# Celestial Sphere Models 1

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# Table of Contents

1. Instructions	1
2. Greek Alphabet	2
3. Constellations	2
4. Spherical Biangles	3
4.1. White on Black Background	3
42 Black on White Background	5
5. Panels (Isoceles Trapezoids and Triangles)	7
5.1. White on Black Background	7
5.2. Black On White Background	9
6. Globes	11
7. Copying	13
7.1. GNU General Public License	15
7.2 GNU Free Documentation License	10

## Instructions

PLEASE NOTE! The author has tried to ensure that the following plans are correct, but as of September 6, 2021, he has not tested them yet himself. As mentioned above, this material is distributed without a warranty. I recommend that users check it themselves before investing a lot of time and effort into cutting out the paper models.

Any corrections will be gratefully received by the author. Contact information can be found on the title page.

The two models are provided in two versions each, white on black and black on white. They include the 200 brightest stars, except for Polaris, which would have been at an inconvenient location on the models, namely at the north pole.

The separate file clstsph1\_a4.pdf in DIN A4 format contains data for the stars on the models.

The first model is made up of spherical biangles. They should not be folded but rather bent and attached to each other using the tabs on the left side, forming a sphere.

The second model uses "panels". While the left and right sides of the sections appear to be curved, they are in fact made up of straight lines. The sections should be folded on the horizontal lines (declination) and again attached using the tabs. The result is an irregular polyhedron approximating a sphere.

The "globes" on pages 11–12 illustrate how the positions of the stars on the spherical biangles and panels were derived.

Assembling the models should present no particular difficulty except possibly for keeping the spherical biangles from slipping while attaching them to each other. A fast-setting glue might be helpful in this case, and/or patience.

The longitudes of the stars are found by rotating counter-clockwise from right ascension  $0h\,0'\,0''$ . I believe that the model represents the celestial sphere as seen by an observer looking at it from the outside. I hope someone will correct me if I'm wrong. The famous early star atlas of Johannes Hevelius from 1690 also shows the stars in this way<sup>1</sup>.

However, in principle it wouldn't be difficult to reverse the representation. The difficulty would be in reversing the labels, but I think this problem could be solved.

The plans could also be generated for larger or smaller models. In addition, the limit of 200 stars is arbitrary and was chosen to correspond to the size of these versions of the models (sphere radius 7cm). As of September 6, 2021, the database table containing the star data has entries for over 1400 stars. However, not all of the entries contain all of the necessary data yet. If you want to make models of a different size and/or with a different number of stars, please send an email to the author at the address listed above.

# **Greek Alphabet**

$\alpha$	alpha	$\nu$	nu
$\beta$	beta	ξ	xi
$\gamma$	gamma	0	omicron
$\delta$	delta	$\pi$ , $\varpi$	pi
$\epsilon,  \varepsilon$	epsilon	$\rho, \varrho$	rho
ζ	zeta	$\sigma$ , $\varsigma$	$_{ m sigma}$
$\eta$	eta	au	tau
$\theta, \vartheta$	theta	v	upsilon
$\iota$	iota	$\phi, \varphi$	phi
$\kappa$	kappa	$\chi$	chi
$\lambda$	lambda	$\psi$	psi
$\mu$	mu	$\omega$	omega

# Constellations

I. Andromeda	21. Cetus	41. Horologium	61. Pavo
2. Antlia	22. Chamaeleon	42. Hydra	62. Pegasu
3. Apus	23. Circinus	43. Hydrus	63. Perseu
4. Aquarius	24. Columba	44. Indus	64. Phoen
5. Aquila	25. Coma Berenices	45. Lacerta	65. Pictor
6. Ara	26. Corona Australis	46. Leo	66. Pisces
7. Aries	27. Corona Borealis	47. Leo Minor	67. Piscis
3. Auriga	28. Corvus	48. Lepus	68. Puppis
). Boötes	29. Crater	49. Libra	69. Pyxis
0. Caelum	30. Crux	50. Lupus	70. Reticu
1. Camelopardalis	31. Cygnus	51. Lynx	71. Sagitta
2. Cancer	32. Delphinus	52. Lyra	72. Sagitta
3. Canes Venatici	33. Dorado	53. Mensa	73. Scorpi
14. Canis Major	34. Draco	54. Microscopium	74. Sculpt
5. Canis Minor	35. Equuleus	55. Monoceros	75. Scutur
6. Capricornus	36. Eridanus	56. Musca	76. Serper
17. Carina	37. Fornax	57. Norma	77. Sextar
8. Cassiopeia	38. Gemini	58. Octans	78. Taurus
9. Centaurus	39. Grus	59. Ophiuchus	79. Telesco
20. Cepheus	40. Hercules	60. Orion	

<sup>62.</sup> Pegasus 63. Perseus 64. Phoenix 65. Pictor 66. Pisces 67. Piscis Austrinus 68. Puppis 69. Pvxis 70. Reticulum 71. Sagitta 72. Sagittarius 73. Scorpius 74. Sculptor 75. Scutum 76. Serpens 77. Sextans 78. Taurus 79. Telescopium

