

# Taylor approximation

## import library

In [168]:



```
import numpy as np
import matplotlib.image as img
import matplotlib.pyplot as plt
from matplotlib import cm
import matplotlib.colors as colors
```

## define a function $f(x) = \cos(x)$

In [169]:



```
def function(x):

    # ++++++
    # complete the blanks
    #
    y = np.cos(x)

    #
    # ++++++

    return y
```

## define the derivative $f'(x)$ of function $f(x)$

In [170]:



```
def derivative_function(x):

    # ++++++
    # complete the blanks
    #
    y_prime = np.sin(-x)
    #
    # ++++++

    return y_prime
```

## define the first order Taylor approximation of the function at $x_0$

- $\hat{f}(x) = f(x_0) + f'(x_0)(x - x_0)$

In [191]:



```
def approximate_function(x, x0):  
  
    # ++++++  
    # complete the blanks  
    #  
    y_hat = function(x0) + derivative_function(x0)*(x-x0)  
    #  
    # ++++++  
  
    return y_hat
```

## functions for presenting the results

In [117]:



```
def function_result_01():  
  
    x = np.linspace(-10, 10, 100)  
    y = function(x)  
  
    plt.figure(figsize=(8,6))  
    plt.plot(x, y, 'b')  
    plt.xlim([-10, 10])  
    plt.ylim([-10, 10])  
    plt.show()
```

In [102]:



```
def function_result_02():  
  
    x = np.linspace(-10, 10, 100)  
    y_prime = derivative_function(x)  
  
    plt.figure(figsize=(8,6))  
    plt.plot(x, y_prime, 'r')  
    plt.xlim([-10, 10])  
    plt.ylim([-10, 10])  
    plt.show()
```

In [103]:



```
def function_result_03():

    x = np.linspace(-10, 10, 100)
    y = function(x)

    x0      = 1
    y0      = function(x0)
    y_hat   = approximate_function(x, x0)

    plt.figure(figsize=(8,6))
    plt.plot(x, y, 'b')
    plt.plot(x, y_hat, 'r')
    plt.plot(x0, y0, 'go')
    plt.xlim([-10, 10])
    plt.ylim([-10, 10])
    plt.show()
```

In [104]:



```
def function_result_04():

    x1      = -1
    x2      = 1
    value1   = function(x1)
    value2   = function(x2)

    print('value1 = ', value1)
    print('value2 = ', value2)
```

In [172]:



```
def function_result_05():

    x1      = -1
    x2      = 1
    value1   = derivative_function(x1)
    value2   = derivative_function(x2)

    print('value1 = ', value1)
    print('value2 = ', value2)
```

---

## results

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In [189]:

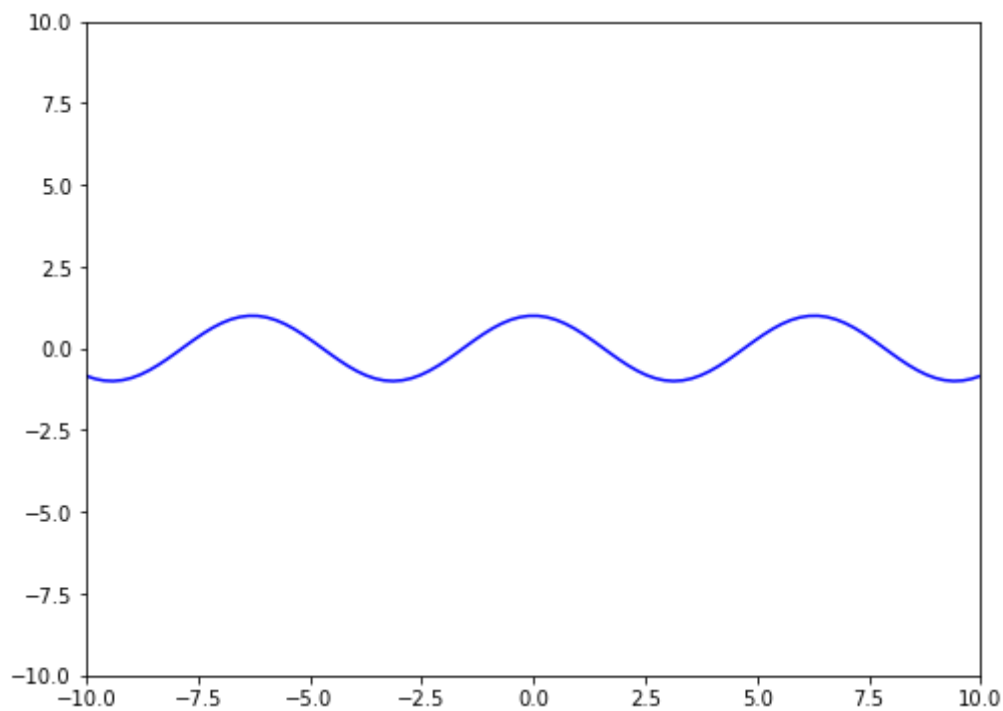


```
number_result = 5

for i in range(number_result):
    title = '## [RESULT {:02d}]'.format(i+1)
    name_function = 'function_result_{:02d}()'.format(i+1)

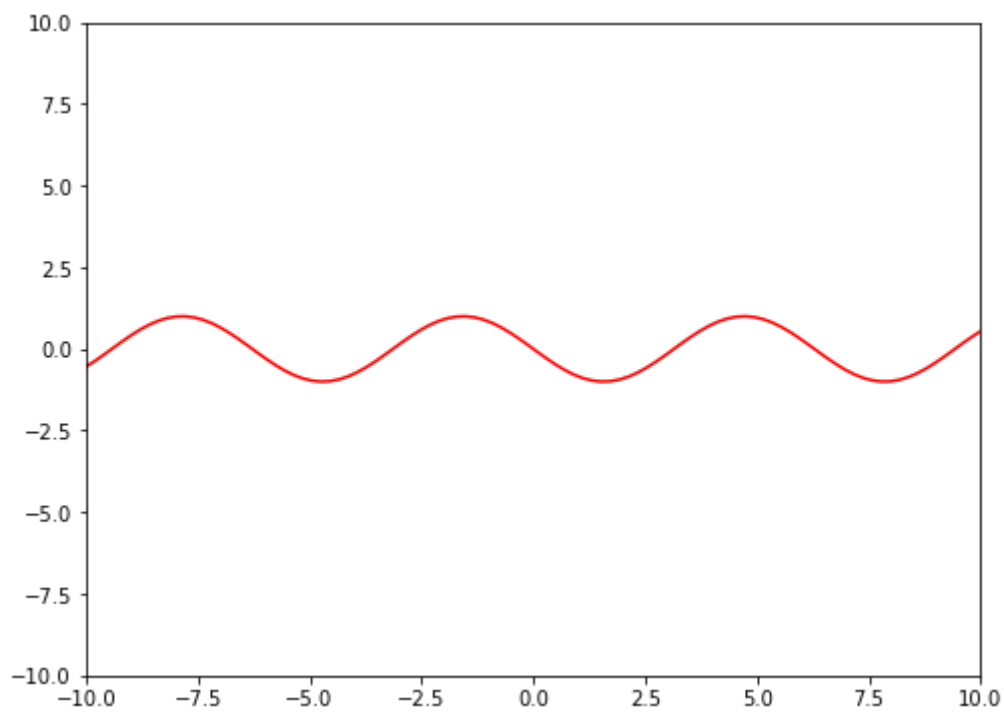
    print('*****')
    print(title)
    print('*****')
    eval(name_function)
```

```
*****
## [RESULT 01]
*****
```

