Taylor approximation

import library

In [168]:

```
import numpy as np
import matplotlib.image as img
import matplotlib.pyplot as plt
from matplotlib import cm
import matplotlib.colors as colors
```

define a function $f(x) = cos(x)$

In [169]:

```
def function(x):

    # ++++++++++++++++++++++++++++++++++++++++++++++++++
    # complete the blanks
    #
    y = np.cos(x)


    #
    # ++++++++++++++++++++++++++++++++++++++++++++++++++

    return y
```

define the derivative $f'(x)$ of function $f(x)$

In [170]:

```
def derivative_function(x):

    # ++++++++++++++++++++++++++++++++++++++++++++++++++
    # complete the blanks
    #
    y_prime = np.sin(-x)
    #
    # ++++++++++++++++++++++++++++++++++++++++++++++++++

    return y_prime
```

define the first order Taylor approxation of the function at x_0

- $\hat{f}(x) = f(x_0) + f'(x_0)(x - x_0)$

In [185]:

```
def approximate_function(x, x0):

    # ++++++++++++++++++++++++++++++++++++++++++++++++++
    # complete the blanks
    #
    y_hat = function(x) + derivative_function(x)*(x-x0)
    #
    # ++++++++++++++++++++++++++++++++++++++++++++++++++

    return y_hat
```

functions for presenting the results

In [117]:

```
def function_result_01():

    x = np.linspace(-10, 10, 100)
    y = function(x)

    plt.figure(figsize=(8,6))
    plt.plot(x, y, 'b')
    plt.xlim([-10, 10])
    plt.ylim([-10, 10])
    plt.show()
```

In [102]:

```
def function_result_02():

    x       = np.linspace(-10, 10, 100)
    y_prime = derivative_function(x)

    plt.figure(figsize=(8,6))
    plt.plot(x, y_prime, 'r')
    plt.xlim([-10, 10])
    plt.ylim([-10, 10])
    plt.show()
```

In [103]:

```
def function_result_03():

    x = np.linspace(-10, 10, 100)
    y = function(x)

    x0      = 1
    y0      = function(x0)
    y_hat   = approximate_function(x, x0)

    plt.figure(figsize=(8,6))
    plt.plot(x, y, 'b')
    plt.plot(x, y_hat, 'r')
    plt.plot(x0, y0, 'go')
    plt.xlim([-10, 10])
    plt.ylim([-10, 10])
    plt.show()
```

In [104]:

```
def function_result_04():

    x1      = -1
    x2      = 1
    value1  = function(x1)
    value2  = function(x2)

    print('value1 = ', value1)
    print('value2 = ', value2)
```

In [172]:

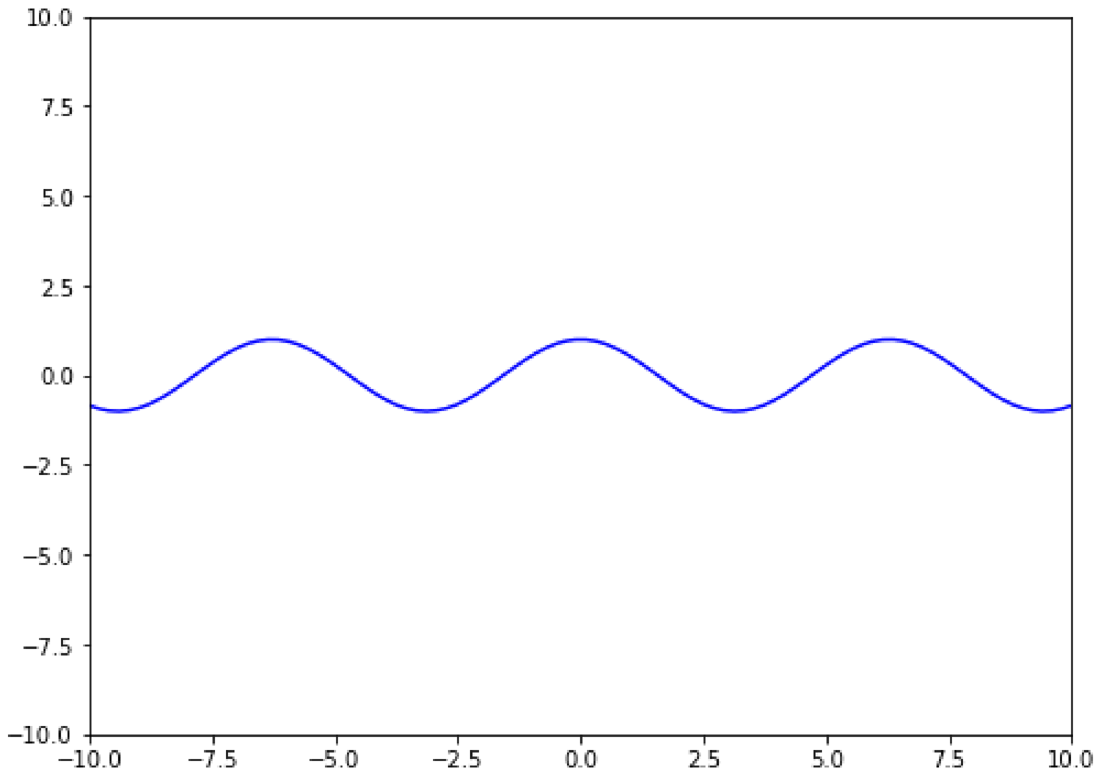
```
def function_result_05():

    x1      = -1
    x2      = 1
    value1  = derivative_function(x1)
    value2  = derivative_function(x2)

    print('value1 = ', value1)
    print('value2 = ', value2)
```