86. Virgo87. Volans88. Vulpecula

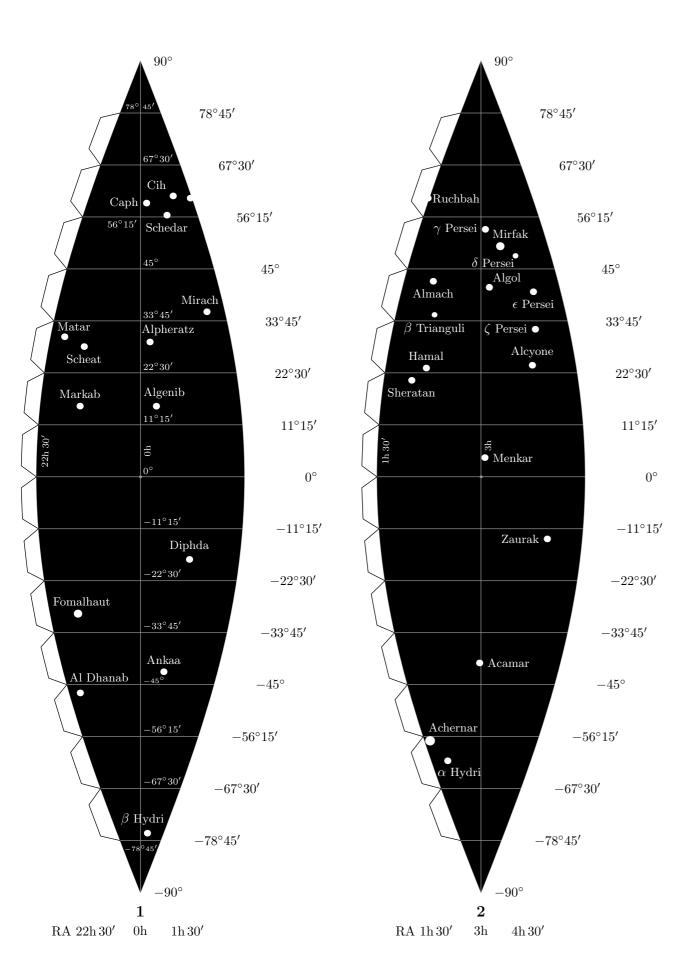
85. Vela

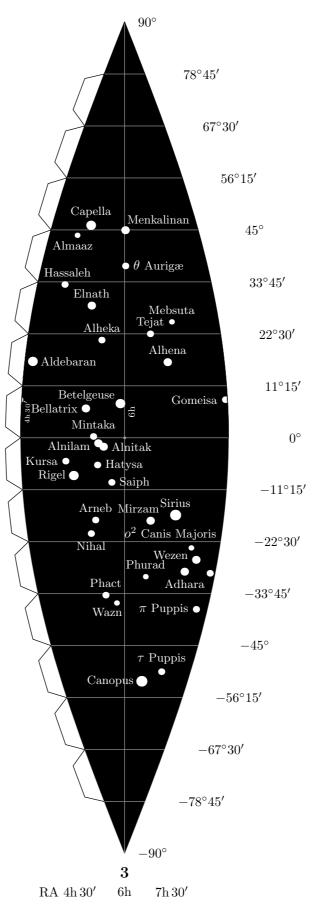
80. Triangulum

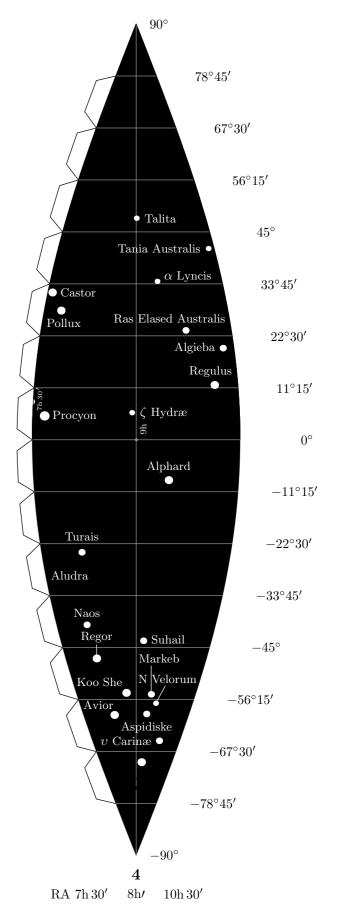
<sup>81.</sup> Triangulum Australe82. Tucana83. Ursa Major84. Ursa Minor

