

# THE INFLUENCE OF A BLUFF BODY IN A TURBULENT FLOW ON THE MIXING OF FLUIDS

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## ABSTRACT

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**Keywords:** CFD, Turbulence, Bluff body .

A complete list of symbols used, with dimensions, is required.

## NOMENCLATURE

### Greek Symbols

$\rho$  Mass density, [ $kg/m^3$ ]  
 $\mu$  Dynamic viscosity, [ $kg/ms$ ]

### Latin Symbols

$a$  PressureCharacteristic length, [ $m$ ].  
 $N$  Total amount,  $[-]$ .  
 $p$  Pressure, [ $Pa$ ].  
 $\mathbf{u}$  VolumeVelocity, [ $m/s$ ].

### Sub/superscripts

$G$  Gas.  
 $i$  Index  $i$ .  
 $j$  Index  $j$ .

## INTRODUCTION

Within industrial applications, mixing of fluids is a well known phenomenon. The mixing of fluids can be initiated by a propeller, driven by a motor, or by obstacles in a flow, as well as a difference in concentration. A simple example of mixing due to concentration difference is the mixing of two paint colours. Starting with half a tank of blue paint and the other half yellow paint, will result in a completely green paint.

This study focusses on the quality of mixing. Mainly the influence of the bluff-body size and its influence on the mixing quality will be discussed, as well as the influence of the turbulent intensity at the inlet. The mixing quality can be measured at the outlet of the geometry by looking at the value of the mixture fraction.

Computational Fluid Dynamics (CFD) is used to solve the system of equations. For this particular problem, the mass, momentum and transport equations are solved. The simulations are performed for fully developed turbulent and incompressible flows. The turbulence is modelled by means

of a  $\kappa - \epsilon$  model.

The expectation is that in a turbulent flow better mixing will be achieved without a bluff body. Prospected is that the bluff body will cause a decrease in turbulence and therefore contribute negative to the mixing.

The first part of this article is concerns the theory and the numerical solver used to attain the solution. Then the CFD model is treated, after which the geometry and boundary conditions applied to the problem are discussed. Subsequently the mesh convergence and executed simulations are explained. Finally, the results of the simulations are displayed with a discussion and conclusion.

## PHYSICS

This chapter covers the theory of the CFD model. Once the theory is explained, the discretization of the governing equations is treated. Additional to that the used solver is explained.

### Turbulent flow

A flow in a channel can be characterized by the Reynolds number, a dimensionless number which represents the ratio of viscous and inertial forces in the flow. The Reynolds number can be calculated upon use of Equation 1 (Versteeg and Malalasekera, 2007). Here  $\rho$  is the fluid density in  $[kg \cdot m^{-3}]$ ,  $u$  is the velocity in  $[m \cdot s^{-1}]$ ,  $D$  is the characteristic length in  $[m]$  and  $\mu$  is the fluids dynamic viscosity in  $[kg \cdot m^{-1} \cdot s^{-1}]$

$$Re = \frac{\rho u D}{\mu} \quad (1)$$

The flow is considered turbulent if the Reynolds number exceeds a value of 2300. A turbulent flow is contemplated as chaotic, containing flow instabilities such as eddies. These eddies cause local fluctuations in the velocity field. Therefore, the normal steady convection and diffusion equations can not be used to solve turbulent flows. To solve the turbulent flow equations one needs to introduce a general equation for unsteady convection and diffusion (Versteeg and Malalasekera, 2007).

#### Unsteady convection-diffusion

$$\frac{\partial \rho \phi}{\partial t} + \text{div}(\rho \phi \mathbf{u}) = \text{div}(\Gamma \text{grad} \phi) + S_\phi \quad (2)$$

Equation 2 consists of four parts. The first part is a time dependent term, the second part represents the convection, the third part the diffusion and the last part of the equation is the sink and or source term.  $\phi$  is the transport term,  $\Gamma$  is the diffusion or conduction coefficient. The transport term changes according to the equation to be solved.

The conservation of mass, momentum and fraction play a major role in a CFD code. All conservation equations are derived for the case of an incompressible flow. The conservation of mass can be extracted from Equation 2, and results in (Deen, 2017):

#### Mass balance

$$\frac{\partial \rho}{\partial t} + \text{div}(\rho \mathbf{u}) = 0 \quad (3)$$

For a two dimensional problem, the conservation of momentum needs to be solved in two directions,  $x$  and  $y$ . The general form for the momentum conservation is treated as:

#### Momentum balance

$$\begin{aligned} \frac{D(\rho u)}{Dt} &= -\frac{\partial P}{\partial x} + \text{div}(\mu \text{grad} u) + S_{Mx} \\ \frac{D(\rho v)}{Dt} &= -\frac{\partial P}{\partial y} + \text{div}(\mu \text{grad} v) + S_{My} \end{aligned} \quad (4)$$

The last important equation is the transport of fractions, and can be computed upon use of Equation 5.

