## Assignment 7 (NCERT Class 12)

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Abstract—This document contains the solution to Question 5 of Exercise 13.1 in Chapter 13 (Probability) of the NCERT Class 12 Mathematics Textbook.

**Exercise 13.1, Q5.** If  $Pr(A) = \frac{6}{11}$ ,  $Pr(B) = \frac{5}{11}$  and  $Pr(A \cup B) = \frac{7}{11}$ , find

- (i)  $Pr(A \cap B)$
- (ii) Pr(A|B)
- (iii) Pr(B|A)

**Solution:** Define the random variables X and Y as follows:

$$X = \begin{cases} 0, & \text{event A occurs} \\ 1, & \text{otherwise} \end{cases}$$
 (1)

$$Y = \begin{cases} 0, & \text{event B occurs} \\ 1, & \text{otherwise} \end{cases}$$
 (2)

We know that, given events A and B,

$$Pr(AB) = Pr(A) + Pr(B) - Pr(A + B)$$
 (3)

and also,

$$Pr(A|B) = \frac{Pr(AB)}{Pr(B)}$$
 (4)

Using (2) and (3), we get

$$\Pr(X = 0, Y = 0) = \frac{6}{11} + \frac{5}{11} - \frac{7}{11} = \frac{4}{11}$$
 (5)

From (4) and (5),

$$\Pr(X = 0|Y = 0) = \frac{\Pr((X = 0)(Y = 0))}{\Pr(Y = 0)} = \frac{4}{5}$$
 (6)

and

$$\Pr(X = 0|Y = 0) = \frac{\Pr((X = 0)(Y = 0))}{\Pr(X = 0)} = \frac{2}{3} \quad (7)$$

The C code ./codes/7\_1.c verifies the solution, within limits of float precision.

**Note:** Derivation of (3) using Boolean Algebra:

$$LHS = A \lor B = (A' \land B')' \tag{8}$$

$$= 1 - (1 - A)(1 - B) \tag{9}$$

$$= A + B - AB = RHS \tag{10}$$

The following identities were used:

(De-Morgan's Law) 
$$(A \lor B)' = A' \land B'$$
 (11)

$$A' = 1 - A \tag{12}$$

$$A \wedge B = AB \tag{13}$$