

PSet 11

4E-2 $x = t + \frac{1}{t}$ $y = t - \frac{1}{t}$

$$x^2 = t^2 + 2 + \frac{1}{t^2} \quad y^2 = t^2 - 2 + \frac{1}{t^2}$$

$$y^2 - x^2 = \cancel{t^2} - 2 + \cancel{\frac{1}{t^2}} - (\cancel{t^2} + 2 + \cancel{\frac{1}{t^2}})$$

$$y^2 - x^2 = -4$$

$$x^2 - y^2 = 4 \quad \checkmark$$

4E-3 $x = 1 + \sin t$ $y = 4 + \cos t$

$$(1 + \sin t)^2 + (4 + \cos t)^2 = 1 + 2\sin t + \sin^2 t + 16 + 8\cos t + \cos^2 t$$

$$\Rightarrow (1 + 16 + \sin^2 t + \cos^2 t) + 2\sin t + 8\cos t$$

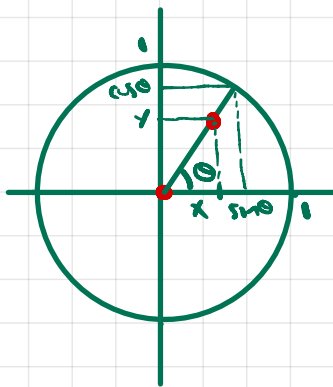
$$\Rightarrow x^2 + y^2 = 18 + 2\sin t + 8\cos t = 18 + 2(x-1) + 8(y-4) = 18 - 2 - 32 + 2x + 8y$$

$$\Rightarrow x^2 - 2x + y^2 - 8y = -16$$

$$(x^2 - 2x + 1) + (y^2 - 8y + 16) = -16 + 16 + 1$$

$$\Rightarrow (x-1)^2 + (y-4)^2 = 1 \quad \checkmark$$

4E-8



$$\theta(t) = \frac{\pi}{2} - \frac{3\pi}{12}t = \frac{6\pi - 3\pi t}{12} = \frac{3\pi - \pi t}{6} = \frac{\pi}{6}(3-t)$$

$$\theta(1) = \frac{\pi}{3}$$

$$r(1) = 1, r(0) = 0, r(t) = t$$

$$r(t) = t \quad \theta(t) = \frac{\pi}{6}(3-t) \Rightarrow \theta = \frac{\pi}{6}(3-r) \Rightarrow 6\theta = 3\pi - \pi r$$

$$\Rightarrow \pi r = 3\pi - 6\theta \Rightarrow r = 3 - \frac{6}{\pi}\theta$$

$$x = r \cos \theta = t \cdot \cos\left[\frac{\pi}{6}(3-t)\right] \quad \checkmark$$

$$y = r \sin \theta = t \cdot \sin\left[\frac{\pi}{6}(3-t)\right]$$