#### Species fraction transport

$$\frac{\partial f \rho}{\partial t} + \text{div}(\rho u f) = \text{div}(D \text{grad} f) + S_i \quad (5)$$

Here  $D$ , is the diffusion coefficient of the fluid. The fraction transport is introduced specifically for this study in order to

keep track of the mixing of the flow. This variable can have any value between 0 and 1. Considering only 2 species, a value of 1 means that the fluid is purely specie 1 and a value of 0 is purely the other specie.

Since this study regards a turbulent flow, the mass and momentum equations have to be solved in a different manner. This is done by means of the Reynolds average approach. In the Reynolds average approach the mean velocity is determined and the turbulence is described by a fluctuation around the mean velocity. Therefore, components in the convection-diffusion and conservation equations are decomposed in a mean and a fluctuating variable. The decomposed variables are given in Equation 6.

#### Decomposed variables

$$u = U + u'; \quad v = V + v'; \quad w = W + w'; \quad p = P + p' \quad (6)$$

In here,  $U$ ,  $V$  and  $W$  are the mean velocities in  $x$ ,  $y$  and  $z$  direction respectively.  $P$  is the average pressure. The apostrophe terms are the fluctuating components. The average term is given by Equation 7.

#### Average velocity

$$U = \frac{1}{\Delta t} \int_0^{\Delta t} u(t) dt \quad (7)$$

The other average terms are calculated in the same manner. After computing the decomposed variables, they are substituted into the system of equations. The time averaged part in Equation 7 transforms the regular Navier-Stokes equations into time averaged Navier-Stokes equations, also called Reynolds averaged Navier-Stokes equations (RANS). By using RANS, a new definition is introduced called Reynolds stresses. The Reynolds stresses are present in all directions, and are calculated by Equation 8 (Deen, 2017).

#### Reynolds stresses

$$\tau_{ij} = -\rho \overline{u'_i u'_j} \quad (8)$$

The  $\kappa - \epsilon$  model is used to close the system of equations. This model is chosen above the Prandtl mixing length model and the Reynolds stress model and algebraic stress model due to its simple implementation and widely proven validation (Versteeg and Malalasekera, 2007).

#### $\kappa - \epsilon$ turbulence model

The standard  $\kappa - \epsilon$  model introduces two extra transport equations to be solved. one for the turbulent kinetic energy,  $\kappa$ , and one for the viscous dissipation of turbulent kinetic energy,  $\epsilon$ .  $\kappa$  and  $\epsilon$  are used to introduce a velocity scale,  $\theta$  and large-scale turbulence length scale  $\ell$ . The velocity scale is calculated upon use of Equation 9, and the turbulence length-scale is calculated with use of Equation 10.

#### Velocity- and turbulence length-scale

$$\theta = \kappa^{1/2} \quad (9)$$

$$\ell = \frac{\kappa^{3/2}}{\epsilon} \quad (10)$$

Equation 10 shows that one is able to use the small eddy variable  $\epsilon$  to describe the large eddy scale,  $\ell$ . This is only permitted if, and only if, the rate at which large eddies extract energy from the mean flow matches the rate of transfer of energy across the energy spectrum to small, dissipating,

eddies if the flow does not change rapidly. (Versteeg and Malalasekera, 2007).

The turbulent viscosity, the eddy viscosity is introduced by Equation 11, where  $C_\mu$  is a dimensionless constant.

*Turbulent viscosity*

$$\mu_t = C_\mu \rho \theta \ell = C_\mu \rho \frac{\kappa^2}{\epsilon} \quad (11)$$

One is now able to describe the equations for both  $\kappa$  and  $\epsilon$ , shown in Equation 12 and 13 respectively.

*$\kappa$ - and  $\epsilon$ -transport equation*

$$\frac{\partial \rho \kappa}{\partial t} + \text{div}(\rho \kappa \mathbf{U}) = \text{div} \left[ \frac{\mu_t}{\sigma_\kappa} \text{grad } \kappa \right] + 2\mu_t S_{ij} \cdot S_{ij} - \rho \epsilon \quad (12)$$

$$\begin{aligned} \frac{\partial \rho \epsilon}{\partial t} + \text{div}(\rho \epsilon \mathbf{U}) = & \text{div} \left[ \frac{\mu_t}{\sigma_\epsilon} \text{grad } \epsilon \right] + \\ & C_{1\epsilon} \frac{\epsilon}{\kappa} 2\mu_t S_{ij} \cdot S_{ij} - \rho C_{2\epsilon} \frac{\epsilon^2}{\kappa} \end{aligned} \quad (13)$$

In both equations, the first term represents the rate of change in  $\kappa$  and  $\epsilon$  respectively. Within the first term  $\mathbf{U}$  is the average velocity magnitude. The second and third term represent the transport driven by convection and diffusion for  $\kappa$  and  $\epsilon$ . The fourth and fifth term are the rate of production and rate of destruction of  $\kappa$  and  $\epsilon$ .