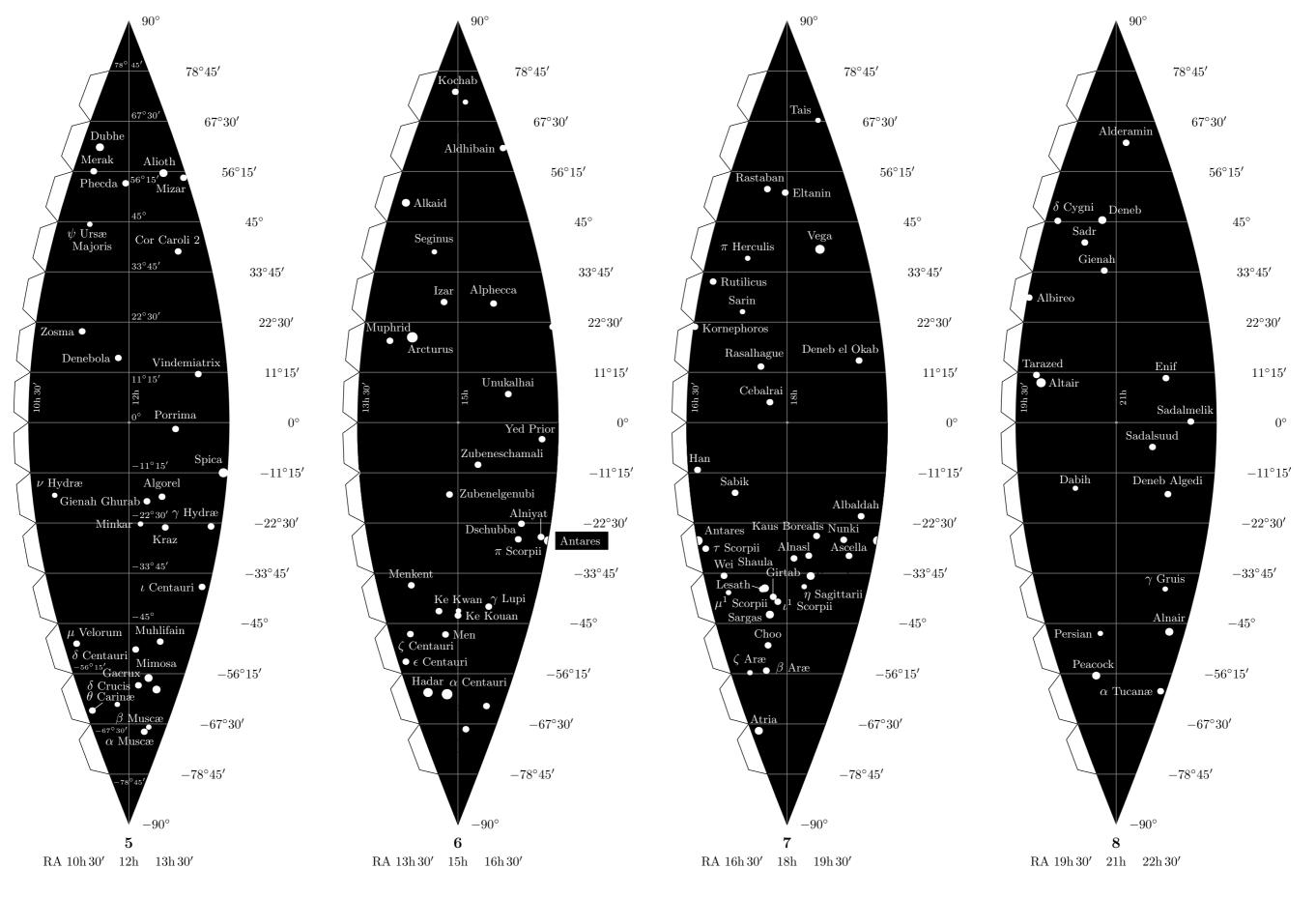
 $<sup>^{\</sup>rm 1}$  Menzel, Donald H. and Pasachoff, Jay M., Stars and Planets. Peterson Field Guides, p. 21.

