Question 1: Please refer to the class notes for more

details.
Assumption:
$$C_f(u \rightarrow v) = \begin{cases} C(u \rightarrow v) - f(u \rightarrow v) & \text{if } u \rightarrow v \in E, \\ f(v \rightarrow u) & \text{if } v \rightarrow u \in E, \\ 0 & \text{otherwise.} \end{cases}$$
No parallel edges

No parallel edges in the graph.

2 marks for this defu.

Residual graph: Gres = (V, Eves) // Vertex set vernains

 $u \rightarrow 0 \in \mathcal{E}_{\text{res}}$ iff $C_{f}(u \rightarrow 0) > 0$.

I made for this.

Question 2:

Case: Ordering matters

Recursive: f(n) = f(n-1) + f(n-2)defin

Base cases: f(1)=1, f(2)=2.

Case: Ordering does not matter.

Earstralently, we are looking for no. of integral solutions to 22+y=n.

 $N(n, x, y) = \sum_{i=1}^{N/2} N(n, x, i)$ No. of integral slns to 2x+y=n# of integral solutions

Give parkal marking as you destre.

Dueston 3: Follow the hint. I make for the set up. For $i \in [0,n]$ and $j \in [0,m]$

 $M_{i,j}$ entry is 1 if $S_3[1,i+j]$ is formed by interleaving of $S_1[1,i]$ and $S_2[1,j]$ in some order.

Consider Mixij. This is true if Mi; is true and ?
if $S_1[i+i] = S_3[i+j+i]$.

2 marks for this

Similarly, Mi,ju is true if Mi,j is true and $S_3[j+1] = S_3[i+j+1]$. 2 marks for this

Base cases: $M_{0,j} = \text{true iff } S_{1,j} = S_{2}[1,j] + j \in [1,m]$ 2 marks $M_{i,0} = \text{true iff } S_{3}[1,i] = S_{1}[1,i] + i \in [1,n]$

for base case.

Moo = true.