## Deep Quiz 2

Date: 19.10.2022

Alloted time: 45 minutes Total marks: 15

## **Instructions:**

- There are a total of 3 questions.
- Discussions amongst the students are not allowed. No electronic devices nor notes/books of any kind are allowed.
- Any dishonesty shall be penalized heavily.
- Place your identity cards on the table for verification.
- Be clear in your arguments. Partial marking is available but vague arguments shall not be given any
  credit.

Question 1 [3 marks]

Let G = (V, E) be a directed graph and for every edge  $u \to v \in E$ , a capacity  $c(u \to v)$  is defined. Let  $f(u \to v)$  (for all  $u \to v \in E$ ) be a given feasible flow. Compute the residual capacities and the residual graph, with respect to f.

Ouestion 2 [5 marks]

Let n be an integer which is much larger than 5. Formulate a recursive function to compute the number of ways of providing change for n rupees only using (sufficient supply of) 1 rupee and 2 rupee coins.

Question 3 [7 marks]

Suppose you are given three strings,  $S_1$ ,  $S_2$ , and  $S_3$ , where  $|S_1| = n$ ,  $|S_2| = m$ , and  $|S_3| = m+n$ . We say that  $S_3$  is an interleaf of  $S_1$  and  $S_2$  if and only if  $S_3$  can be formed by interleaving sequences of characters from  $S_1$  and  $S_2$  in a way that maintains the left-to-right ordering of  $S_1$  and  $S_2$ . For example, "split" is an interleaving of "spit" and "l", but "splti" is not, and "cchocohilaptes" is an interleaf of "chocolate" and "chips".

Give an efficient dynamic programing algorithm<sup>1</sup> that takes  $S_1$ ,  $S_2$ , and  $S_3$  as parameters and determines whether  $S_3$  is an in interleaf of  $S_1$  and  $S_2$ .

<sup>&</sup>lt;sup>1</sup>Hint: Memoization matrix could take True or False values in each entry where True in entry  $M_{i,j}$  could represent if the first i+j letters of  $S_3$  are formed by interleaving of first i letters of  $S_1$  and first j letters of  $S_2$ .