The equations use five dimensionless constants, the standard  $\kappa - \epsilon$  model uses values that have been determined through comprehensive data fitting for a wide range of turbulent flows (Versteeg and Malalasekera, 2007):

*Dimensionless constants:*

$$C_\mu = 0.09 \quad \sigma_\kappa = 1.00 \quad \sigma_\epsilon = 1.30 \quad C_{1\epsilon} = 1.44 \quad C_{2\epsilon} = 1.92$$

*discretization of governing equations*

To solve the turbulence model, all of the partial differential equations (PDE's) need to be solved. Solving a PDE takes a few steps. First of all let us consider a two dimensional grid consisting of several grid cells. To find the value for  $\phi$  from Equation 2 at a centre point P of the grid cell, one needs the values of the neighbouring cells. In CFD these values are called north(N), west(W), south(S) and east(E). Thereafter, Equation 2 is integrated over the control volume, yielding the results shown in Equation 14.

*Intergrated diffusion convection equation*

$$\begin{aligned} \frac{(\rho_p^0) \phi}{\Delta t} \Delta V + [(\rho u A \phi)_e - (\rho u A \phi)_w] + [(\rho u A \phi)_n - \\ (\rho u A \phi)_s] = & \left[ \left( \Gamma A \frac{\partial \phi}{\partial x} \right)_e - \left( \Gamma A \frac{\partial \phi}{\partial x} \right)_w \right] + \\ & \left[ \left( \Gamma A \frac{\partial \phi}{\partial x} \right)_n - \left( \Gamma A \frac{\partial \phi}{\partial x} \right)_s \right] + S_u + S_p \phi_p^0 \end{aligned} \quad (14)$$

Now let us introduce variables  $F$  and  $D$  to represent the convective mass flux per unit area and the diffusive conductance at the cell faces (Versteeg and Malalasekera, 2007).

$$F = \rho u \quad (15)$$

$$D = \frac{\Gamma}{\partial x} \quad (16)$$

Substitution variables  $F$  and  $D$  into Equation 14 forms Equation 17 after some rearranging (Versteeg and Malalasekera, 2007).

$$\frac{\rho_p^0 \Delta V}{\Delta t} \phi_P = a_W \phi_W + a_E \phi_E + a_S \phi_S + a_N \phi_N + \Delta F \quad (17)$$

The coefficients of  $a$  are dependent on the differencing scheme. The discretization scheme has some properties. First property is the conservativeness which means the flux  $\phi$  leaving a control volume has to be equal to the flux  $\phi$  entering the control volume through the same face. By using a hybrid differencing scheme, the conservativeness is automatically satisfied. The second property is the boundedness. The boundedness describes the value of  $\phi$  in case there is no source term. In that case, the nodal value of  $\phi$  must be equal to the value of  $\phi$  at the boundary. Besides the restricted value of  $\phi$ , the coefficients  $a$  of the discretized equation must have equal signs. The last important property is the transportiveness. This requires that the transportiveness changes according to the magnitude of the Péclet number ( $Pe = F/D$ ). Hence, if  $Pe$  is zero,  $\phi$  equally diffuses in all directions. The hybrid differencing scheme satisfies the three properties. However, this comes at the price of only first order accuracy (Versteeg and Malalasekera, 2007). The obtained values for  $F$  and  $D$  determine the values of the  $a$  coefficients. They can be determined as shown in Table 1.

**Table 1:**  $a$  coefficients.

	Two-Dimensional Flow
$a_W$	$\max \left[ F_w, \left( D_w + \frac{F_w}{2}, 0 \right) \right]$
$a_E$	$\max \left[ -F_e, \left( D_e + \frac{F_e}{2}, 0 \right) \right]$
$a_N$	$\max \left[ -F_n, \left( D_n + \frac{F_n}{2}, 0 \right) \right]$
$a_S$	$\max \left[ F_s, \left( D_s + \frac{F_s}{2}, 0 \right) \right]$
$\Delta F$	$F_e - F_w + F_n - F_s$

The discretized equation can now be solved using the transient SIMPLE algorithm. SIMPLE stands for Semi-Implicit Method for Pressure-Linked Equations. In essential the algorithm is a guess and correct procedure for pressure calculations in a staggered grid which is used (Versteeg and Malalasekera, 2007). The transient SIMPLE algorithm is used due to the unsteady convection-diffusion equations used to describe the problem. The difference with the regular SIMPLE algorithm is the time  $t$ , discretized in time steps,  $\Delta t$  for which the equations are solved. The transient SIMPLE algorithm works in the following manner. First the variables  $u$ ,  $v$ ,  $p$  and  $\phi$  are initialized and a time step  $\Delta t$  is defined. The time iteration starts at  $t_0$  and continues until  $t > t_{max}$ .

