

# CHE221A

## Assignment 06

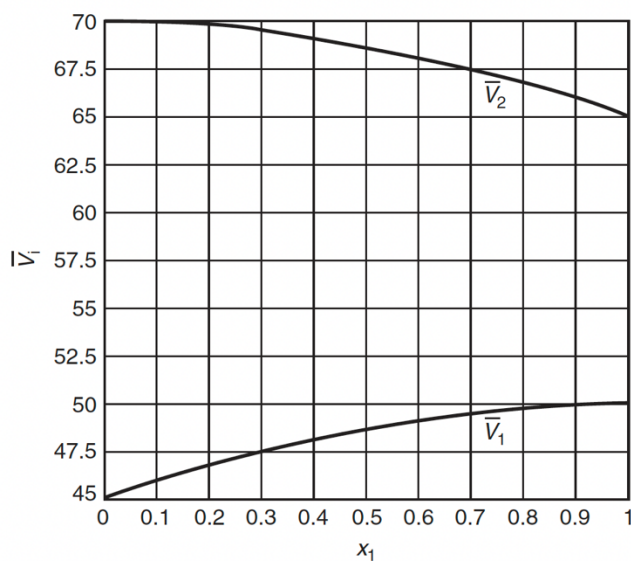
1. Consider an ideal gas mixture at 83.14 kPa and 500 K. It contains 2 moles of species A and 3 moles of species B. Calculate the following:  $\bar{V}_A$ ,  $\bar{V}_B$ ,  $v_A$ ,  $v_B$ ,  $V_A$ ,  $V_B$ ,  $V$ ,  $v$ ,  $\Delta V_{\text{mix}}$ ,  $\Delta v_{\text{mix}}$ .
2. For a given binary system at constant T and P, the molar volume (in cm<sup>3</sup>/mol) is given by

$$v = 100y_a + 80y_b + 2.5y_a y_b$$

(a) What is the pure species molar volume for species a,  $v$ ?

(b) Come up with an expression for the partial molar volume,  $\bar{V}_A$ , in terms of  $y_b$ . What is the partial molar volume at infinite dilution,  $\bar{V}_a^\infty$ ?

3. Consider a binary mixture of species 1 and species 2. A plot of the partial molar volumes in [cm<sup>3</sup>/mol] of species 1 and 2,  $\bar{V}_1$ , and  $\bar{V}_2$ , vs. mole fraction of species 1 is shown below. For a mixture of 1 mole of species 1 and 4 moles of species 2, determine the following quantities for this mixture:  $\bar{V}_1$ ,  $\bar{V}_2$ ,  $v_1$ ,  $v_2$ ,  $V_1$ ,  $V_2$ ,  $V$ ,  $v$ ,  $\Delta V_{\text{mix}}$ .



4. For a given binary system, the partial molar volume of species 1 is constant. What can you say about species 2? Explain.
5. Consider the Berthelot equation of state:
 
$$P = \frac{RT}{v - b} - \frac{a}{Tv^2}$$
  - (a) Develop an expression for the fugacity and fugacity coefficient of a pure species.
  - (b) Use the results of Problem 4.29 to write the result of part (a) in terms of reduced pressure, reduced temperature, and reduced volume.
6. Experimental data taken from 0 to 50 bar give the fugacity of a pure gas to be:

$$f = P e^{-CP}$$

where  $P$  is the pressure in bar and  $C$  is a constant that depends only on temperature. For the region of  $0^\circ\text{C}$  to  $100^\circ\text{C}$ .  $\alpha$  is given by:

$$C = -0.065 + \frac{30}{T}$$

where  $T$  is in Kelvin.

- (a) Find an equation of state for this gas that is valid from  $0^\circ\text{C}$  to  $100^\circ\text{C}$ .
  - (b) What is the molar volume (in  $\text{m}^3/\text{mole}$ ) at  $80^\circ\text{C}$  and 30 bar?
7. Consider a mixture of species 1, 2, and 3. The following equation of state is available for the vapor phase:

$$P_v = RT + P^2[A(y_1 - y_2) + B]$$

Where,

$$\frac{A}{RT} = -9.0 * 10^{-5} \left[ \frac{1}{\text{atm}^2} \right]$$

$$\frac{B}{RT} = 3.0 * 10^{-5} \left[ \frac{1}{\text{atm}^2} \right]$$

and  $y_1, y_2$  and  $y_3$  are the mole fractions of species 1, 2 and 3, respectively

A vapor mixture of 1 mole of species 1, 2 moles of species 2, and 2 moles of species 3 is cooled to 300 K at constant pressure of 50 atm, where some of it condenses into a liquid phase.

- (a) Calculate an expression for the pure species fugacity coefficient for species 1 in the vapor  $\varphi_1^v$  and the fugacity coefficient,  $\widehat{\varphi}_1^v$ , of species 1 in the mixture.
- (b) If the fugacity of species 1 in the liquid,  $\hat{f}_1^l$ , is 15 atm, calculate the mole fraction of vapor species 1 in equilibrium with the liquid

8. Verify that,

$$\left( \frac{\partial g_i}{\partial P} \right)_T = v_i = RT \left( \frac{\partial (\ln f_i)}{\partial P} \right)_T$$