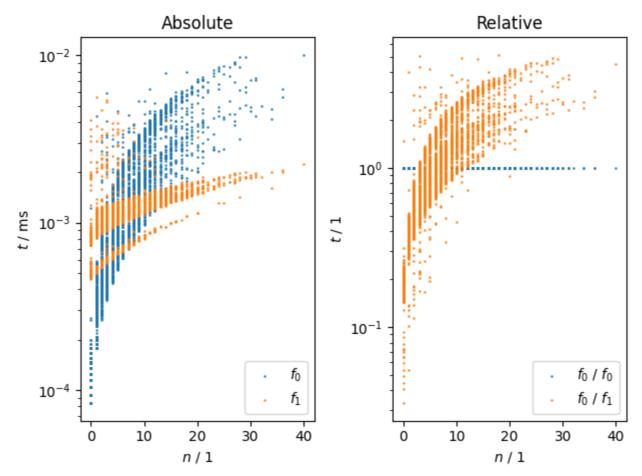
profiling

```
In [1]: import numpy as np
        import matplotlib.pyplot as plt
        from random import random
        def randt(n):
            return tuple(random() for _ in range(n))
        def isclose(*a):
            return all(np.isclose(a[0], ai) for ai in a[1:])
        def allclose(*a):
            return all(np.allclose(a[0], ai) for ai in a[1:])
        def compare(x, *ys, title=None):
            fig, axs = plt.subplots(ncols=2, sharex=True)
            for i, y in enumerate(ys):
                 axs[0].scatter(x, np.multiply(y, 1e3), marker='o', s=(72./fig.dpi
            axs[0].set_yscale('log')
            axs[0].set_xlabel('$n$ / 1')
            axs[0].set_ylabel('$t$ / ms')
            axs[0].legend()
            axs[0].set_title('Absolute')
            for i, y in enumerate(ys):
                axs[1].scatter(x, np.divide(ys[0], y), marker='o', s=(72./fig.dpi
            #axs[1].axhline(1, linestyle='--', lw=0.5)
            axs[1].set_yscale('log')
            axs[1].set_xlabel('$n$ / 1')
            axs[1].set_ylabel('$t$ / 1')
            axs[1].set_title('Relative')
            axs[1].legend()
            plt.tight_layout()
            plt.show()
        #def measure(supplier, *f, N=10000, n=4):
        #
             x, y = [], [[] for \_ in range(len(f))]
             for _ in range(N):
        #
        #
                 args = supplier()
        #
                 x += [args[0]]
        #
                 args = args[1:]
        #
                 try:
        #
                     assert all(np.isclose(f[0](*args), fi(*args)) for fi in f[1:
        #
                 except ValueError:
        #
                      assert all(np.allclose(f[0](*args), fi(*args)) for fi in f[1
        #
                  for fi, yi in zip(f, y):
        #
                     yi += [timeit(lambda: fi(*args), number=n) / n]
             return x, *y
```

trim

```
In [2]: def trim0(v, tol):
            while v and abs(v[-1])<=tol:
                v = v[:-1]
            return v
        def trim1(v, tol):
            return v[:len(v)-next((i for i, vi in enumerate(reversed(v)) if abs(v
In [3]: from random import randint
        from timeit import timeit
        N = 4 #number of executions in timeit
        tol = 0.8
        x, y0, y1 = [], [], []
        for _ in range(10000):
            v = randt(randint(0, 100))
            assert trim0(v, tol) == trim1(v, tol)
            x += [len(v)-len(trim0(v, tol))]
            y0 += [timeit(lambda: trim0(v, tol), number=N) / N]
            y1 += [timeit(lambda: trim1(v, tol), number=N) / N]
        compare(x, y0, y1)
```