## CFD PROBLEM

This chapter will describe the entire CFD model used during simulations. First of all the geometry will be introduces, after which the applied boundary conditions are explained.

### Geometry and Cases

Figure 1 shows the geometry used during the research. The rectangular domain with dimensions length,  $L$  and width  $D$ , contains a bluff-body with height and width  $h$  and  $b$  respectively.

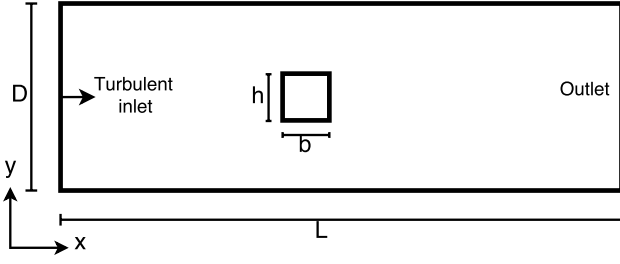


Figure 1: Schematic diagram of geometry.

For this research numerous cases are investigated. Since the main purpose is to find the influence of a bluff body on the mixing in a turbulent flow. The geometry of the bluff-body is varied from. The size of the bluff body is defined as  $h/D$ . The size is varied in three steps. These results are compared to a flow without a bluff-body.

Besides varying the bluff-body size, the entrance turbulence intensity  $T_i$  and the inlet velocity  $U_{in}$  are varied. Throughout the simulations the viscosity, turbulence entrance intensity and length scale and the density are not altered. The diffusion coefficient for species transport is chosen to be  $D = 10^{-5}$ , corresponding to diffusion coefficients in gasses. Diffusion coefficients for liquids are typically four orders lower. Therefore, liquids would need a longer domain for reaching the same quality of mixing as gases hence a more computational expensive simulation.

### Boundary conditions

Boundary conditions are prescribed to this CFD problem. Since this study focusses on turbulent flows only, the applied boundary conditions are solely turbulent as well. First of all A fully developed turbulent profile enters the geometry at the left side. This boundary condition is applied to reduce computational time. Without the fully developed inlet profile, the flow needs some time to adapt to a fully developed profile, which demands computational power. The inlet boundary condition can be applied with help of Equation 18, called the power law velocity profile.

### Power law velocity profile

$$u(y) = \begin{cases} U_{IN} \cdot \left[ \frac{y}{D/2} \right]^{1/n}, & \text{if } y \leq \frac{D}{2} \\ U_{IN} \cdot \left[ 2 - \frac{y}{D/2} \right]^{1/n}, & \text{if } y > \frac{D}{2} \end{cases} \quad (18)$$

The equation is constructed of a lower and upper half since the geometry has its origin in the lower left corner. In the equation  $D$  is defined as the maximum height in the channel,  $U_{IN}$  is the maximum inlet velocity. The height of the profile can be altered by a change in  $U_{IN}$ . The power  $n$  is chosen to be 7, which is a value suited for a wide range of turbulent flows (Morrison, 2003). Figure 2 shows the analytical inlet, as presented in Equation 18, the inlet profile as extracted from the simulation and the profile at the exit of the geometry as extracted from the simulation.

One can clearly see the agreement of the analytical expression for the inlet profile with the numerical result at the inlet.

The outlet however, shows a slight deviation from the inlet condition. This is due to the fact that the analytical expression is an approximation of the turbulent profile.

The second prescribed condition is the kinetic energy and dissipation rate at the inlet of the geometry. The inlet values can be calculated upon use of Equation 19.

$$\kappa_{IN} = \frac{2}{3}(U_{IN}T_i)^2, \quad \epsilon_{IN} = C_\mu^0.25 \frac{\kappa_{IN}^{1/3}}{0.035D} \quad (19)$$

In these equations  $T_i$  is the turbulent intensity, set to a value of 4%. The value for  $T_i$  for the inlet boundary is in general taken between 1% and 6% (Versteeg and Malalasekera, 2007).

Since the focus of this problem is about the mixing quality of a turbulent flow, an important initial condition is the fractions inside the geometry. Initially the entire bottom half of the domain has a fraction  $f = 1$  and the top half  $f = 0$ . If the fluid were to be perfectly mixed at the exit, the exit fraction would be  $f = 0.5$ . Therefore, the fraction is a direct measure for the mixing quality.

