n integer array grid. There is a robot initially located at the **top-left corner** (i.e., grid[0][0]). The robot tries to move to the **bottom-right corner** (i.e., grid[m - 1][n - 1]). The robot can only move either down or right at any point in time.

An obstacle and space are marked as 1 or 0 respectively in grid. A path that the robot takes cannot include **any** square that is an obstacle.

Return the number of possible unique paths that the robot can take to reach the bottom-right corner.

```
public class Solution {
   public int uniquePathsWithObstacles(int[][] obstacleGrid) {
       int m = obstacleGrid.length; // Number of rows
       int n = obstacleGrid[0].length; // Number of columns
       // Initialize a 2D array to store the number of unique paths to reach
each cell
       int[][] dp = new int[m][n];
       // Base case: Initialize the first cell with 1 if it's not an obstacle,
0 otherwise
       dp[0][0] = (obstacleGrid[0][0] == 0) ? 1 : 0;
       // Initialize the first row: number of unique paths to reach each cell
       for (int j = 1; j < n; j++) {
           if (obstacleGrid[0][j] == 0) {
               dp[0][j] = dp[0][j - 1];
           }
       }
       // Initialize the first column: number of unique paths to reach each
cell
       for (int i = 1; i < m; i++) {</pre>
           if (obstacleGrid[i][0] == 0) {
               dp[i][0] = dp[i - 1][0];
```

```
}
}

// Compute the number of unique paths to reach each cell
for (int i = 1; i < m; i++) {
    for (int j = 1; j < n; j++) {
        // If the current cell is not an obstacle, compute the number of unique paths

    if (obstacleGrid[i][j] == 0) {
        dp[i][j] = dp[i - 1][j] + dp[i][j - 1];
      }
}

// Return the number of unique paths to reach the bottom-right corner return dp[m - 1][n - 1];
}
</pre>
```

5. Longest Palindromic Substring

Given a string s, return the longest Palindromic substring in s

Example 1:

Input: s = "babad"
Output: "bab"

Explanation: "aba" is also a valid answer

Example 2:

Input: s = "cbbd"

Output: "bb"

```
public class Solution {
   public String longestPalindrome(String s) {
     int n = s.length();
```

```
boolean[][] dp = new boolean[n][n];
       String longestPalindrome = "";
       // Base case: single characters are palindrome
       for (int i = 0; i < n; i++) {
           dp[i][i] = true;
           longestPalindrome = s.substring(i, i + 1);
       }
       // Check for palindromic substrings of length 2
       for (int i = 0; i < n - 1; i++) {
           if (s.charAt(i) == s.charAt(i + 1)) {
               dp[i][i + 1] = true;
               longestPalindrome = s.substring(i, i + 2);
       }
       // Check for palindromic substrings of length greater than 2
       //here dp is based on length of the string considered for palindrome and
is made of 2 d array of that string length.
       for (int length = 3; length <= n; length++) {</pre>
           for (int i = 0; i <= n - length; i++) {</pre>
               int j = i + length - 1;
               // because i and j chars are length apart and are checked for
equality to check for palindrome
               //checking if i and j chars are same and dp in between is sorted
already.
               if (s.charAt(i) == s.charAt(j) && dp[i + 1][j - 1]) {
                   dp[i][j] = true;
                   longestPalindrome = s.substring(i, j + 1);
       }
      return longestPalindrome;
}
```

97. Interleaving String

Given strings s1, s2, and s3, find whether s3 is formed by an **interleaving** of s1 and s2.

An **interleaving** of two strings s and t is a configuration where s and t are divided into n and m

substrings

respectively, such that:

- $S = S_1 + S_2 + ... + S_n$
- $t = t_1 + t_2 + ... + t_m$
- |n m| <= 1
- The interleaving is $s_1 + t_1 + s_2 + t_2 + s_3 + t_3 + ...$ or $t_1 + s_1 + t_2 + s_2 + t_3 + s_3 + ...$

Note: a + b is the concatenation of strings a and b.

Note: here it is such that S3 len = s1 + s2 length.

```
public class Solution {
  public boolean isInterleave(String s1, String s2, String s3) {
       int m = s1.length(), n = s2.length();
       if (m + n != s3.length()) return false;
       boolean[][] dp = new boolean[m + 1][n + 1];
       // Initialize dp[0][0] as true
       dp[0][0] = true;
       // Fill the first row
       for (int j = 1; j \le n; j++) {
           dp[0][j] = dp[0][j-1] \&\& s2.charAt(j-1) == s3.charAt(j-1);
       }
       // Fill the first column
       for (int i = 1; i <= m; i++) {
           dp[i][0] = dp[i - 1][0] \&\& s1.charAt(i - 1) == s3.charAt(i - 1);
       }
       // Fill the remaining cells
       for (int i = 1; i <= m; i++) {
```