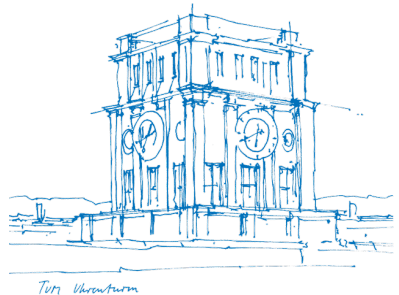


Introduction to Python for MLcomm

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Machine Learning for Communications – TUM LNT

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Overview

Introduction

Python Basics

Libraries for Numerical Computations

- NumPy

- SciPy

- Pandas

Outlook

Practice problems

What is Python?

- Python is an **interpreted, non-statically** typed¹ language.
- It supports different programming paradigms (functional, object-oriented, imperative, etc.).
- It supports **all major operating systems** and comes with a **huge standard library**.
- Python as a language has **different implementations**:
 - CPython – standard, reference implementation.
 - PyPy – based on a just-in-time (JIT) compiler. Major speedups compared to CPython.
 - Cython – compiles Python to C.
- Python is **open source**.

¹Since Python 3.5 type hints are possible and should be used extensively. See also PEP483, PEP484.

Why Python for ML?

- Python has established a **good reputation** in the data science field.
- It is a language that is **easy to start with**.
- It is freely available (compare²: Matlab 2000 Euro + Statistics and Machine Learning toolbox: 1000 Euro).

²<https://de.mathworks.com/pricing-licensing.html>

³<https://www.tensorflow.org/>

⁴<https://keras.io/>

⁵<http://scikit-learn.org/>

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- **Extend your horizon**: There's a world beyond Matlab.

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Programming Environment: Jupyter Notebooks

- Following **good practice** in the ML community, we use **Jupyter Notebooks**⁶.



- Provides an interactive console, where you can type in commands which facilitates trial & error.
- Can be installed locally on Windows, Linux and Mac: Use the **Anaconda distribution**⁷.

⁶<http://jupyter.org/>

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But there is also an easier way . . .

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Programming Environment: Google Colab (I)

- Google provides hosted Jupyter Notebooks.

CO Hello, Colaboratory

File Edit View Insert Runtime Tools Help

CODE TEXT CELL CELL COPY TO DRIVE

Table of contents Code snippets Files X

Getting Started

Highlighted Features

- TensorFlow execution
- GitHub
- Visualization
- Forms
- Examples
- Local runtime support

SECTION

Welcome to Colaboratory!

Colaboratory is a free Jupyter notebook environment that requires no setup and runs entirely in the cloud. See our [FAQ](#).

Getting Started

- [Overview of Colaboratory](#)
- [Loading and saving data: Local files, Drive, Sheets, Google Cloud Storage](#)
- [Importing libraries and installing dependencies](#)
- [Using Google Cloud BigQuery](#)
- [Forms, Charts, Markdown, & Widgets](#)
- [TensorFlow with GPU](#)
- [TensorFlow with TPU](#)
- [Machine Learning Crash Course: Intro to Pandas & First Steps with TensorFlow](#)
- [Using Colab with GitHub](#)

Highlighted Features

Seedbank

Looking for Colab notebooks to learn from? Check out [Seedbank](#), a place to discover interactive machine learning examples.

TensorFlow execution

Colaboratory allows you to execute TensorFlow code in your browser with a single click. The example below adds two matrices.

$$\begin{bmatrix} 1. & 1. & 1. \\ 1. & 1. & 1. \end{bmatrix} + \begin{bmatrix} 1. & 2. & 3. \\ 4. & 5. & 6. \end{bmatrix} = \begin{bmatrix} 2. & 3. & 4. \\ 5. & 6. & 7. \end{bmatrix}$$

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 - Might not be available in the evening, when all the west coast kiddies get up and start doing their homework.
- Drawback: You need a Google account for this. Sorry!