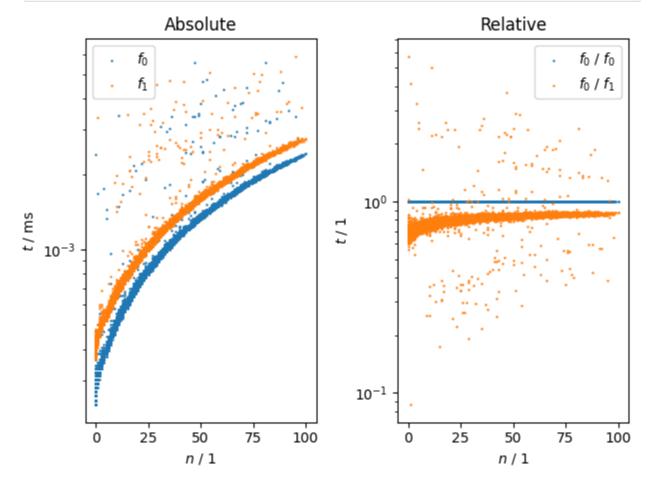
dot

```
In [4]: from itertools import starmap
from operator import mul
```

```
def dot0(v, w):
    return sum(map(mul, v, w))

def dot1(v, w):
    #https://docs.python.org/3/library/itertools.html
    return sum(starmap(mul, zip(v, w)))
```

```
In [5]: x, y0, y1 = [], [], []
for _ in range(10000):
    v, w = randt(randint(0, 100)), randt(randint(0, 100))
    assert isclose(dot0(v, w), dot1(v, w))
    x += [min(len(v), len(w))]
    y0 += [timeit(lambda: dot0(v, w), number=N) / N]
    y1 += [timeit(lambda: dot1(v, w), number=N) / N]
compare(x, y0, y1)
```



norm

```
In [6]: from math import sqrt, sumprod, hypot

def norm0(v):
    return hypot(*v)

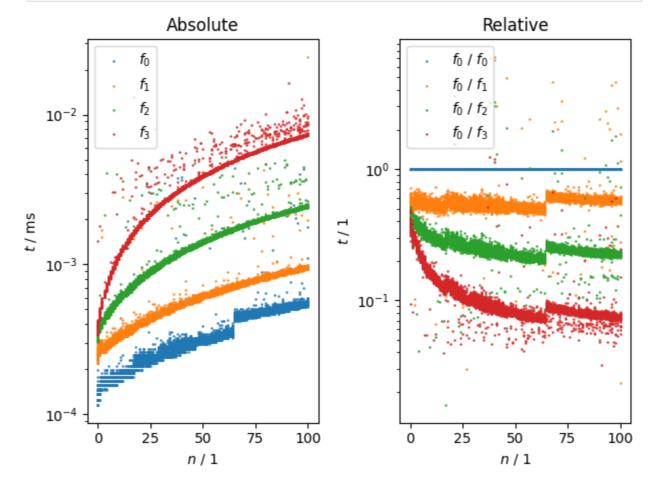
def norm1(v):
    return sqrt(sumprod(v, v))

def dot(v, w):
    return sum(map(mul, v, w))
```

```
def norm2(v):
    return sqrt(dot(v, v))

def norm3(v):
    return sqrt(sum(vi**2 for vi in v))
```

```
In [7]: x, y0, y1, y2, y3 = [], [], [], [], []
for _ in range(10000):
    v = randt(randint(0, 100))
    assert isclose(norm0(v), norm1(v), norm2(v), norm3(v))
    x += [len(v)]
    y0 += [timeit(lambda: norm0(v), number=N) / N]
    y1 += [timeit(lambda: norm1(v), number=N) / N]
    y2 += [timeit(lambda: norm2(v), number=N) / N]
    y3 += [timeit(lambda: norm3(v), number=N) / N]
    compare(x, y0, y1, y2, y3)
```



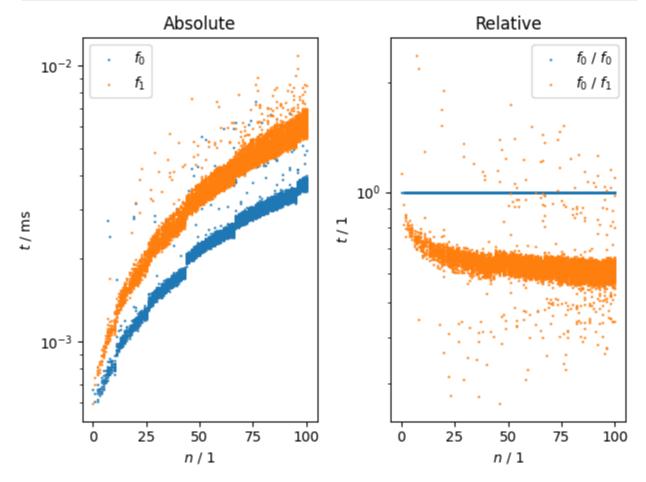
add

```
In [8]: from itertools import zip_longest
from operator import add

def add0(v, w):
    return tuple(starmap(add, zip_longest(v, w, fillvalue=0)))

def add1(v, w):
    return tuple(vi+wi for vi, wi in zip_longest(v, w, fillvalue=0))
```

```
In [9]: x, y0, y1 = [], [], []
for _ in range(10000):
    v, w = randt(randint(0, 100)), randt(randint(0, 100))
    assert allclose(add0(v, w), add1(v, w))
    x += [max(len(v), len(w))]
    y0 += [timeit(lambda: add0(v, w), number=N) / N]
    y1 += [timeit(lambda: add1(v, w), number=N) / N]
compare(x, y0, y1)
```



addscalar

```
In [10]: from itertools import repeat

def addscalar0(v, a):
    return tuple(map(add, v, repeat(a)))

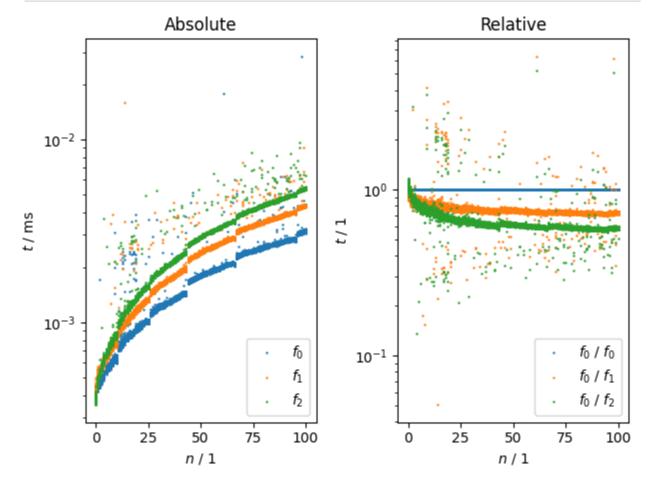
def addscalar1(v, a):
    return tuple(vi+a for vi in v)

def addscalar2(v, a):
    return tuple(map(lambda vi: vi+a, v))

In [11]:

x, y0, y1, y2 = [], [], [], []
for _ in range(10000):
    v, a = randt(randint(0, 100)), random()
    assert allclose(addscalar0(v, a), addscalar1(v, a), addscalar2(v, a))
    x += [len(v)]
```

```
y0 += [timeit(lambda: addscalar0(v, a), number=N) / N]
y1 += [timeit(lambda: addscalar1(v, a), number=N) / N]
y2 += [timeit(lambda: addscalar2(v, a), number=N) / N]
compare(x, y0, y1, y2)
```



sub

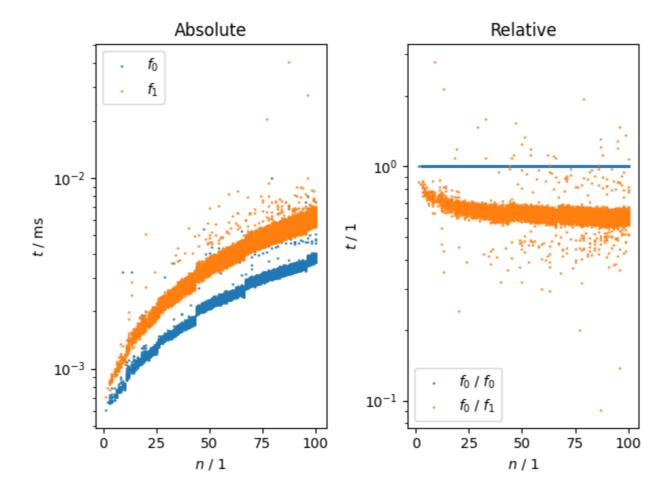
```
In [12]: from operator import sub

def sub0(v, w):
    return tuple(starmap(sub, zip_longest(v, w, fillvalue=0)))

def sub1(v, w):
    return tuple(vi-wi for vi, wi in zip_longest(v, w, fillvalue=0))

In [13]:

x, y0, y1 = [], [], []
for _ in range(10000):
    v, w = randt(randint(0, 100)), randt(randint(0, 100))
    assert allclose(sub0(v, w), sub1(v, w))
    x += [max(len(v), len(w))]
    y0 += [timeit(lambda: sub0(v, w), number=N) / N]
    y1 += [timeit(lambda: sub1(v, w), number=N) / N]
    compare(x, y0, y1)
```



subscalar

```
In [14]: def subscalar0(v, a):
    return tuple(map(sub, v, repeat(a)))

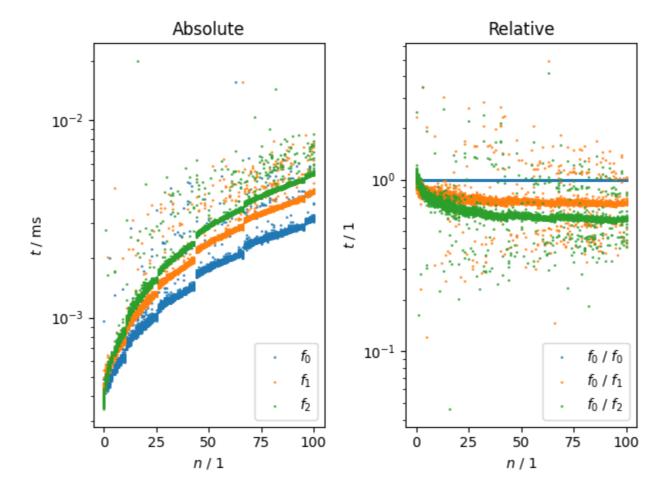
def subscalar1(v, a):
    return tuple(vi-a for vi in v)

def subscalar2(v, a):
    return tuple(map(lambda vi: vi-a, v))

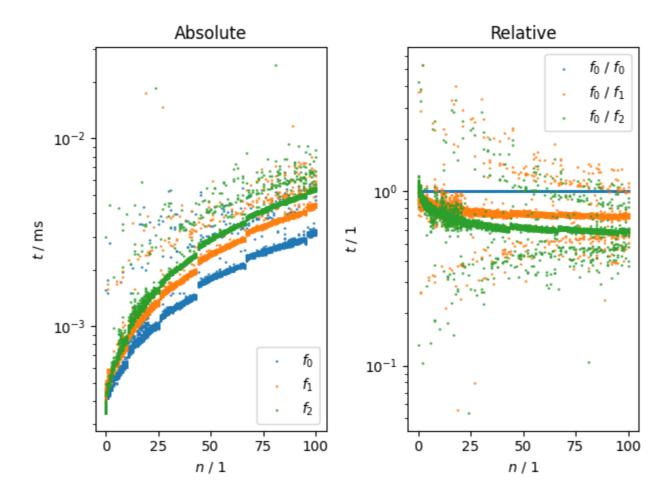
In [15]:

x, y0, y1, y2 = [], [], [], []

for _ in range(10000):
    v, a = randt(randint(0, 100)), random()
    assert allclose(subscalar0(v, a), subscalar1(v, a), subscalar2(v, a))
    x += [len(v)]
    y0 += [timeit(lambda: subscalar0(v, a), number=N) / N]
    y1 += [timeit(lambda: subscalar1(v, a), number=N) / N]
    y2 += [timeit(lambda: subscalar2(v, a), number=N) / N]
    compare(x, y0, y1, y2)
```



mul

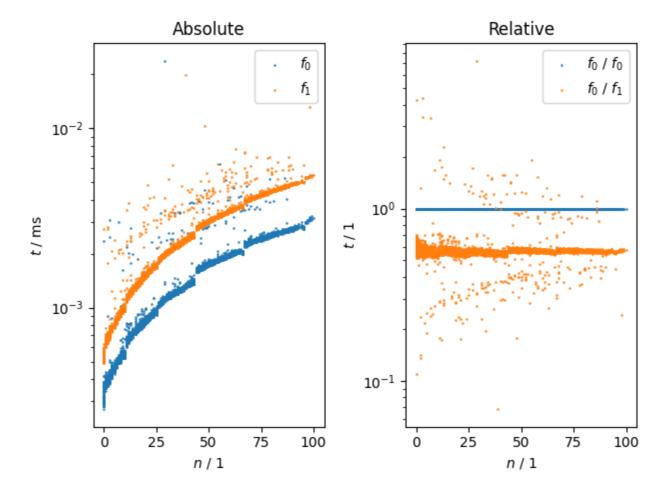


mulelementwise

```
In [18]: def mulelementwise0(v, w):
    return tuple(map(mul, v, w))

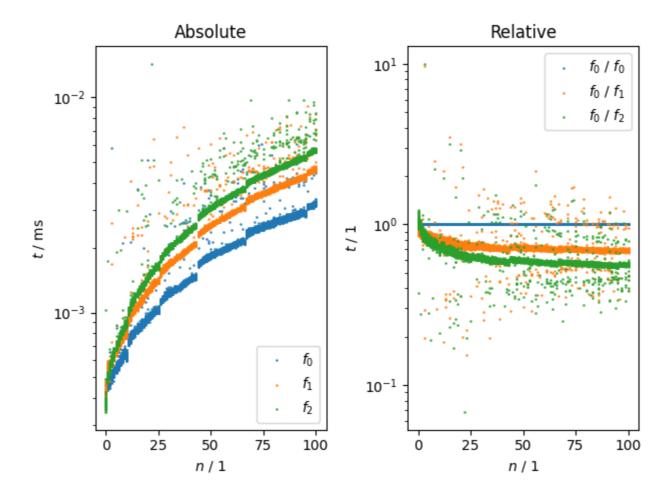
def mulelementwise1(v, w):
    return tuple(vi*wi for vi, wi in zip(v, w))

In [19]: x, y0, y1 = [], [], []
for _ in range(10000):
    v, w = randt(randint(0, 100)), randt(randint(0, 100))
    assert allclose(mulelementwise0(v, w), mulelementwise1(v, w))
    x += [min(len(v), len(w))]
    y0 += [timeit(lambda: mulelementwise0(v, w), number=N) / N]
    y1 += [timeit(lambda: mulelementwise1(v, w), number=N) / N]
    compare(x, y0, y1)
```



div

```
In [20]: from operator import truediv
         def div0(v, a):
             return tuple(map(truediv, v, repeat(a)))
         def div1(v, a):
             return tuple(vi/a for vi in v)
         def div2(v, a):
             return tuple(map(lambda vi: vi/a, v))
In [21]: x, y0, y1, y2 = [], [], []
         for _ in range(10000):
             a, v = random(), randt(randint(0, 100))
             assert allclose(div0(v, a), div1(v, a), div2(v, a))
             x += [len(v)]
             y0 += [timeit(lambda: div0(v, a), number=N) / N]
             y1 += [timeit(lambda: div1(v, a), number=N) / N]
             y2 += [timeit(lambda: div2(v, a), number=N) / N]
         compare(x, y0, y1, y2)
```



divelementwise

```
In [22]: def divelementwise0(v, w):
    return tuple(map(truediv, v, w))

def divelementwise1(v, w):
    return tuple(vi/wi for vi, wi in zip(v, w))

In [23]:

x, y0, y1 = [], [], []
for _ in range(10000):
    v, w = randt(randint(0, 100)), randt(randint(0, 100))
    assert allclose(divelementwise0(v, w), divelementwise1(v, w))
    x += [min(len(v), len(w))]
    y0 += [timeit(lambda: divelementwise0(v, w), number=N) / N]
    y1 += [timeit(lambda: divelementwise1(v, w), number=N) / N]
    compare(x, y0, y1)
```

