

1st case:
a and b operants
are positive:

$$\begin{array}{r} +3 \\ +7 \\ \hline 10 \end{array}$$
$$\begin{array}{r} 0000011 \\ 0000111 \\ \hline 0001010 \end{array}$$

2nd case:

1st number is +
2nd number is -

$$\begin{array}{r} +3 \\ (-10) \\ \hline -7 \end{array}$$
$$\begin{array}{r} +0000011 \\ +1110101 \\ \hline 1111000 \end{array}$$

→ missing value

göstriz

$$\begin{array}{r} 10 \\ \overline{-10} \\ 0 \end{array} \left| \begin{array}{r} 2 \\ | \\ 5 \\ \overline{-4} \\ 1 \end{array} \right| \begin{array}{r} 2 \\ | \\ 2 \\ \overline{-1} \\ 1 \end{array}$$

↓

00001010
↓ 11110101

$$\begin{array}{r} 3 \\ \overline{-2} \\ 1 \end{array} \left| \begin{array}{r} 2 \\ | \\ 1 \\ \overline{1} \\ . \end{array} \right.$$

3rd case:

1st number is -

2nd number is -

absolute value of

2nd number is less than
1st number

$$\begin{array}{r} 10 \\ + 3 \\ \hline \end{array} \quad \begin{array}{r} 00001010 \\ + 1111100 \\ \hline 000000110 \\ + 1 \\ \hline 00000111 \end{array}$$

carry bit

$$3 \rightarrow 0000011$$

$$-3 \rightarrow 1111100$$

4th case;

1st number is —

2nd number is

$$\begin{array}{r} & \begin{array}{c} 1 \\ + 1 \\ + 1 \\ \hline \end{array} & 1111100 \\ + & \begin{array}{c} -3 \\ -1 \\ \hline -10 \end{array} & \begin{array}{c} 1111000 \\ \hline 1110800 \\ 1 \\ \hline 1110101 \end{array} \\ \hline & \begin{array}{c} 2 \\ 3 \\ 1 \\ 1 \\ \hline \end{array} & 00000111 \\ -6 & \begin{array}{c} 2 \\ 1 \\ 1 \\ \hline \end{array} & 1111000 \end{array}$$

Cases of the overflow:

1st case: a and b are +

$$A + B \geq 2^{n-1}$$

in our case

$$n=8 \text{ and } 2^{n-1} = 128$$

$$\begin{array}{r} 65 \\ + 97 \\ \hline 162 \end{array} \quad \begin{array}{r} 01000001 \\ 01100001 \\ \hline 1010010 \end{array}$$

↓ sum is -

but we added two
+ numbers.

signs are different.

we have overflow in
this case.

2nd case

A and B are
The sum of absolute
values of A and B
is $\geq 2^{n-1}$

$$\begin{array}{r} -63 \\ + -85 \\ \hline 158 \end{array} \quad \begin{array}{r} 1 \\ + 1 \\ \hline 10 \end{array} \quad \begin{array}{r} 10000000 \\ 01000000 \\ \hline 1100000 \end{array}$$

carry ← ↓ → 1

bit

It's overflow too.
but idk why :-(

$$\begin{array}{r} +2 \\ -8 \\ \hline -f\bar{f} \end{array}$$

$$\begin{array}{r} +0 \\ +1 \\ \hline 1111000 \end{array}$$

$$\begin{array}{r} \leftarrow 8 \\ -3 \\ \hline 1 \end{array} \quad \begin{array}{r} 2 \\ 4 \\ -6 \\ \hline 0 \end{array} \quad \begin{array}{r} 2 \\ 2 \\ -2 \\ \hline -1 \end{array}$$

$$\begin{array}{r} 0 \\ 1 \\ \hline 00001001 \\ 4\text{evic} \end{array}$$

$$1110110$$

$$-20$$

$$\begin{array}{r}
 + -10 \\
 \hline
 -20 | 2 \\
 -20 | 10 | 2 \\
 \hline
 0 \\
 -16 | 5 | 2 \\
 \hline
 0 \quad 4 - 2 | 2 \\
 \hline
 1 \quad 0 \\
 \hline
 \end{array}$$

0 0000101
1 1111010

$$\begin{array}{r}
 10 | 2 \\
 -10 | 5 | 2 \\
 \hline
 0 \quad -4 | 2 | 2 \\
 \hline
 1 \quad \underline{2} \\
 \hline
 0 \\
 \hline
 \end{array}$$

0000 1010

11110101

1 111010

1 110101

1 1101111
33 401

f

1

1 0000 ?

?

?

?

