

InstaFlow: One-Step Stable Diffusion from Straight Probability Flows

Xingchao Liu

UT Austin

AI Generated Contents



Images



Text-to-Video generation: "a horse galloping on a street"



Text-to-Video generation: "a panda is playing guitar on times square"

Videos

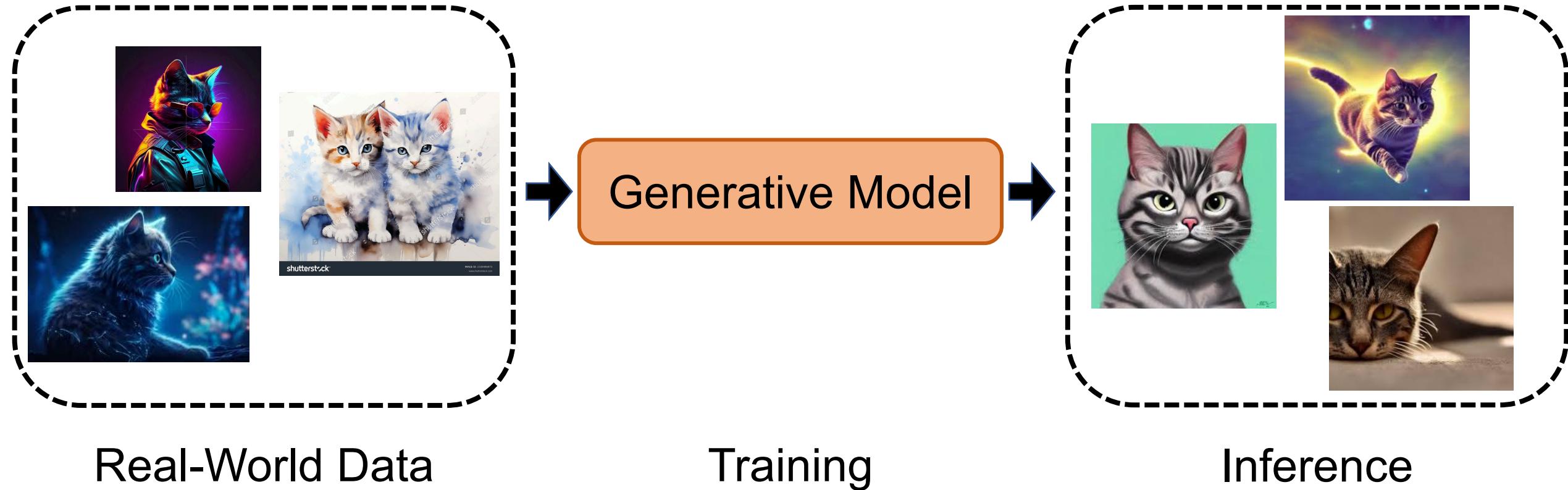


Texts & Codes



Policies

AIGC Pipeline

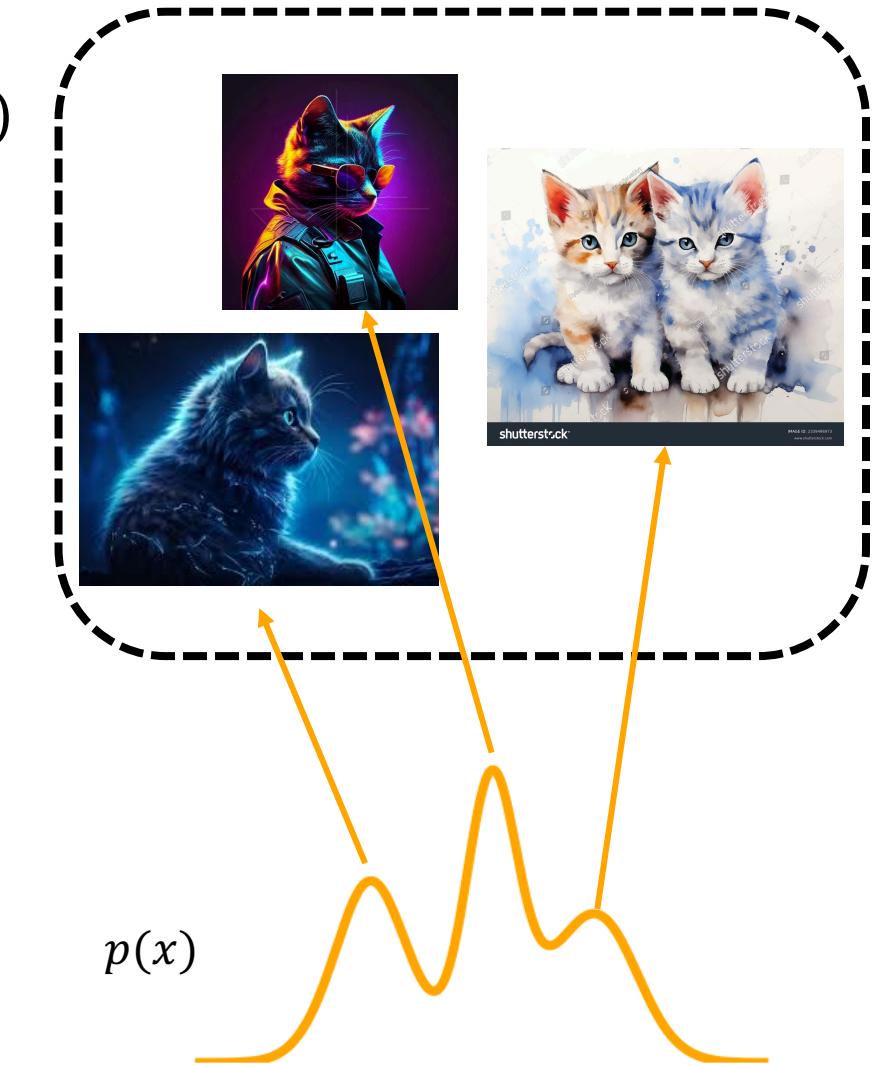


Generative Models

Given: observed data points $\{x_i\}_{i=1}^n$

Unknown: the groundtruth data distribution $p(x)$

Training Data



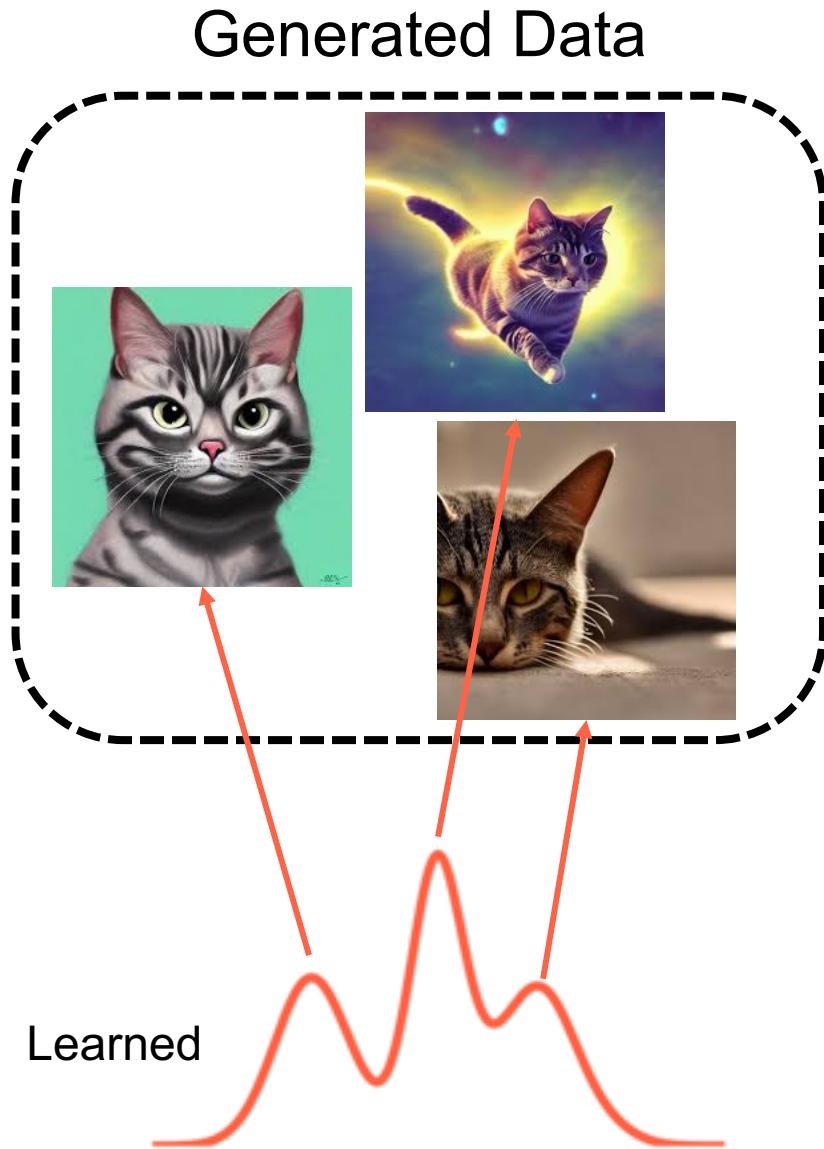
Generative Models

Given: observed data points $\{x_i\}_{i=1}^n$

Unknown: the groundtruth data distribution $p(x)$

Training: to learn a **model** to capture $p(x)$

Sampling: generate from the learned distribution



Generative Models

Given: observed data points $\{x_i\}_{i=1}^n$

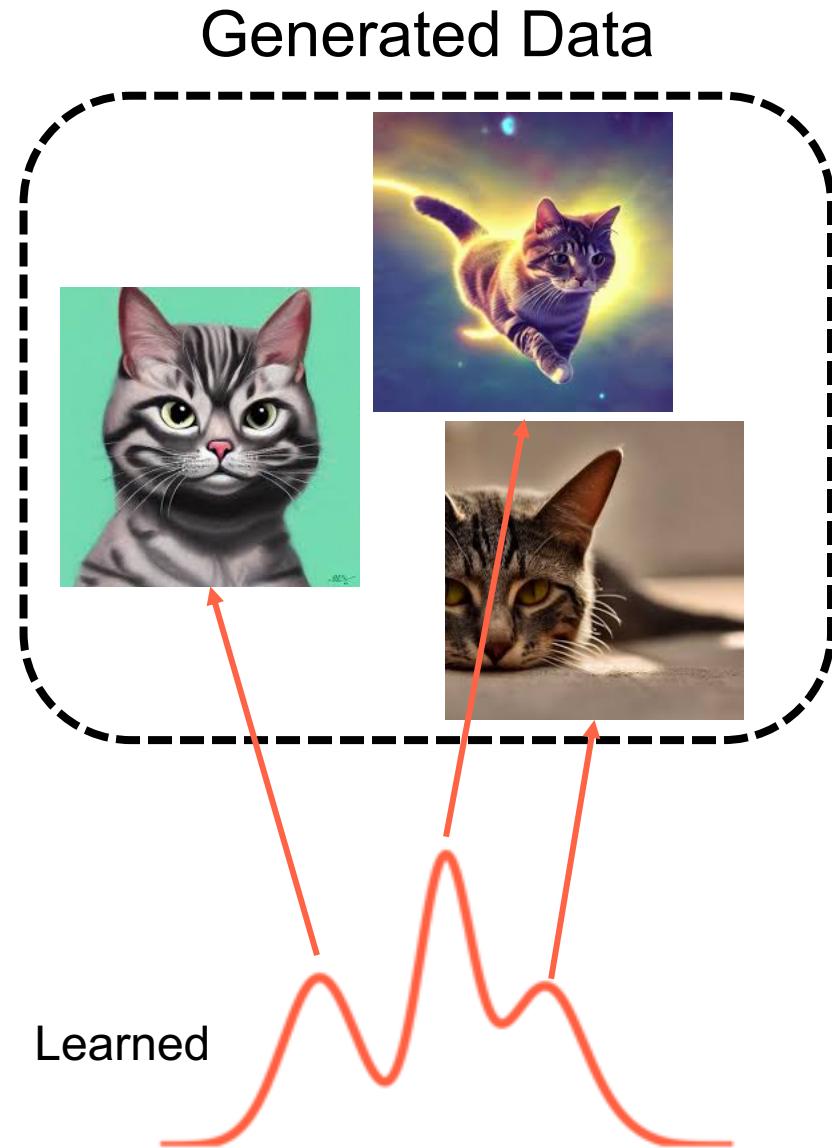
Unknown: the groundtruth data distribution $p(x)$

Training: to learn a **model** to capture $p(x)$

Sampling: generate from the learned distribution



What do we expect for good generative model frameworks?