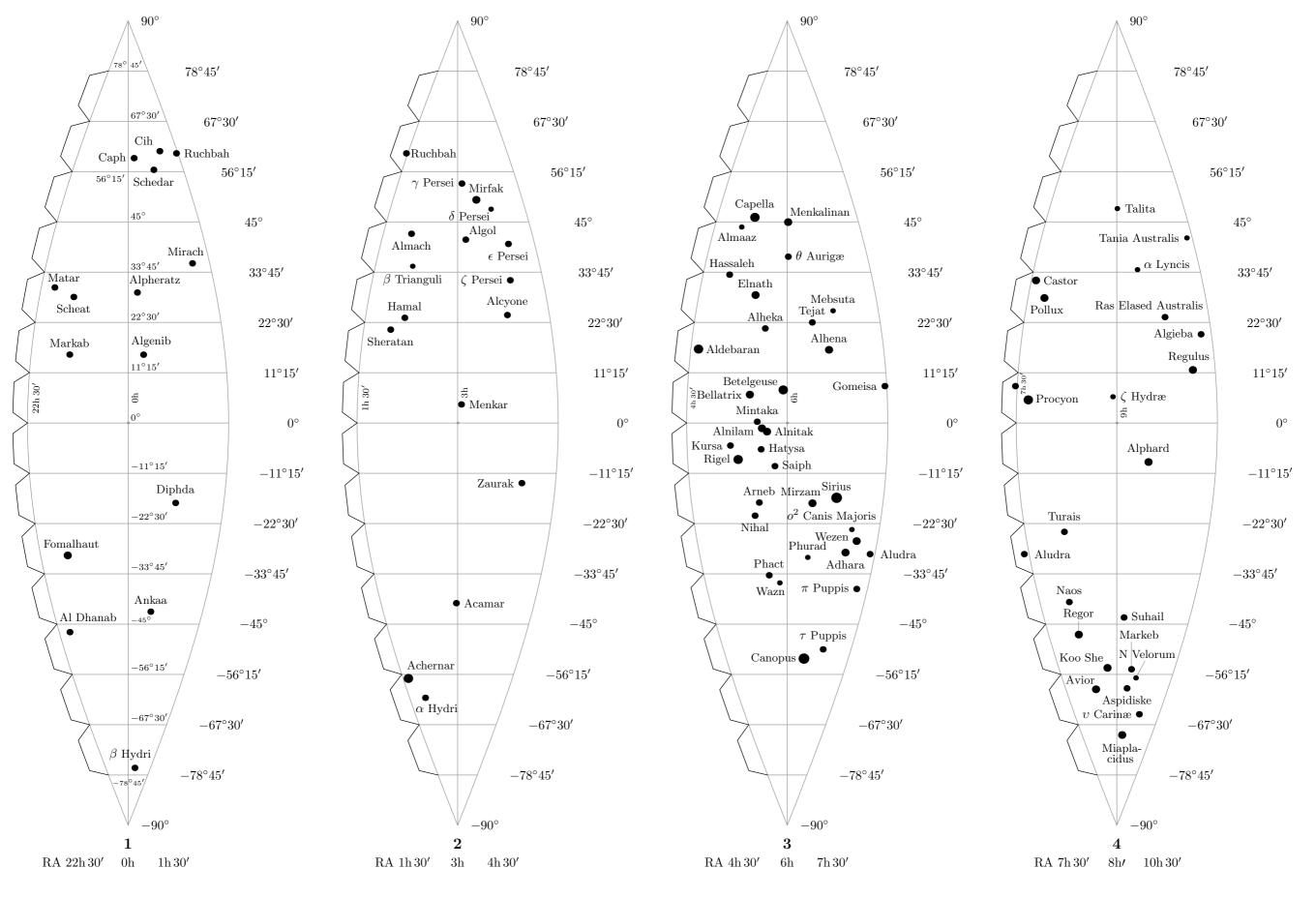
# **Spherical Biangles**

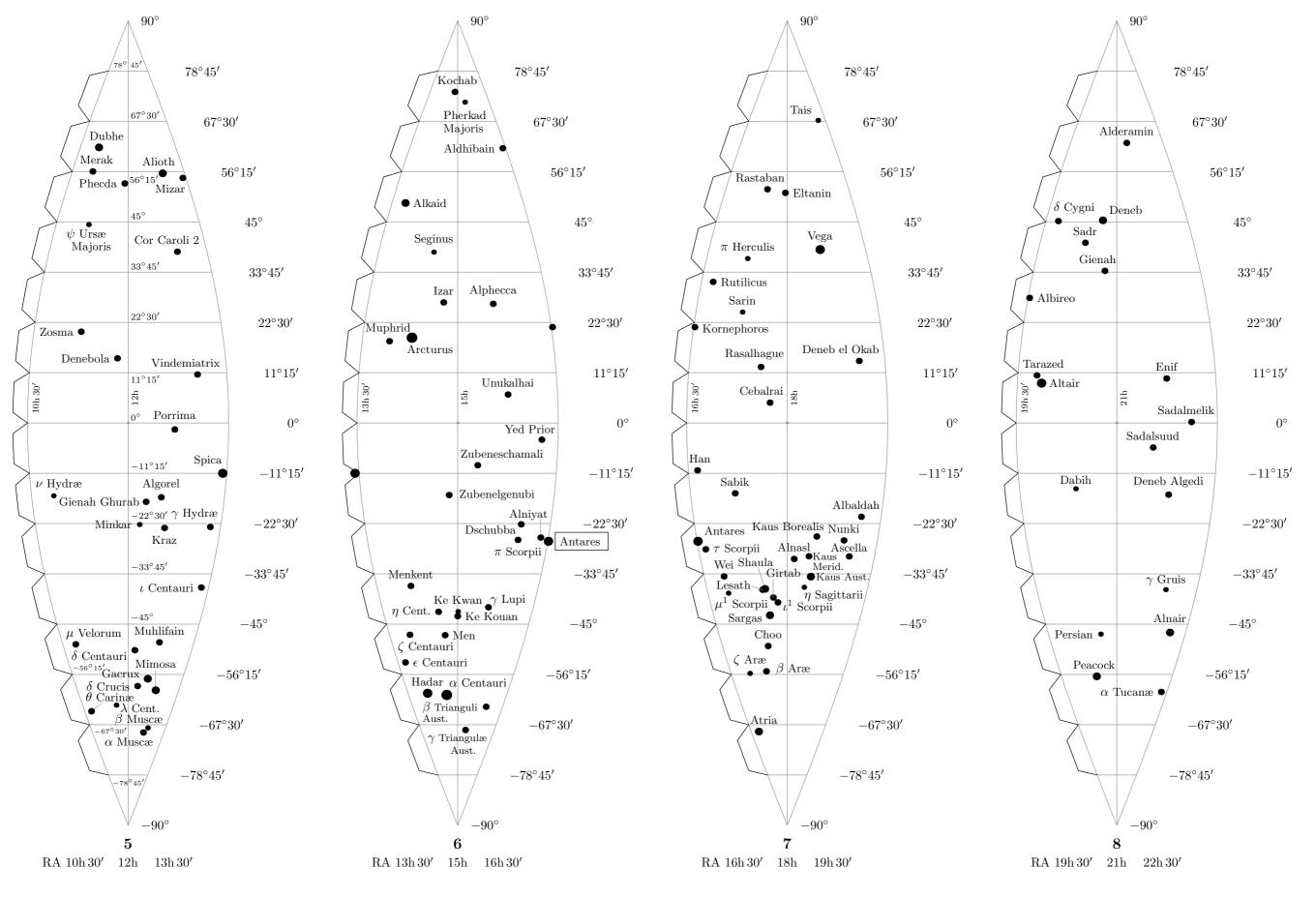




