

Exploring Topological Data Analysis: In the perspective of Data Science

VISITING LECTURER:

EXPLORING TOPOLOGICAL DATA ANALYSIS 2021
 Date: 19 March 2021
 Time: 1.30-3.30PM (Indonesian Time)
 2.30PM-4.30PM (Malaysian Time)

INVITED LECTURE:
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 2.30PM-4.30PM (Malaysian Time)

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<https://sites.google.com/site/gobithaasan/>
 Sample codes: <https://github.com/gobithaasan/UndipTDA2021/>

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Content:
From theorems to applications

1. Motivation: Lifecycle of Data Science and job prospects
2. Introduction to Dataset & Machine Learning
3. Exploratory Data Analysis: Topological Data Analysis
4. Persistent Homology.
 - I. Invariants: Euler Characteristics & Betti Numbers
 - II. Homology computation & Persistence Diagrams
 - III. PH Applications
5. Mapper:
 - V. Mapper Computation & Graphs
 - VI. Mapper Applications
6. Acknowledgement

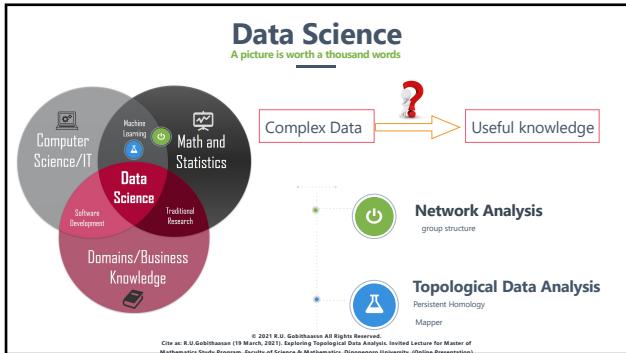
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Motivation: Data Science

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Indonesia as Regional Data Center

<https://news.microsoft.com/apac/2021/02/25/microsoft-to-establish-first-datacenter-region-in-indonesia-as-part-of-berdayakan-digital-economy-indonesia-initiative/>

Microsoft increases its investment in Indonesia's digital economy, with plans to establish a new datacenter region and a commitment to skill over 24 million Indonesians by end of 2021 through its decades' long skilling investment

Jakarta, Indonesia, 25 February 2021 – Microsoft today announced its *Berdayakan Ekonomi Digital Indonesia* initiative, which marks a significant commitment to advancing growth and digital transformation for Indonesia, its vibrant developer and startup ecosystem, enterprises, and the public sector. As part of the plan, Microsoft will establish its first datacenter region in Indonesia to deliver trusted cloud services locally, with world-class data security, privacy, and the ability to store data in country. Microsoft also announced plans to skill an additional 3 million Indonesians to achieve its goal of empowering over 24 million Indonesians by the end of 2021, through its long-established skills programs designed to create inclusive economic opportunities in the digital era.

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Data Center equipped with Microsoft Azure

<https://news.microsoft.com/apac/2021/02/25/microsoft-to-establish-first-datacenter-region-in-indonesia-as-part-of-berdayakan-digital-economy-indonesia-initiative/>

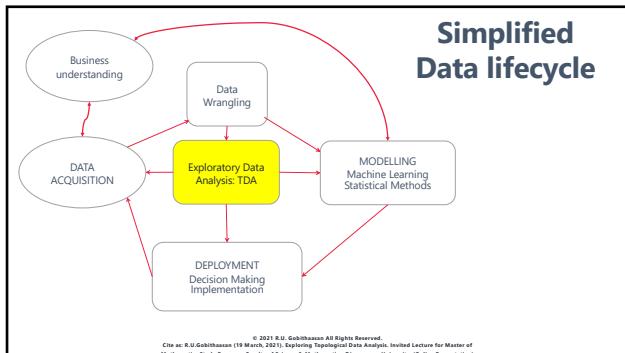
Azure Capabilities on Azure Stack

Virtual machines (VM), VM scale sets	Rapid deployment and scaling on demand	Containers	Networking	Storage	Key Vault	Azure App Service	Functions	Azure Marketplace
Virtual network, load balancer, VPN gateway	Virtual machines, Windows Server containers	Relational databases	Securely protect application keys and secrets	Web and API apps	Serverless Computing	Ready-to-go Apps from the Azure Marketplace		

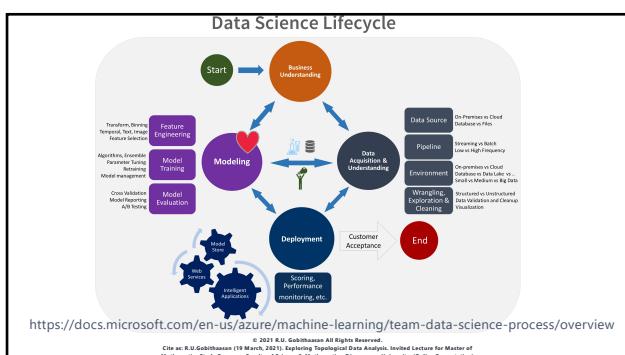
The Azure Stack is for operating businesses

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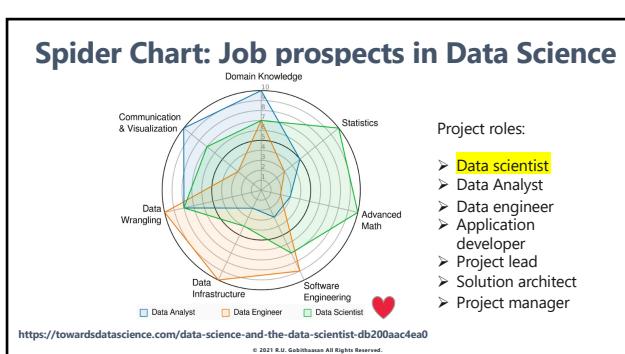
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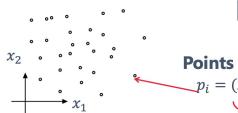
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Introduction: Dataset & Machine Learning

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Datasets!



Points $p_i = (x_1, x_2), (x_1, x_2) \in \mathbb{R}^2$

Columns: two features is usually the dimension.

Point cloud $X = \{p_1, p_2, \dots, p_m\} \quad X \in \mathbb{R}^2$

Rows: m observations

Points with label

age	height	gender
32	160	female
41	183	female
30	123	female
21	175	male
11	150	male
52	164	female

Dimension: 6 x 2

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Datasets!



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Example: Iris Dataset (labelled)

Points $p_i = (\text{Sepal Length}, \text{Sepal Width}, \text{Petal Length}, \text{Petal Width}, \text{Species})$

$p_i \in \mathbb{R}^4$: variables x_j can be used as a predictor variable called **feature**

(7.6, 3.0, 6.6, 2.1) -> "virginica";
(4.8, 3.4, 1.9, 0.2) -> "setosa";
(6.4, 2.9, 4.3, 1.3) -> "versicolor";

Label species = {versicolor, setosa, virginica}

Point cloud $X = \{p_1, p_2, \dots, p_{50}\}$

Classification problem: Find Species?

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Point cloud from an image
Higher Dimension: MNIST database of handwritten digits

$$G = \begin{pmatrix} 130 & 113 & 127 & 140 & 132 \\ 125 & 40 & 30 & 25 & 111 \\ 110 & 30 & 200 & 10 & 120 \\ 135 & 20 & 6 & 15 & 123 \\ 115 & 109 & 100 & 150 & 116 \end{pmatrix}$$

Each pixel is a feature

Each picture as a point: A picture: $p_i = (G_{11}, G_{12}, \dots, G_{15}, G_{21}, \dots, G_{55})$
(linearized vector)

L: Picture \mapsto Vector $= (x_1, x_2, \dots, x_{25}) \quad p_i \in \mathbb{R}^{25}$

Point cloud as a collection of pictures: $X = \{p_1, p_2, \dots, p_n\} \quad p_i \in \mathbb{R}^n$

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MNIST database of handwritten digits (labeled)
Higher Dimension:

$$\{ \text{8} \rightarrow 8, \text{ 6 } \rightarrow 6, \text{ 0 } \rightarrow 0, \text{ q } \rightarrow 9 \}$$

One scanned picture: $p_i = (G_{11}, G_{12}, \dots, G_{15}, G_{21}, \dots, G_{28,28})$
 $= (x_1, x_2, \dots, x_{784}) \quad p_i \in \mathbb{R}^{784}$

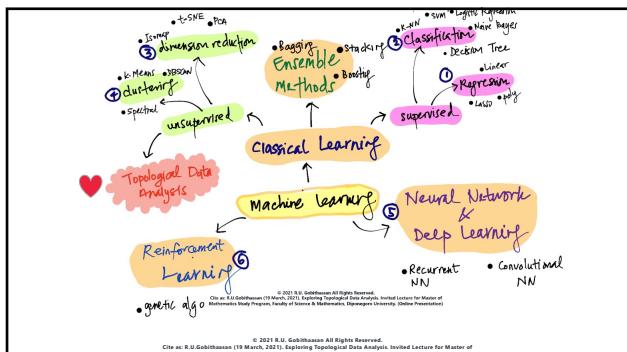
Training dataset (60,000 pictures): Dimension: $60,000 \times 784 \quad p_i \in \mathbb{R}^{784}$

Test dataset (10,000 pictures): Dimension: $10,000 \times 784 \quad p_j \in \mathbb{R}^{784}$

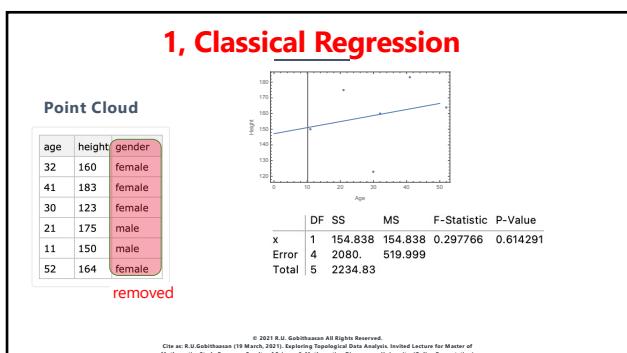
Point cloud as a collection of MINIST dataset: $X = (p_1, p_2, \dots, p_{70,000}) \quad p_i \in \mathbb{R}^{784}$

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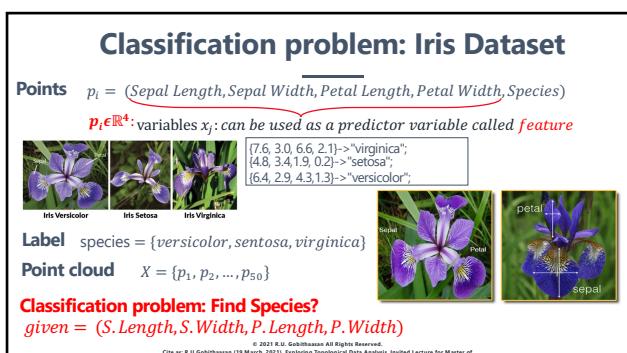
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2, Classification examples

Point Cloud

age	height	gender
32	160	female
41	183	female
30	123	female
21	175	male
11	150	male
52	164	female

```

LogisticRegression[<|"age" → 12, "height" → 120|, "Probabilities"]
↳ female → 0.523778, male → 0.476222]

RandomForest[<|"age" → 12, "height" → 120|, "Probabilities"]
↳ female → 0.324388, male → 0.675612]

NeuralNet[<|"age" → 12, "height" → 120|, "Probabilities"]
↳ female → 0.000185764, male → 0.999814]

```

- Spam filtering: logistic regression
- Sentiment Analysis: Naive Bayes
- Fraud Detection

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3, Dimension reduction:

Handwriting (assume we lost its labels)

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3, Dimension reduction:

Iris Dataset (assume we lost its labels)