At both top and bottom walls of the geometry the axial velocity is set to  $u = 0 [m \cdot s^{-1}]$ . Since the flow is turbulent not only the value at the boundary itself should be restricted, but also the so called near wall region. These regions need wall functions to describe the flow near the walls. Closest to the walls there is a viscous sub-layer. Within this layer the eddies decrease in size and dissipate their energy due to viscous forces dominating in this area. When one looks more towards the centre of the geometry a log-law layer appears. In order to implement such conditions one needs to introduce  $y^+$  and  $u^+$ , as seen in Equation 20 (Versteeg and Malalasekera, 2007).

$$y^+ = \frac{\rho u_\tau y}{\mu}, \quad u^+ = \frac{U}{u_\tau} \quad (20)$$

In this equation,  $u_\tau$  represents the friction velocity and  $U$  is the average mean flow velocity. The friction velocity is calculated with Equation 21

$$u_\tau = \left( \frac{\tau_w}{\rho} \right)^{1/2} \quad (21)$$

$\tau_w$  is the shear stress in the boundary layer in [Pa]. In the viscous sub-layer, which is defined in the layer where  $y^+ \leq 11.63$ , the value of  $u^+$  is equal to the value of  $y^+$ . The shear stress in this region can be evaluated by Equation 22

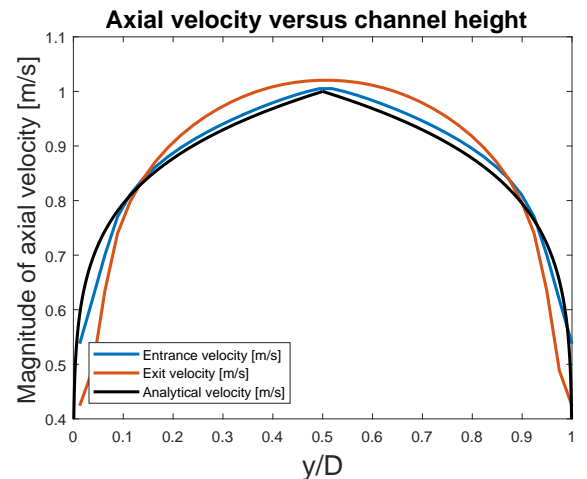


Figure 2: Schematic diagram of geometry.

$$\tau_w = \mu \frac{\partial u}{\partial y} \quad (22)$$

If the value of the dimensionless height  $y^+$  grows beyond 11.63 one enters the log-law regime. Within this layer  $u^+$  is calculated with Equation 23, where the values for  $\kappa$  and  $E$  are 0.4187 and 9.793 respectively.

$$u^+ = \frac{1}{\kappa} \ln(Ey^+) \quad (23)$$

The shear stress in the log-law area, used to calculate  $y^+$ , is determined upon us of Equation 24

$$\tau_w = \frac{\rho C_\mu^{0.25} \kappa^{1/2} \partial u}{u^+} \quad (24)$$

At the exit of the geometry the gradient of velocity and temperature in both  $u$  and  $y$  directions set to zero. This is done in order to comply with the mass balance equation since otherwise mass may disappear through the exit.

The velocity boundary conditions at the walls of the bluff body are treated in the same manner as explained in the previous section. Additional to that, the velocities inside the bluff body are set to zero values by prescribing  $S_p = -10^{30}$ . Additionally, at each of the faces of the bluff body, the  $a$  coefficient is set to zero.

## RESULTS

This section will cover the results obtained for the simulated cases. Besides the visualization of the simulations, the results will be analysed and discussed. Once all results are treated, a conclusion and discussion will follow. But first of all a grid convergence is performed to choose the right grid.

### Grid convergence

Choosing a simulation grid is a trade of between simulation quality and simulation speed. Therefore, choosing the right grid is of great importance for the result of the simulation. To detect the grid convergence the maximum analytical inlet velocity is compared to the numerical maximum inlet velocity. This shows how well the analytical formula is discretized and thus is able to describe the equation in a decent manner. To show the quality of discretisation the error is computed. The error is the absolute difference between the maximum analytical inlet velocity and the numerical maximum inlet velocity. The grid is refined from NPI=10 and NPJ=20, to NPI = 160 and NPJ = 320 in steps of a factor 2. For every grid the error is determined and plotted versus the refinement number.

Figure 3 shows the refinement number on the horizontal axis, with 1 corresponding to the coarsest grid (NPI=10 and NPJ=20) and 5 to the finest grid. It can be seen from the graph that for all of the grids, the error is very small. The figure shows a clear converging result towards the more refined grids. This shows that the fifth refinement comes the closest to the analytical expression. However, the grids corresponding to refinement 4 and 5 were computationally too expensive. Therefore, refinement 3, corresponding to a grid of NPI=40 and NPJ=80 is chosen.

Important to note is that the total simulation time for all results is set to 1.0s, using a time step of  $\Delta t = 1.0 \cdot 10^{-2}$ . This value satisfies the time step condition which is determined with  $\Delta t = (\rho(\Delta x)^2)/(\Gamma_i)$ , with  $\Delta x$  the grid spacing and  $\Gamma_i$  the transport value for equation  $i$

### Simulation results

Now, after all the cases are simulated on the previously chosen grid. The results will be discussed in this section. First the influence of the velocity and turbulence entrance intensity will be discussed. Thereafter, the results with bluff-body are discussed, looking at the influence of bluff-body size on the mixing.

