

ECE341 Homework No. 8 Solution

Problem No. 1

For each 16M x 8 memory chip:

Word size = 8 bits

Memory capacity = $16\text{M} * 8 = 2^{24} * 2^3 = 2^{27}$ bits

For the entire 64M x 128 memory:

Word size = 128 bits

Total memory capacity = $64\text{M} * 128 = 2^{26} * 2^7 = 2^{33}$ bits

Number of memory chips needed = Total memory size / Size of each chip = $2^{33}/2^{27} = 2^6 = 64$

Number of memory chips needed per row = Word size for entire memory / Word size for each chip = $128/8 = 16$

Number of rows needed = Total number of memory chips / Memory chips per row = $64 / 16 = 4$

The required structure is essentially the same as in Figure 8.10, except that each of the **four** rows has **sixteen** 16M x 8 chips. Address lines A_{19-0} should be connected to all chips. Address lines A_{21-20} should be connected to a 2-bit decoder to select one of the 4 rows.

Problem No. 2

- (a) Temporal locality refers to the program property that recently accessed data/instructions are likely to be accessed again very soon. Spatial locality refers to the property that if one address is accessed by a program, then the data/instructions in the spatially adjacent (or nearby) addresses are likely to be accessed as well.
- (b) Loop-A is expected to have more instruction cache hits. This is because loop-A has more iterations and thus the same instructions keep on getting accessed over and over again. Furthermore, loop-A has fewer instructions in each iteration, causing the instruction footprint to easily fit in a small cache.
- (c) Increasing the cache block size results in more data being transferred from the main memory to the cache on every cache miss.

Advantage: This can result in a higher cache hit ratio, if the application exhibits high spatial locality.

Disadvantages: (i) This can increase the cache miss latency, (ii) It can result in fragmentation and wastage of capacity, if the program does not exhibit high spatial locality.

Problem No. 3

Block size = 64 bytes = 2^6 bytes = 2^6 words (since 1 word = 1 byte)

Therefore, **Number of bits in the Word field = 6**

Cache size = 64K-byte = 2^{16} bytes

Number of cache blocks = Cache size / Block size = $2^{16}/2^6 = 2^{10}$

Therefore, **Number of bits in the *Block* field = 10**

Total number of address bits = 46

Therefore, **Number of bits in the *Tag* field = 46 - 6 - 10 = 30**

Problem No. 4

(a) Block size = 64 bytes = 2^6 bytes = 2^6 words

Cache size = 2M-byte = 2^{21} bytes

Number of cache blocks per set = $16 = 2^4$

Number of sets = Cache size / (Block size * Number of blocks per set) = $2^{21} / (2^6 * 2^4) = 2^{11} =$
2048

(b) **Number of bits in the *Word* field = 6**

Number of bits in the *Set* field = 11

Total number of address bits = 46

Therefore, **Number of bits in the *Tag* field = 46 - 6 - 11 = 29**

Problem No. 5

Block size = 16 words = 2^4 words \Rightarrow No. of bits in the *Word* field = 4

Number of cache blocks = 8 = 2^3 \Rightarrow No. of bits in the *Block* field = 3

Total number of address bits = 10 \Rightarrow No. of bits in the *Tag* field = 10 - 4 - 3 = 3

For a given 10-bit address, the 3 most significant bits represent the *Tag*, the next 3 bits represent the *Block*, and the 4 least significant bits represent the *Word*.

(a) The cache is initially empty. Therefore, all the cache blocks are invalid.

Access # 1:

Address = $(20)_{10} = (0000010100)_2$

For this address, *Tag* = 000, *Block* = 001

Since the cache block 001 is empty before this access, this will be a cache **miss**

After this access, *Tag* field for **cache block 001** is set to **000**

Access # 2:

Address = $(32)_{10} = (0000100000)_2$

For this address, *Tag* = 000, *Block* = 010

Since the cache block 010 is empty before this access, this will be a cache **miss**

After this access, *Tag* field for **cache block 010** is set to **000**

Access # 3:

Address = $(512)_{10} = (1000000000)_2$

For this address, *Tag* = 100, *Block* = 000

Since the cache block 000 is empty before this access, this will be a cache **miss**

After this access, *Tag* field for **cache block 000** is set to **100**

Access # 4:

Address = $(160)_{10} = (0010100000)_2$

For this address, *Tag* = **001**, *Block* = 010

Current tag for cache block 010 = **000** (set in access # 2)
 Address tag does not match the block tag => cache **miss**
 After this access, *Tag* field for **cache block 010** is set to **001**

Access # 5:

Address = $(32)_{10} = (0000100000)_2$
 For this address, *Tag* = **000**, *Block* = 010
 Current tag for cache block 010 = **001** (set in access # 4)
 Address tag does not match the block tag => cache **miss**
 After this access, *Tag* field for **cache block 010** is set to **000**

Access # 6:

Address = $(896)_{10} = (1110000000)_2$
 For this address, *Tag* = **111**, *Block* = 000
 Current tag for cache block 000 = **100** (set in access # 3)
 Address tag does not match the block tag => cache **miss**
 After this access, *Tag* field for **cache block 000** is set to **111**

Access # 7:

Address = $(904)_{10} = (1110001000)_2$
 For this address, *Tag* = **111**, *Block* = 000
 Current tag for cache block 000 = **111** (set in access # 6)
 Address tag matches the block tag => cache **hit**