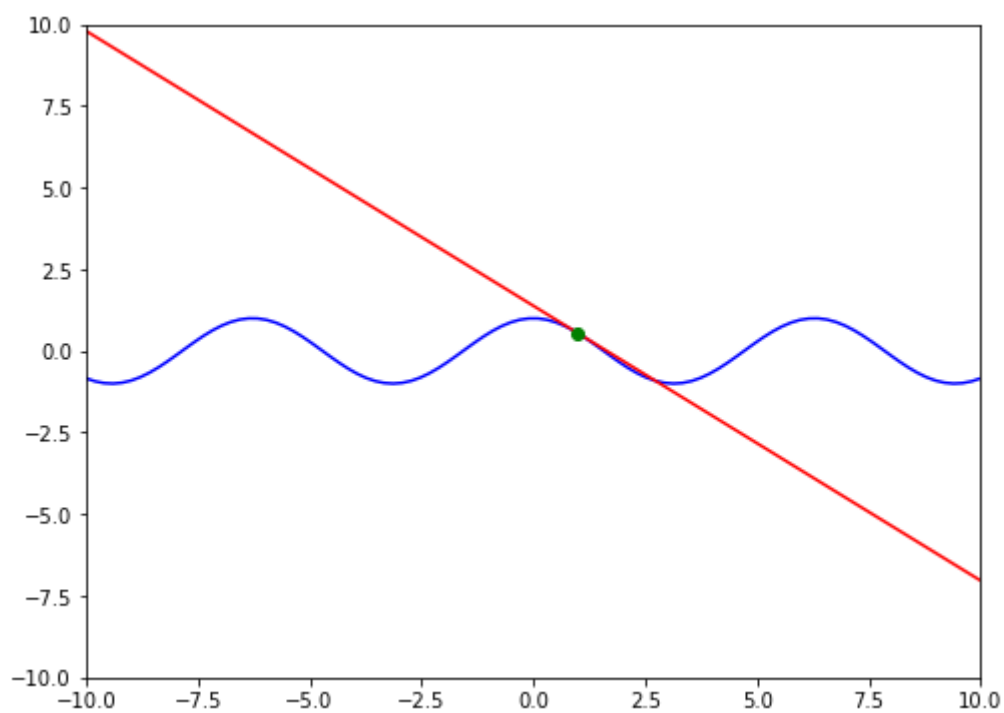


```
*****
## [RESULT 02]
*****
```





```
*****
## [RESULT 03]
*****
```



```
*****
## [RESULT 04]
*****
value1 = 0.5403023058681398
value2 = 0.5403023058681398
*****
## [RESULT 05]
*****
value1 = 0.8414709848078965
value2 = -0.8414709848078965
```

In [ ]:



In [ ]:

