速算方法介绍

- 1. 和十速算法
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和十速算法

计算: $\overline{ab} \times \overline{ad}$

当个位数之和等于 10, 即: b+d=10 时, 可以使用《和十速算法》, 即:

设: e = a + 1, $a(a + 1) = \overline{AB}$, $bd = \overline{CD}$ 则:

$$\overline{ab} \times \overline{ad} = (10a + b)(10a + d) = 100a^2 + 10a(b + d) + bd = 100a(a + 1) + bd = \overline{ABCD}$$

例题:

1.
$$21 \times 29 = 100 \times 2 \times 3 + 1 \times 9 = 600 + 9 = 609$$

2.
$$32 \times 38 = 100 \times 3 \times 4 + 2 \times 8 = 1200 + 16 = 1216$$

3.
$$43 \times 47 = 100 \times 4 \times 5 + 3 \times 7 = 2000 + 21 = 2021$$

4.
$$45 \times 45 = 100 \times 4 \times 5 + 5 \times 5 = 2000 + 25 = 2025$$

5.
$$74 \times 76 = 100 \times 7 \times 8 + 4 \times 6 = 5600 + 24 = 5624$$

思考: 和十速算法速利用了乘法的什么规律? 数字有什么特点?

每人出 2 道类似的题目

和十速算法

1. 21×29

$$\therefore 2 \times 3 = 6, \quad 1 \times 9 = 9, \quad \therefore 21 \times 29 = \overline{06} \quad \overline{09} = 609$$

2. 32 × 38

$$\therefore 3 \times 4 = 12, \quad 2 \times 8 = 16, \quad \therefore 32 \times 38 = \overline{12} \quad \overline{16} = 1216$$

 $3.43 \times 47 =$

$$\therefore 4 \times 5 = 20, \quad 3 \times 7 = 21, \quad \therefore 43 \times 47 = \overline{20} \quad \overline{21} = 2021$$

4. 45 × 45

$$\therefore 4 \times 5 = 20, \quad 5 \times 5 = 25, \quad \therefore 45 \times 45 = \overline{20} \quad \overline{25} = 2025$$

5. 74×76

逢五凑十法

计算: $\overline{ab} \times \overline{cd}$

当 b=5, d 为偶数时,通常可以使用《逢五凑十法》,即:

对 \overline{cd} 先除以 2, 再乘以 2, 即: $\overline{cd} = \overline{ef} \times 2$, 则:

$$\overline{ab} \times \overline{cd} = \overline{ab} \times \overline{cd} \div 2 \times 2 = (\overline{ab} \times 2) \times \overline{ef}$$

例题:

- 1. $15 \times 18 = 15 \times 2 \times 9 = 30 \times 9 = 270$
- **2.** $25 \times 34 = 25 \times 2 \times 17 = 50 \times 17 = 850$
- **3.** $35 \times 16 = 35 \times 2 \times 8 = 70 \times 8 = 560$
- **4.** $75 \times 14 = 75 \times 2 \times 7 = 150 \times 7 = 1050$

思考: 逢五凑十法本质就是乘五等于乘十除二, 利用了乘法的什么规律?

总结逢五凑十法的数字特点,每人出 2 道类似的题目

计算下列各式的值:

1.
$$25 \times 48 = 25 \times 4 \times 12 = 100 \times 12 = 1200$$

2.
$$35 \times 28 = 35 \times 2 \times 14 = 70 \times 14 = 980$$

3.
$$45 \times 16 = 45 \times 2 \times 8 = 90 \times 8 = 720$$

4.
$$55 \times 18 = 55 \times 2 \times 9 = 110 \times 9 = 990$$

5.
$$25 \times 36 = 25 \times 4 \times 9 = 100 \times 9 = 900$$

6.
$$23 \times 44 = (25 - 2) \times 44 = 25 \times 44 - 2 \times 44 = 1100 - 88 = 1012$$

7.
$$22 \times 36 = 22 \times (35 + 1) = 22 \times 35 + 22 \times 1 = 770 + 22 = 792$$

8.
$$22 \times 37 = 22 \times (35 + 2) = 22 \times 35 + 22 \times 2 = 770 + 44 = 814$$

9.
$$24 \times 28 = (25 - 1) \times 28 = 25 \times 4 \times 7 - 28 = 700 - 28 = 672$$

平方差公式的证明

平方差公式是: $a^2 - b^2 = (a + b)(a - b)$, 如何证明呢?