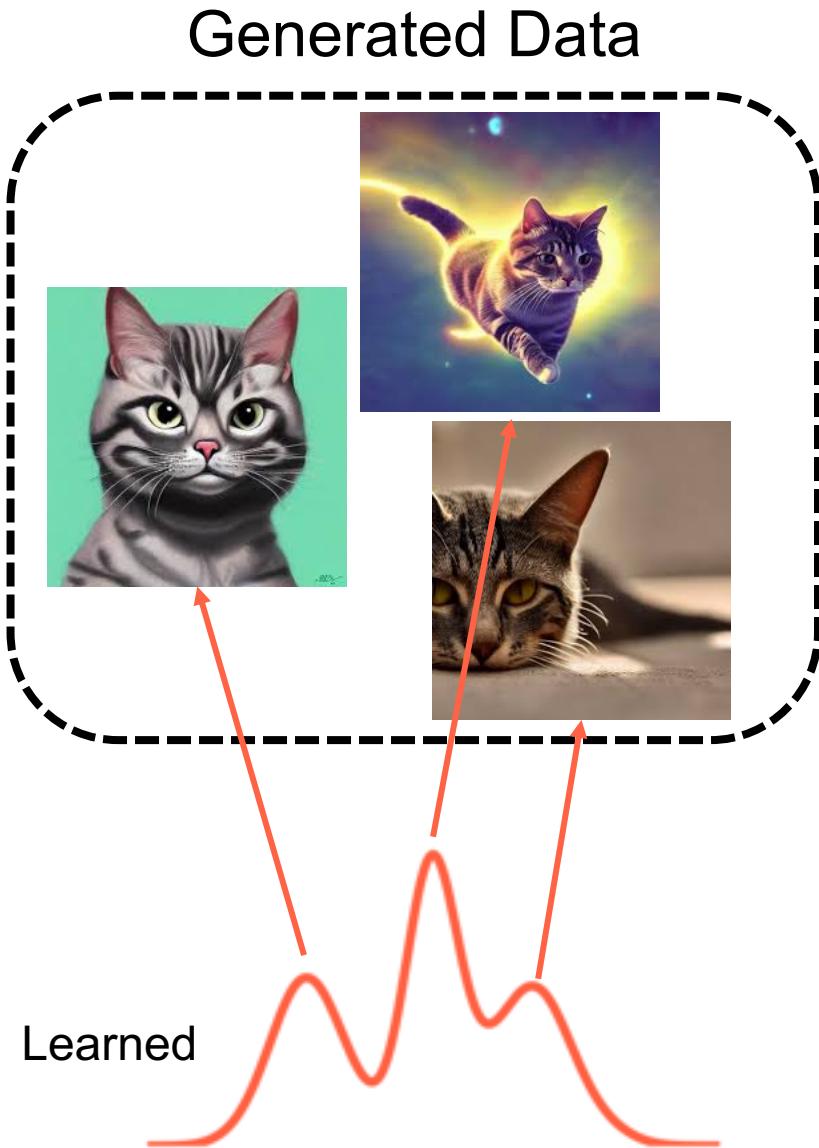
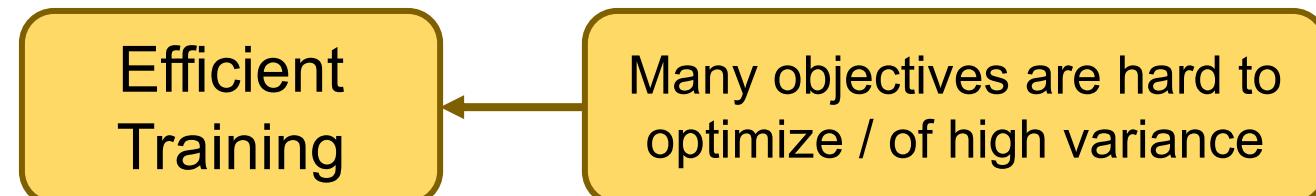
Generative Models

Given: observed data points $\{x_i\}_{i=1}^n$

Unknown: the groundtruth data distribution $p(x)$

Training: to learn a **model** to capture $p(x)$

Sampling: generate from the learned distribution



Generative Models

Given: observed data points $\{x_i\}_{i=1}^n$

Unknown: the groundtruth data distribution $p(x)$

Training: to learn a **model** to capture $p(x)$

Sampling: generate from the learned distribution

Efficient Sampling

Sampling from general distributions is slow

[Liu et al., NeurIPS 2021 **spotlight**
[Zhang, Liu et al., ICML 2022]

Generated Data



Learned

Frameworks of Generative Models

Efficient Training

Efficient Sampling

Energy-Based Model [Hinton 1999, 2002]	✗	✗
Autoregressive Model [Frey 1998, Bengio & Bengio 2000]	✓	✗
GAN [Goodfellow et al. 2014]	✗	✓
VAE [Kingma & Welling 2014]	✗	✓
Normalizing Flow [Rezende & Mohamed 2015]	✗	✓
Diffusion Model [Sohl-Dickstein et al. 2015, Ho et al. 2020, Song et al. 2021]	✓	✗

Frameworks of Generative Models

Efficient Training

Efficient Sampling

Energy-Based Model [Hinton 1999, 2002]	✗	✗
Autoregressive Model [Frey 1998, Bengio & Bengio 2000]	✓	✗
GAN [Goodfellow et al. 2014]	✗	✓
VAE [Kingma & Welling 2014]	✗	✓
Normalizing Flow [Rezende & Mohamed 2015]	✗	✓
Diffusion Model [Sohl-Dickstein et al. 2015, Ho et al. 2020, Song et al. 2021]	✓	✗

Frameworks of Generative Models

Efficient Training

Efficient Sampling

Model	Efficient Training	Efficient Sampling
Energy-Based Model [Hinton 1999, 2002]	✗	✗
Autoregressive Model [Frey 1998, Bengio & Bengio 2000]	✓	✗
GAN [Goodfellow et al. 2014]	✗	✓
VAE [Kingma & Welling 2014]	✗	✓
Normalizing Flow [Rezende & Mohamed 2015]	✗	✓
Diffusion Model [Sohl-Dickstein et al. 2015, Ho et al. 2020, Song et al. 2021]	✓	✗

Frameworks of Generative Models

Efficient Training

Efficient Sampling

Energy-Based Model [Hinton 1999, 2002]	✗	✗
Autoregressive Model [Frey 1998, Bengio & Bengio 2000]	✓	✗
GAN [Goodfellow et al. 2014]	✗	✓
VAE [Kingma & Welling 2014]	✗	✓
Normalizing Flow [Rezende & Mohamed 2015]	✗	✓
Diffusion Model [Sohl-Dickstein et al. 2015, Ho et al. 2020, Song et al. 2021]	✓	✗

Frameworks of Generative Models

Efficient Training

Efficient Sampling

Energy-Based Model [Hinton 1999, 2002]	✗	✗
Autoregressive Model [Frey 1998, Bengio & Bengio 2000]	✓	✗
GAN [Goodfellow et al. 2014]	✗	✓
VAE [Kingma & Welling 2014]	✗	✓
Normalizing Flow [Rezende & Mohamed 2015]	✗	✓
Diffusion Model [Sohl-Dickstein et al. 2015, Ho et al. 2020, Song et al. 2021]	✓	✗

Frameworks of Generative Models

Efficient Training

Efficient Sampling

Model	Efficient Training	Efficient Sampling
Energy-Based Model [Hinton 1999, 2002]	✗	✗
Autoregressive Model [Frey 1998, Bengio & Bengio 2000]	✓	✗
GAN [Goodfellow et al. 2014]	✗	✓
VAE [Kingma & Welling 2014]	✗	✓
Normalizing Flow [Rezende & Mohamed 2015]	✗	✓
Diffusion Model [Sohl-Dickstein et al. 2015, Ho et al. 2020, Song et al. 2021]	✓	✗

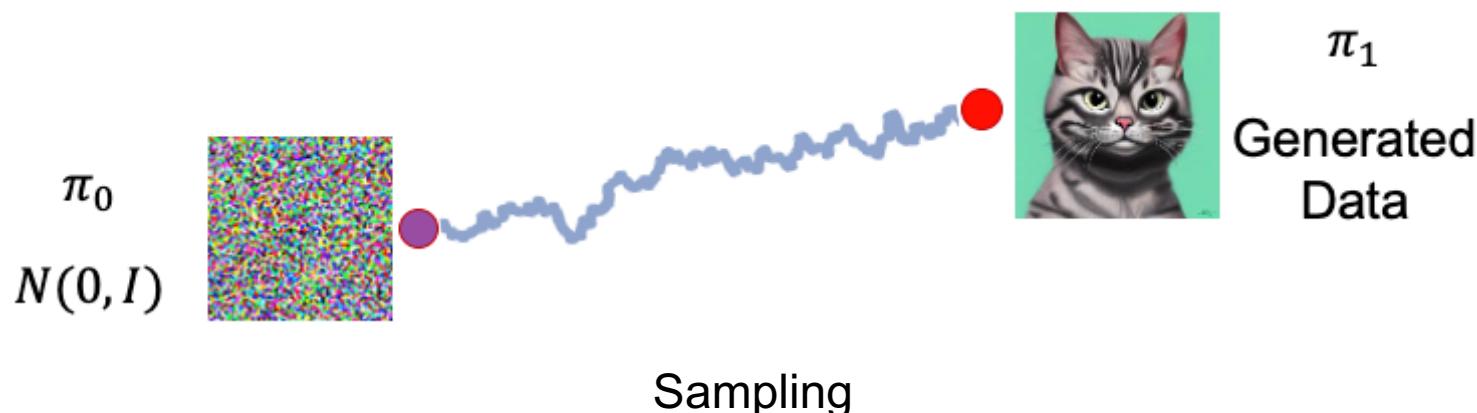
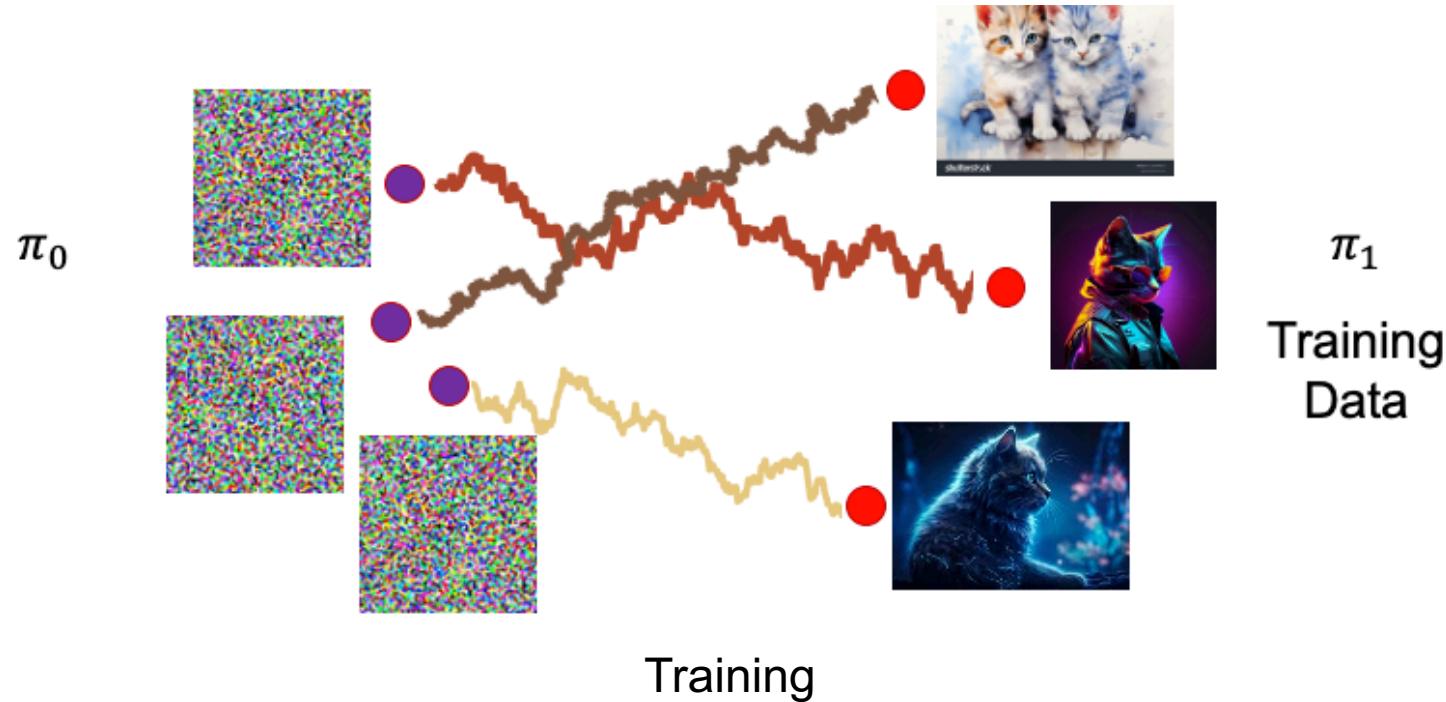
Frameworks of Generative Models

Efficient Training

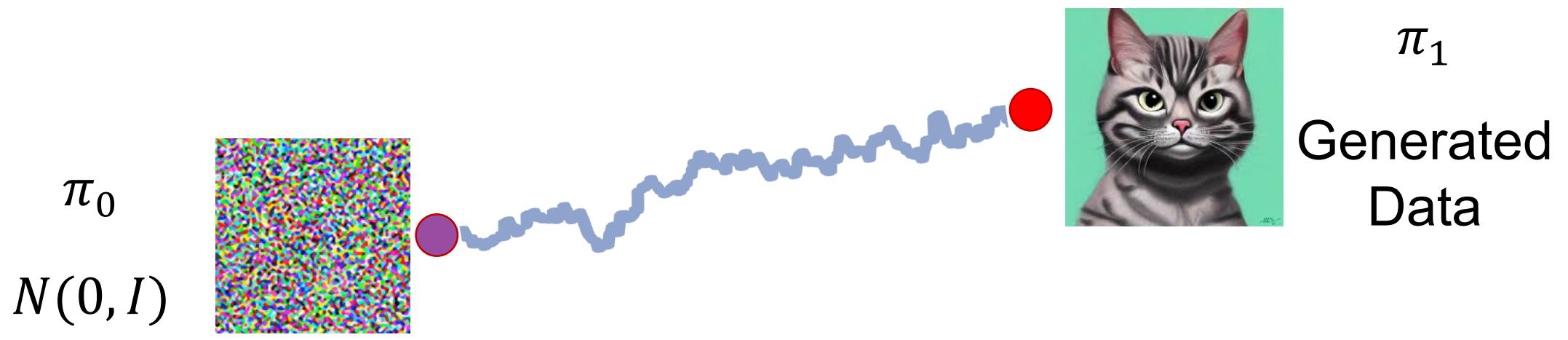
Efficient Sampling

Model [Reference]	Efficient Training	Efficient Sampling
Energy-Based Model [Hinton 1999, 2002]	✗	✗
Autoregressive Model [Frey 1998, Bengio & Bengio 2000]	✓	✗
GAN [Goodfellow et al. 2014]	Can we get both?	
VAE [Kingma & Welling 2014]	✗	✓
Normalizing Flow [Rezende & Mohamed 2015]	✗	✓
Diffusion Model [Sohl-Dickstein et al. 2015, Ho et al. 2020, Song et al. 2021]	✓	✗

Diffusion Models



Why are they slow?



