

Software Tools Lab 5

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Installation

This assignment requires *symbolic* package to be installed in octave. My system is Linux.

Run in octave:

```
pkg install -forge symbolic
pkg load symbolic
```

Run in terminal: (Requires python installed)

```
$ pip install --user sympy
$ pip install --user mpmath
```

Solutions

A. Solve the following quadratic equation in Matlab and display their roots.

1) $x^2 - 7x + 12 = 0$

```
pkg load symbolic;
clc;
clear all;

syms x;
eqn = x^2 - 7*x + 12 == 0;

S = solve(eqn);

ans = double(S);
ans
```

Command Window

```
Symbolic pkg v2.9.0: Python communication link active, SymPy v1.5.1.
ans =

     3
     4

>>
```

$$2) (x - 3)^2(x - 7) = 0$$

```
pkg load symbolic;
clc;
clear all;

syms x;
eqn = ((x - 3)^2)*(x - 7) == 0;

S = solve(eqn);

ans = double(S);
ans
```

Command Window

Symbolic pkg v2.9.0: Python communication link active, SymPy v1.5.1.
ans =

```

    3
    7

>> |
```

$$3) x^4 - 7x^3 + 3x^2 - 5x + 9 = 0$$

```
pkg load symbolic;
clc;
clear all;

syms x;
eqn = x^4 - 7*x^3 + 3*x^2 - 5*x + 9 == 0;

S = solve(eqn);

ans = double(S);
ans
```

Command Window

Symbolic pkg v2.9.0: Python communication link active, SymPy v1.5.1.
ans =

```
6.63040 + 0.00000i  
-0.34509 - 1.07784i  
-0.34509 + 1.07784i  
1.05978 + 0.00000i
```

>> |

4) $6x^2 + 11x - 35 = 0$

```
pkg load symbolic;  
clc;  
clear all;  
  
syms x;  
eqn = 6*x^2 + 11*x - 35 == 0;  
  
S = solve(eqn);  
  
ans = double(S);  
ans
```

Command Window

Symbolic pkg v2.9.0: Python communication link active, SymPy v1.5.1.
ans =

```
-3.5000  
1.6667
```

>>

5) $(x - 2)^2 - 12 = 0$

```
pkg load symbolic;  
clc;  
clear all;  
  
syms x;  
eqn = (x - 2)^2 - 12 == 0;  
  
S = solve(eqn);
```

```
ans = double(S);  
ans
```

Command Window

```
Symbolic pkg v2.9.0: Python communication link active, SymPy v1.5.1.  
ans =  
  
-1.4641  
5.4641  
  
>>
```

6) $6x^5 - 41x^4 + 97x^3 - 97x^2 + 41x - 6 = 0$

```
pkg load symbolic;  
clc;  
clear all;  
  
syms x;  
eqn = 6*x^5 - 41*x^4 + 97*x^3 - 97*x^2 + 41*x - 6 == 0;  
  
S = solve(eqn);  
  
ans = double(S);  
ans
```

Command Window

```
Symbolic pkg v2.9.0: Python communication link active, SymPy v1.5.1.  
ans =  
  
0.33333  
0.50000  
1.00000  
2.00000  
3.00000  
  
>>
```

7) Find the values of x, y, z of the equations $x + y + z = 3, x + 2y + 3z = 4, x + 4y + 9z = 6$

```
pkg load symbolic;  
clc;  
clear all;
```

```

syms x y z;
eqn = [x + y + z == 3, x + 2*y + 3*z == 4, x + 4*y + 9*z == 6];

S = solve(eqn, [x y z]);

x = double(S.x);
y = double(S.y);
z = double(S.z);
x
y
z

```

Command Window

```

Symbolic pkg v2.9.0: Python communication link active, SymPy v1.5.1.
x = 2
y = 1
z = 0
>>