思考: 如果从左向右证明一下找不到

思路,那么可以先从右边向左边验证:

证明:

$$(a + b)(a - b) = a(a - b) + b(a - b)$$

$$= a^{2} - ab + ba - b^{2}$$

$$= a^{2} - ab + ab - b^{2}$$

$$= a^{2} - b^{2}$$

有了上述的验证过程,从下往上写, 就找到构造公式,并予以证明。 证明:

$$a^{2} - b^{2} = a^{2} - ab + ab - b^{2}$$

$$= a^{2} - ab + ba - b^{2}$$

$$= a(a - b) + b(a - b)$$

$$= (a + b)(a - b)$$

平方差法

平方差公式: $a^2 - b^2 = (a+b)(a-b)$

或: $(a+b)(a-b) = a^2 - b^2$

或: $(a-b)(a+b) = a^2 - b^2$

或反向平方差: $a^2 = (a-b)(a+b) + b^2$

例题:

1.
$$28 \times 32 = (30 - 2)(30 + 2) = 30^2 - 2^2 = 900 - 4 = 896$$

2.
$$39 \times 41 = (40 - 1)(40 + 1) = 40^2 - 1^2 = 1600 - 1 = 1599$$

3.
$$45 \times 55 = (50 - 5)(50 + 5) = 50^2 - 5^2 = 2500 - 25 = 2475$$

4.
$$62 \times 78 = (70 - 8)(70 + 8) = 70^2 - 8^2 = 4900 - 64 = 4836$$

5.
$$63 \times 87 = (75 - 12)(75 + 12) = 75^2 - 12^2 = 5625 - 144 = 5481$$

6.
$$45 \times 45 = 45^2 - 5^2 + 5^2 = (45 + 5)(45 - 5) + 25 = 50 \times 40 + 25 = 2000 + 25 = 2025$$

总结利用平方差法的数字特点,每人出2道类似的题目

1.
$$15 \times 25 = (20 - 5)(20 + 5) = 20^2 - 5^2 = 400 - 25 = 375$$

2.
$$25 \times 35 = (30 - 5)(30 + 5) = 30^2 - 5^2 = 900 - 25 = 875$$

3.
$$24 \times 36 = (30 - 6)(30 + 6) = 30^2 - 6^2 = 900 - 36 = 864$$

4.
$$35 \times 45 = (40 - 5)(40 + 5) = 40^2 - 5^2 = 1600 - 25 = 1575$$

5.
$$15 \times 35 = (25 - 10)(25 + 10) = 25^2 - 10^2 = 625 - 100 = 525$$

6.
$$24 \times 46 = (35 - 11)(35 + 11) = 35^2 - 11^2 = 1225 - 121 = 1104$$

7.
$$75 \times 75 = 70 \times 80 + 5 \times 5 = 5600 + 25 = 5625$$

8.
$$85 \times 85 = 80 \times 90 + 5 \times 5 = 7200 + 25 = 7225$$

9.
$$95 \times 95 = 90 \times 100 + 5 \times 5 = 9000 + 25 = 9025$$

思考: 还有没有其它速算方法可以计算上述代数式?



大数凑十法

计算: $\overline{ab} \times \overline{cd}$

当尾数(或个位数) $b \ge 6$ 时,通常可以使用《大数凑十法》,即:

设: e = a + 1, f = 10 - b, 则:

$$\overline{ab} \times \overline{cd} = \overline{e0} \times \overline{cd} - \overline{f} \times \overline{cd}$$

例题:

- 1. $22 \times 37 = 22 \times (40 3) = 22 \times 40 22 \times 3 = 880 66 = 814$
- **2.** $22 \times 37 = 22 \times (35 + 2) = 22 \times 35 + 22 \times 2 = 770 + 44 = 814$
- 3. $32 \times 39 = 32 \times (40 1) = 32 \times 40 32 = 1280 32 = 1248$
- **4.** $52 \times 39 = 52 \times (40 1) = 52 \times 40 52 = 2080 52 = 2028$
- **5.** $48 \times 43 = (50 2) \times 43 = 50 \times 43 2 \times 43 = 2150 86 = 2064$
- **6.** $37 \times 37 = (40 3)(40 3) = 40^2 2 \times 40 \times 3 + 3^2 = 1600 240 + 9 = 1369$

思考:大数凑十法速利用了乘法的什么规律?数字有什么特点?