results

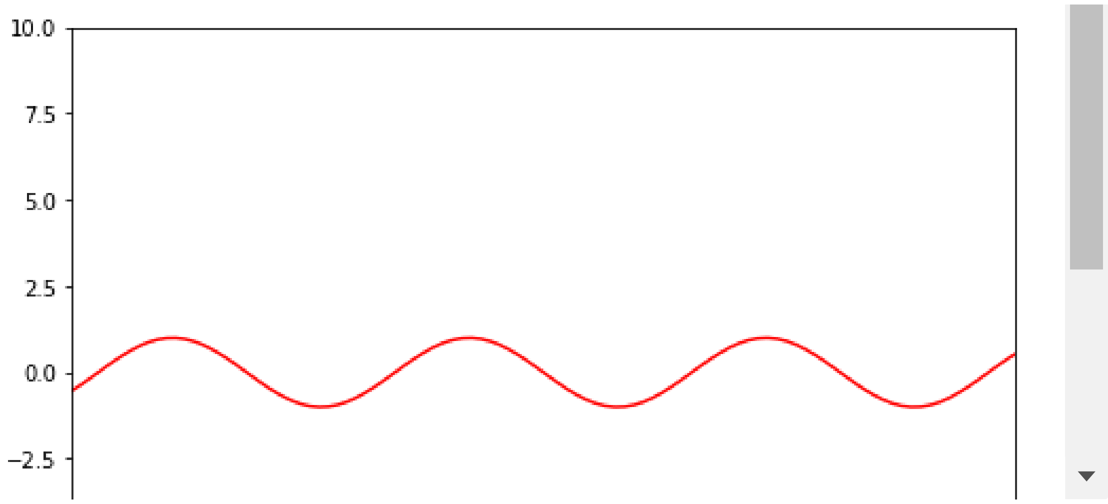
In [186]:

```
number_result = 5

for i in range(number_result):
    title = '## [RESULT {:02d}]'.format(i+1)
    name_function = 'function_result_{:02d}()'.format(i+1)

    print('***************************************************')
    print(title)
    print('***************************************************')
    eval(name_function)
```

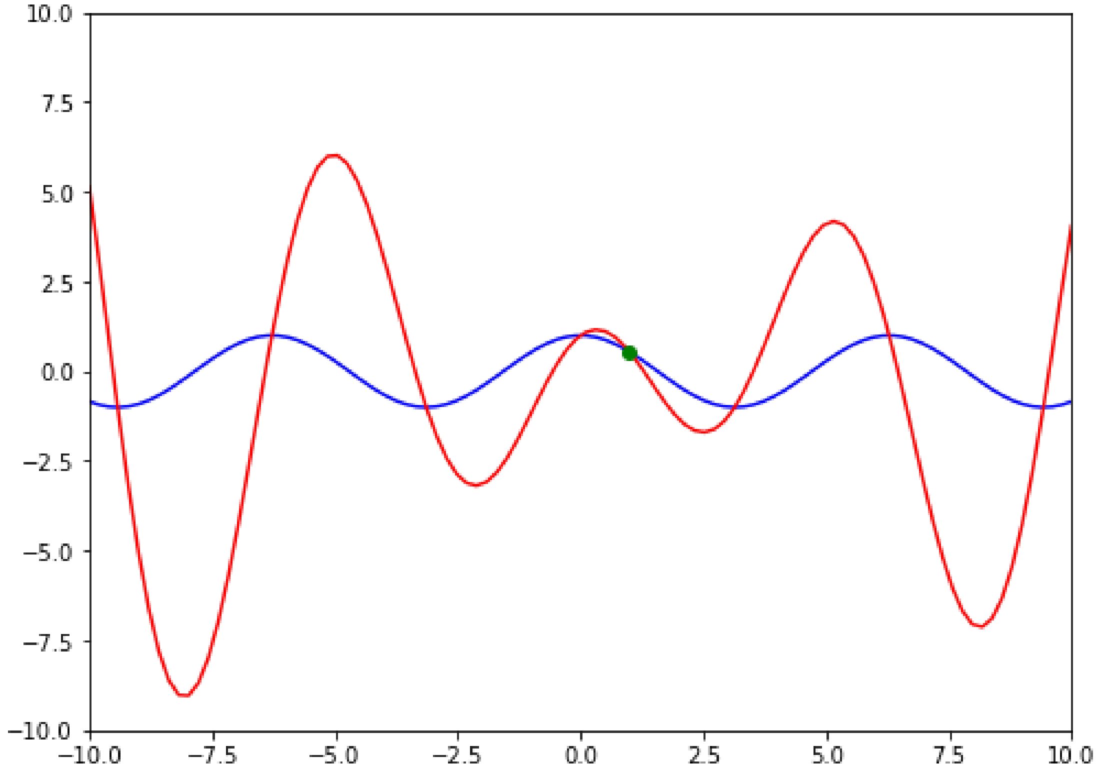
```
***************************************************
## [RESULT 01]
***************************************************
```




```
***************************************************
## [RESULT 02]
***************************************************
```




```
**************************************************
## [RESULT 03]
**************************************************
```




```
**************************************************
## [RESULT 04]
**************************************************
value1 =  0.5403023058681398
value2 =  0.5403023058681398
**************************************************
## [RESULT 05]
**************************************************
value1 =  0.8414709848078965
value2 =  -0.8414709848078965
```

In [ ]:

In [ ]: