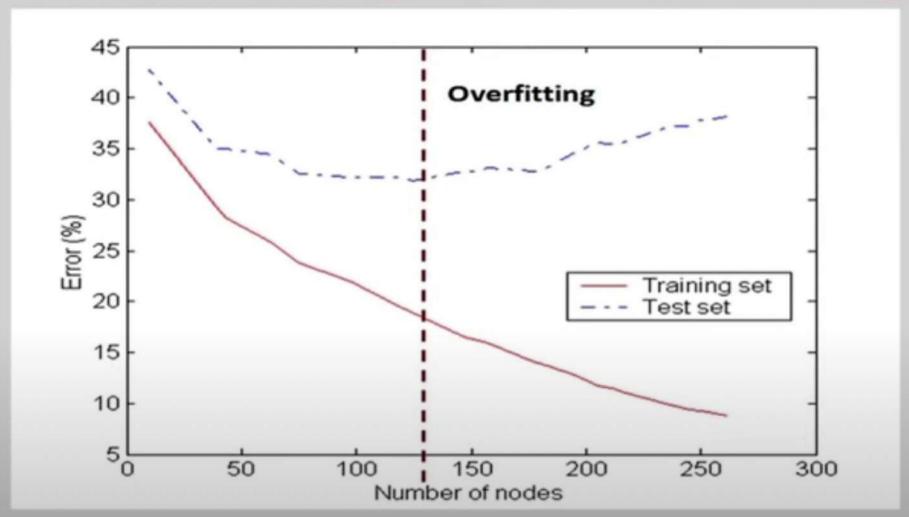
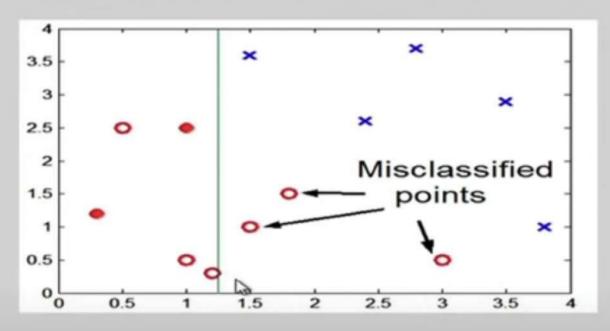


## **Underfitting and Overfitting**



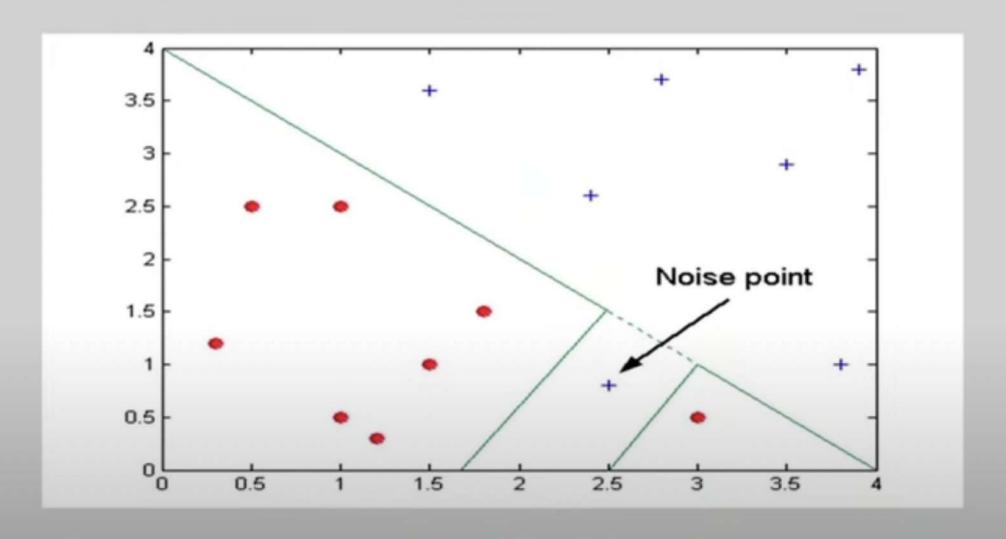
Underfitting: when model is too simple, both training and test errors are large

#### Overfitting due to Insufficient Examples



Lack of data points makes it difficult to predict correctly the class labels of that region

## Overfitting due to Noise



Decision boundary is distorted by noise point

#### **EXAMPLE**



Input singular nouns and get the plural nouns for any word

Bottle Bottles
Cup Cups
Pencil Pencils





Train the model and it learns the pattern that 's' needs to be added at the end of every word.

New Input Prediction
Window Windows
Desk Desks



Over-Generalization



But the model fails to predict plural nouns for the words like

box boxs boxes man mans men leaf leafs leaves

#### Reasons for Overfitting

- Data used for training is not cleaned and contains noise (garbage values) in it
- The model has a high variance
- The size of the training dataset used is not enough
- The model is too complex

#### Reasons for Underfitting

- · Data used for training is not cleaned and contains noise (garbage values) in it
- The model has a high bias
- The size of the training dataset used is not enough
- The model is too simple

### Notes on Overfitting

- overfitting happens when a model is capturing idiosyncrasies of the data rather than generalities.
  - Often caused by too many parameters relative to the amount of training data.
  - E.g. an order-N polynomial can intersect any N+1 data points

### Pre-Pruning (Early Stopping)

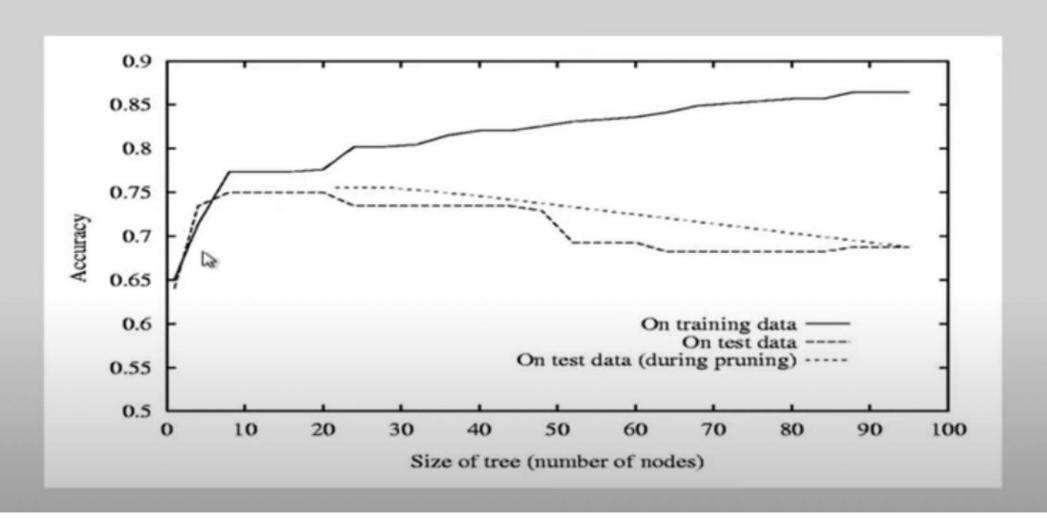
- Typical stopping conditions for a node:
  - Stop if all instances belong to the same class
  - Stop if all the attribute values are the same
- More restrictive conditions:
  - Stop if number of instances is less than some user-specified threshold
  - Stop if class distribution of instances are independent of the available features (e.g., using  $\chi^2$  test)
  - Stop if expanding the current node does not improve impurity measures (e.g., Gini or information gain).

### Reduced-error Pruning

- A post-pruning, cross validation approach
  - Partition training data into "grow" set and "validation" set.
  - Build a complete tree for the "grow" data
  - Until accuracy on validation set decreases, do:
    - For each non-leaf node in the tree
    - Temporarily prune the tree below; replace it by majority vote Test the accuracy of the hypothesis on the validation set Permanently prune the node with the greatest increase in accuracy on the validation test.
- Problem: Uses less data to construct the tree
- Sometimes done at the rules level

General Strategy: Overfit and Simplify

## Reduced Error Pruning



#### Model Selection & Generalization

- Learning is an ill-posed problem; data is not sufficient to find a unique solution
- The need for inductive bias, assumptions about H
- Generalization: How well a model performs on new data
- Overfitting: H more complex than C or f
- Underfitting: H less complex than C or f

#### **Triple Trade-Off**

- There is a trade-off between three factors:
  - Complexity of H, c (H),
  - Training set size, N,
  - Generalization error, E on new data
- As N increases-, E decreases
- As c (H) increases-, first E decreases and then E- increases
- As c (H)- increases, the training error decreases for some time and then stays constant (frequently at 0)

#### Notes on Overfitting

- Overfitting results in decision trees that are more complex than necessary
- Training error no longer provides a good estimate of how well the tree will perform on previously unseen records

## Dealing with Overfitting

- Use more data
- Use a tuning set
- Regularization
- Be a Bayesian

### **Avoid Overfitting**

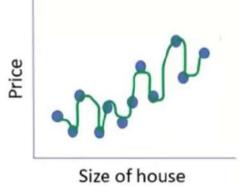
- How can we avoid overfitting a decision tree?
  - Prepruning: Stop growing when data split not statistically significant
  - Postpruning: Grow full tree then remove nodes
- Methods for evaluating subtrees to prune:
  - Minimum description length (MDL):
  - Minimize: size(tree) + size(misclassifications(tree))
  - Cross-validation

To avoid this condition regularization is used. Regularization is a technique used for tuning the function by adding an additional penalty term in the error function. The additional term controls the excessively fluctuating function such that the coefficients don't take extreme values. This technique of keeping a check or reducing the value of error coefficients are called shrinkage methods or weight decay in case of neural networks.

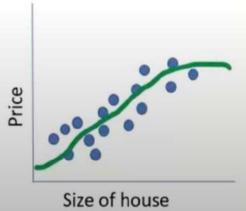
## Regularization

 In a linear regression model overfitting is characterized by large weights.

	M = 0	M = 1	M = 3	M = 9
₩o	0.19	0.82	0.31	0.35
W <sub>1</sub>		-1.27	7.99	232.37
W <sub>2</sub>			-25.43	-5321.83
W <sub>3</sub>	1		17.37	48568.31
W4				-231639.30
W <sub>5</sub>				640042.26
W <sub>6</sub>				-1061800.52
W <sub>7</sub>				1042400.18
W8				-557682.99
W9				125201.43



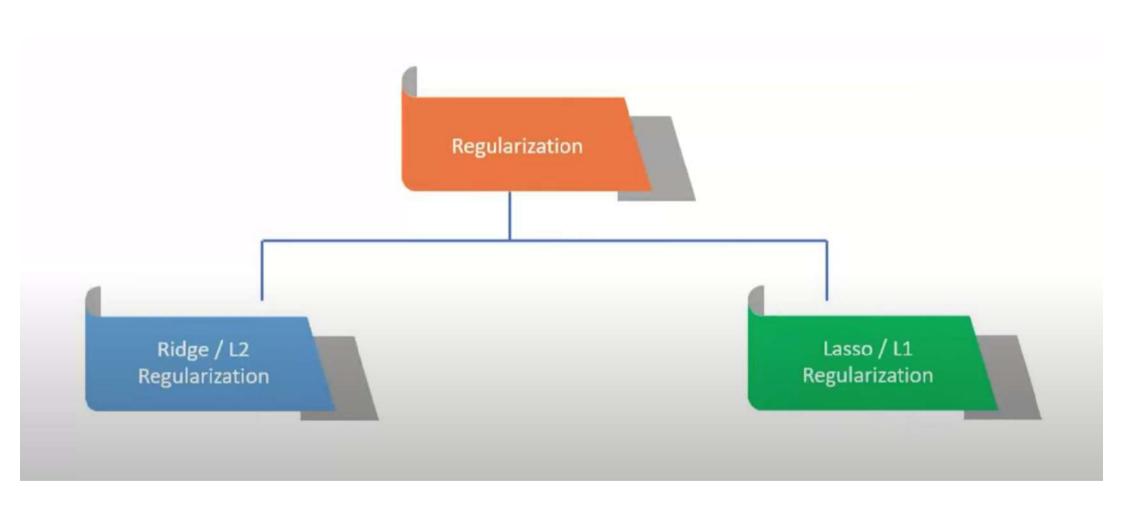




Price = 
$$\beta_0 + \beta_1 * \text{size} + \beta_2 * \text{size}^2 + \beta_3 * \text{size} 3 + \beta_4 * \text{size} 4$$

reduce  $\beta_3$  and  $\beta_4$  close to zero

Price =  $\beta_0 + \beta_1 * \text{size} + \beta_2 * \text{size}^2$ 



# Which Technique To Use?

#### Ridge

Lot of features In the dataset and all features have small coefficients.

#### Lasso

Small number of features and few features have high coefficient value.

### Mean Squared Error

$$ms\varepsilon = \frac{1}{n} \sum_{i=1}^{n} (y_i - h_{\theta}(x_i))^2$$

$$h_{\theta}(x_i) = \theta_0 + \theta_1 x_1 + \theta_2 x_2^2 + \theta_3 x_3^3$$

# Lasso Regularization

$$MSE = \frac{1}{n} \sum_{i=1}^{n} (y_{i \text{ (actual }} - y_{i \text{ (predicted)}}))^{2}$$

$$Loss = \sum_{i=1}^{n} (y_i - \widehat{y}_i)^2 + \lambda \sum_{j=1}^{p} |\beta_j|$$

Penalty term regularizes the coefficients

$$\lambda$$
 = Tuning parameter

# Ridge Regularization

$$MSE = \frac{1}{n} \sum_{i=1}^{n} (y_{i \text{ (actual }} - y_{i \text{ (predicted)}})^{2}$$

Loss = 
$$\sum_{i=1}^{n} (y_i - \hat{y}_i)^2 + \lambda \sum_{j=1}^{p} \beta_j^2$$

Penalty term regularizes the coefficients

$$\lambda$$
 = Tuning parameter

#### Penalize large weights in Linear Regression

Introduce a penalty term in the loss function.

$$E(\vec{w}) = \frac{1}{2} \sum_{n=0}^{N-1} \{t_n - y(x_n, \vec{w})\}^2$$

#### Regularized Regression

1. (L2-Regularization or Ridge Regression)

$$E(\vec{w}) = \frac{1}{2} \sum_{n=0}^{N-1} (t_n - y(x_n, \vec{w}))^2 + \frac{\lambda}{2} ||\vec{w}||^2$$

1. L1-Regularization

$$E(\vec{w}) = \frac{1}{2} \sum_{n=0}^{N-1} (t_n - y(x_n, \vec{w}))^2 + \lambda |\vec{w}|_1$$