每人出 2 道类似的题目

计算下列各式的值:

1.
$$15 \times 49 = 15 \times (50 - 1) = 15 \times 50 - 15 = 750 - 15 = 735$$

2.
$$23 \times 29 = 23 \times (30 - 1) = 23 \times 30 - 23 = 690 - 23 = 667$$

3.
$$24 \times 28 = 24 \times (30 - 2) = 24 \times 30 - 24 \times 2 = 720 - 48 = 672$$

4.
$$32 \times 57 = 32 \times (60 - 3) = 32 \times 60 - 32 \times 3 = 1920 - 96 = 1824$$

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双向凑十法

计算: $\overline{a9} \times \overline{c9}$

当两个尾数都等于9时,通常可以使用《双向凑十法》,即:

设: e = a + 1, f = d + 1, 则:

$$\overline{a9} \times \overline{c9} = (\overline{e0} - 1) \times (\overline{f0} - 1) = \overline{e0} \times \overline{f0} - \overline{e0} - \overline{f0} + 1$$

例题:

1.
$$29 \times 39 = (30 - 1) \times (40 - 1) = 30 \times 40 - 30 - 40 + 1 = 1200 - 70 + 1 = 1131$$

2.
$$19 \times 59 = (20 - 1) \times (60 - 1) = 20 \times 60 - 20 - 60 + 1 = 1200 - 80 + 1 = 1121$$

3.
$$29 \times 69 = (30 - 1) \times (70 - 1) = 30 \times 70 - 30 - 70 + 1 = 2100 - 100 + 1 = 2001$$

思考: 双向凑十法速利用了乘法的什么规律?

每人出 2 道类似的题目

因数分解法

例题:

1.
$$15 \times 28 = 15 \times 4 \times 7 = 60 \times 7 = 420$$

2.
$$25 \times 36 = 25 \times 4 \times 9 = 100 \times 9 = 900$$

3.
$$33 \times 12 = 3 \times 11 \times 12 = 3 \times 121 = 363$$

4.
$$74 \times 27 = 2 \times 37 \times 27 = 2 \times 999 = 1998$$

5.
$$91 \times 22 = 91 \times 11 \times 2 = 1001 \times 2 = 2002$$

总结利用因数分解法的数字特点,每人出2道类似的题目

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1. $125 \times 72 = 125 \times 8 \times 9 = 1000 \times 9 = 9000$

2. $14 \times 28 = 7 \times 2 \times 7 \times 4 = 49 \times 8 = 400 - 8 = 392$

思考: 逢五凑十法是不是因数分解法的特例?

二项式速算法

$$(a+b)(a+c) = a^2 + a(b+c) + bc$$

1.
$$26 \times 26 = (25+1)(25+1) = 25^2 + 2 \times 25 + 1^2 = 625 + 50 + 1 = 676$$

2.
$$27 \times 27 = (25 + 2)(25 + 2) = 25^2 + 2 \times 25 \times 2 + 2^2 = 625 + 100 + 4 = 729$$

3.
$$36 \times 36 = (35+1)(35+1) = 35^2 + 2 \times 35 + 1^2 = 1225 + 70 + 1 = 1296$$

4.
$$37 \times 37 = (35 + 2)(35 + 2) = 35^2 + 2 \times 35 \times 2 + 2^2 = 1225 + 140 + 4 = 1369$$

5.
$$37 \times 38 = (40 - 3)(40 - 2) = 40^2 - 40 \times (3 + 2) + 3 \times 2 = 1600 - 200 + 6 = 1406$$