$X = (p_1, p_2, \dots, p_{50}), p_i \in \mathbb{R}^4$

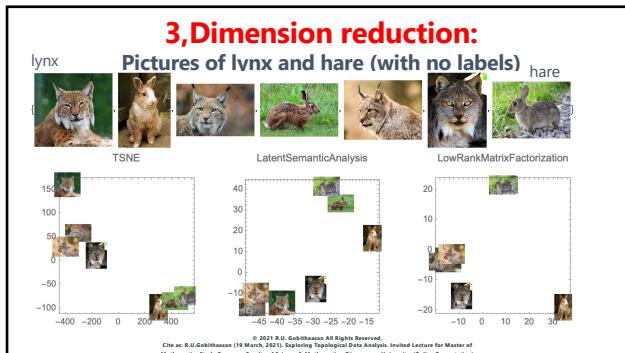
t-SNE: Stochastic Neighbor Embedding
➤ low dimensional neighborhood similar to its original neighborhood (preserve local structure).

Applications

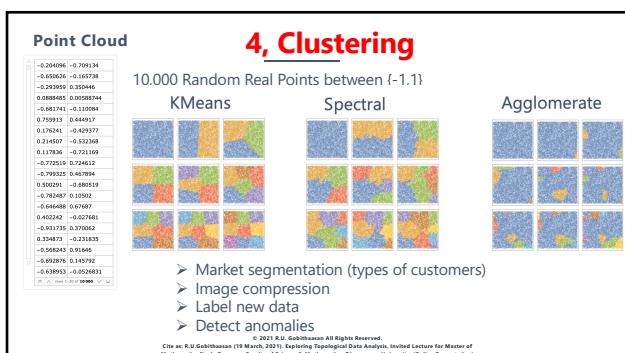
- Recommender systems
- Visualization
- Fake image analysis
- Risk management

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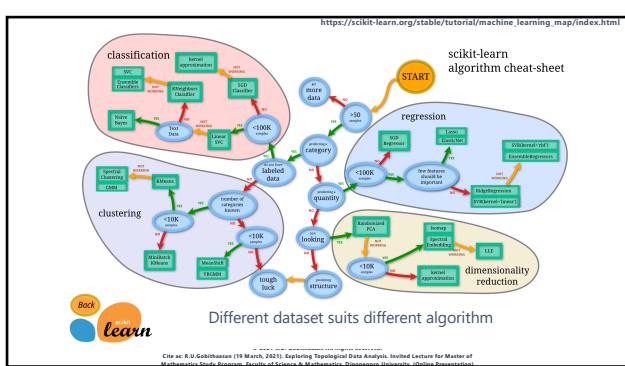
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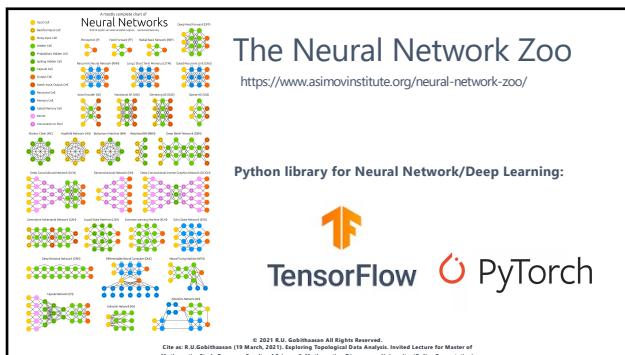
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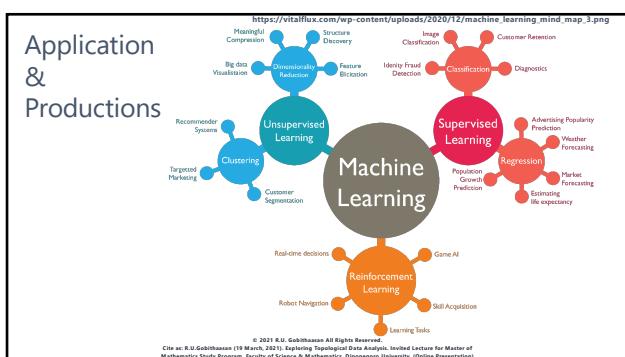
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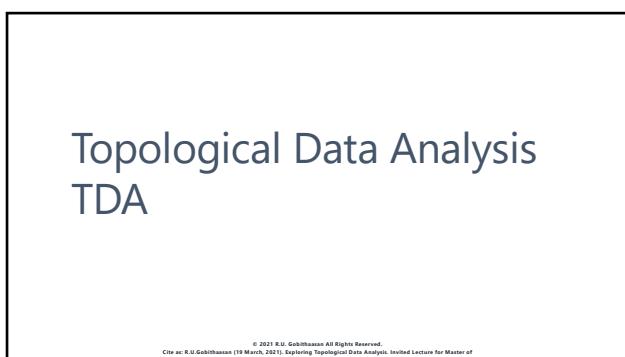
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The failure of Descriptive Stat: Datasaurus Dozen