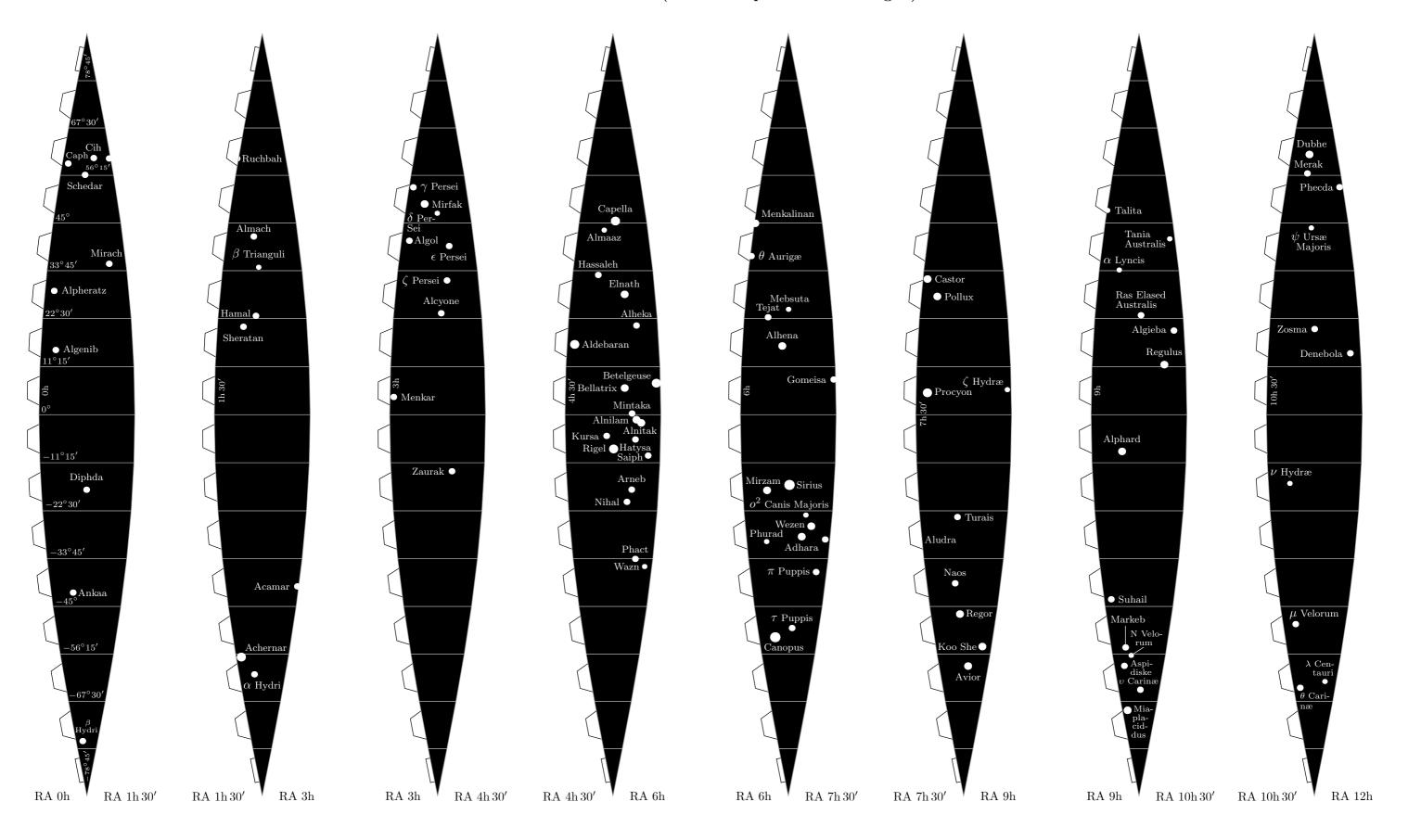


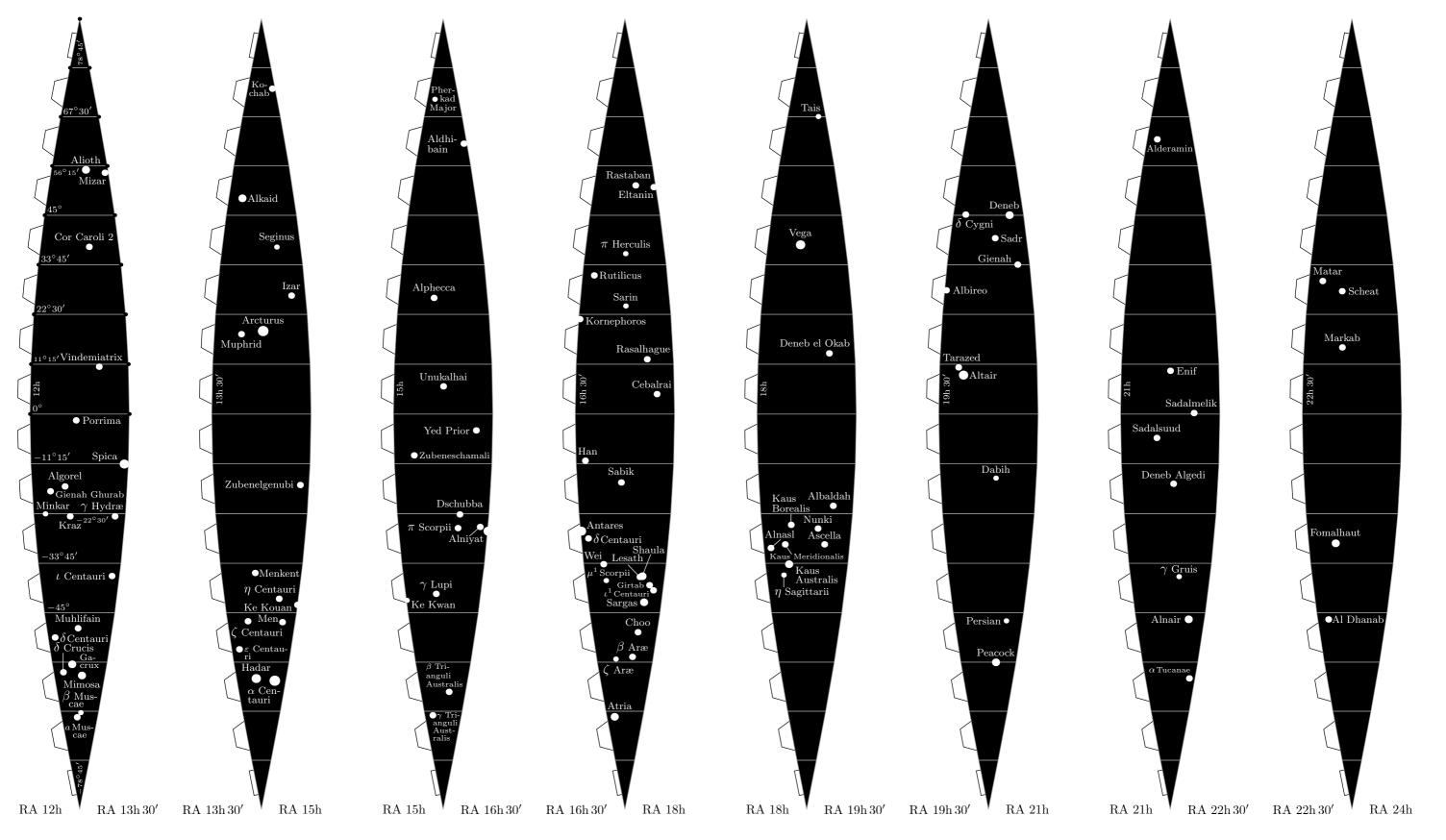


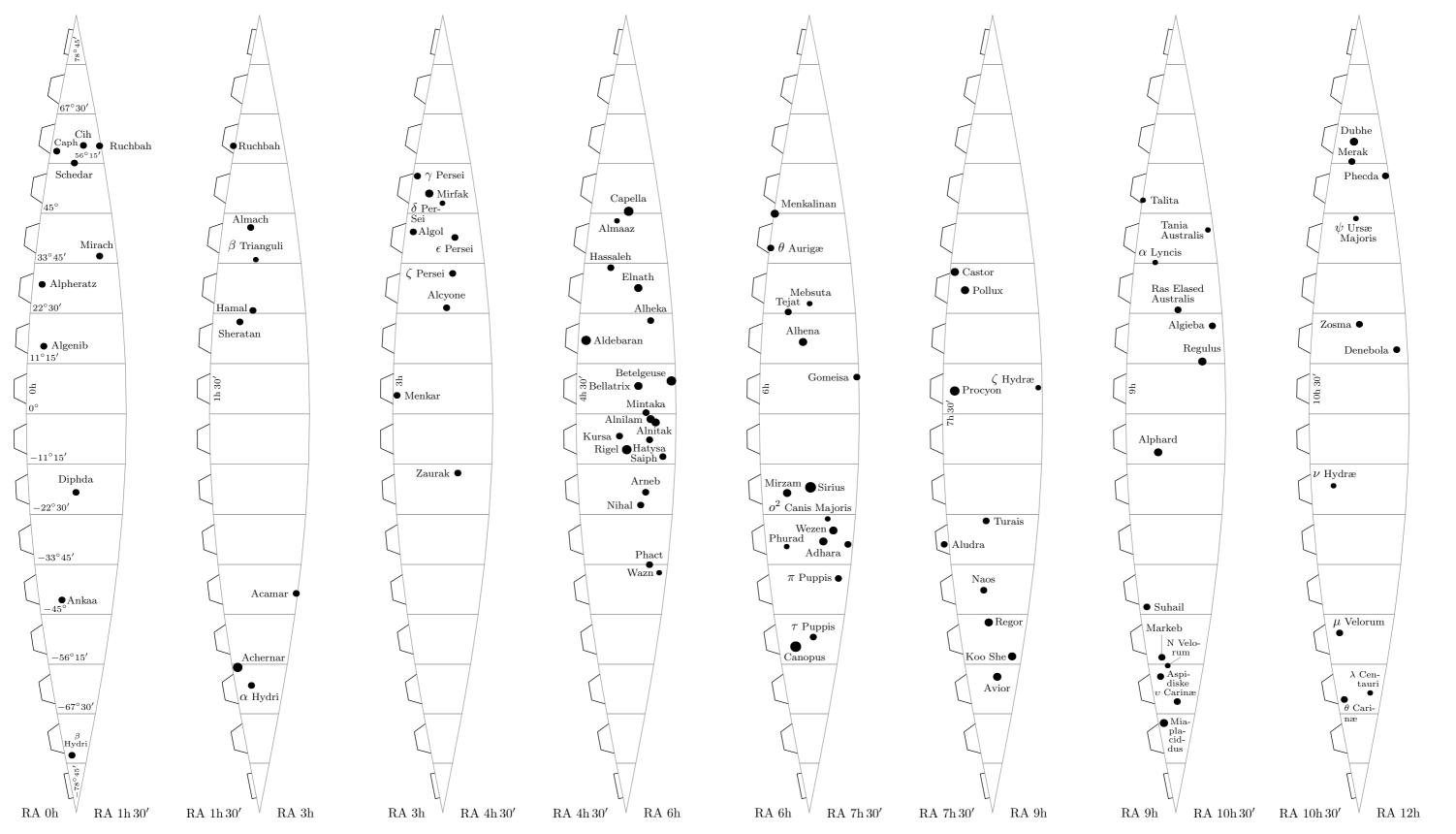