Python Basics

Basics: Data Types

Python 3 supports the following data types:

- Integers (`int`)
- Floats (`float`)
- Booleans (`bool`)
- Strings (`str`)
- Lists (`list`)
- Tuples (`tuple`)
- Sets (`set`)
- Dictionaries (`dict`)

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- Lists (`list`)
- Tuples (`tuple`)
- Sets (`set`)
- Dictionaries (`dict`)

The **methods** of each data type can be **inspected** via `help`, e.g., `help(int)`.

Basics: Data Types (Integer)

- Integer numbers (int):

```
>>> a = 5; type(a)  
<type 'int'>
```

- Important method/property: `.real`, `.imag`, `.conjugate()`

Basics: Data Types (Floats)

- Floating point numbers (float):

```
>>> a = 5.0; type(a)  
<type 'float'>
```

- Important methods: `.real`, `.imag`, `.conjugate()`

Basics: Data Types (Booleans)

- Booleans (bool):

```
>>> a = True; type(a)  
<type 'bool'>
```

Basics: Data Types (Strings)

- Strings (`str`):

```
>>> a = 'test'; type(a)
<type 'str'>
```

- Important methods: `.format()`, `.find()`, `.join()`, `.split()`.

Basics: Data Types (List)

- Lists (`list`):

```
>>> a = [1, 2, 3]; type(a)
<type 'list'>
>>> a[0]
1
```

- Sequence of arbitrary Python objects that **can be modified** (mutable) after it has been created.
- Builtin function `len()` returns the **number of objects** in the tuple.
- Important methods: `.append()`, `.extend()`, `.insert()`, `.remove()`.

Basics: Data Types (Tuples)

- Tuples (tuple):

```
>>> a = (1, 2, 3); type(a)
<type 'tuple'>
>>> a[0]
1
```

- Sequence of arbitrary Python objects that **can not be modified** (immutable) after it has been created.
- Builtin function `len()` returns the **number of objects** in the tuple.

Basics: Data Types (Sets)

- Sets (set):

```
>>> a = set((1,2,3,4)); type(a)
<type 'set'>
```

- A set object is an unordered, mutable collection of distinct Python objects, i.e., `set((1,2,3)) == set((3,2,1,1))`.
- Represents the mathematical concept of a set.
- Supports the associated mathematical operations `.intersection()`, `.union()`, `.difference()`.
- Builtin function `len()` returns the **number of objects** in the tuple.

Basics: Data Types (Dictionaries)

- Dictionary (dict):

```
>>> alphabet = {'a': 1, 'b': 2, 'c': 3}; type(alphabet)
<type 'dict'>
>>> alphabet['b']
2
```

- Build dictionary from list of keys and values:

```
d = dict(zip(mykeys, myvals))
```

- Important methods: `.keys()`, `.values()`, `.items()`.

Basics: Printing and Formatting (I)

- Printing is done via the `print()` function.
- Each string has a corresponding `format()` method.

```
>>> print('Hello {}'.format('Fabian'))
Hello Fabian!
>>> print('Hello {} {}'.format('Fabian', 'Steiner'))
Hello Fabian Steiner!
>>> print('Hello {firstname} {lastname}!'.
      format(firstname='Fabian', lastname='Steiner'))
Hello Fabian Steiner!
```

Basics: Printing and Formatting (II)

- Similar to C's `printf()`, several **format specifiers** are supported.
- Syntax of format specifiers: `<field_width>.<precision><data_type>`

```
>>> print('Num: {:d}'.format(2))
Num: 2
>>> print('Num: {:10d}'.format(2))
Num:          2
>>> print('Num: {:10d}'.format(223))
Num:         223
>>> print('Num: {:.3f}'.format(3.14159))
Num: 3.142
```

Basics: Conditions and If Statements

- Conditions:
equals: `a == b`, not equals: `a != b`, less then or equal to: `a <= b`, ...
- If Statements

```
if a == b:  
    print('a and b equal!')  
elif a < b:  
    print('a smaller than b!')  
else:  
    print('none of the two conditions is true!')
```

- **Indentation is important:** use four spaces
- This is how Python identifies blocks of code (cf. curly brackets in C, end in matlab)