<https://www.autodesk.com/research/publications/same-stats-different-graphs>

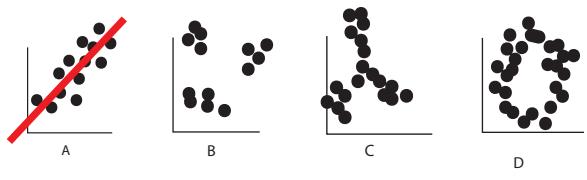
- How to differentiate when they are quantitatively similar?
 - qualitative approach**
 - Investigate the **shape visually**
- How to visually see high dimensional dataset?
 - $p_i \in \mathbb{R}^n$
 - Dimension reduction:**
We lose some info while reducing dimension...

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What method to use?

- Supervised (regression / classification)
- Unsupervised (clustering / dimension reduction)



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DATA HAS SHAPES!

Topological Data Analysis: Shape has a meaning, meaning has a value

Advantage of TDA:

- Investigation at different scale:** TDA sensitive to both large and small scale patterns.
- Resistance to noise and missing data:** TDA retains significant features of the data.
- Invariance under deformation.** The stretch, resize, or orientation of data does not fundamentally change the 'underlying shape' of the data.

As a tool for:

A data exploration tool. Topological exploration of data: qualitative approach.

Point cloud as a signature: TDA can identify global topology and local geometry

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TDA: Two Methodologies

Point cloud
 $X = (p_1, p_2, \dots, p_m), p_i \in \mathbb{R}^n$

Persistence Diagram:
 Topological structures: n -dimension holes

Persistent Homology

TDA Mapper

A graph $G(V,E)$:
 Topological structures: loops & flares

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Topological Invariants & Persistent Homology

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Topology: Study of shape in \mathbb{R}^n

- A fundamental problem of topology is that determining whether given two spaces are **homeomorphic**. (Munkres, elements of algebraic topology)
 - A suitable shape descriptor is known as **invariant**.
- Def. A **(topological) invariant** is a map that assigns the same object to spaces of the same topological type.
- **Euclidean geometry** studies invariants under rigid motion in \mathbb{R}^n , e.g., moving a cube in space does not change its geometry.
- **Topology** studies invariants under continuous, and continuously invertible, transformations; e.g., mold and stretch a play-doh ball into a filled cube, but not into a donut shape.

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Invariants in Euclidean Geometry

- **Congruence:** similar in shape and size.
- **Unchanged property is called invariants.**
- **Rigid motions does not change the shape or size.**

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Topology: Study of shape in \mathbb{R}^n

- Topology studies the **connectivity**.
- Homeomorphism: Shapes can be deformed into each other **without cutting or gluing**.

➤ **Homeomorphic:**

- Continuous **bijective** map
- Continuous inverse map

➤ Length and area are not preserved.
- invariant under deformation

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Invariant: Betti number!

The k th Betti $\beta_k(X)$ number refers to the number of **k -dimensional holes** in a topological space.

- β_0 : # connected components.
- β_1 : # one-dimensional or "circular" holes.
- β_2 : # two-dimensional "voids".
- β_k : # k th-dimensional 'hole'.

the maximum number of cuts (must **cut through**) that must be made **before separating** a topological surface into two pieces or 0-cycles, 1-cycles, etc.