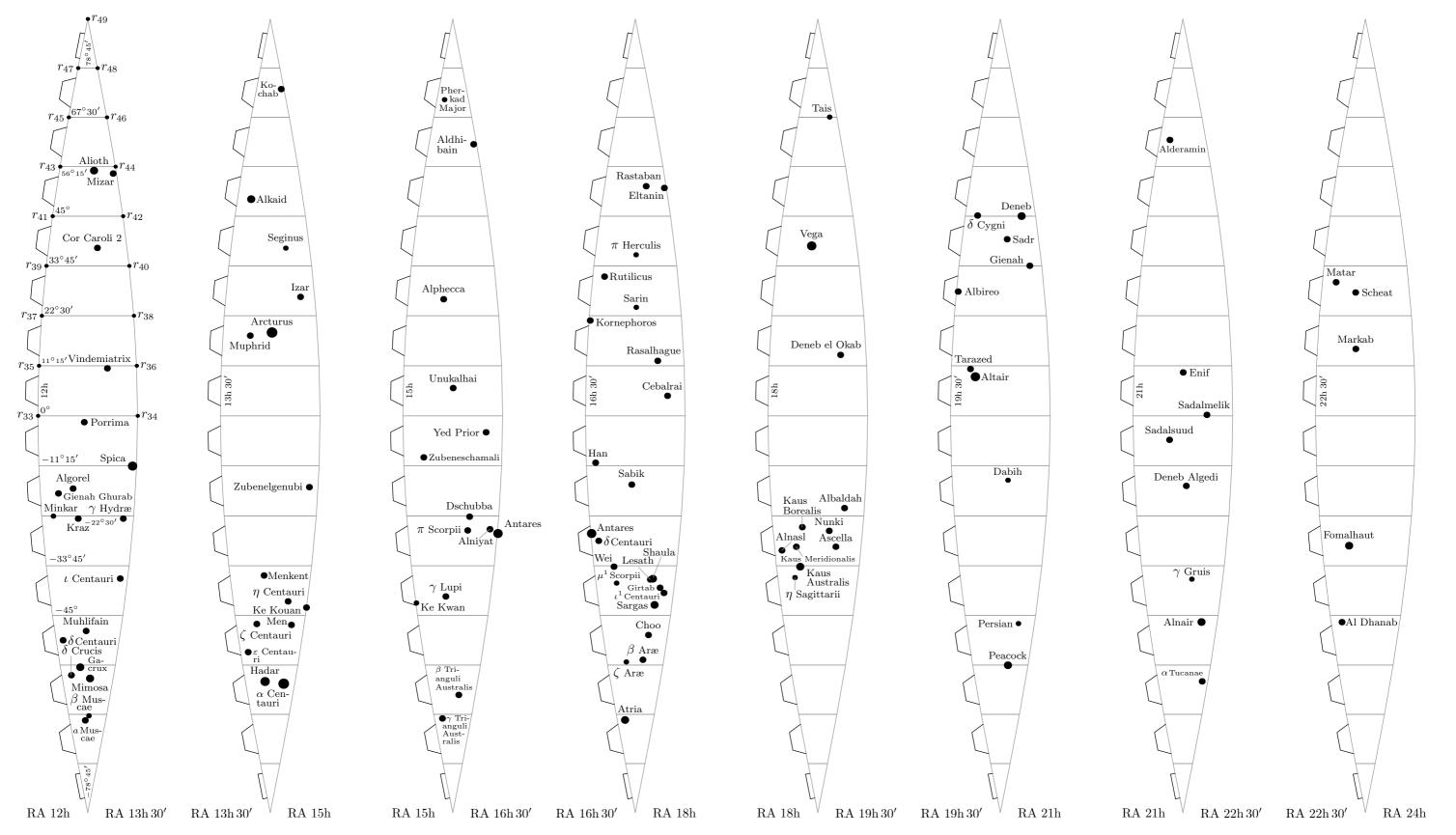


# Panels (Isoceles Trapezoids and Triangles)

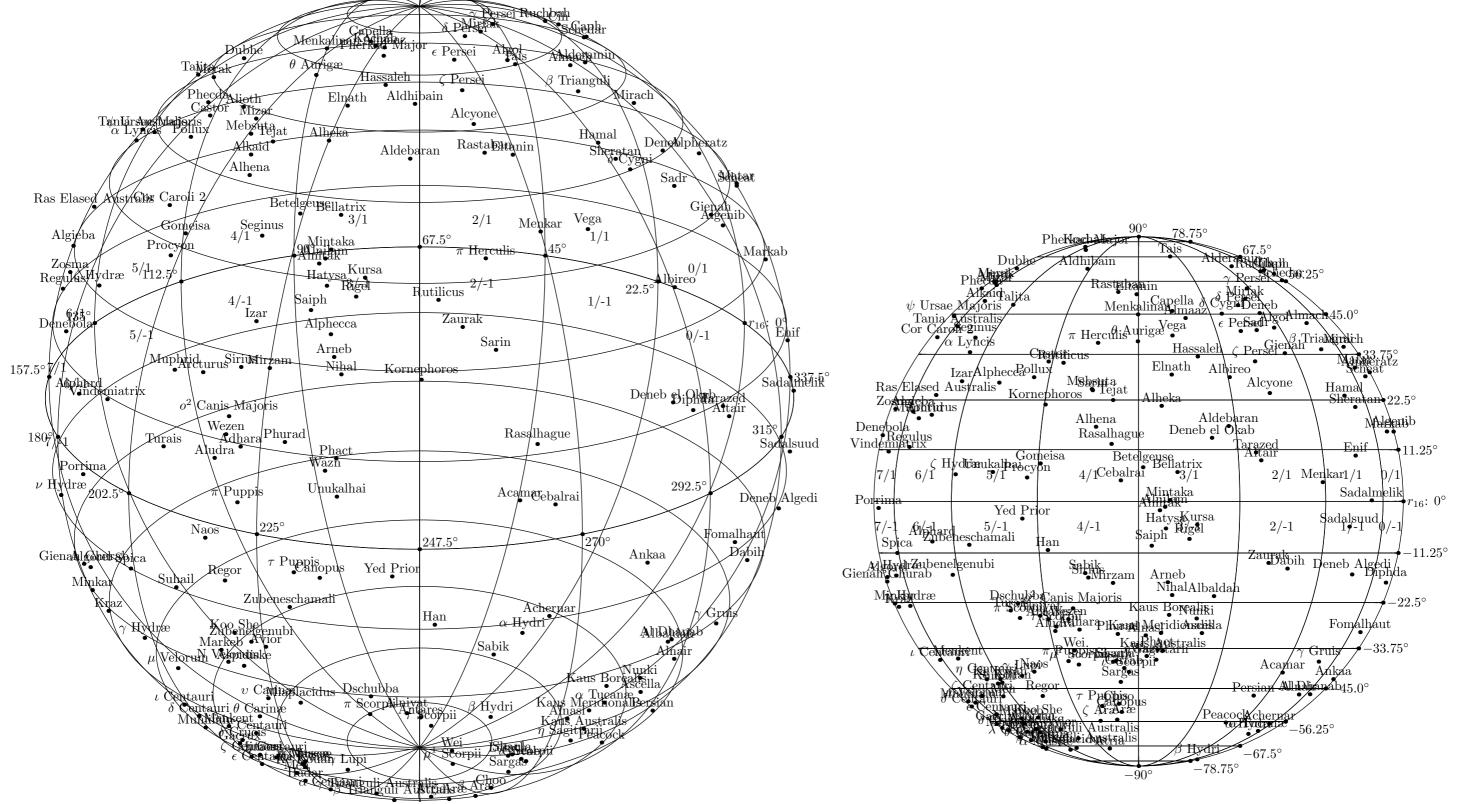






