

TUTORIAL - 4

INFIX , PREFIX , POST-FIX

PART I

A.2

a) Infix : $A + B * C + D$

Scanned	Operator Stack	Expression
	(
A	(A
+	(+	A
B	(+	AB
*	(+ *	AB
C	(+ *	ABC
+	(+	ABC*+
D	(+	ABC*+D
		POSTFIX ABC*+D+

b) Infix : $(A+B) * (C+D)$

Scanned	Operator Stack	Expression
	(
(((
A	((A
+	((+	A
B	((+	AB
)	(AB+
*	(*	AB+
((* (AB+
C	(* (AB+C
+	(* (+	AB+C
D	(* (+	AB+CD
)	(*	AB+CD+
		POSTFIX AB+CD+*

(c) Infix : $A * B + (C / D) / E - F$

Scanned	Operator Stack	Expression
	(
A	(A
*	(*	A
B	(*	AB
+	(+	AB*
C	(+ (AB*
C	(+ (AB*C
/	(+ (/	AB*C
D	(+ (/	AB*CD
)	(+	AB*CD/
/	(+ /	AB*CD/
E	(+ /	AB*CD/E
-	(-	AB*CD/E/+
F	(-	AB*CD/E/+F

POSTFIX $AB * CD / E / + F -$

d) Infix : $X^Y / (5 * Z) + 2$

Scanned	Operator Stack	Expression
	(
X	(X
^	(^	X
Y	(^	XY
/	(^ /	XY
((^ / (XY
5	(^ / (XY5
*	(^ / (*	XY5
Z	(^ / (*	XY5Z
)	(^ /	XY5Z*
+	(+	XY5Z* / ^
2	(+	XY5Z* / ^ 2

$XY5Z* / ^ 2 +$

e) Infix : $A + (B * C - (D / E \wedge F) * G) * H$

Scanned Operator Stack Expression

	(A
A	(A
+	(+	A
((+ (A
B	(+ (AB
*	(+ (*	AB
C	(+ (*	ABC
-	(+ (* -	ABC
((+ (* - (ABC
D	(+ (* - (ABCD
/	(+ (* - (/	ABCD
E	(+ (* - (/	ABCDE
\wedge	(+ (* - (\wedge	ABCDE/
F	(+ (* - (\wedge	ABCDE/F
)	(+ (* -	ABCDE/F \wedge
*	(+ (*	ABCDE/F \wedge - *
G	(+ (*	ABCDE/F \wedge - *G
)	(+	ABCDE/F \wedge - *G*
*	(+ *	ABCDE/F \wedge - *G*
H	(+ *	ABCDE/F \wedge - *G*

POSTFIX $ABCDE/F\wedge - *G** +$

g) Infix : $(A + B * (C - D)) / E$

Scanned Operator Stack Expression

	(
(((
A	((A
+	((+	A
B	((+	AB
*	((+ *	AB
(((+ * (AB

C	((+*(ABC
-	((+*(ABC
D	((+*(ABCD
)	((+*(ABCD-
)	(ABCD-*
/	(/	ABCD-*/
E	(/	ABCD-*/+E
:		ABCD-*/+E/

f) Infix: $K+L-M*N+(O^P)*W/U/V*T+Q$.

Scanned	Operator Stack	Expression
	(
K	(K
+	(+	K
L	(+	KL
-	(-	KL+
M	(-	KL+M
*	(-*	KL+M
N	(-*	KL+MN
+	(+	KL+MN*
((+ (KL+MN* -
O	(+ (KL+MN* - O
^	(+ (^	KL+MN* - O
OP	(+ (^	KL+MN* - O P
)	(+	KL+MN* - O P ^
*	(+ *	KL+MN* - O P ^
W	(+ *	KL+MN* - O P ^ W
/	(/	KL+MN* - O P ^ W *
U	(/	KL+MN* - O P ^ W * + U
/	(//	KL+MN* - O P ^ W * + U
V	(//	KL+MN* - O P ^ W * + U V
*	(*	KL+MN* - O P ^ W * + U V //
T	(*	KL+MN* - O P ^ W * + U V // T
+	(*+	KL+MN* - O P ^ W * + U V // T +

α $(+$ $KL+MN* / OP^{\wedge}W*+UV//T*\alpha$

POSTFIX

 $KL+MN* / OP^{\wedge}W*+UV//T*\alpha +$

A.1 Infix to Postfix -

1. Initialize a stack for operators, output list
2. Split the input into a list of tokens.
3. Repeat step 4 to 9 for each token (left to right).
4. if it is operand : append to output
5. if it is '(' : push into operators' stack
6. if it is in '+ - * /' :
7. While stack[top] has precedence \geq it
8. pop & append ~~into~~ to the output list
9. Push onto stack
10. Pop and append the rest of the stack.