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Invariant: Betti number!

Diagram illustrating Betti numbers for a line and a circle.

Line:

- β_0 (line)=1
- β_1 (line)=0

Circle:

- β_0 (circle)=1
- β_1 (circle)=1

Topological shapes:

- A torus-like shape with a hole: β_0 (cd)=1, β_1 (cd)=1
- Three separate circles: β_0 (3 discs)=3, β_1 (3 discs)=0

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Invariant: Betti number!

Diagram illustrating Betti numbers for a Möbius strip and a sphere.

Möbius strip:

- β_0 (mobius strip)=1
- β_1 (mobius strip)=1

Sphere:

- β_0 (sphere)=1
- β_1 (sphere)= 0
- β_2 (sphere)= 1

Topological shapes:

- A torus-like shape with a hole: β_0 (Torus)=1, β_1 (Torus)=2, β_2 (Torus)=1
- A genus-2 surface with a hole: β_0 (Torus)=1, β_1 (Torus)=2, β_2 (Torus)=1

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Invariant: Betti number!

Diagram illustrating Betti numbers for a Möbius strip and a sphere.

Möbius strip:

- β_0 (mobius strip)=1
- β_1 (mobius strip)=1

Sphere:

- β_0 (sphere)=1
- β_1 (sphere)= 0
- β_2 (sphere)= 1

Topological shapes:

- A torus-like shape with a hole: β_0 (Torus)=1, β_1 (Torus)=2, β_2 (Torus)=1

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Algo: Persistent Homology

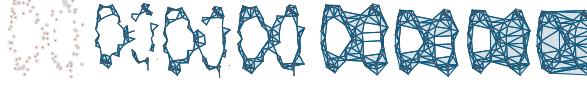
- 1. Simplicial Complexes**
 - > Vary scale distance, ϵ , to get various filtrations level
 - > Various types of filtrations:
 - α : alpha complex
 - C : Čech complex
 - VR: Vietoris-Rips complex
- 2. Boundary Matrix Reduction**
 - > Operation on mathematical structure of simplicial complex.
 - The n th homology group H_n
 - $H_n = \ker \partial_n / \text{Im } \partial_{n+1}$.
 - $\beta_n = \text{rank } (H_n)$
- 3. Persistent Homology**
 - Birth/death: track homological features across the entire filtration:
 - > Barcodes
 - > Persistence Diagram (PD)
- 4. Persistence Summaries**
 - > Various kinds of PD representation as features.
 - > Statistics of PDs: Averages, standard deviations, distributions, etc.

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Multiresolution and various kind of filtrations

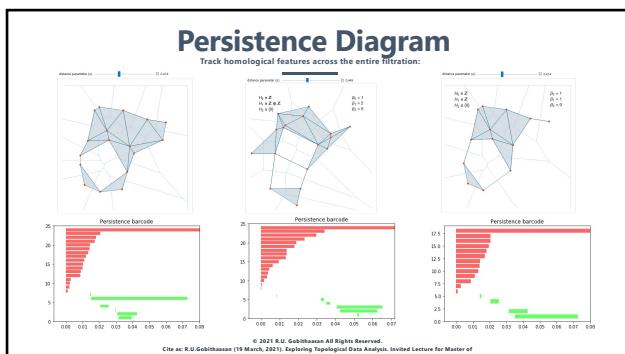
FILTRATION DEMO



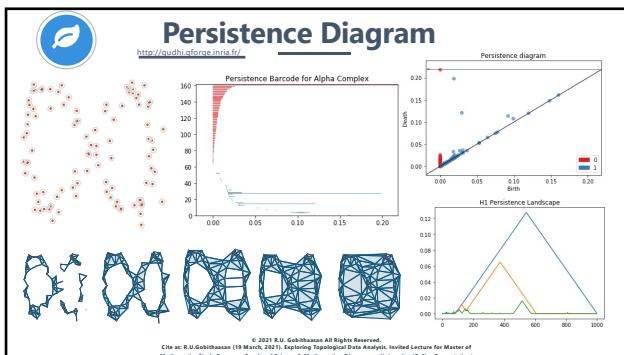
Can I identify the n th dimension hole which persist over various resolution?

