## Assignment 10

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## Outline

Problem

Solution

## Problem Statement

(Papoulis/Pillai Exercise 2-26) Show that a set S with n elements has

$$\frac{n(n-1)...(n-k+1)}{1.2...k} = \frac{n!}{k!(n-k)!}$$
(1)

subsets of k elements.



## Solution

We begin by choosing any k elements of a set consisting of n elements. The first element can be chosen in n ways, the second in n-1 ways, and so on. The  $k^{th}$  element can be chosen in n-k+1 ways. However, the order of elements in a set does not matter. This gives a total of

$$\frac{n(n-1)\dots(n-k+1)}{1\cdot2\dots k} \tag{2}$$

$$=\frac{n(n-1)...1}{(1.2...k)(1.2...(n-k))}$$
 (3)

$$=\frac{n!}{k!(n-k)!}=\binom{n}{k}\tag{4}$$

subsets containing k elements. Here,  $0 \le k \le n$ . The Python code codes/10\_1.py verifies the identity.

