无限循环小数化为分数

将 0.3 转化为分数

解: 设
$$a = 0.3$$
, 则:

$$10a = 3.\dot{3} = 3 + 0.\dot{3} = 3 + a$$

$$9a = 3$$

$$\therefore a = \frac{3}{9} = \frac{1}{3}$$

无限循环小数化为分数

将 0.25 转化为分数

解: 设 a = 0.25, 则:

$$100a = 25.\dot{2}\dot{5} = 25 + a$$

$$99a = 25$$

$$\therefore a = \frac{25}{99}$$

无限循环小数化为分数

将 0.325 转化为分数

解: 设
$$a = 0.3\dot{2}\dot{5}$$
, 则:

$$10a = 3 + 0.\dot{2}\dot{5} = 3 + \frac{25}{99}$$

$$10a = \frac{3 \times 99 + 25}{99} = \frac{322}{99}$$

$$a: a = \frac{322}{990} = \frac{161}{495}$$