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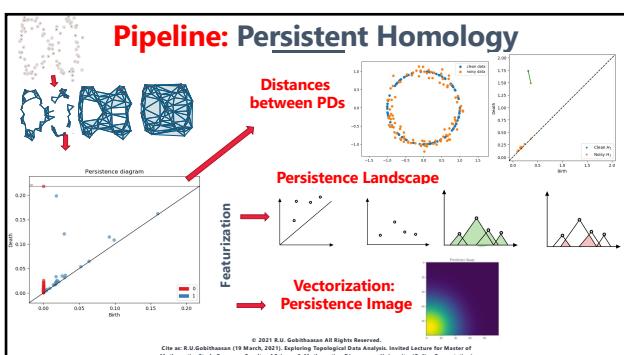
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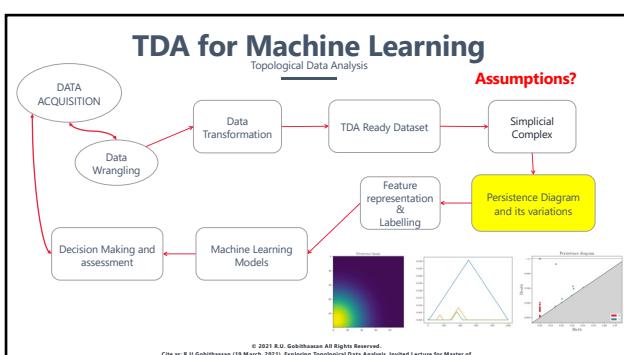
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PH: Success stories

- o Jose Perea (MSU), Elizabeth Munch (MSU), Chris Tralie (Ursinus College)
- time series dataset (dynamical systems, audio and video dataset)
- o Robert Ghrist's Gr. (math. UPenn)
-network flow, sensor network
- o Yasuaki Hiraoka (Riken, Kyoto)
-materials science
- o Michelle Feng & Mason A. Porter (UCLA)
-political science: voting (geospatial Data)

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Software: Persistent Homology

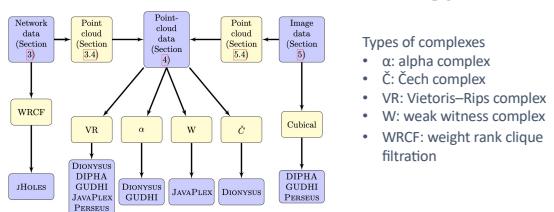


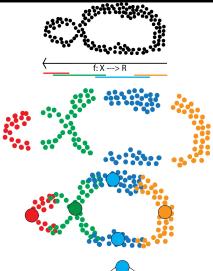
Figure 1: Schematic for how to navigate the tutorial.

<https://github.com/n-otter/PH-roadmap>

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TDA Mapper



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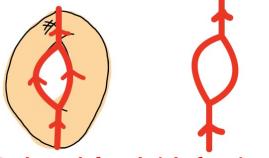
 **TDA Mapper**

- Compressed representation approximating Reeb graph

Extracting insights from the shape of complex data using topology

P. Y. Lum, G. Singh, A. Lehman, T. Ishkanov, M. Vejdemo-Johansson, M. Alagappan, J. Carlsson & G. Carlsson
Affiliations | Contributions | Corresponding authors
Scientific Reports 3, Article number: 1236 | doi:10.1038/srep01236
Received: 13 September 2012 | Accepted: 06 December 2012 | Published: 07 February 2013

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Reeb graph from height function

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Mapper: Discrete approximation of Reeb Graph