Basics: Loops

- For Loops

```
for i in range(1,5):  
    print(i)
```

```
for i in [1,2,3,5,7]:  
    print(i)
```

- While Loops

```
i = 1  
while i <= 5  
    print(i)  
    i += 1
```

- **Indentation is important:** use four spaces

Basics: List comprehension

- Create lists from existing lists or an iterable object.

```
y = [x**2 for x in range(1, 10)]
```

- This can be combined with conditions.

```
y = [x**2 for x in mylist if x % 2 == 0]
```

- A n -dimensional extension is possible.

```
z = [x*y for x in mylist1 for y in mylist2]
```

Basics: Generators (I)

In many cases, a new list **should not be generated explicitly**, because the individual list members are not needed. Hence, memory can be saved.

- **Traditional**

```
res = sum( [x**2 for x in range(1,10)] )
```

- **Generator**

```
res = sum( (x**2 for x in range(1,10)) )
```

Basics: Generators (II)

More elaborate example:

```
def gen_combs(set1, set2):  
    l = []  
    for s1 in set1:  
        for s2 in set2:  
            l.append((s1,s2))  
    return l
```

```
def gen_combs(set1, set2):  
    for s1 in set1:  
        for s2 in set2:  
            yield (s1, s2)
```

```
>>> for item in gen_combs((1,2,3),(4,5,6)):  
    print(item)
```

Basics: Defining functions

```
def mysum(arg1, arg2):  
    result = arg1 + arg2  
    return result
```

- **Indentation** is important: Use four spaces.
- Automatic cleanup tool: `autopep8`.
- Functions help to **structure** your program and to write **reusable** code.

Basics: Functions with Type Annotations

```
def mysum(arg1: int, arg2: int): -> int
    result: int = arg1 + arg2
    return result
```

- As mentioned before, Python is **dynamically linked**.
- Since Python 3.5, **type annotations** in the code itself are possible.
- Very helpful for collaborations in teams and a large code base.
- Type annotations are not enforced by the interpreter.
- Complex or composite types are also possible, use `typing` module.
- Check out MyPy (<http://mypy-lang.org/>) for static type checking.

Basics: with Statement

- Many times you will encounter the following pattern:
 - Open a file/database connection.
 - Retrieve and work with the data.
 - Close the connection.
- For convenience, Python **takes care of the opening and closing**:

```
>>> with open('file.txt') as f:
        data = f.read()
        print(item)
>>> f.read()
Traceback (most recent call last):
  File "<stdin>", line 1, in <module>
ValueError: I/O operation on closed file.
```

Basics: Organizing your code (I)

- To avoid **clogging your namespace**, put your code into separate files and **import** them if required.
- Example: File `ml_tools.py` with function `entr()`.

```
>>> import ml_tools  
>>> H = ml_tools.entr([0.3, 0.7])
```

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- Example: File `ml_tools.py` with function `entr()`.

```
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```

- If the import name is too long, it can be abbreviated by `import longname as ln`.
- For larger code bases, **modules** are more appropriate.
- For this, we first create the **module folder** `mlcomm`, mark it as a module for Python by placing an **empty `__init__.py` file** and then add the corresponding files.

Basics: Organizing your code (II)

An example module may look like:

```
mlcomm
├── __init__.py
├── tools
│   ├── __init__.py
│   └── it.py
└── em
    ├── __init__.py
    └── em.py
```

The individual parts can be imported as (inspect your namespace with `dir()` afterwards):

```
>>> from mlcomm import em
>>> import mlcomm.tools.it
```

Basics: LBYL vs. EAFP / Exception handling

LBYL

Look before you leap.

EAFP

Easier to ask for forgiveness than permission.

Basics: LBYL vs. EAFP / Exception handling

LBYL

Look before you leap.

EAFP

Easier to ask for forgiveness than permission.

Python's paradigm follows the EAFP style:

```
>>> d = {'name': ['Peter', 'George'], 'age': [20, 30]}
>>> try:
...     places = d['places']
... except KeyError:
...     print('No key named places')
...     places = None
No key named places
```

Coding Style

- You do not write code for yourself, but for others to read it.
- Additionally, you read your own code more often than you will actually write it.
- It is **essential** to stick to a **good practice and common conventions**.

⁸<https://www.python.org/dev/peps/pep-0008/>

Coding Style

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- Additionally, you read your own code more often than you will actually write it.
- It is **essential** to stick to a **good practice and common conventions**.
- For Python, these rules are summarized in PEP8⁸.
 - Naming conventions for variables, functions, classes.
 - Indentation style.
 - Comment style.
- **Stick to it.** Every (reasonable) company/project leader will enforce this as well!

⁸<https://www.python.org/dev/peps/pep-0008/>

Libraries for Numerical Computations

NumPy

- NumPy is the fundamental package for numerical computing with Python.
- It provides
 - functions for dealing with n -dimensional arrays,
 - various mathematical functions,
 - a Matlab-like interface.
- NumPy uses 0-based indexing.
- NumPy assigns by reference.
- Import NumPy into your code as

```
>>> import numpy as np
```

NumPy: Arrays (I)

- Create matrix $\begin{pmatrix} 1 & 2 \\ 3 & 4 \end{pmatrix}$:

```
>>> a = np.array([[1, 2], [3, 4]])
```

- Index single element

```
>>> a[0,1]
```

- Index first row:

```
>>> a[0,:]
```

- Index first column:

```
>>> a[:,0]
```

NumPy: Arrays (II)

- Get size

```
>>> a.shape
```

- Get number of elements

```
>>> a.size
```

- Vertically concatenate the arrays a and b:

```
>>> c = vstack((a,b))
```

- Horizontally concatenate the arrays a and b:

```
>>> c = hstack((a,b))
```

NumPy: Arrays (III)

- Serialize array

```
>>> a.flatten()
```

- Create zero 3×3 matrix

```
>>> a = np.zeros((3,3))
```

- Create 3×3 all ones matrix

```
>>> a = np.ones((3,3))
```

- Create 3×3 identity matrix

```
>>> a = np.eye(3)
```

NumPy: Arrays (IV)

- Create list of values ranging from 1.0 to 4.9 in step sizes of 0.1.

```
>>> a = np.arange(1.0,5.0,0.1)
```

- Transpose.

```
>>> a.T
```

- Conjugate transpose, i.e., Hermitian.

```
>>> a.conj().T
```

NumPy: Linear Algebra

- Inner product of two vectors (1D arrays) a and b .

```
>>> a.dot(b)
```

- Matrix-vector product of matrix A and vector b .

```
>>> A.dot(b)
```

- Matrix-matrix product of matrix A and matrix B .

```
>>> A.dot(B)
```

- Componentwise product of two matrices A and B .

```
>>> A*B
```


NumPy: Broadcasting

- We want to apply a certain operation to all columns or rows of a matrix.
- Example: Add the vector $(10 \ 10)$ to all rows of the matrix $\begin{pmatrix} 1 & 2 \\ 3 & 4 \end{pmatrix}$:

NumPy: Broadcasting

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- Example: Add the vector $(10 \ 10)$ to all rows of the matrix $\begin{pmatrix} 1 & 2 \\ 3 & 4 \end{pmatrix}$:

```
>>> A = np.array([[1,2], [3, 4]])  
>>> B = A + np.array([10, 10])  
>>> B  
array([[11, 12],  
       [13, 14]])
```

- This operation is called **broadcasting** in NumPy. It's a powerful tool!

NumPy: Random Numbers

- Create vector of n normally distributed random numbers:

```
>>> N = np.random.randn(n)
```

- Create vector of n uniformly distributed, integer random numbers between lb and ub:

```
>>> N = np.random.randint(lb, ub + 1)
```

- For more, see `help(np.random)`.

NumPy: Passing by reference (I)