- 120

+ 15

$$\begin{array}{r} 120 \\ - 100 \\ \hline 20 \end{array}$$
$$\begin{array}{r} 60 \\ - 60 \\ \hline 0 \end{array}$$
$$\begin{array}{r} 30 \\ - 30 \\ \hline 0 \end{array}$$
$$\begin{array}{r} 15 \\ - 15 \\ \hline 0 \end{array}$$
$$\begin{array}{r} 72 \\ - 72 \\ \hline 0 \end{array}$$
$$\begin{array}{r} 2 \\ - 2 \\ \hline 0 \end{array}$$
$$\begin{array}{r} 372 \\ - 372 \\ \hline 0 \end{array}$$
$$\begin{array}{r} 1 \\ - 1 \\ \hline 0 \end{array}$$
$$\begin{array}{r} 1 \\ - 1 \\ \hline 0 \end{array}$$

0 000 1111
111 0000

$$\begin{array}{r} 15 \\ - 14 \\ \hline 1 \end{array}$$
$$\begin{array}{r} 7 \\ - 7 \\ \hline 0 \end{array}$$
$$\begin{array}{r} 2 \\ - 2 \\ \hline 0 \end{array}$$

$$\begin{array}{r} \overline{1} \\ - 6 \ 3 \\ \hline 1 \end{array}$$

0 000 £ £ £ £

£ £ £ £ 0000

1 1110000

1 1110000

1 1100000

1 100 + 15 = 1357128
overflow

Two's complement

two's complement
addition.

1st case :-

1st num is +

2nd num is -
abs value of 2nd

number is > than

1st number .

$$\begin{array}{r} + 3 \\ - 10 \\ \hline - 7 \end{array}$$

+ 0 0000011
+ 1 1110110

$$\begin{array}{r}
 \text{W} \boxed{1}^2 \\
 - \frac{10 \boxed{5}}{0} \boxed{-4} \boxed{\underline{2}}^2 \\
 \hline
 1
 \end{array}
 \quad \begin{array}{l}
 \text{one's comp} \\
 \text{TOP} \\
 \text{using 1's compl} \\
 = \text{two's comp.}
 \end{array}$$

0000 + 010

$$\begin{array}{r}
 1111 0101 \\
 + \overline{1110 110} \\
 \hline
 \end{array}$$

2nd case:

1st is -

2nd is -

$$\begin{array}{r} 10 \\ f - 3 \\ \hline f \end{array} \quad \begin{array}{r} 0 \ 0001010 \\ + 1 \ 111101 \\ \hline 0 \ 0000111 \end{array}$$

l¹ carry bit is discarded

3rd case

A and B are -

$$\begin{array}{r} -3 \\ f - f \\ \hline -10 \end{array} \quad \begin{array}{r} 1 \ 111101 \\ + 1 \ 111001 \\ \hline 1 \ 1110110 \end{array}$$

sign bit.

$$\begin{array}{r} 00000111 \\ 11111000 \\ + \qquad \qquad \qquad 1 \\ \hline 11111001 \end{array}$$

Exercise

two's comp.

f - 8

$$\begin{array}{r}
 9 \overline{)12} \\
 -8 \\
 \hline
 1 \quad -4 \\
 \hline
 0 \quad 1
 \end{array}$$

0. 000 1 00 1

1 1 1 0 1 1 0

+

1 1 1 0 1 1 1

+ 0 0 0 0 0 1 0

1 1 1 1 0 0 1

-5
-7

$$\begin{array}{r} 0 & 0000101 \\ 1 & 111010 \\ + & \quad \quad \quad 1 \\ \hline & 11111011 \\ & 1111001 \\ \hline & 1110100 \end{array}$$

- 126

+ -1

$$\begin{array}{r} 126 \\ \underline{-} 126 \\ 0 \end{array}$$
$$\begin{array}{r} 63 \\ \underline{-} 62 \\ 1 \end{array}$$
$$\begin{array}{r} 30 \\ \underline{-} 30 \\ 0 \end{array}$$
$$\begin{array}{r} 14 \\ \underline{-} 14 \\ 0 \end{array}$$
$$\begin{array}{r} 15 \\ \underline{-} 14 \\ 1 \end{array}$$
$$\begin{array}{r} 1 \\ \underline{-} 1 \\ 0 \end{array}$$
$$\begin{array}{r} 3 \\ \underline{-} 2 \\ 1 \end{array}$$
$$\begin{array}{r} 1 \\ \underline{-} 1 \\ 0 \end{array}$$

0 0 1 1 1 1 1

$$\begin{array}{r} + \\ \begin{array}{r} 1 & 1000000 \\ 1 & 10000001 \\ \hline \end{array} \end{array}$$

$$\begin{array}{r} + \\ \begin{array}{r} 0 & 0000001 \\ 1 & 11110 \\ 1 \\ \hline \begin{array}{r} 1 & 1111111 \\ 1 & 0000001 \\ \hline 1 & 10000000 \end{array} \end{array} \end{array}$$

$$= 12 \cancel{5}$$

$$- 1 \quad - 1$$

$$\begin{array}{r}
 128 | 2 \\
 - 126 | 2 \\
 \hline
 8 \quad - 64 | 2 \\
 \hline
 0 \quad 32 | 2 \\
 \hline
 0 \quad 16 | 2 \\
 \hline
 0 \quad 8 | 2 \\
 \hline
 0 \quad 4 | 2 \\
 \hline
 0 \quad 2 | 2 \\
 \hline
 0 \quad 1
 \end{array}
 \qquad
 \begin{array}{r}
 4 \quad 20
 \end{array}$$

1 000 000 1
 0 111 111 0

f I
0 1 1 1 1 1 1
f 1 1 1 1 1 1

0