```

8) For $f(x) = 8x^8 - 7x^7 + 12x^6 - 5x^5 + 8x^4 + 13x^3 - 12x + 9$
compute $f(2)$, roots of $f(x)$ and plot for 0 20

```

clc;
clear all;

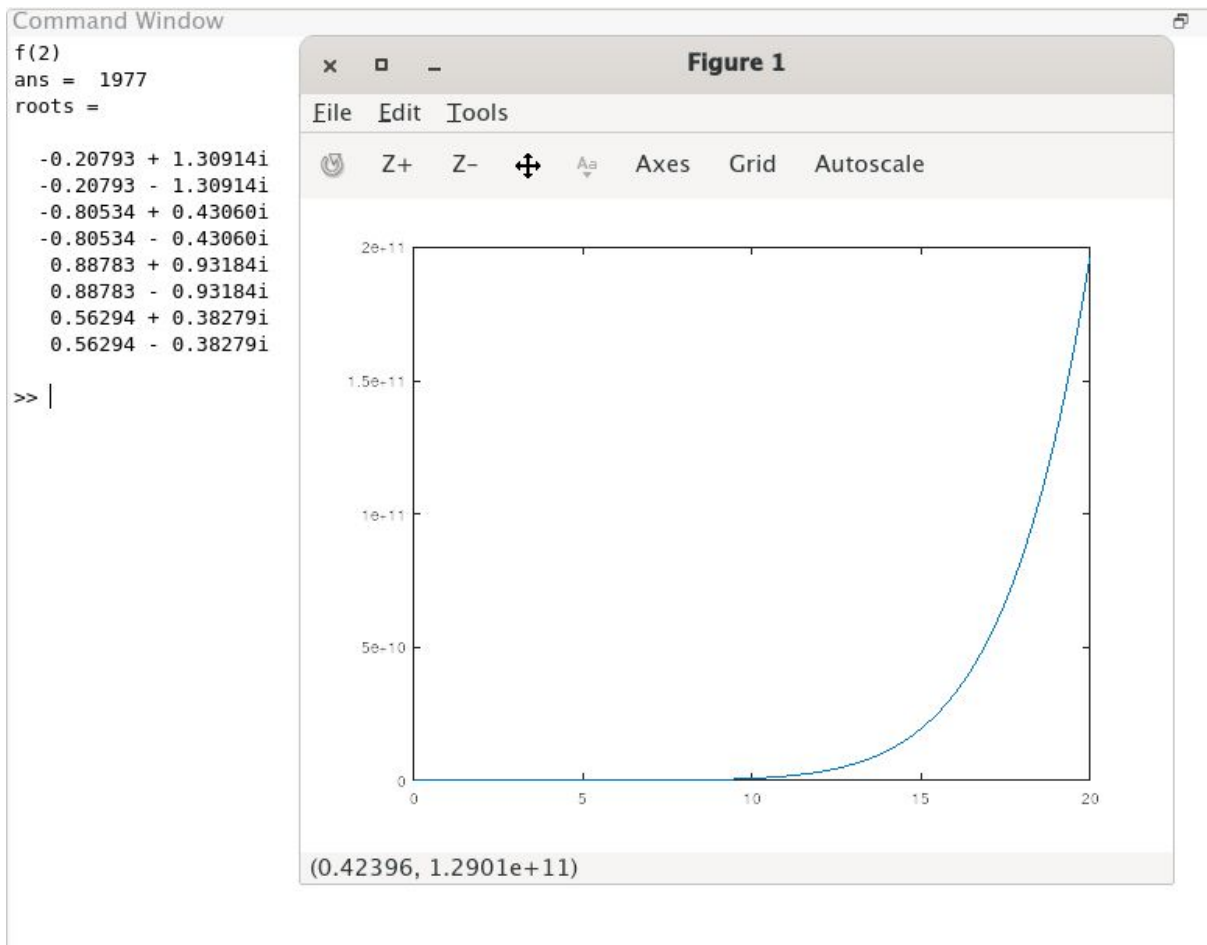
p = [8 -7 12 -5 8 13 0 -12 9];

disp("f(2)");
polyval(p, 2)

roots = roots(p)

t = [0:0.1:20];
plot(t, polyval(p, t))

```



B. Solve the following equation in Matlab.

1) $5x + 9y = 5$; $3x - 6y = 4$

```
pkg load symbolic;
clc;
clear all;

syms x y;
eqn = [5*x + 9*y == 5, 3*x - 6*y == 4];

S = solve(eqn, [x y]);

x = double(S.x);
y = double(S.y);
x
y
```

Command Window

Symbolic pkg v2.9.0: Python communication link active, SymPy v1.5.1.

```
x = 1.1579  
y = -0.087719  
>> |
```

2) $x + 3y - 2z = 5$; $3x + 5y + 6z = 7$; $2x + 4y + 3z = 8$

```
pkg load symbolic;  
clc;  
clear all;  
  
syms x y z;  
eqn = [x + 3*y - 2*z == 5, 3*x + 5*y + 6*z == 7, 2*x + 4*y + 3*z == 8];  
  
S = solve(eqn, [x y z]);  
  
x = double(S.x);  
y = double(S.y);  
z = double(S.z);  
x  
y  
z
```

Command Window

Symbolic pkg v2.9.0: Python communication link active, SymPy v1.5.1.

```
x = -15  
y = 8  
z = 2  
>>
```

3) $7x + 5y - 3z = 16$ $3x - 5y + 2z = -8$ $5x + 3y - 7z = 0$

```
pkg load symbolic;  
clc;  
clear all;  
  
syms x y z;  
eqn = [7*x + 5*y - 3*z == 16, 3*x - 5*y + 2*z == -8, 5*x + 3*y - 7*z == 0];  
  
S = solve(eqn, [x y z]);  
  
x = double(S.x);
```

```
y = double(S.y);
z = double(S.z);
x
y
z
```

Command Window

Symbolic pkg v2.9.0: Python communication link active, SymPy v1.5.1.

```
x = 1
y = 3
z = 2
>>
```

4) $3x + 2y = 16$; $7x + y = 19$

```
pkg load symbolic;
clc;
clear all;

syms x y;
eqn = [3*x + 2*y == 16, 7*x + y == 19];

S = solve(eqn, [x y]);

x = double(S.x);
y = double(S.y);
x
y
```