Problem: Noise in the diffusion process [Liu et al., ICLR2023 **spotlight**]



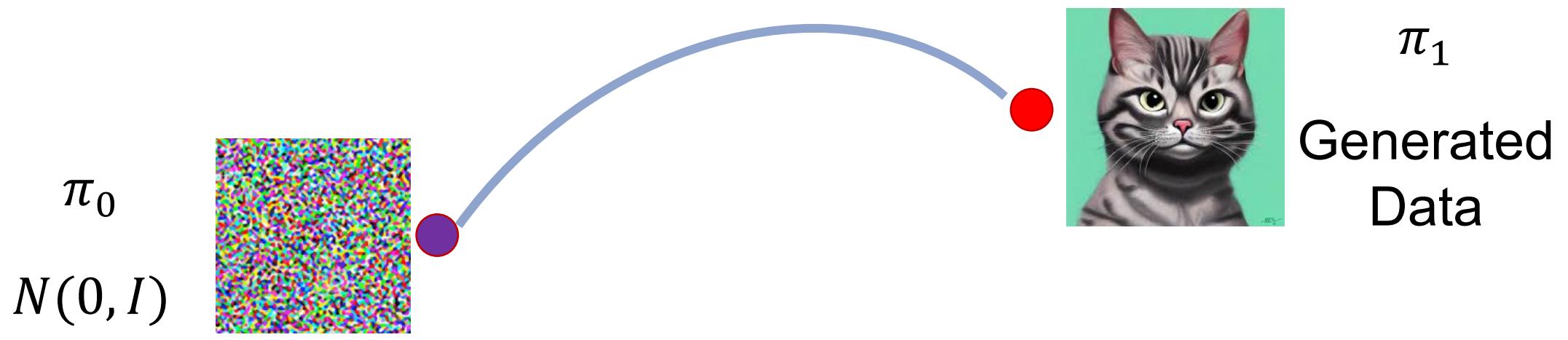
Solution: Marginal-preserving ordinary differential equation (ODE)

DDIM [Song et al. 2021], Heun [Karras et al. 2022], DPM-Solver [Lu et al. 2022], etc.

$$dX = [f(X, t) - g^2(t) \nabla_X \log p_t(X)] dt + \boxed{g(t) dW_t} \text{ Noise}$$

Reverse Stochastic Differential Equation (SDE)

Why are they slow?



Problem: Noise in the diffusion process [Liu et al., ICLR2023 **spotlight**]



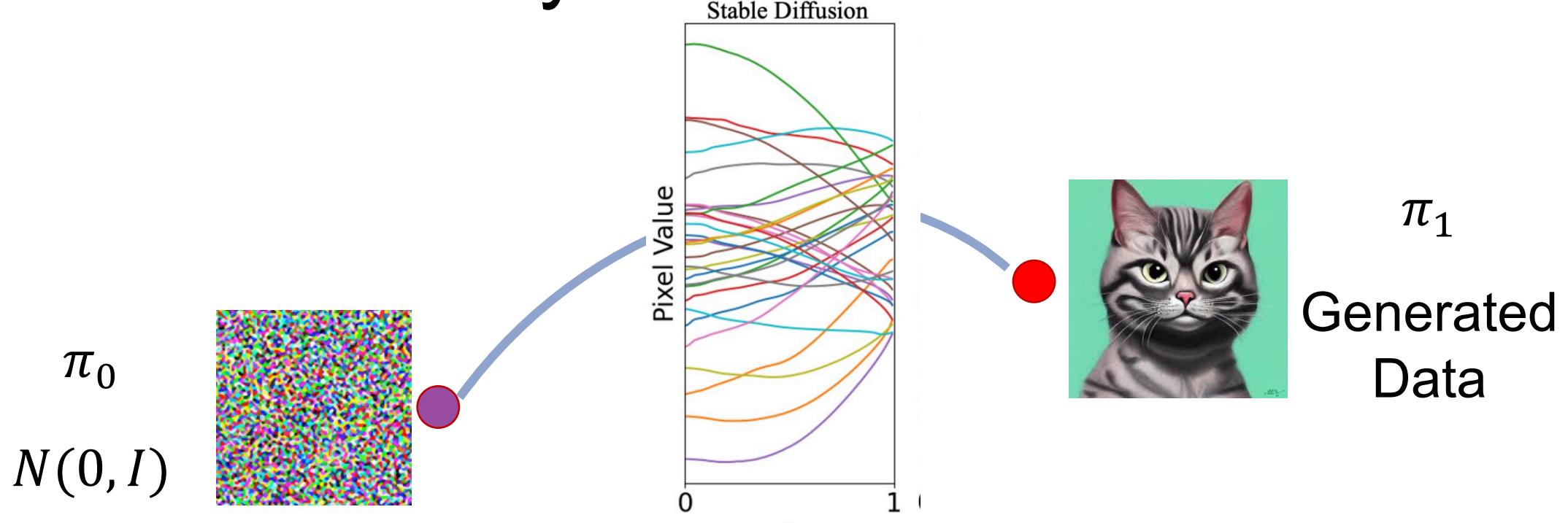
Solution: Marginal-preserving ordinary differential equation (ODE)

DDIM [Song et al. 2021], Heun [Karras et al. 2022], DPM-Solver [Lu et al. 2022], etc.

$$dX = \left[f(X, t) - \frac{1}{2} g^2(t) \nabla_X \log p_t(X) \right] dt$$

Probability Flow Ordinary Differential Equation

Why are they slow?



New Problem: Curved ODE trajectory

Velocity $v(X, t)$

$$dX = \boxed{[f(X, t) - \frac{1}{2}g^2(t)\nabla_X \log p_t(X)]dt}$$

Probability Flow Ordinary Differential Equation

Discretization of ODE

- In computer, we solve ODEs by Euler discretization

$$X_{t+\epsilon} = X_t + \epsilon v(X_t, t)$$

ϵ : step size

Large ϵ : Fast, inaccurate ; Small ϵ : Accurate, slow



$$dX = v(X, t)dt$$

Probability Flow Ordinary Differential Equation

Research Question



How do we learn straight generative ODEs?

Diffusion models connect two distribution with diffusion processes



Idea: Connect with straight lines!

Rectified Flow

- Learn from straight-line teachers
- Purely ODE-based; no more conversion from SDE to ODE
- A unified framework for both generative modeling and transfer learning
- Bridge the gap between one-step and continuous-time models **Reflow**

Rectified Flow: Problem of Interest

Given: observed data points from two distributions

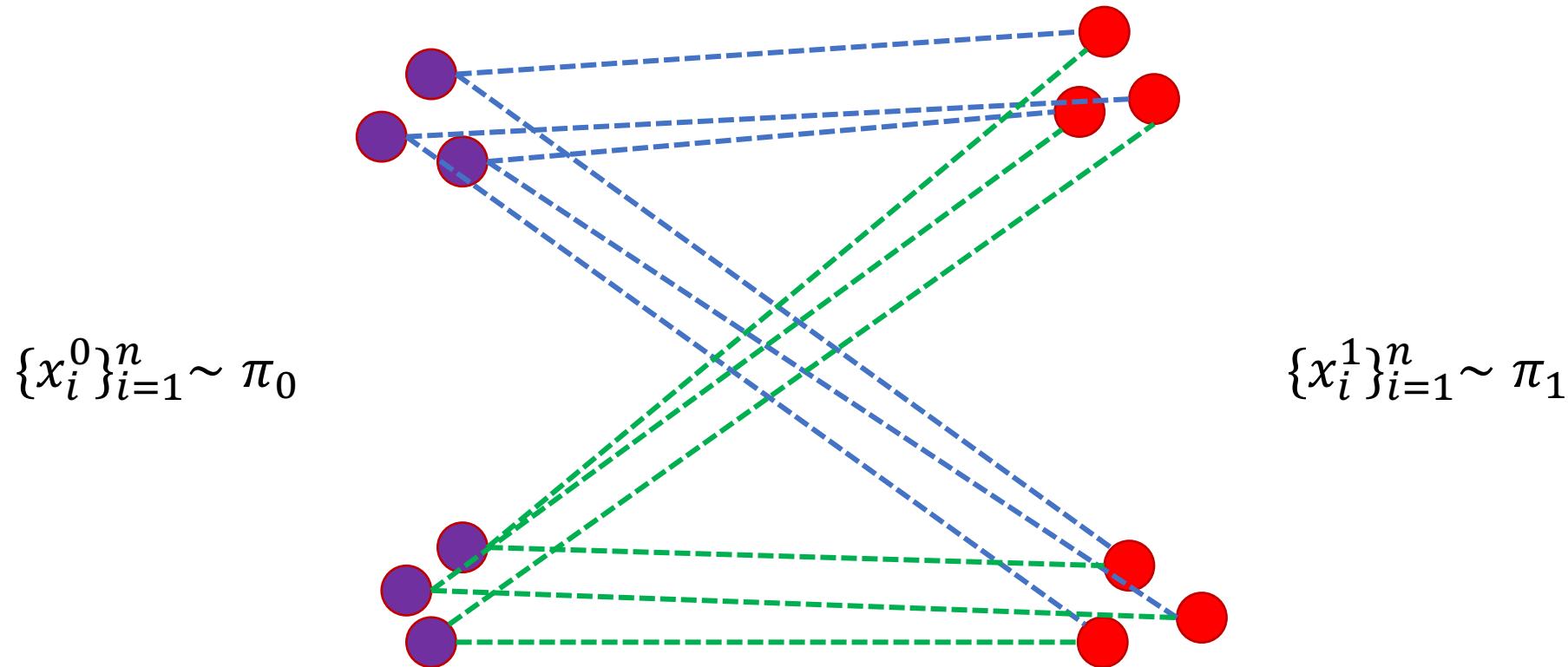
$$\{x_i^0\}_{i=1}^n \sim \pi_0, \quad \{x_i^1\}_{i=1}^n \sim \pi_1$$

Goal: find a transport map T such that,

$$Z_1 := T(Z_0) \sim \pi_1 \text{ when } Z_0 \sim \pi_0$$



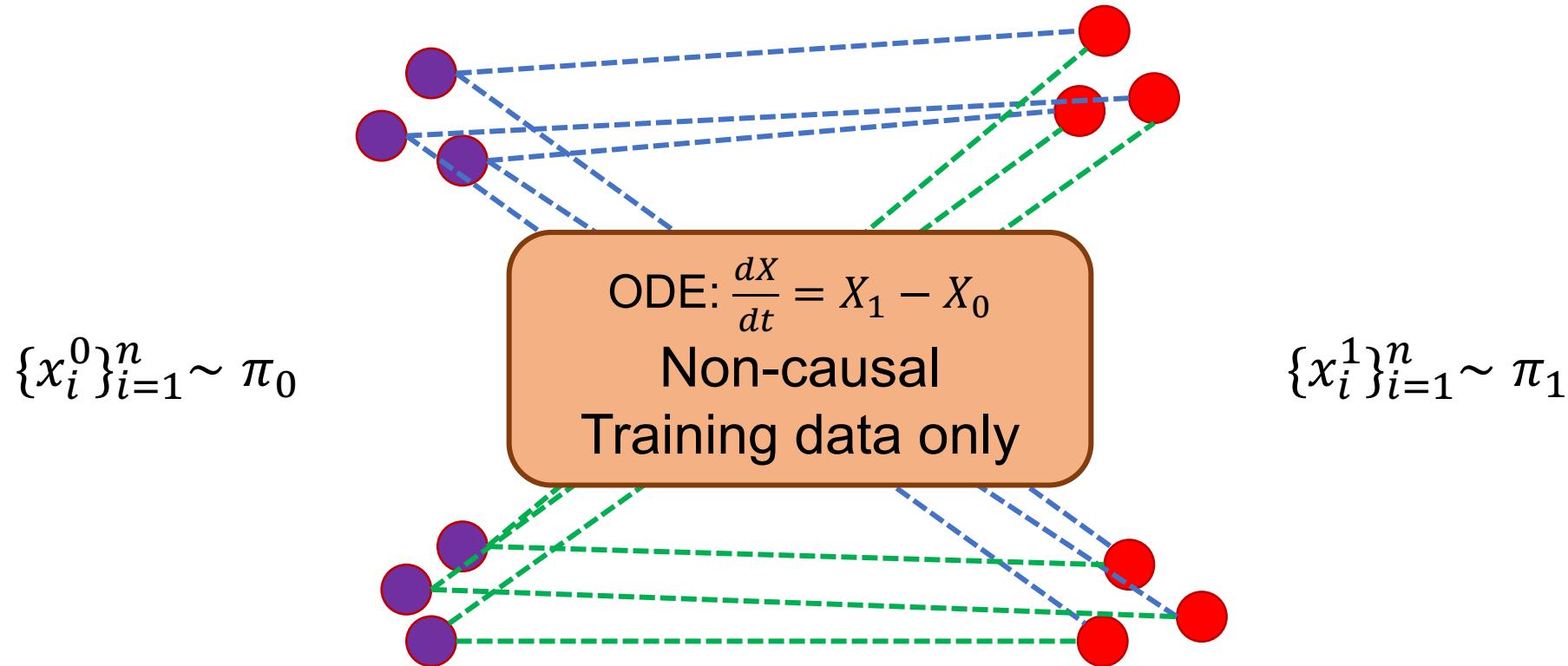
Step 1: Construct Straight-Line Teachers



Linear Interpolation: $X_t = tX_1 + (1 - t)X_0$

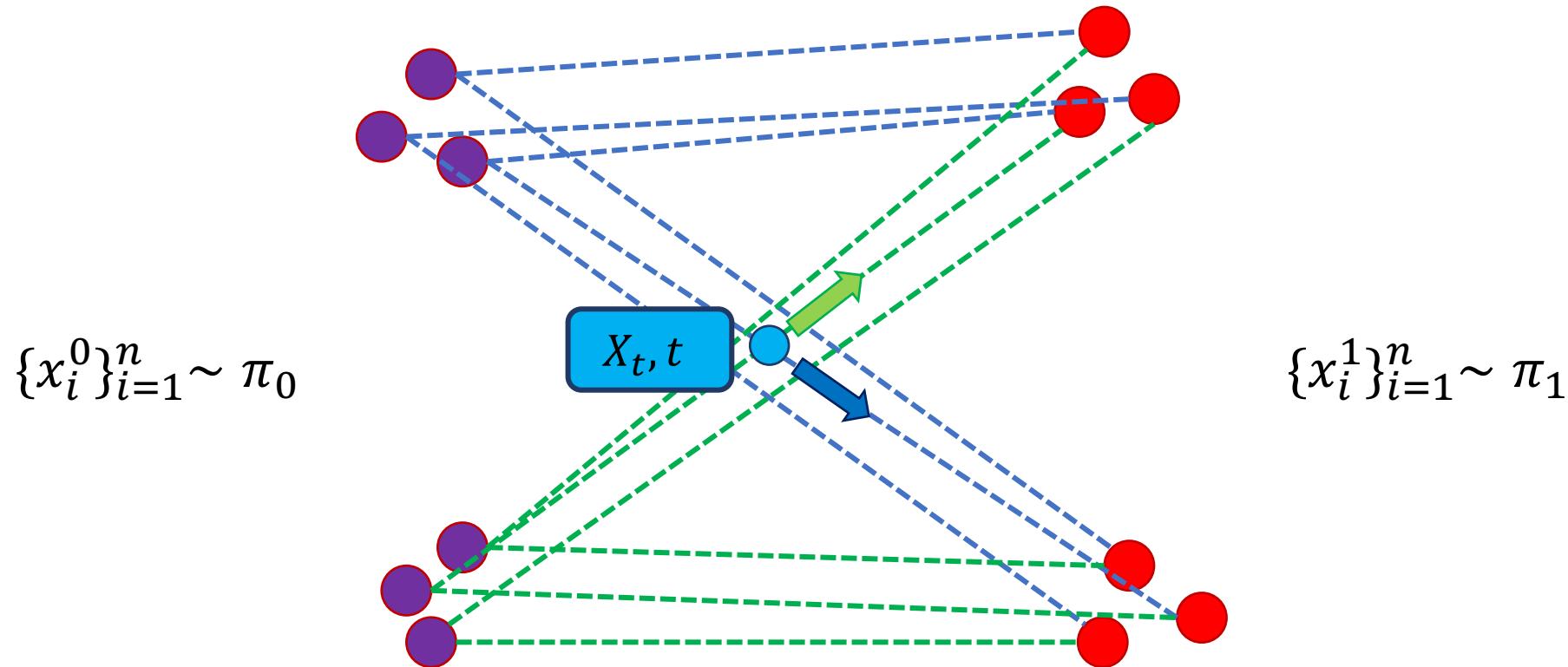
$$\text{ODE: } \frac{dX}{dt} = X_1 - X_0$$

Step 1: Construct Straight-Line Teachers



Linear Interpolation: $X_t = tX_1 + (1 - t)X_0$
ODE: $\frac{dx}{dt} = X_1 - X_0$

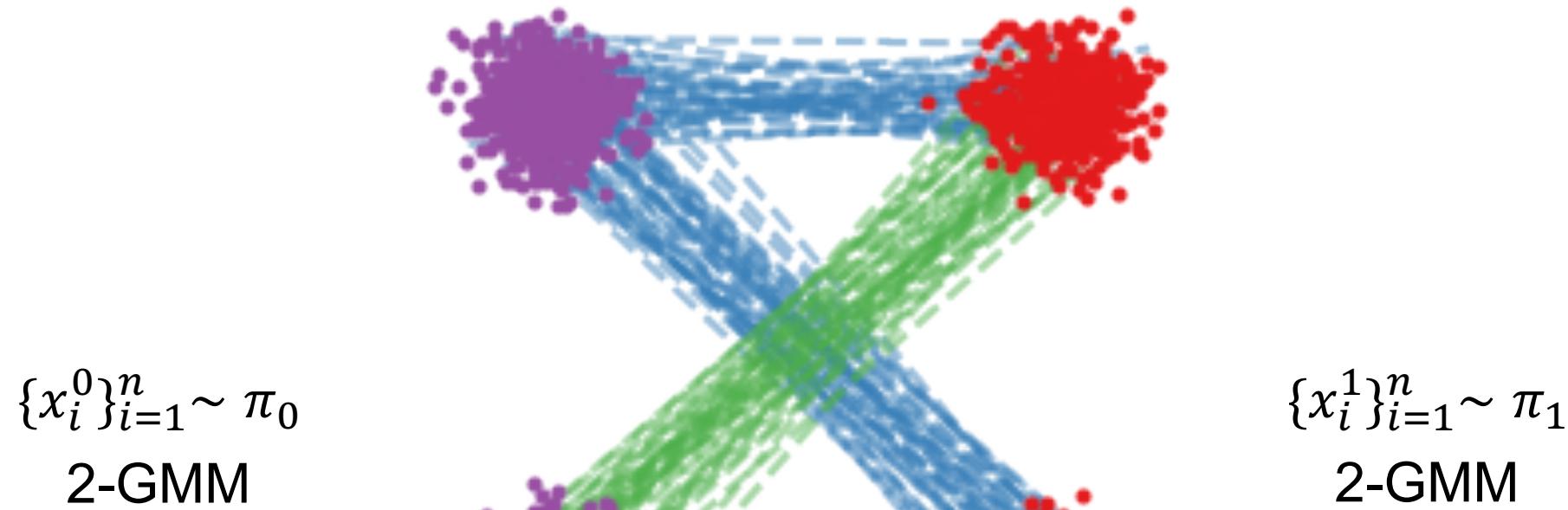
Step 1: Construct Straight-Line Teachers



Linear Interpolation: $X_t = tX_1 + (1 - t)X_0$

$$\text{ODE: } \frac{dX}{dt} = X_1 - X_0$$

Step 1: Construct Straight-Line Teachers



Linear Interpolation: $X_t = tX_1 + (1 - t)X_0$

$$\text{ODE: } \frac{dX}{dt} = X_1 - X_0$$

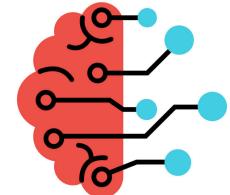
Step 2: Project to Causal Students

Teacher ODE (Non-causal)

$$\frac{dX}{dt} = X_1 - X_0$$

Student ODE (Causal)

$$\frac{dX}{dt} = v_\theta(X, t)$$



NEURAL NETWORK

Projection Loss

$$\min_{\theta} \int_0^1 \mathbb{E}_{X_0 \sim \pi_0, X_1 \sim \pi_1} \left[\left\| \boxed{(X_1 - X_0)} - \boxed{v_\theta(X_t, t)} \right\|^2 \right] dt$$

Teacher
velocity Student
velocity

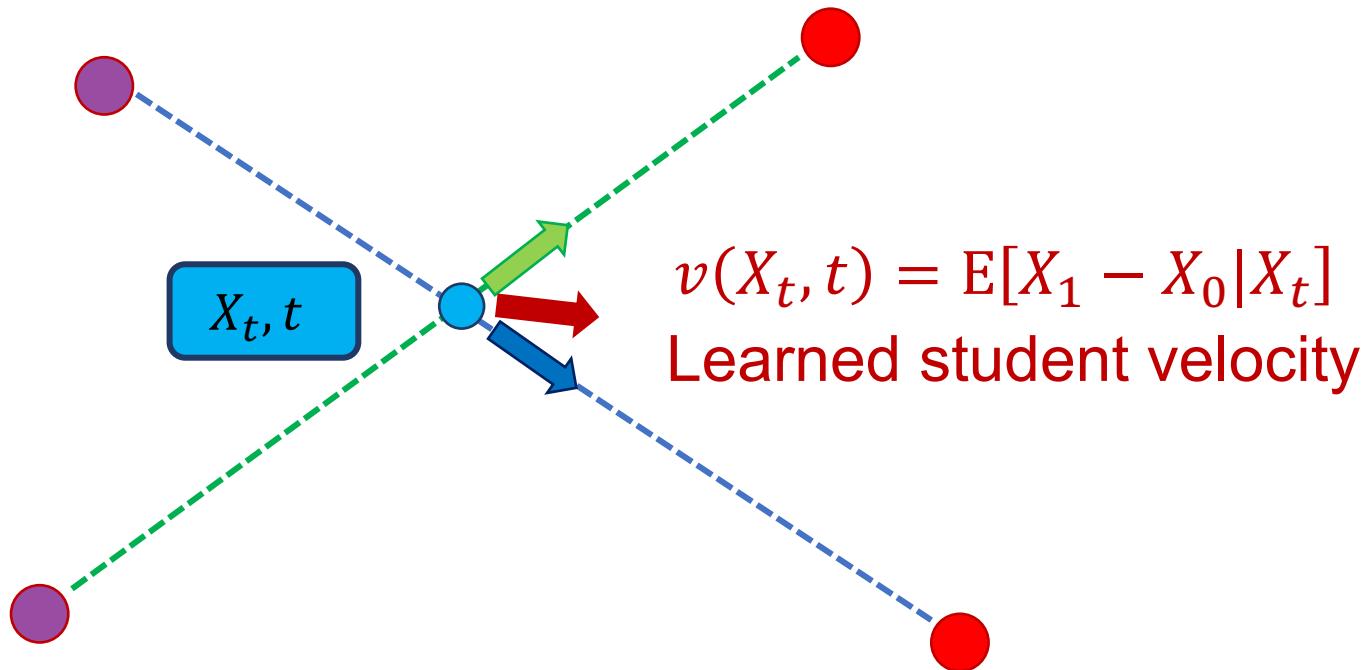
Step 2: Project to Causal Students

Projection Loss

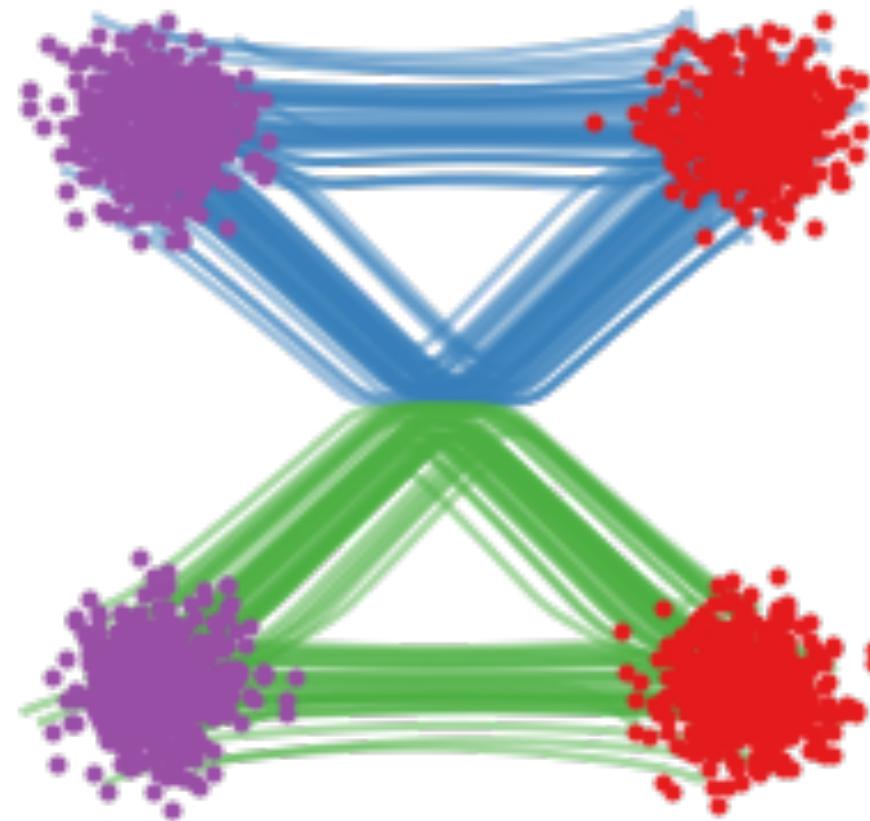
$$\min_{\theta} \int_0^1 \mathbb{E}_{X_0 \sim \pi_0, X_1 \sim \pi_1} \left[\left\| (X_1 - X_0) - v_{\theta}(X_t, t) \right\|^2 \right] dt$$