Access # 8:

Address = $(512)_{10} = (1000000000)_2$
 For this address, *Tag* = **100**, *Block* = 000
 Current tag for cache block 000 = **111** (set in access # 6)
 Address tag does not match the block tag => cache **miss**
 After this access, *Tag* field for **cache block 000** is set to **100**

Cache hit ratio = Number of hits / Number of accesses = $1 / 8 = 0.125$

(b) The tag contents for the cache are shown below:

| | | | | | | | | |
|--------------|-----|-----|-----|---------|---------|---------|---------|---------|
| Block | 000 | 001 | 010 | 011 | 100 | 101 | 110 | 111 |
| Tag | 100 | 000 | 000 | Invalid | Invalid | Invalid | Invalid | Invalid |

Problem No. 6

Block size = 16 words = 2^4 words => No. of bits in the *Word* field = 4

Number of cache blocks = $8 = 2^3$

Cache blocks per set = 2 (2-way set-associative cache)

Therefore, number of sets = $8 / 2 = 4 = 2^2$ => No. of bits in the *Set* field = 2

Total number of address bits = 10 => No. of bits in the *Tag* field = $10 - 4 - 2 = 4$

For a given 10-bit address, the 4 most significant bits represent the *Tag*, the next 2 bits represent the *Set*, and the 4 least significant bits represent the *Word*.

The cache is initially empty. Therefore, all the cache blocks are invalid.

Access # 1:

Address = $(20)_{10} = (0000010100)_2$

For this address, $Tag = 0000$, $Set = 01$

Since the cache is empty before this access, this will be a cache **miss**

Cache contents after this access are:

| | | | | | | | | |
|--------------|-----------|---------|-------------|---------|-----------|---------|-----------|---------|
| Set | 00 | | 01 | | 10 | | 11 | |
| Block | 0 | 1 | 0 | 1 | 0 | 1 | 0 | 1 |
| Tag | Invalid | Invalid | 0000 | Invalid | Invalid | Invalid | Invalid | Invalid |

Access # 2:

Address = $(32)_{10} = (0000100000)_2$

For this address, $Tag = 0000$, $Set = 10$

Since the set “10” is empty before this access, this will be a cache **miss**

Cache contents after this access are:

| | | | | | | | | |
|--------------|-----------|---------|-----------|---------|-------------|---------|-----------|---------|
| Set | 00 | | 01 | | 10 | | 11 | |
| Block | 0 | 1 | 0 | 1 | 0 | 1 | 0 | 1 |
| Tag | Invalid | Invalid | 0000 | Invalid | 0000 | Invalid | Invalid | Invalid |

Access # 3:

Address = $(512)_{10} = (1000000000)_2$

For this address, $Tag = 1000$, $Set = 00$

Since the set “10” is empty before this access, this will be a cache **miss**

Cache contents after this access are:

| | | | | | | | | |
|--------------|-------------|---------|-----------|---------|-----------|---------|-----------|---------|
| Set | 00 | | 01 | | 10 | | 11 | |
| Block | 0 | 1 | 0 | 1 | 0 | 1 | 0 | 1 |
| Tag | 1000 | Invalid | 0000 | Invalid | 0000 | Invalid | Invalid | Invalid |

Access # 4:

Address = $(160)_{10} = (0010100000)_2$

For this address, $Tag = 0010$, $Set = 10$

Address tag does not match any of the block tags in set 10 => cache **miss**

New contents are inserted in block-1 of set 10. Cache contents after this access are:

| | | | | | | | | |
|--------------|-----------|---------|-----------|---------|-----------|------|-----------|---------|
| Set | 00 | | 01 | | 10 | | 11 | |
| Block | 0 | 1 | 0 | 1 | 0 | 1 | 0 | 1 |
| Tag | 1000 | Invalid | 0000 | Invalid | 0000 | 0010 | Invalid | Invalid |

Access # 5:

Address = $(32)_{10} = (0000100000)_2$

For this address, $Tag = 0000$, $Set = 10$

Current tag for cache block “0” in set 00 = **0000**

Address tag matches the block tag => cache **hit**. There is no change in cache contents.

Access # 6:

Address = $(896)_{10} = (1110000000)_2$

For this address, $Tag = 1110$, $Set = 00$

Address tag does not match any of the block tags in set 00 => cache miss

New contents are inserted in block-1 of set 00. Cache contents after this access are:

| Set | 00 | | 01 | | 10 | | 11 | |
|-------|------|------|------|---------|------|------|---------|---------|
| Block | 0 | 1 | 0 | 1 | 0 | 1 | 0 | 1 |
| Tag | 1000 | 1110 | 0000 | Invalid | 0000 | 0010 | Invalid | Invalid |

Access # 7:

Address = $(904)_{10} = (1110001000)_2$

For this address, $Tag = 1110$, $Set = 00$

Current tag for cache block “1” in set 00 = **1110**

Address tag matches the block tag => cache hit. There is no change in cache contents.

Access # 8:

Address = $(512)_{10} = (1000000000)_2$

For this address, $Tag = 1000$, $Set = 00$

Current tag for cache block “0” in set 00 = **1000**

Address tag matches the block tag => cache hit. There is no change in cache contents.

Cache hit ratio = Number of hits / Number of accesses = $3 / 8 = 0.375$