The quality of mixing is evaluated at the exit of the domain. A mixture fraction of 1 enters at the bottom half, and a fraction of 0 at the top half. Figure 4 shows an example of the mixture fraction inside the simulation domain without bluff-body. Figure 5 shows the mixture fraction in the domain with a bluff-body. The figures show the separated inlet of both fractions. The mixture at the outlet of the domain, shows that the turbulence and diffusion have mixed the two fractions. For a measure of the quality of mixing, the value of the mixture fraction along the  $y$ -axis is visualized in a graph at the outlet of the domain. The best possible mixing at the outlet would be a uniform mixture fraction value of 0.5, representing fully mixed.

First of all the influence of the entrance velocity is visualized. Then the influence of the turbulence entrance intensity is discussed, after which the bluff-body results are shown in the same sequence.

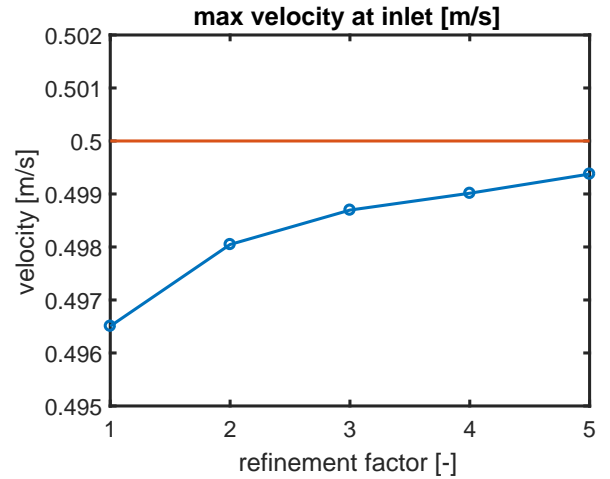


Figure 3: Grid convergence

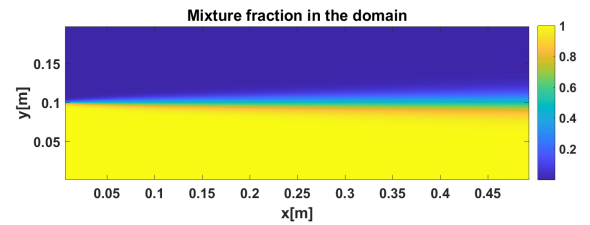


Figure 4: mixture fraction

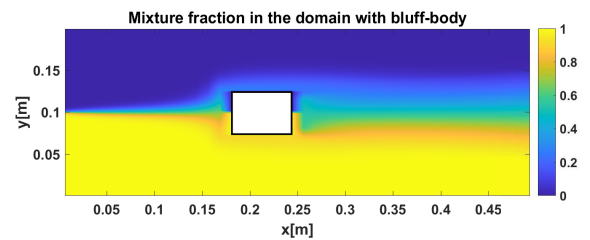


Figure 5: mixture fraction with bluff-body

### Results without bluff-body

First of all the results without the bluff-body. As explained The inlet velocity is treated first, for a constant turbulent entrance intensity. Figure 6 shows the mixture fraction at the outlet of the geometry as a function of height. The graph corresponds to a turbulence inlet intensity of 1%. The three differently coloured lines represent the three different inlet velocities of 0.5, 1 and 5 [m/s]. As one increases the velocity further, the mixing quality will decrease too much since the residence time of a fluid element inside the domain is too short. From the figure one can conclude that the lowest velocity yields the highest mixing quality. This is because for the lowest velocity the mixture fraction over the outlet is closest to perfectly mixed. The higher the inlet velocity, the lower the quality of mixing. This result can be easily explained by the Péclet number ( $Pe$ ). The  $Pe$  number is calculated by  $Pe = (U_{in}L)/(D)$ , where  $L$  is the length of the domain and  $D$  the diffusion coefficient. The  $Pe$  number represents the ratio of advection of an element by the flow to the rate of diffusion. Thus, when keeping the diffusion coefficient constant, increasing the inlet velocity will increase the  $Pe$  number. A higher  $Pe$  number yields that the flow dominates the diffusion and will decrease the quality of mixing.