Teacher
velocity

Student
velocity



Step 3: Generation with ODE solver



Randomly sample $X_0 \sim \pi_0$

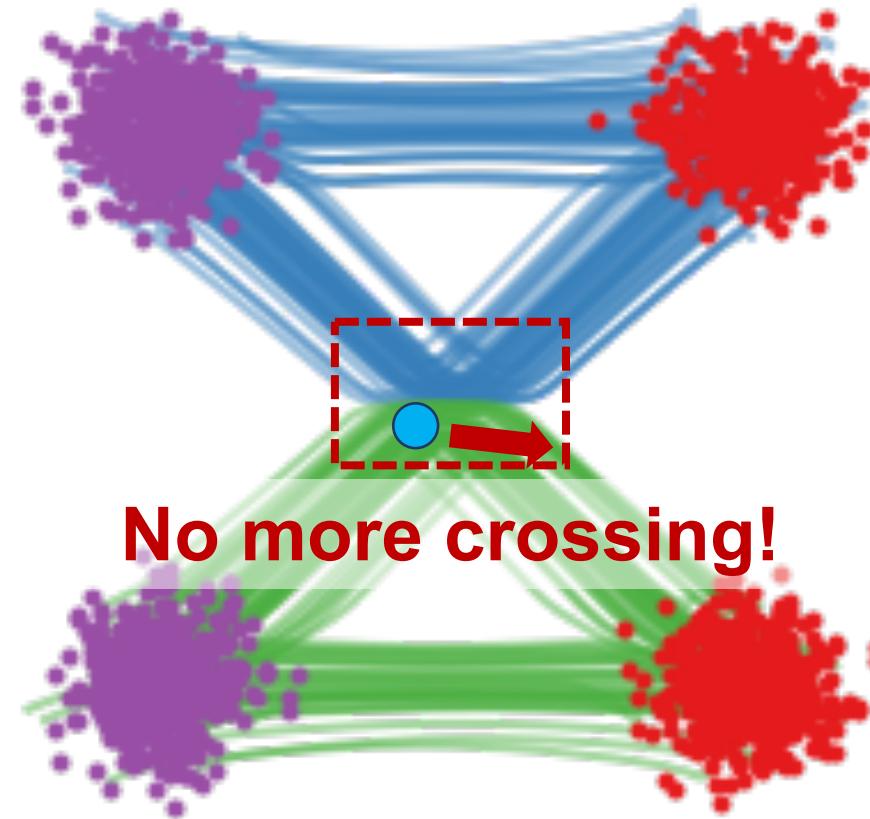
Generated distribution $X_1 \sim \pi_1$

Guaranteed by math

Simulate with ODE solver, e.g., Euler

$$\text{ODE: } \frac{dX}{dt} = v_\theta(X, t)$$

Step 3: Generation with ODE solver



Randomly sample $X_0 \sim \pi_0$

Generated distribution $X_1 \sim \pi_1$

Guaranteed by math

Simulate with ODE solver, e.g., Euler

$$\text{ODE: } \frac{dX}{dt} = v_\theta(X, t)$$

Algorithm: Rectified Flow

- **Given:** $\{x_i^0\}_{i=1}^n \sim \pi_0$, $\{x_i^1\}_{i=1}^n \sim \pi_1$
- **Training Iteration (Batch size = 1):**
 - Step 1: Randomly sample $X_0 \in \{x_i^0\}_{i=1}^n$ and $X_1 \in \{x_i^1\}_{i=1}^n$
 - Step 2: Randomly sample $t \in [0,1]$
 - Step 3: Compute gradient with loss

$$L(\theta) := \left\| X_1 - X_0 - v_\theta(X_t, t) \right\|^2,$$

where $X_t = tX_1 + (1-t)X_0$

Empirical Results

CIFAR10

Method	NFE (\downarrow)	IS (\uparrow)	FID (\downarrow)
VP SDE	2000	9.58	2.55
subVP SDE	2000	9.56	2.61
VP ODE	140	9.37	3.93
subVP ODE	146	9.46	3.16
Rectified Flow	127	9.60	2.58

Fast sampling + high-quality



(A) LSUN Church



(B) CelebA HQ



(C) LSUN Bedroom

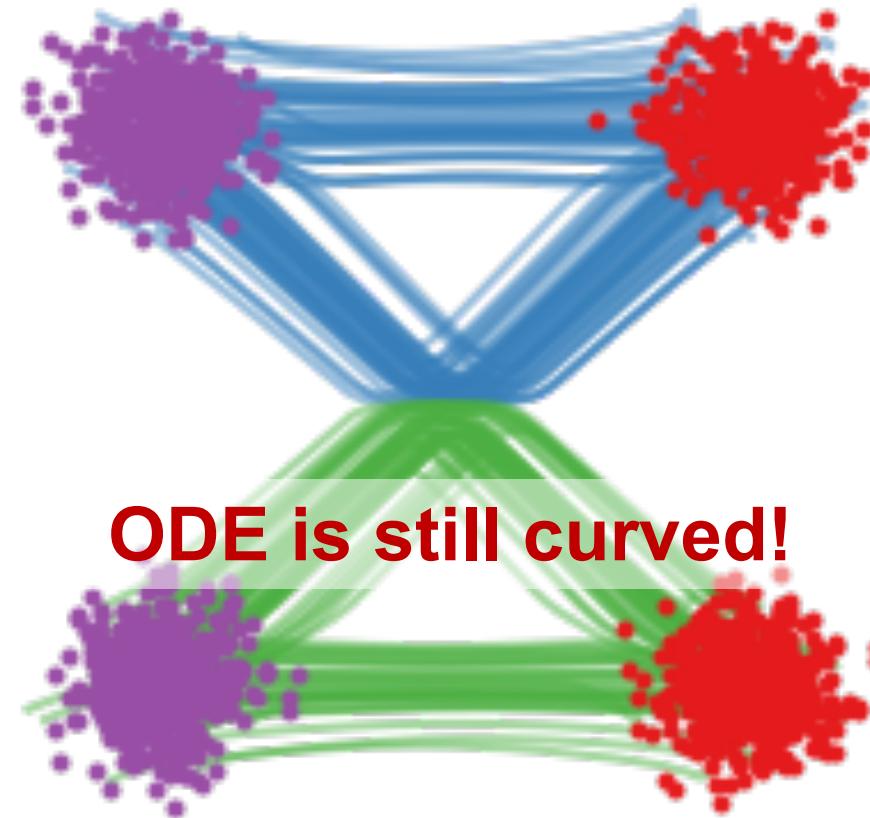


(D) AFHQ Cat

256 Resolution

Not There Yet

Randomly sample $X_0 \sim \pi_0$



Generated distribution $X_1 \sim \pi_1$

Guaranteed by theory

Simulate with ODE solver, e.g., Euler

$$\text{ODE: } \frac{dX}{dt} = v_\theta(X, t)$$

Prior Attempts

Learning straight probability flow ODEs is investigated in the Neural ODE works

When continuous normalizing flows were hot

1. Jacobian and Kinetic Regularization [Finlay et al. 2020]

$\sum_{i=1}^N \log p_\theta(x_i)$	$\int_0^1 \ \nu_\theta(X_t, t)\ ^2 dt$	$\int_0^1 \left\ \nabla_{X_t} \nu_\theta(X_t, t) \right\ _F^2 dt$	$-\int_0^1 \operatorname{div}(\nu_\theta)(X_t, t) dt$
Likelihood of the training data	Kinetic energy	Integral of Frobenius norm of Jacobian	Log-determinant of Jacobian

2. Optimal Transport-Flow

[Onken et al. 2021]

$\sum_{i=1}^N \log p_\theta(x_i)$	$\int_0^1 \ \nu_\theta(X_t, t)\ ^2 dt$	$\int_0^1 \left\ \partial_t \Phi(X_t, t) - \frac{1}{2} \left\ \nabla_{X_t} \Phi(X_t, t) \right\ \right\ ^2 dt$ <p>s.t. $\nu(X_t, t) = -\nabla_{X_t} \Phi(X_t, t)$</p>
Likelihood of the training data	Transport Cost	Hamilton–Jacobi–Bellman Regularization



Hard to Optimize

Limited Capacity

Fail to Scale up

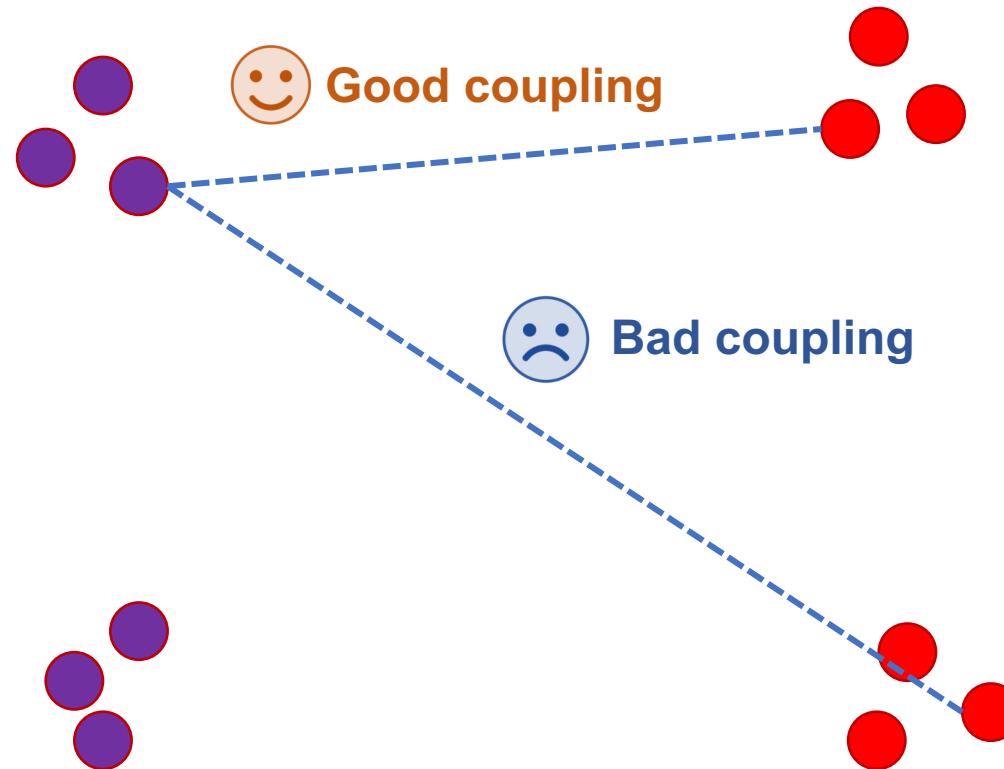
Our Solution: Reflow!



Idea: Re-connect with straight lines!

Our Solution: Reflow!

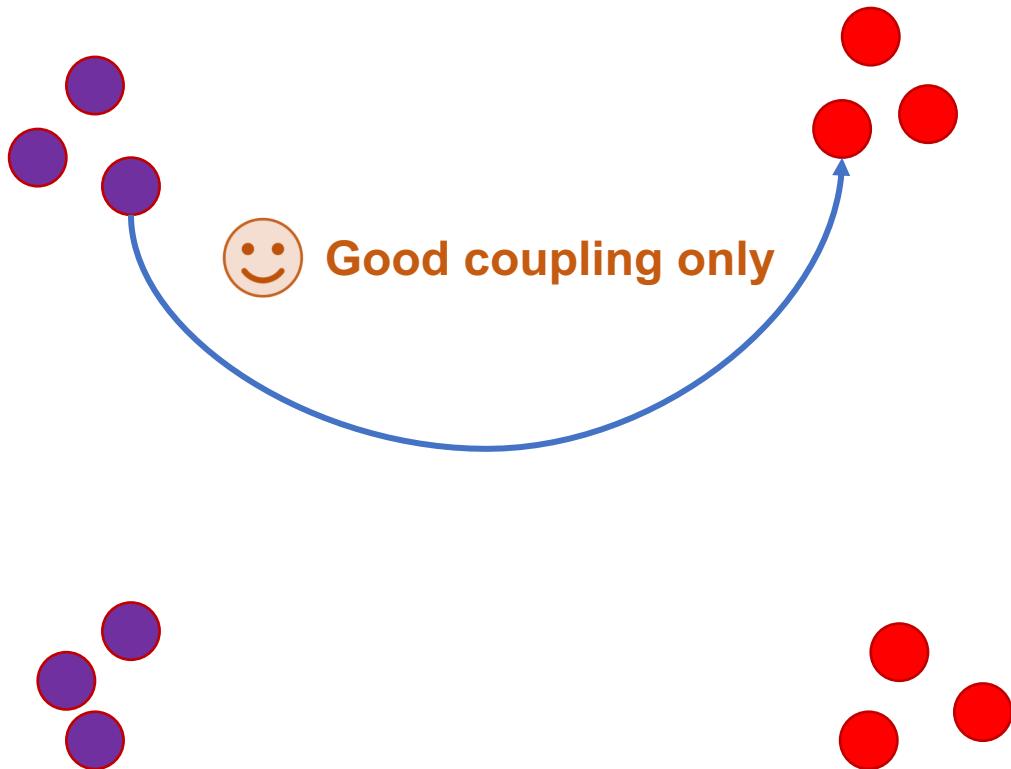
Curved student comes from crossing in training



We have no better coupling than random

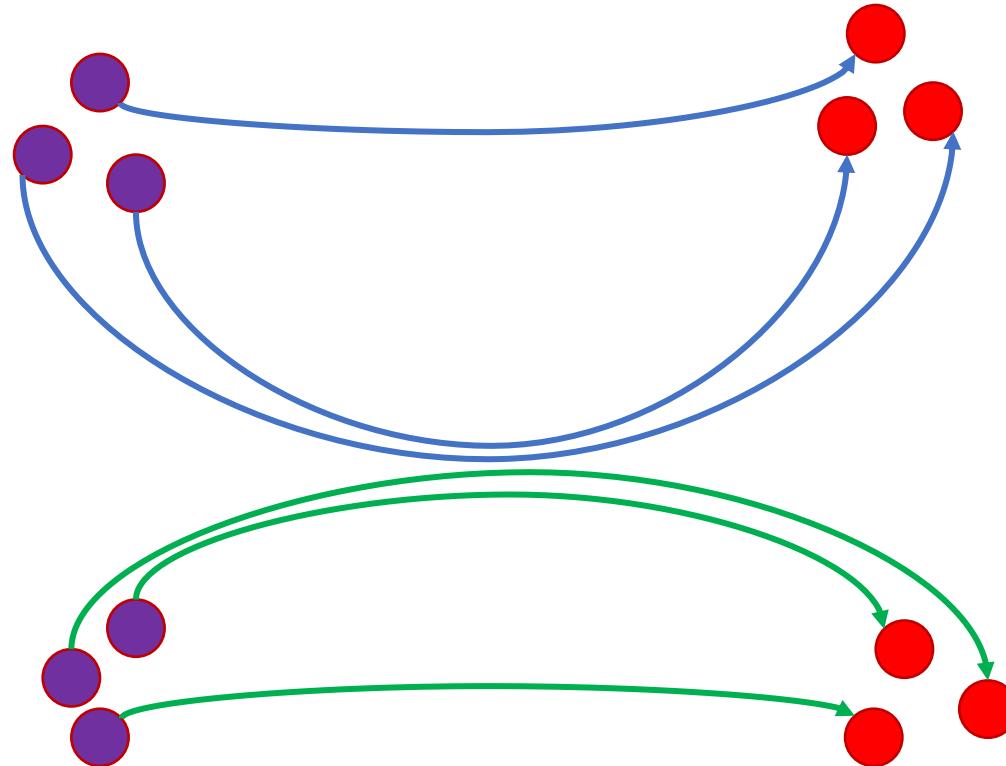
Our Solution: Reflow!

