

Geometric Programming Assignment

Gautam Singh

Abstract—This document contains the solution to Question 25 of Exercise 5 in Chapter 6 of the class 12 NCERT textbook.

- 1) Show that the semi-vertical angle of the cone of the maximum volume and of given slant height is $\tan^{-1} \sqrt{2}$.

Solution: We use geometric programming. Taking the radius to be r and height to be h , the objective function to be maximized is

$$Z = r^2 h \quad (1)$$

subject to the constraints (where we take the slant height to be 1)

$$r^2 + h^2 = 1 \quad (2)$$

$$r \geq 0 \quad (3)$$

$$h \geq 0 \quad (4)$$

The Python code `codes/gp.py` solves this problem using `cvxpy`. The solutions are

$$r_M = \sqrt{\frac{2}{3}}, \quad h_M = \frac{1}{\sqrt{3}} \quad (5)$$

Hence, from (5), the required semi-vertical angle is

$$\alpha = \tan^{-1} \frac{r}{h} = \tan^{-1} \sqrt{2} \quad (6)$$

as required.