

① In a Quant test of CAT exam, population S.D. is 100. A sample of 25 test takers has sample mean 520. Construct an 80% C.I. about mean.

Given: $\sigma = 100$; $\bar{x} = 520$; $n = 25$.

$$\text{Significance Value } (\alpha) = 1 - \text{Confidence Interval} \\ = 1 - 80\%$$

$$\alpha = 0.20$$

$$\text{Parameter} = \text{Point Estimate} \pm \text{Margin of Error} \\ = \bar{x} \pm Z_{\alpha/2} \frac{\sigma}{\sqrt{n}}$$

$$\text{Higher Fence} = 520 + Z_{0.10} \frac{100}{\sqrt{25}}$$

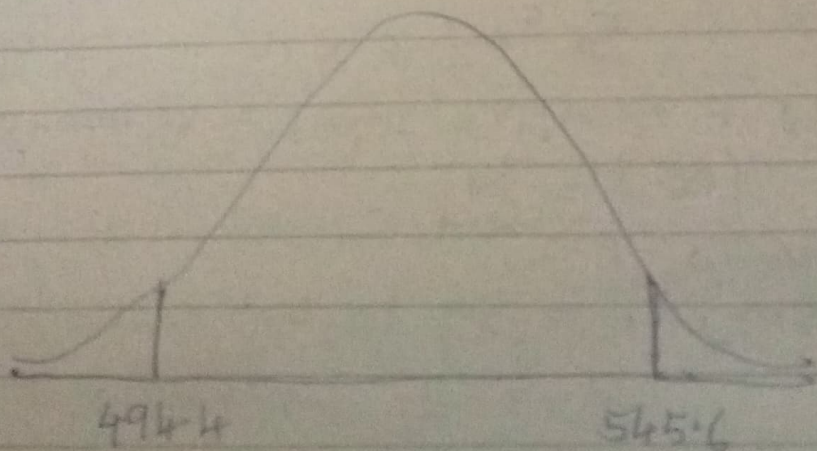
$$= 520 + (1.28 \times 20)$$

$$\boxed{\text{Higher Fence} = 545.6}$$

$$\text{Lower Fence} = 520 - Z_{0.10} \times 20$$

$$= 520 - (1.28 \times 20)$$

$$\boxed{\text{Lower Fence} = 494.4}$$



② In a company there are 100k employees. We need to order L & XL T shirts for them. For sample 500, there are 300 XL and 200 L T shirts. How many XL & L T shirts need to be ordered.

XL T-shirt: $n_1 = 300$, $\bar{x} = 500$, $s(\text{Sample SD}) = 150$

Degrees of freedom = $n_1 - 1 = 299$.

$$\begin{aligned}\text{Lower Fence} &= 500 - t_{299/2} \cdot s/\sqrt{n} \\ &= 500 - 1.6551 \times \frac{150}{\sqrt{300}} = \boxed{485.67}\end{aligned}$$

$$\boxed{\text{Higher Fence} = 500 + 14.334 = 514.334}$$

~~2nd~~ L T-shirt:

$n_2 = 200$, $\bar{x} = 500$, $s = 150$

$$\text{Lower Fence} = 500 - t_{79.5} \left(\frac{150}{\sqrt{200}} \right) = 500 - 17.614$$

$$\boxed{\text{Lower Fence} = 482.39}$$

$$\text{Higher Fence} = 500 + 17.614 =$$

$$\boxed{\text{Higher Fence} = 517.614}$$