Command Window

Symbolic pkg v2.9.0: Python communication link active, SymPy v1.5.1.

```
x = 2
y = 5
>>
```

5) $4x + 3y = -2$; $8x - 2y = 12$

```
pkg load symbolic;
clc;
clear all;

syms x y;
eqn = [4*x + 3*y == -2, 8*x - 2*y == 12];
```



```
S = solve(eqn, [x y]);
```

```
x = double(S.x);
```

```
y = double(S.y);
```

```
x
```

```
y
```

Command Window

Symbolic pkg v2.9.0: Python communication link active, SymPy v1.5.1.

```
x = 1
```

```
y = -2
```

```
>> |
```

C. Factorize and simplify the following Algebraic equation

1) $x^2 - y^2$

```
pkg load symbolic;
```

```
clc;
```

```
clear all;
```

```
syms x y;
```

```
factor(x^2 - y^2)
```

Command Window

Symbolic pkg v2.9.0: Python communication link active, SymPy v1.5.1.

```
ans = (sym) (x - y)·(x + y)
```

```
>> |
```

2) $x^3 + y^3$

```
pkg load symbolic;
```

```
clc;
```

```
clear all;
```

```
syms x y;
```

```
factor(x^3 + y^3)
```

Command Window

Symbolic pkg v2.9.0: Python communication link active, SymPy v1.5.1.

ans = (sym)

$$(x + y) \cdot \begin{pmatrix} x^2 & -x \cdot y & y^2 \end{pmatrix}$$

>>

3) $(x^4 - 16) / (x^2 - 4)$

```
pkg load symbolic;
```

```
clc;
```

```
clear all;
```

```
syms x y;
```

```
factor((x^4 - 16)/(x^2 - 4))
```

Command Window

Symbolic pkg v2.9.0: Python communication link active, SymPy v1.5.1.

ans = (sym)

$$x^2 + 4$$

>>

4) $x^4 + y^4$

```
pkg load symbolic;
```

```
clc;
```

```
clear all;
```

```
syms x y;
```

```
factor(x^4 + y^4)
```

Command Window

Symbolic pkg v2.9.0: Python communication link active, SymPy v1.5.1.

ans = (sym)

$$x^4 + y^4$$

>>

5) $x^5 - y^5$

```
pkg load symbolic;
clc;
clear all;

syms x y;
factor(x^5 - y^5)
```

Command Window

```
Symbolic pkg v2.9.0: Python communication link active, SymPy v1.5.1.
ans = (sym)
      4      3      2 2      3      4
(x - y)·(x + x·y + x·y + x·y + y )
>>
```

D. Find the limit of following functions

1) $\lim_{x \rightarrow 0} \frac{x^3 + 5}{x^4 + 7}$

```
pkg load symbolic;
clc;
clear all;

syms x;
f = (x^3 + 5)/(x^4 + 7);

limit(f, x, 0)
```

Command Window

```
Symbolic pkg v2.9.0: Python communication link active, SymPy v1.5.1.
ans = (sym) 5/7
>>
```

$$2) \lim_{x \rightarrow 1} \frac{x-3}{x-1}$$

```
pkg load symbolic;
clc;
clear all;

syms x;
f = (x - 3)/(x - 1);

limit(f, x, 1)
```

Command Window

```
Symbolic pkg v2.9.0: Python communication link active, SymPy v1.5.1.
ans = (sym) -∞
>>
```

$$3) \lim_{x \rightarrow 1} \frac{1-\sqrt{x}}{1-x}$$

```
pkg load symbolic;
clc;
clear all;

syms x;
f = (1 - x^(0.5))/(1 - x);

limit(f, x, 0)
```

Command Window

```
Symbolic pkg v2.9.0: Python communication link active, SymPy v1.5.1.
warning: passing floating-point values to sym is dangerous, see "help sym"
warning: called from
    double_to_sym_heuristic at line 50 column 7
    sym at line 379 column 13
    mpower at line 76 column 5
    qd3 at line 6 column 3
ans = (sym) 1
>>
```

$$4) \lim_{x \rightarrow 0} \frac{\sin 5x}{3x}$$

```
pkg load symbolic;
clc;
clear all;

syms x;
f = (sin(5*x))/(sin(3*x));

limit(f, x, 0)
```

Command Window

```
Symbolic pkg v2.9.0: Python communication link active, SymPy v1.5.1.
ans = (sym) 5/3
>> |
```

E. Show that limit of given function does not exist using left and right sided limits and also plot the graph for it.

```
pkg load symbolic;
clc;
clear all;

syms x;
f = (x - 3)/abs(x - 3);

left_limit = limit(f, x, 3, 'left')
right_limit = limit(f, x, 3, 'right')
left_limit == right_limit

t = [-10:0.1:10];
y = (t - 3)./abs(t - 3);

plot(t, y)
axis([-10 10 -2 2])
```

Command Window

Symbolic pkg v2.9.0: Python communication link active, SymPy v1.5.1.

```
left_limit = (sym) -1
```

```
right_limit = (sym) 1
```

```
ans = (sym) False
```

```
> |
```