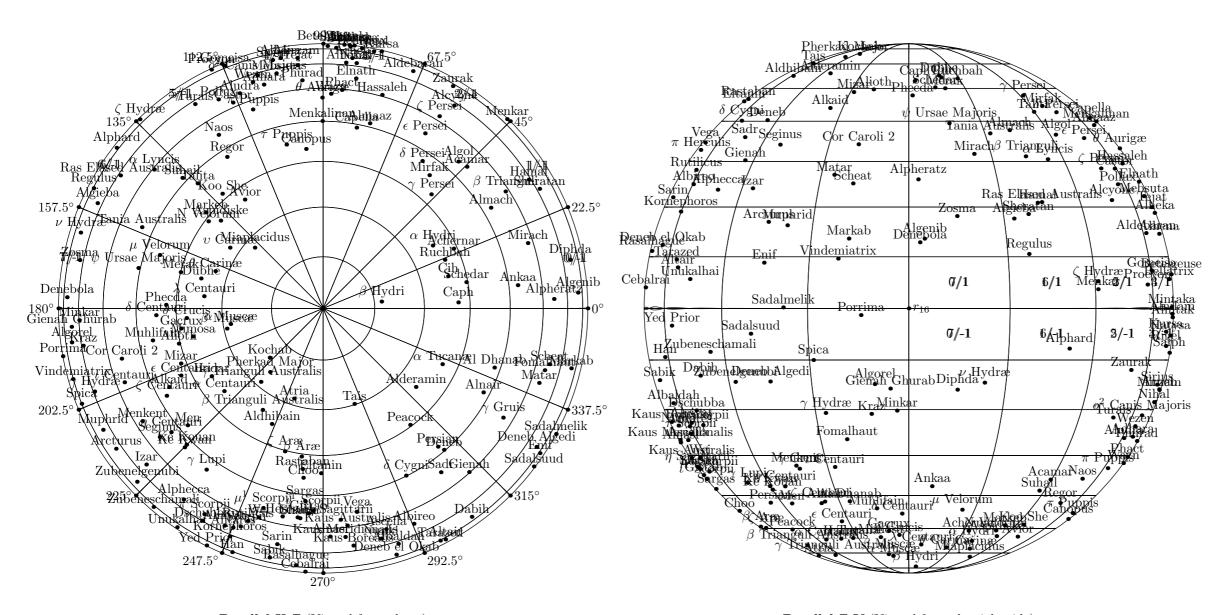


# Globes



Perspective Projection

Parallel X-Y (Viewed from the front)



Parallel X-Z (Viewed from above)

Parallel Z-Y (Viewed from the right side)

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