But the new student eliminates crossing!



It is a better teacher than random
Moreover, it keeps the target distribution π_1

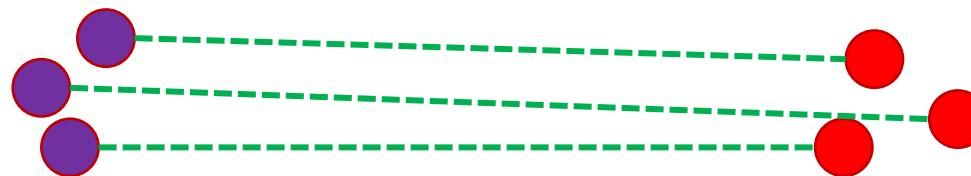
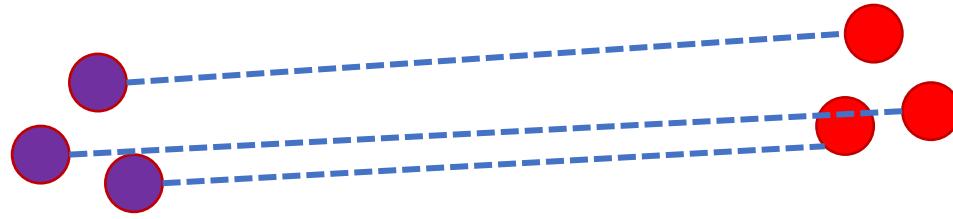
Reflow Step-1: Construct Straight-Line Teachers



Get the coupling by simulating with ODE solver, e.g., Euler

$$\text{ODE: } \frac{dX}{dt} = v_\theta(X, t)$$

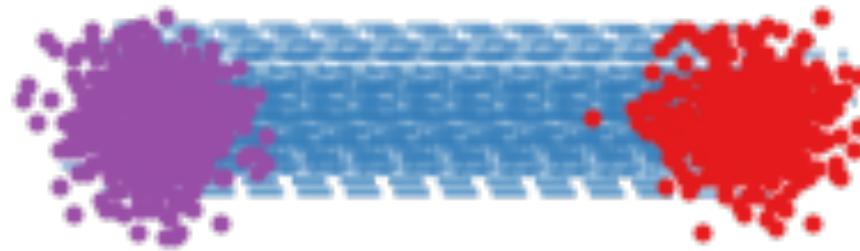
Reflow Step-1: Construct Straight-Line Teachers



Linear Interpolation (again): $X_t = tX_1 + (1 - t)X_0$

$$\text{ODE: } \frac{dX}{dt} = v_\theta(X, t)$$

Reflow Step-1: Construct Straight-Line Teachers

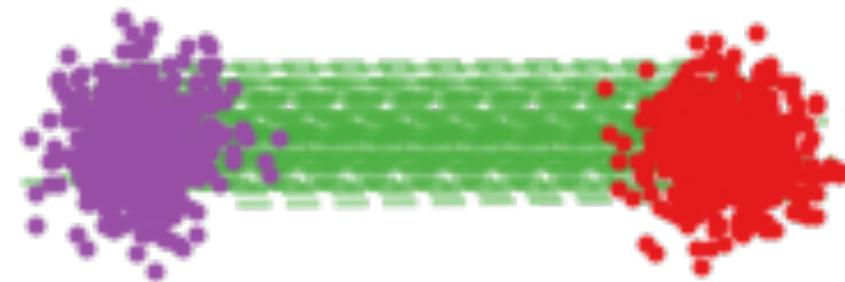


$\{x_i^0\}_{i=1}^n \sim \pi_0$

2-GMM

$\{x_i^1\}_{i=1}^n \sim \pi_1$

2-GMM



Linear Interpolation (again): $X_t = tX_1 + (1 - t)X_0$

ODE: $\frac{dX}{dt} = v_\theta(X, t)$

Reflow Step-2: Project to Causal Students

Projection Loss (previous)

$$\min_{\theta} \int_0^1 \mathbb{E}_{X_0 \sim \pi_0, X_1 \sim \pi_1} \left[\left\| (X_1 - X_0) - v_{\theta}(X_t, t) \right\|^2 \right] dt$$

Independent

Projection Loss (now)

$$\min_{\theta} \int_0^1 \mathbb{E}_{X_0 \sim \pi_0, X_1 = ODE_{v_{old}}(X_0)} \left[\left\| (X_1 - X_0) - v_{\theta}(X_t, t) \right\|^2 \right] dt$$

Generated by ODE

Reflow Step-3: Generation with ODE solver

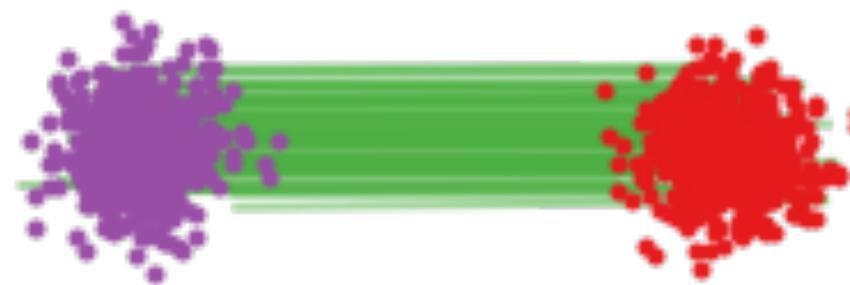


Randomly sample $X_0 \sim \pi_0$

ODE is straightened!

Generated distribution $X_1 \sim \pi_1$

Guaranteed by math



Simulate with ODE solver, e.g., Euler

$$\text{ODE: } \frac{dX}{dt} = v_\theta(X, t)$$

Algorithm: Reflow

- **Given:** $\{x_i^0\}_{i=1}^n \sim \pi_0$, $\{x_i^1\}_{i=1}^n \sim \pi_1$, old flow v_{old}
- **Training Iteration (Batch size = 1):**
 - Step 1: Randomly sample $X_0 \in \{x_i^0\}_{i=1}^n$
 - Step 2: Generate $X_1 = ODE_{v_{old}}(X_0)$
 - Step 3: Randomly sample $t \in [0,1]$
 - Step 4: Compute gradient with loss

$$L(\theta) := \left\| X_1 - X_0 - v_\theta(X_t, t) \right\|^2,$$

where $X_t = tX_1 + (1-t)X_0$

Reflow: Theoretical Properties



Guarantee straight ODE trajectories after infinite reflow

In practice, one reflow already has magic

k-Rectified Flow (ν_k)

Reflow: Theoretical Properties



Reflow is a multi-objective OT solver

Every reflow monotonically decrease the transport cost
for all convex cost functions c :

$$\mathbb{E}_{(X_0, X_1) \sim p_{\nu_k}(X_0, X_1)}[c(X_1 - X_0)] \leq \mathbb{E}_{(X_0, X_1) \sim p_{\nu_{k+1}}(X_0, X_1)}[c(X_1 - X_0)]$$

Distillation

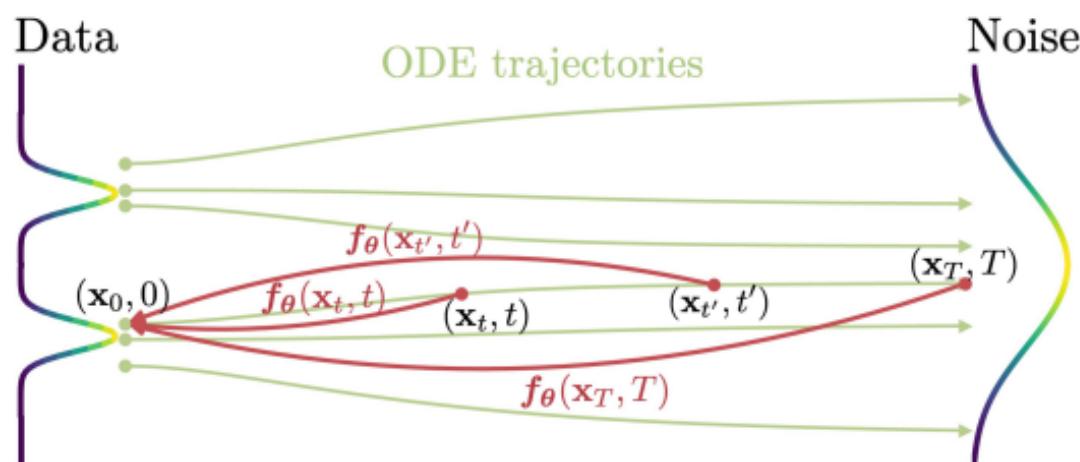
- **Distillation**

$$\min_{\phi} \mathbb{E}_{X_0 \sim \pi_0, X_1 = ODE_{\nu}(X_0)} \|f_{\phi}(X_0) - X_1\|^2$$

- **Data-free Distillation**

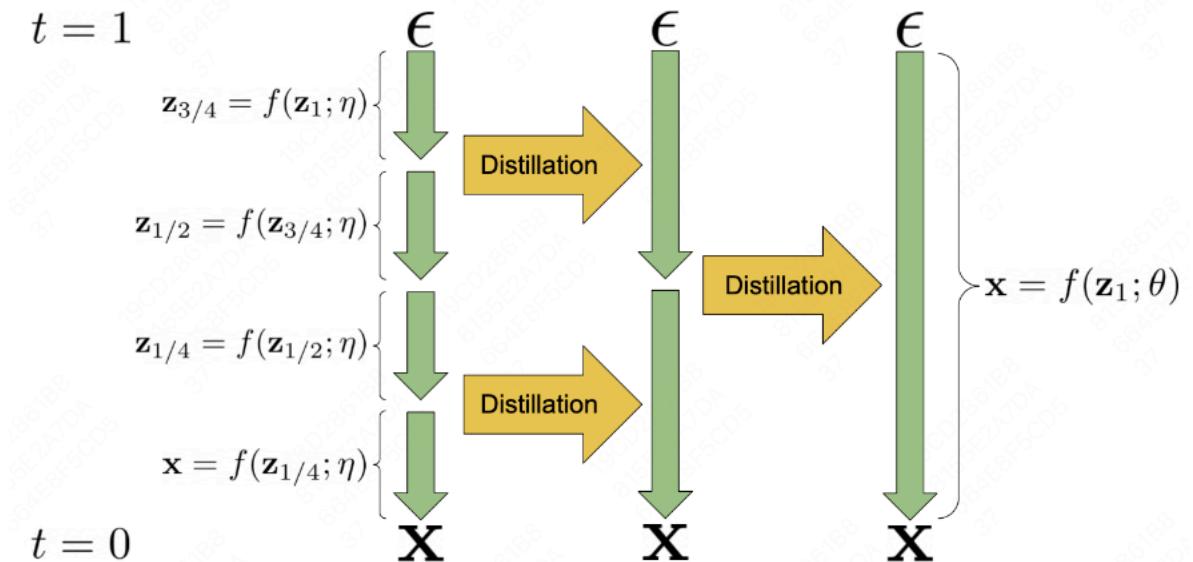
Consistency Distillation

[Song et al. 2023]



Progressive Distillation

[Salimans et al. 2022]