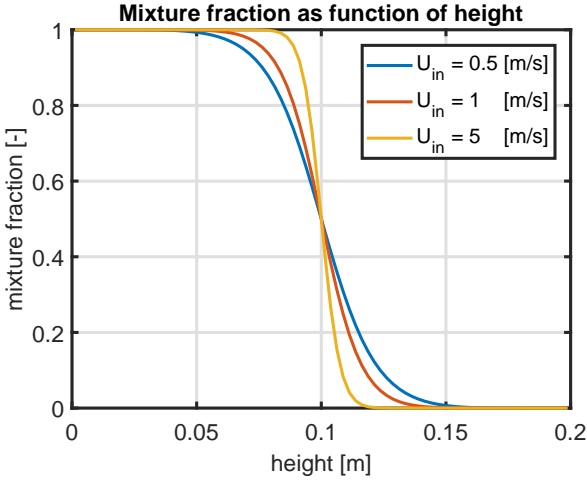


Figure 6: mixture fraction at constant turbulent intensity of 1 %

When looking at the influence of the turbulence inlet intensity, the velocity at the inlet is taken as a constant value. Then the turbulence entrance intensity is varied from 1% to 3% and 6%. Figures 7 and 8 show the results of the turbulent entrance intensity for constant inlet velocity.

The results in both figures look very similar. At an inlet velocity of 0.5[m/s] the best mixing seems to be achieved at a turbulence entrance intensity of 1%. However at an inlet velocity of 1[m/s] the best mixing is achieved at 6% and 1% turbulence entrance intensity. In general, the turbulence entrance intensity seems to have a negligible effect on the mixing quality of the two fractions.

The reason that the entrance turbulence has little to none effect on the mixing is due to the fact that the entrance turbulence is only applied at the inlet. And therefore influencing  $\kappa$  only at the entrance, the influence inside the domain is mainly dominated by turbulent viscosity. KLOPT DIT???

### Results with bluff-body

Since the aim is to find the influence of a bluff-body on the mixing quality, a bluff-body was added in the geometry and varied in size. In order to look at influence of a bluff-body

in a flow, it is important to look at the velocity magnitude. Figure 11 shows the velocity magnitude field, the influence of the bluff-body is clear. The bluff-body forces the fluid over the bluff body, creating a recirculation zone at the end of the bluff body.

The size of the bluff-body is changed, while changing the size, the turbulence entrance intensity is kept constant at 1%. For every bluff-body size, the same velocities are simulated as done in the cases without bluff-body.

Figure 10 shows the results for the first bluff-body, with  $h/D = 0.25$ . Again, the mixture fraction is extracted at the outlet of the geometry. The graph indicates again that for this bluff-body the inlet velocity of 0.5[m/s] accounts for the best mixing quality. Another important remark to Figure 10 regards to the case without bluff-body. When looking at the quality of mixing, the case with bluff-body shows an signifi-

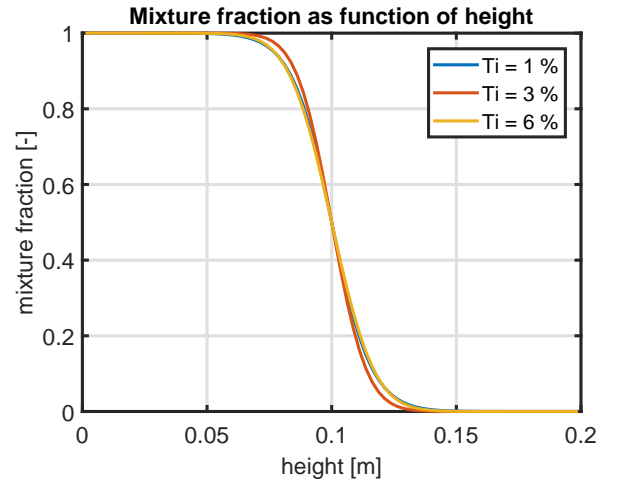


Figure 7: mixture fraction at constant inlet velocity of 1[m/s]

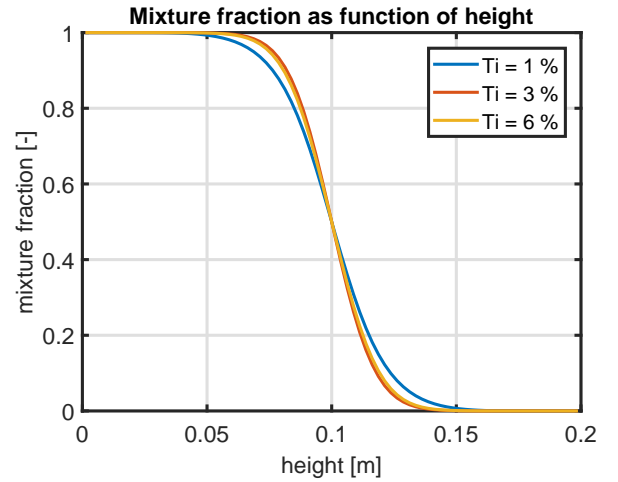


Figure 8: mixture fraction at constant inlet velocity of 0.5[m/s]

