

## Lecture 4: 27 January 2025

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## 4.1 Attack on DES

The iterative characteristic by itself is not enough to break 16-round DES due to its low probability. However, it was enough for DES reduced to 15 rounds. To retain this probability, we use a new round 1. This new round 1 will generate plaintexts with XOR  $(\psi, 0)$  which can then be fed into the characteristic.

Suppose  $P$  is a 64-bit plaintext and let  $v_i$  be a 32-bit constant with the first 12 bits equal to the possible outputs of S1, S2, S3 after the first round and 0 elsewhere for  $0 \leq i < 2^{12}$ . Define for  $0 \leq i < 2^{12}$

$$P_i = P \oplus (v_i, 0) \quad \bar{P}_i = P_i \oplus (0, \psi) \quad (4.1)$$

$$T_i = \text{DES}(P_i, K) \quad \bar{T}_i = \text{DES}(\bar{P}_i, K). \quad (4.2)$$

Then,  $P_i \oplus P_j = (v_k, \psi)$ . Out of the  $2^{24}$  possibilities of  $(i, j)$ , each  $v_k$  occurs exactly  $2^{12}$  times. Now, an XOR of  $\psi$  is fed into the first round, but we do not know which  $v_k$  is to be chosen initially to cancel the output of the  $F$  function and give us the desired  $(\psi, 0)$  input to the second round. Trying all  $2^{24}$  possibilities is slow. To find the right  $v_k$ , we exploit the cross-product structure of  $P_i$  and  $\bar{P}_j$ . Notice that a right pair will have zero outputs at S4, ..., S8 at the last round. Thus, we can feed in the plaintexts  $P_i$  and  $\bar{P}_j$  to get outputs  $T_i$  and  $\bar{T}_j$ . These  $2^{13}$  outputs can then be hashed by these 20 positions.