Infix to Prefix -

1. Reverse the infix expression.
2. Initialize a stack for operators, output list.
3. Split the input ~~data~~ into a list of tokens.
4. Repeat step 5 to 10 for each token (left to right)
5. if it is operand : append into operators' stack
6. if it is '(' : push into operators' stack
7. if it is in '+ - * /' :
8. while stack[top] has precedence \geq it
9. pop & append to the output list.
10. Push into stack.
11. Pop and append the rest of the stack.

PART II

A.2

a) Infix: $A + B * C + D$ Reverse: $D + C * B + A$

Scanned

Operator Stack

Expression

	(
A	(AD
D	(AD
+	(+	DC
B	(+	DC
C	(+*	DCB
*	(+*	DCB*+
B	(+	DCB*+A
+	(+	DCB*+A
A	(+	DCB*+A+

 \therefore Prefix: $+A+*BCD$

b)

Infix: $(A+B) * (C+D)$ Reverse: $)D+C(*)B+A($ $\Rightarrow (D+C) * (B+A)$

Scanned

Operator Stack

Expression

(((
D	((D
+	((+	D
C	((+	DC
)	(DC+
*	(*	DC+
((*(DC+
B	(*(DC+B
+	(*(+	DC+B
A	(*(+	DC+BA
)	(*	DC+BA+

 $DC+BA+*$ Prefix: $*+AB+CD$

c) Infix: $A * B + (C / D) / E - F$ Reverse: $F - E / (C / D) + B * A$

Scanned	Operator Stack	Expression
	(
F	(F
-	(-	F
E	(-	FE
/	(-/	FE
((-/ (FE
D	(-/ (FED
/	(-/ (/	FED
C	(-/ (/	FEDC
)	(-/	FEDC/
+	(+	FEDC// -
B	(+	FEDC// - B
*	(+*	FEDC// - B
A	(+*	FEDC// - BA
		FEDC// - BA * +

 \therefore Prefix = $+ * AB - // CDEF$ d) Infix: $X^Y / (5 * Z) + 2$ Reverse: $2 + (Z * 5) / Y^X$

Scanned	Operator Stack	Expression
	(
2	(2
+	(+	2
((+ (2
Z	(+ (2Z
*	(+ (*	2Z
5	(+ (*	2Z5*
)	(+ *	2Z5*
/	(+/	2Z5*
Y	(+/	2Z5*Y
^	(^	2Z5*Y/+
X	(^	2Z5*Y/+X
		2Z5*Y/+X

 \therefore Prefix: $^X + / Y * 5 Z 2$

(c) Infix : $A + (B * C - (D / E ^ F) * G) * H$

Reverse : $H * (G * (F ^ E / D) - C * B) + A$

Scanned	Operator Stack	Expression
	(
H	(H
*	(*	H
((*(H
G	(*(HG
*	(**	HG
((**	HG
F	(**	HGF
^	(**^(HGF
E	(**^(HGF E
/	(**^(/	HGF E
D	(**^(/	HGF E D
)	(**^(/	HGF E D /
-	(**^(/	HGF E D / ^
C	(**^(/	HGF E D / ^ *
*	(**^(/	HGF E D / ^ * C
B	(**^(/	HGF E D / ^ * C B
)	(**^(/	HGF E D / ^ * C B *
+	(**^(/	HGF E D / ^ * C B * -
A	(**^(/	HGF E D / ^ * C B * - *
		HGF E D / ^ * C B * - * A +

Prefix = $+ A * - * B C * ^ / D E F G H$

f. Infix: $K+L-M*N+(O^P)*W/U/V*T+Q$
Reverse: $Q+T*V/U/W*(P^O)+N*M-L+K$

Scanned Operator Stack Expression

	- (
Q	(Q
+	(+	Q
T	(+	QT
*	(+ *	QT
V	(+ *	QTV
/	(** /	QTV* +
U	(/	QTV* + U
/	(//	QTV* + U
W	(//	QTV* + UW
*	(*	QTV* + UW //
((* (QTV* + UW //
P	(* (QTV* + UW // P
^	(* (^	QTV* + UW // P ^
O	(* (^	QTV* + UW // P O
)	(*	QTV* + UW // P O ^

Q3. What is the result of evaluating the following expression? (Infix to Postfix and Infix to prefix)

a) $10 + 3 * 5 / (16 - 4)$

→ $10, 3, 5, 16, 4, -, /, +$
 $10, 15, 12, /, +$
 $10, 1.25, +$
 $= 11.25$

→ $(4 - 16) / 5 * 3 + 10$

$4, 16, -, 5, /, 3, *, 10, +$
 $\Rightarrow +, 10, *, 3, /, 5, -, 16, 4$

$\Rightarrow +, 10, *, 3 / 5, 12 \Rightarrow +, 10, 1.25$

$\Rightarrow 11.25$

b) $(5+3) * (8-2)$

→ 5, 3, +, 8, 2, -, * → Postfix

→ 20, 6, *

→ 48

→ $(2-8) * (3+5)$

→ 2, 8, -, 3, 5, +, *

→ *, +, 5, 3, -, 8, 2 → Prefix

→ *, 8, 6

→ 48