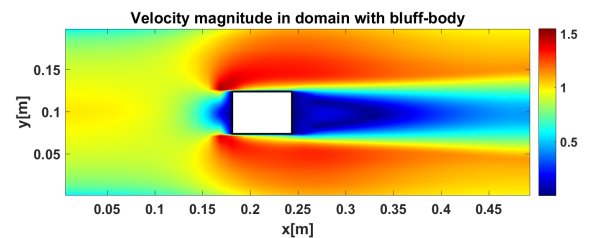


Figure 9: Velocity field with inlet velocity of 1[m/s]

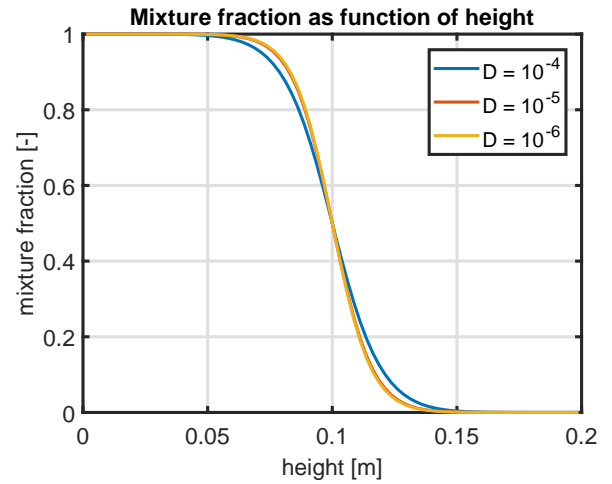


cant increase in mixing quality. Also, the inlet velocity seems to have less influence on the mixing. This can be explained by the velocity magnitude as shown in Figure 11. The bluff-body introduces a recirculation zone, which accounts for a large amount of mixing of the fractions. This circulation zone is present for all inlet velocities. Consequently, the fractions will be mixed.

T. Decreasing the size of the bluff-body to  $h/D = XXXXXXX$  and  $h/D = XXXXXXX$  as shown in Figures ?? and ?? shows little to none influence on the quality of mixing at the outlet of the geometry. This may be due to the Pe number having a value of 100. Again, decreasing should increase the quality of mixing.

**Table 2:** Modelling conditions.

CFD Run	$\omega$	$N_D$	$\chi_a/\chi_b$	$\frac{a}{b_i}$	$\Gamma_a$	$\Gamma_b$
First a						
AA01	0.0391	0.82	0.9469	0.041	203	0.123
AA02	0.8741	0.553	0.9528	0.399	7215	0.283
AA03	0.3654	0.958	0.5304	0.807	3049	0.35
AA04	0.8548	0.203	0.817	0.332	561	0.556
AA05	0.8676	0.215	0.7895	0.509	9207	0.123
AA06	0.1763	0.409	0.0698	0.995	7991	0.123
First b						
BA11	0.9654	0.443	0.5503	0.927	9257	0.284
BA12	0.6548	0.191	0.5146	0.337	3357	0.042
BA13	0.9476	0.535	0.2801	0.939	9389	0.108
BA14	0.3063	0.071	0.364	0.454	4534	0.896
BA15	0.3982	0.091	0.9544	0.521	7331	0.911
BA16	0.9734	0.161	0.0897	0.388	1144	0.144
BA17	0.8912	0.123	0.4564	0.198	7744	0.912
BA18	0.2312	0.723	0.0218	0.12	6612	0.893
BA19	0.1243	0.107	0.849	1.289	2859	0.698


**Figure 11:** Velocity field with inlet velocity of 1[m/s]

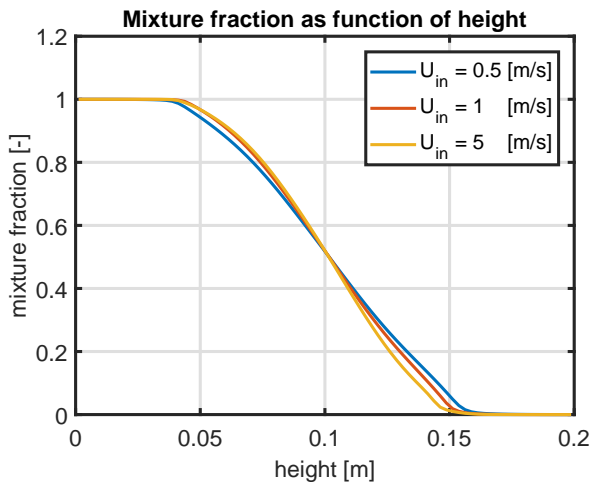
## CONCLUSION

The conclusions are:

1. Trondheim is a nice city.
2. CFD is great fun, and useful too.

## REFERENCES

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- VERSTEEG, H. and MALALASEKERA, W. (2007). Edinburgh Gate, Harlow, England.


**Figure 10:** mixture fraction at constant turbulent intensity of 1 %, with large bluff body

## **APPENDIX A**

Give any additional information here.