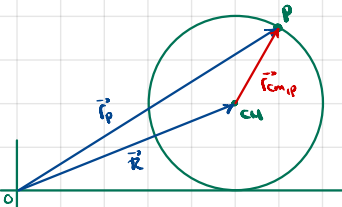


## The wheel



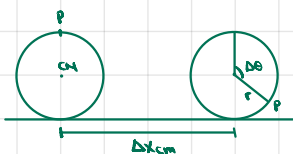
The wheel rotates with angular speed  $|\omega(t)| = |\dot{\theta}(t)|$ . Points on the rim have tangential speed  $R|\omega(t)|$ , relative to the CM.

From the ground frame the velocity vector has two components:  $\vec{v}_{CM}$ , and  $\vec{v}_{CM,P}$ .

$\vec{v}_{CM}$  is just a horizontal vector when the wheel is rolling on a flat surface as above.

$\vec{v}_{CM,P} = -r\omega(t)\hat{\theta}$ . This vector is different at each point on the wheel.

Not slipping or skidding means the displacement of the CM  $\Delta x_{CM}$  equals the arc length displacement of a point on the rim.



$$s = r\Delta\theta = \Delta x_{CM} = v_{CM}\Delta t$$

$$\Rightarrow v_{CM,avg} = r \frac{\Delta\theta}{\Delta t}$$

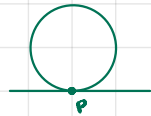
$$\lim v_{CM,avg} = \lim r \frac{\Delta\theta}{\Delta t}$$

$$\Rightarrow v_{CM} = r\omega(t)$$

The CM component of velocity from ground frame needs to have magnitude equal to the tangential speed of a point on the rim.

If  $v_{CM} \neq r\omega$  then the wheel is either slipping ( $v_{CM} < r\omega$ ) or skidding ( $v_{CM} > r\omega$ ).

The no-slipping condition  $v_{CM} = r\omega$  has implications for the contact point of the wheel w/ the ground.



$$\vec{v}_{S,P} = \vec{v}_{CM} + \vec{v}_{CM,P}$$

$$|\vec{v}_{CM}| = r\omega$$

$$|\vec{v}_{CM,P}| = r\omega$$

$$\vec{v}_{S,P} = r\omega\hat{i} - r\omega\hat{i} = \vec{0}$$

Point of contact is at rest relative to the ground.

## Friction