Reflow is Orthogonal to Distillation



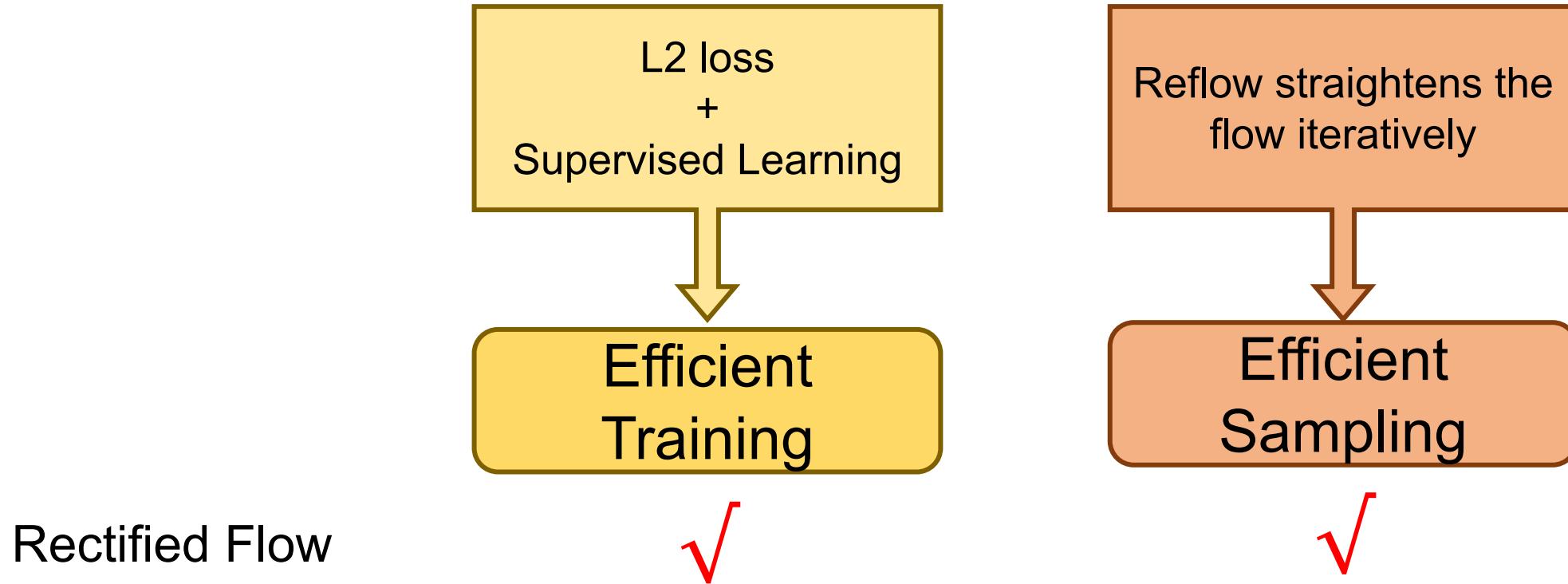
Reflow is a multi-objective OT solver

It changes coupling, while distillation imitates

Reflow: Create better probability flow teacher

Distillation: Train one-step student from teacher

Rectified Flow



Reflow: Empirical Results

CIFAR10

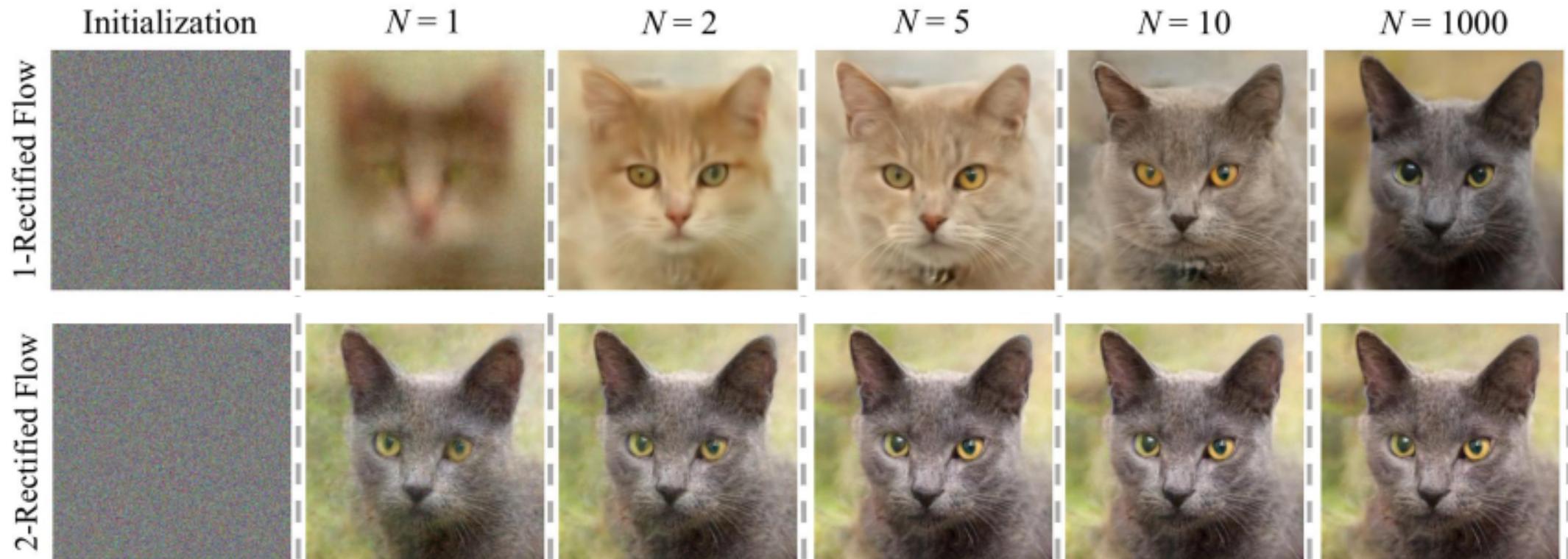
Method	NFE (↓)	IS (↑)	FID (↓)
1-Rectified Flow	127	9.60	2.58
2-Rectified Flow	110	9.24	3.36
3-Rectified Flow	104	9.01	3.96

Method	NFE (↓)	IS (↑)	FID (↓)
1-Rectified Flow	1	1.13	378
2-Rectified Flow	1	8.08	12.21
3-Rectified Flow	1	8.47	8.15

Method	NFE (↓)	IS (↑)	FID (↓)
1-Rectified Flow+Distill	1	9.08	6.18
2-Rectified Flow+Distill	1	9.01	4.85
3-Rectified Flow+Distill	1	8.79	5.21

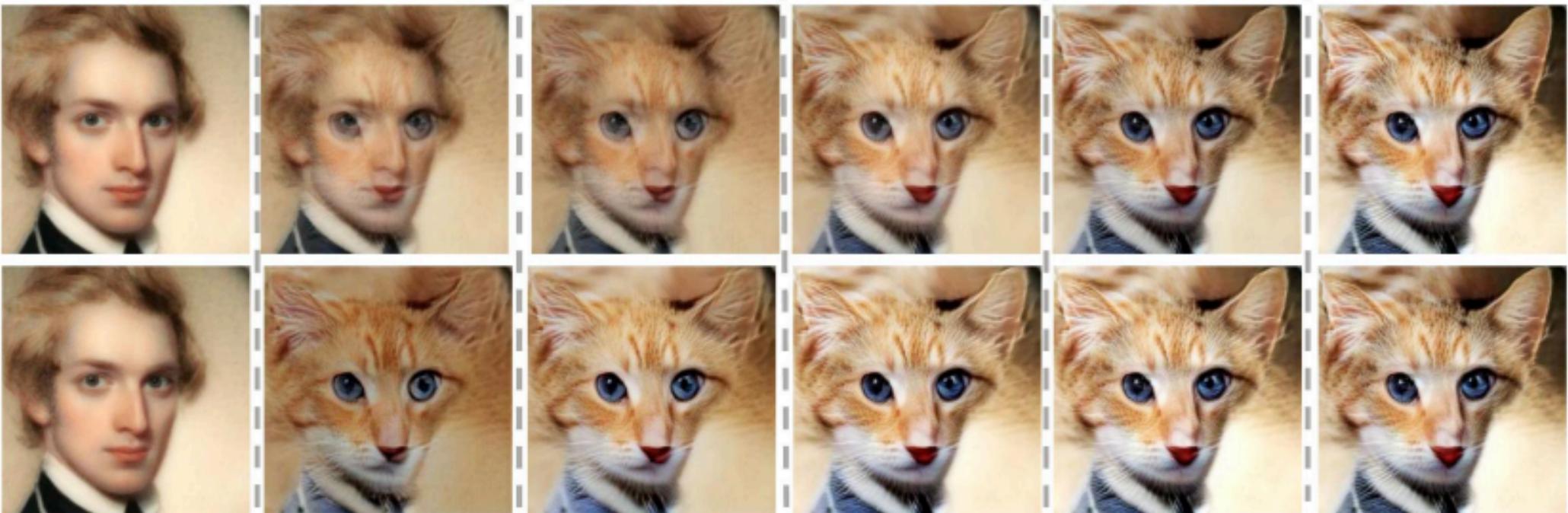
SOTA
(when arXiv)

Reflow: Generative Modeling



Reflow: Domain Transfer

2-Rectified Flow 1-Rectified Flow



InstaFlow: Scale Up Rectified Flow

- Today's common sense: scaling-up makes things different!
- Will the rectified flow pipeline (reflow+distill) still work in Stable Diffusion level?

InstaFlow: Scale Up Rectified Flow



One-step InstaFlow-0.9B (0.09s per image, 512×512)



One-step InstaFlow-1.7B
(0.12s per image, 512×512)

InstaFlow: Scale Up Rectified Flow

- **Text-Conditioned Reflow:**

$$v_{k+1} = \arg \min_v \mathbb{E}_{X_0 \sim \pi_0, \mathcal{T} \sim D_{\mathcal{T}}} \left[\int_0^1 \| (X_1 - X_0) - v(X_t, t \mid \mathcal{T}) \|^2 dt \right],$$

with $X_1 = \text{ODE}[v_k](X_0 \mid \mathcal{T})$ and $X_t = tX_1 + (1-t)X_0$,

Random text from text dataset Text-conditioned model

Text-conditioned generation

- **Text Dataset:** 1.6M data points from LAION-2B (aesthetics score 6.0+)
- **Model:** Stable Diffusion (as 1-Rectified Flow)
- **Training cost:** 199 A100 GPU days (InstaFlow 0.9B)

Reflow Makes a Difference

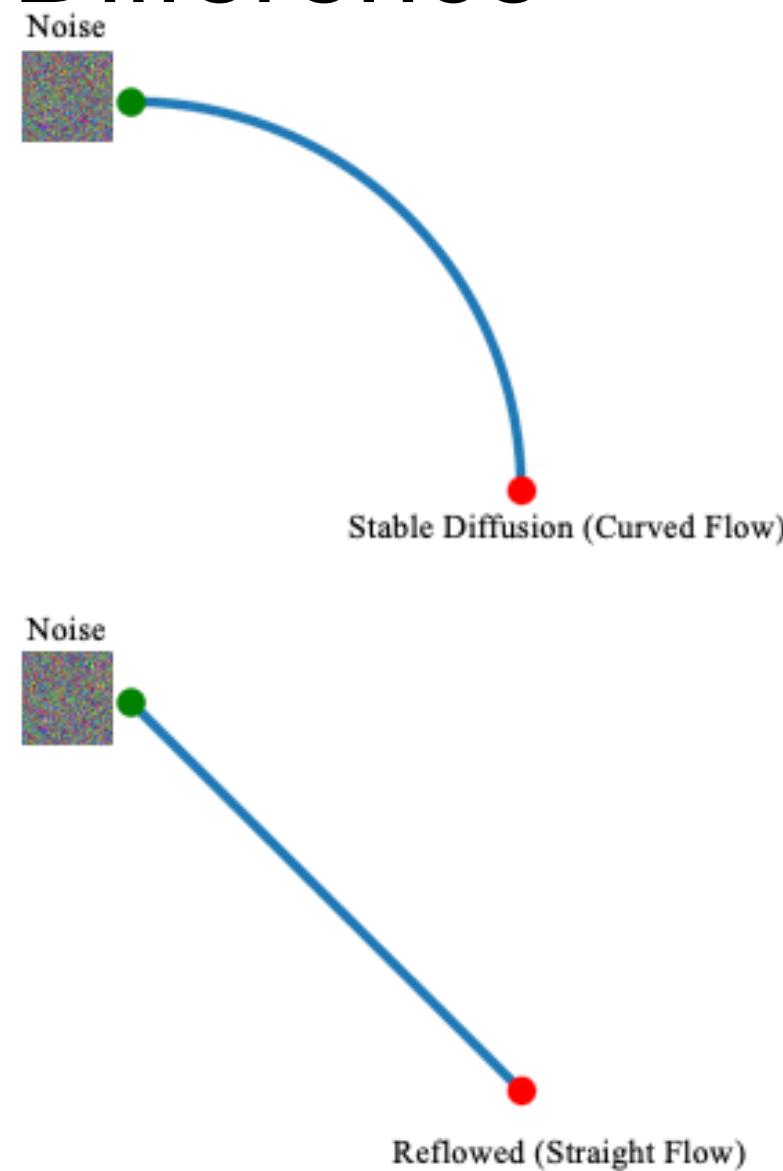
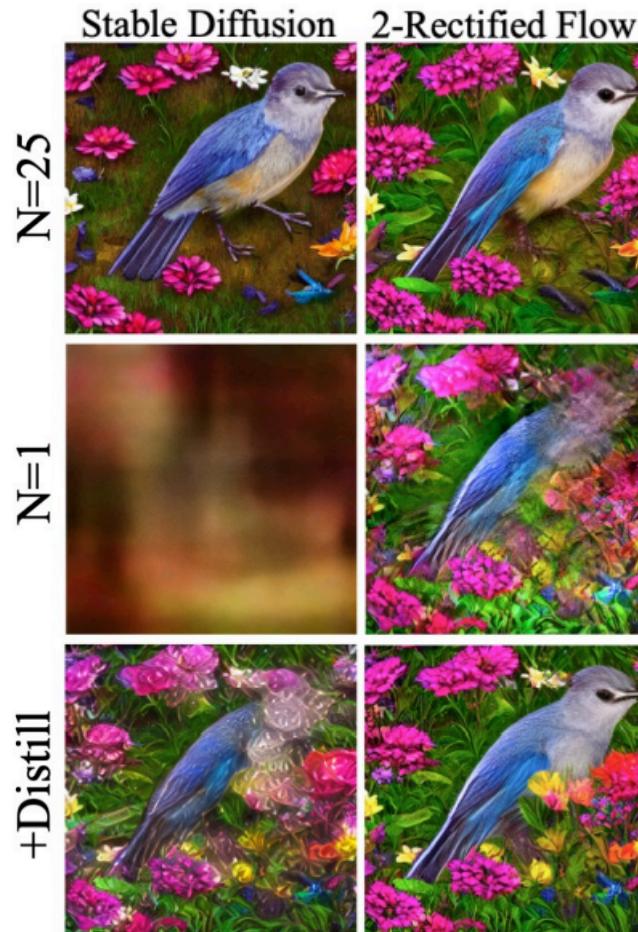
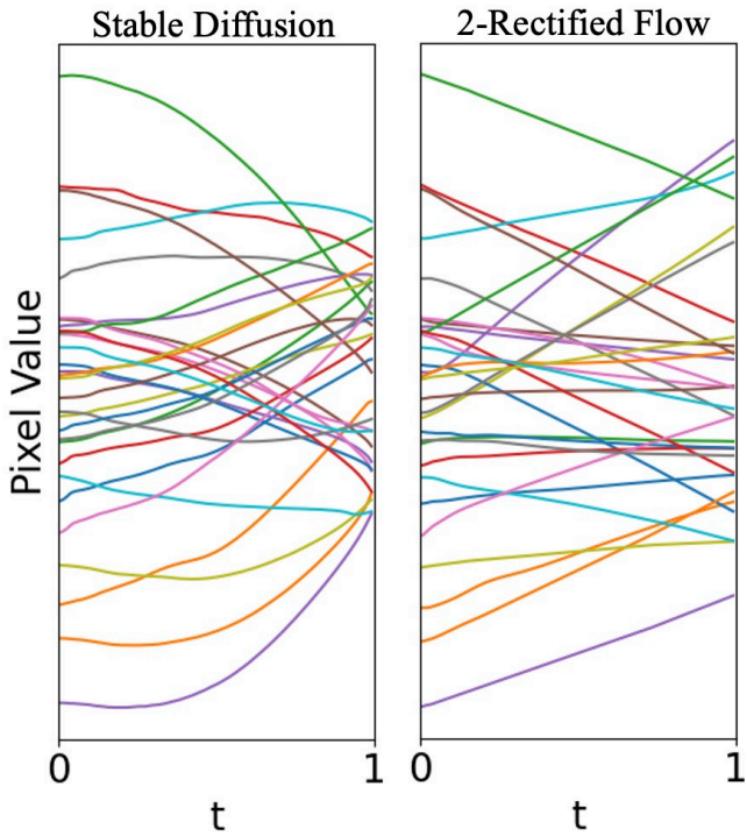
- **Direct Distillation:** 100k training steps
- **Reflow + Distillation:** 50k training steps + 50k training steps