6.
$$27 \times 38 = (30 - 3)(40 - 2) = 30 \times 40 - 2 \times 30 - 3 \times 40 + 3^2 = 1200 - 180 + 6 = 1026$$

7.
$$27 \times 48 = (30-3)(50-2) = 30 \times 50 - 30 \times 2 - 3 \times 50 + 3 \times 2 = 1500 - 60 - 150 + 6 = 1296$$

总结利用二项式速算法的数字特点,每人出2道类似的题目

速算习题

1.
$$19 \times 24 = (20 - 1) \times 24 = 480 - 24 = 456$$

2.
$$16 \times 39 = 16 \times (40 - 1) = 640 - 16 = 624$$

3.
$$17 \times 47 = 17 \times (50 - 3) = 850 - 51 = 799$$

4.
$$24 \times 25 = 6 \times 4 \times 25 = 6 \times 100 = 600$$

5.
$$27 \times 23 = 20 \times 30 + 7 \times 3 = 600 + 21 = 621$$

6.
$$26 \times 29 = 26 \times (30 - 1) = 780 - 26 = 754$$

7.
$$37 \times 43 = (40 - 3)(40 + 3) = 1600 - 9 = 1591$$

8.
$$36 \times 44 = (40 - 4)(40 + 4) = 1600 - 16 = 1584$$

9.
$$42 \times 25 = 21 \times 2 \times 25 = 21 \times 50 = 1050$$

速算习题

1.
$$36 \times 24 = (30 + 6) \times (30 - 6) = 30^2 - 6^2 = 900 - 36 = 864$$

2.
$$36 \times 24 = 36 \times (25 - 1) = 9 \times 4 \times 25 - 36 = 900 - 36 = 864$$

3.
$$26 \times 48 = 26 \times (50 - 2) = 26 \times 50 - 52 = 1300 - 52 = 1248$$

4.
$$26 \times 22 = (25 + 1) \times 22 = 25 \times 22 + 22 = 550 + 22 = 572$$

5.
$$43 \times 27 = (23 + 20) \times 27 = 23 \times 27 + 20 \times 27 = 621 + 540 = 1161$$

6.
$$33 \times 28 = 33 \times (30 - 2) = 33 \times 30 - 33 \times 2 = 990 - 66 = 924$$

7.
$$48 \times 28 = (50 - 2) \times 28 = 50 \times 28 - 2 \times 28 = 1400 - 56 = 1344$$

8.
$$44 \times 14 = (45 - 1) \times 14 = 45 \times 2 \times 7 - 14 = 90 \times 7 - 14 = 630 - 14 = 616$$

9.
$$48 \times 45 = 48 \times (50 - 5) = 2400 - 240 = 2160$$

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速算习题

1.
$$38 \times 19 = 38 \times (20 - 1) = 38 \times 20 - 38 = 760 - 38 = 722$$

2.
$$46 \times 27 = 46 \times (25 + 2) = 46 \times 25 + 46 \times 2 = 1150 + 92 = 1242$$

3.
$$44 \times 23 = 44 \times (25 - 2) = 44 \times 25 - 44 \times 2 = 1100 - 88 = 1012$$

4.
$$44 \times 39 = 44 \times (40 - 1) = 44 \times 40 - 44 = 1760 - 44 = 1716$$

5.
$$36 \times 48 = 36 \times (50 - 2) = 36 \times 50 - 72 = 1800 - 72 = 1728$$

6.
$$47 \times 48 = (50 - 3) \times 48 = 50 \times 48 - 3 \times 48 = 2400 - 144 = 2256$$

7.
$$47 \times 48 = (50 - 3)(50 - 2) = 2500 - 50(3 + 2) + 6 = 2500 - 250 + 6 = 2256$$

8.
$$47 \times 48 = (42 + 5) \times 48 = 42 \times 48 + 5 \times 48 = 2016 + 240 = 2256$$

9.
$$37 \times 48 = 37 \times (50 - 2) = 37 \times 50 - 74 = 1850 - 74 = 1776$$

10.
$$37 \times 48 = (40 - 3)(50 - 2) = 2000 - 80 - 150 + 6 = 2000 - 200 - 30 + 6 = 1800 - 30 + 6 = 1776$$

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