- 1. INPUT (dissimilarity measure)**
 - Choose a filter function $f: X \rightarrow \mathbb{R}$
 - Density measure, score of measure difference, eccentricity measure.
 - a cover U of $f(X)$
 - Resolution r (diameter of intervals)
 - Gain g (% of interval overlaps);
- 2. Decompose into clusters**
 - From the covering $U = \{U_\alpha\}_{\alpha \in \mathcal{A}}$ construct the clusters: $X_\alpha = f^{-1}(U_\alpha) \subseteq X$
 - k-NN, Rips, various Clustering methods
- 3. Compute The Nerve**
 - A vertex for each cluster.
 - An edge iff the clusters have a common point
- 4. OUTPUT: Simplicial Complex**
 - Graph $G(V, E)$ with connected vertices of nonempty intersection

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Mapper: What to investigate from the graph?

get a higher-level understanding of the structure of data

exhibit relations between clusters, variables, etc.

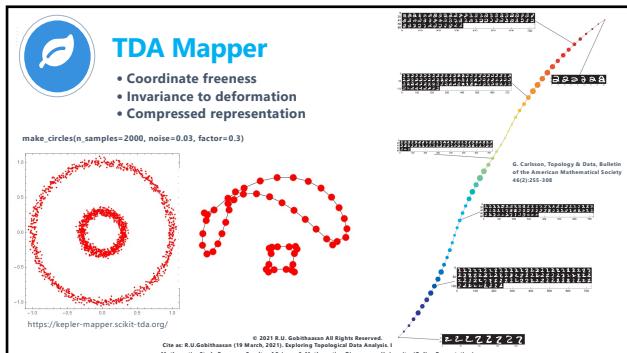
visualize topology on the data directly

avoid paying the algorithmic price of persistence

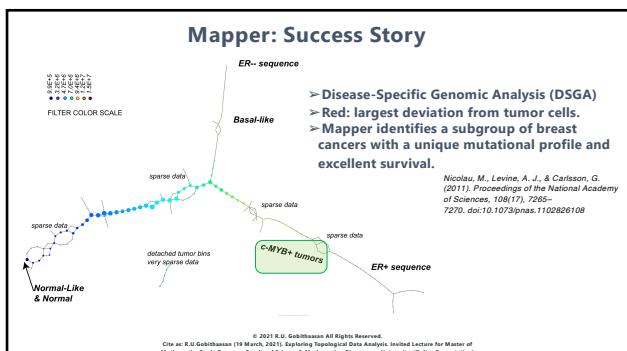
<http://www.enseignement.polytechnique.fr/informatique/INF556/index.html>

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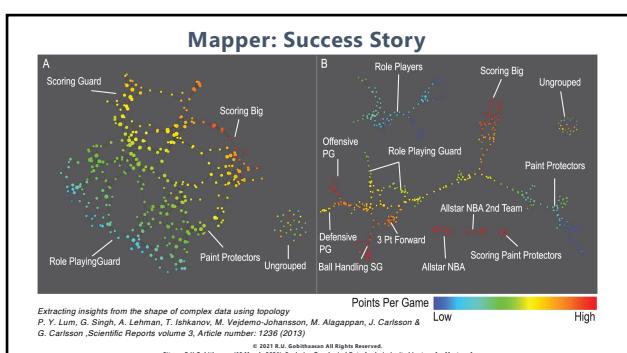
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Mapper: Success stories

Symphony
AYASDI

- o Financial Crimes,
- o Disease Recovery,
- o Genomics,
- o Spinal Cord Injury/Traumatic Brain Injury,
- o Asthma, Diabetes, Oncology, Proteomics,
- o Predicting Earthquakes,
- o Macroeconomic loops,
- o Remote sensing

<https://www.ayasdi.com/knowledge-center/?type=publication>

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Software: Mapper

- Python Mapper
- Skicit-tda: Keppler Mapper



Scikit-TDA
Topological Data Analysis for the Python ecosystem.
ø <http://scikit-tda.org>
<https://kepler-mapperscikit-tda.org/en/latest/>

- Giotto-tda



https://giotto-ai.github.io/gtda-docs/0.4.0/notebooks/mapper_quickstart.html

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Demo codes using Python is available at:

<https://github.com/gob1thaasan/UndipTDA2021/>

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