MS COCO 2017 – 5k images

Method	Inf t (↓)	FID (↑)	CLIP (↑)
SD 1.4	0.88s	22.8	0.315
2-Rectified Flow	0.88s	22.1	0.313

Method	Inf t (↓)	FID (↑)	CLIP (↑)
SD 1.4+Distill	0.09s	40.9	0.255
Progressive Distill	0.09s	37.2	0.275
2-Rectified Flow +Distill	0.09s	31.0	0.285

Reflow Makes a Difference



InstaFlow: Further Scaling Up

- The preliminary experiments only spends 24.65 A100 GPU days in training
- **Reflow + Distillation:** 24.65 A100 GPU days → 199 A100 GPU days



InstaFlow-0.9B

- **Expand Network:** 0.9B → 1.7B



InstaFlow-1.7B

InstaFlow: Empirical Results

MS COCO 2017 – 5k images

Method	Inf t (↓)	FID (↑)	CLIP (↑)
SD 1.4+Distill	0.09s	40.9	0.255
Progressive Distill (1-step)	0.09s	37.2	0.275
2-Rectified Flow+Distill (24.65 A100 GPU days)	0.09s	31.0	0.285
InstaFlow-0.9B (199 A100 GPU days)	0.09s	23.4	0.304
InstaFlow-1.7B	0.12s	22.4	0.309

MS COCO 2014 – 30k images

Method	Inf t (↓)	FID (↑)
Stable Diffusion	2.9s	9.62
StyleGAN-T	0.1s	13.90
GigaGAN	0.13s	9.09
InstaFlow-0.9B	0.09s	13.10
InstaFlow-1.7B	0.12s	11.83

InstaFlow as Fast Previewer

One-Step

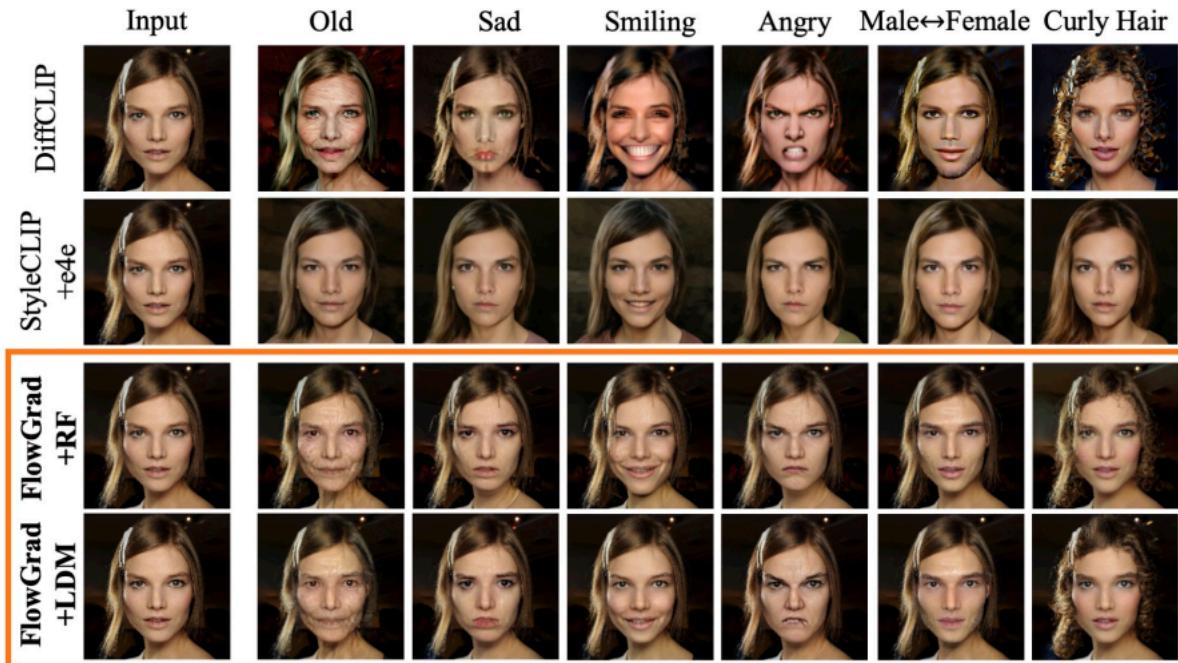


+SDXL
Refiner



Fast preview + Slow Refiner

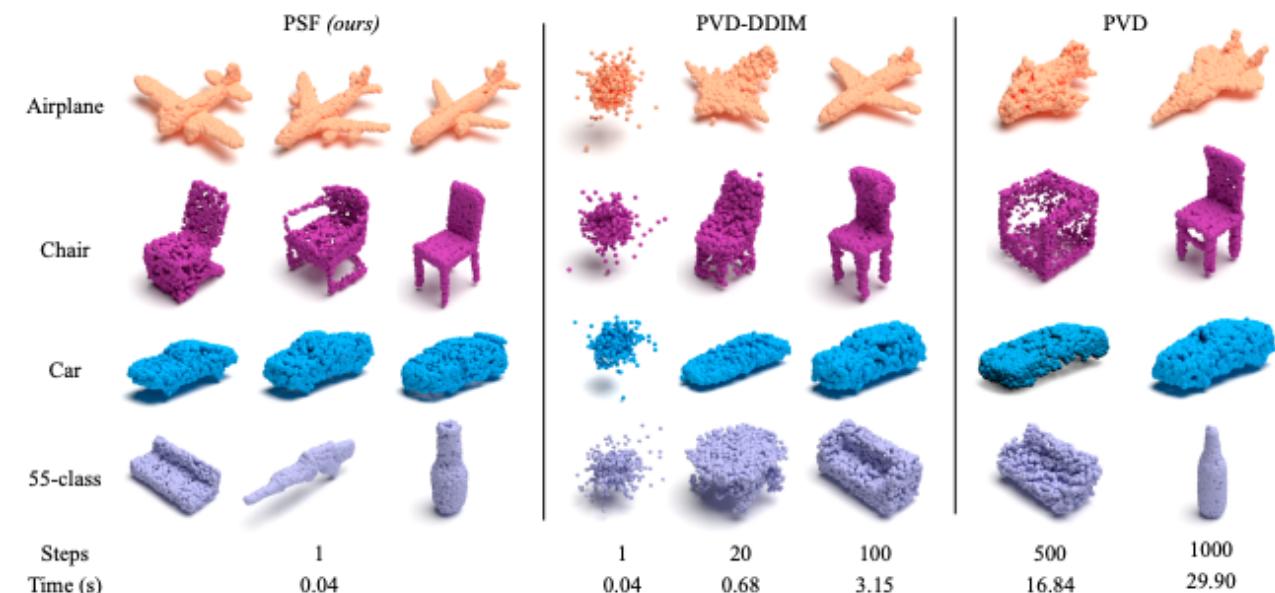
Other Works from Our Group



FlowGrad

Fast gradient-based editing with probability flows

[Liu et al., CVPR 2023]

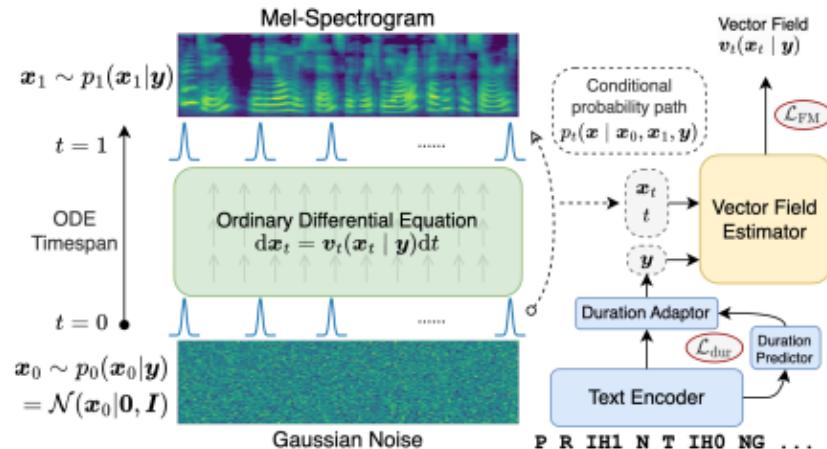


Point Straight Flow

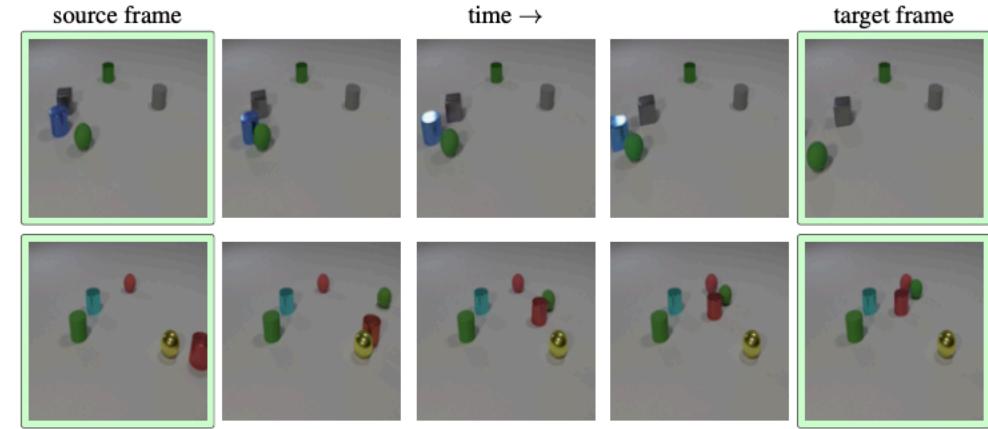
One-step point cloud generation (100x faster)

[Wu et al., CVPR 2023]

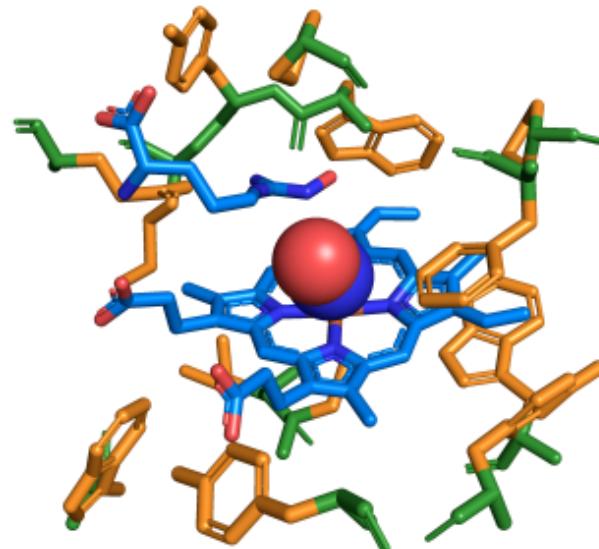
Applications From Other Labs



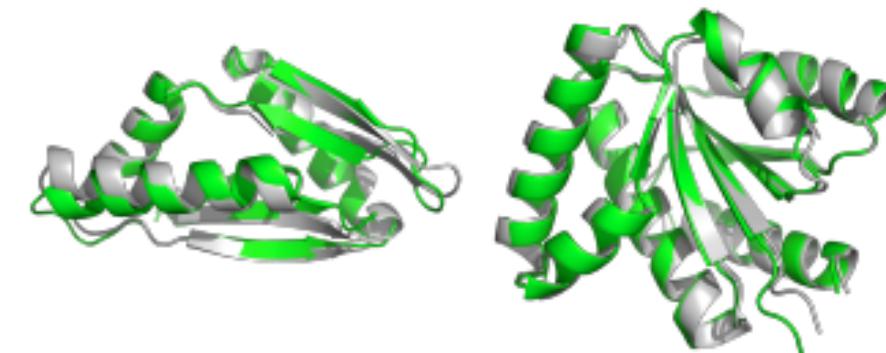
VoiceFlow (text-to-speech) [Guo et al. 2023]



RIVER (video prediction) [Davtyan et al. 2023]



FlowSite (binding site design) [Stark et al. 2023]



FoldFlow (protein structure design) [Yim et al. 2023]

Take-Aways

- Straight = Fast !
- Made possible by Rectified Flow !
- Scale up perfectly in large models !

Thank you!

Questions?



Demo: <https://huggingface.co/spaces/XCLiu/InstaFlow>

Many thanks to my collaborators: Chengyue Gong, Qiang Liu, Xiwen Zhang, Jianzhu Ma, Jian Peng

Concurrent works

There were concurrent works with the same idea, different names:

- Flow matching [Lipman et al. 2023]
- Stochastic Interpolants [Albergo et al. 2023]
- α -(de)blending [Heitz et al. 2023]
- Action matching [Neklyudov et al. 2023]