```
>>> a = np.array([[1,2], [3,4]])
>>> a
array([[1, 2],
       [3, 4]])
>>> b = a[:,0]
>>> b
array([1, 3])
>>> b[:] = 8
>>> a
array([[8, 2],
       [8, 4]])
```

NumPy: Passing by reference (II)

- If **real copies** are needed:

```
>>> a = np.array([[1,2], [3,4]])  
>>> b = a.copy()  
>>> c = a[:,0].copy()
```

NumPy: Importing Data

- Read simple text files:

```
>>> data = np.loadtxt('filename.txt')
```

- Save simple text files:

```
>>> np.savetxt('filename.txt', data)
```

- Detailed reference of all parameters can be found online⁹.

⁹<https://docs.scipy.org/doc/numpy-1.13.0/reference/generated/numpy.loadtxt.html>

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>>> data = np.loadtxt('filename.txt')
```

- Save simple text files:

```
>>> np.savetxt('filename.txt', data)
```

- Detailed reference of all parameters can be found online⁹.
- Read Matlab files:

```
>>> data = scipy.io.loadmat('filename.mat')
```

⁹<https://docs.scipy.org/doc/numpy-1.13.0/reference/generated/numpy.loadtxt.html>

NumPy: Plotting (I)

- Import the necessary functionality:

```
>>> import matplotlib.pyplot as plt
```

- Generate data and plot:

```
>>> x = np.linspace(1,10,10)
>>> y = 2*x
>>> plt.plot(x, y)
>>> plt.show()
```

- Result can be saved with

```
>>> plt.savefig('fig.png')
```


NumPy: Plotting (II)

- Exposed interface is **similar to the Matlab plotting** functionality.
- If **logarithmic plots** are desired:
 - `plt.semilogx(x,y)`
 - `plt.semilogy(x,y)`
 - `plt.loglog(x,y)`
- The **axis** can be modified via
 - `plt.xlabel('X-Label')`
 - `plt.ylabel('Y-Label')`
 - `plt.xlim((0, 10))`
 - `plt.ylim((0, 10))`

NumPy: Outlook

- Full NumPy reference¹⁰.
- Guide for users **transitioning from Matlab**¹¹.
- Use `timeit` module for benchmarking¹² small snippets of your code.
- Further information on improving NumPy performance¹³.

¹⁰<https://docs.scipy.org/doc/numpy/reference/>

¹¹<https://docs.scipy.org/doc/numpy-dev/user/numpy-for-matlab-users.html>

¹²<https://docs.python.org/2/library/timeit.html>

¹³<http://ipython-books.github.io/featured-01/>

SciPy

What's the relation¹⁴ of SciPy and NumPy?

“In an ideal world, NumPy would contain nothing but the array data type and the most basic operations: indexing, sorting, reshaping, basic elementwise functions, et cetera. All numerical code would reside in SciPy. However, one of NumPy's important goals is compatibility, so NumPy tries to retain all features supported by either of its predecessors. Thus NumPy contains some linear algebra functions, even though these more properly belong in SciPy. [...]”

¹⁴<https://www.scipy.org/scipylib/faq.html#id16>

SciPy

- The SciPy module therefore contains the actual numerical algorithms.
- Import module as

```
>>> import scipy as sc
```

- `sc.integrate`: Numerical integration, quadrature rules.
- `sc.optimize`: Constrained/unconstrained optimization algorithms, root finding.
- `sc.linalg`: Supersedes `np.linalg`.
- `sc.stats`: Implements various distributions, their PDFs, CDFs and moments.

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 - `sc.linalg`: Supersedes `np.linalg`.
 - `sc.stats`: Implements various distributions, their PDFs, CDFs and moments.
- Instead of re-inventing the wheel (numerical algorithms can be super hard to implement reliably!), use the provided ones.
 - But: Make always sure that they actually implement what you would like to have.

Pandas

- Machine learning is closely associated with “big data”.
- Before being able to work with big data, you first have to get it into Python.

Pandas

- Machine learning is closely associated with “big data”.
- Before being able to work with big data, you first have to get it into Python.
- Pandas provides convenient abstraction layers for handling data.
 - Reading and writing spreadsheets.
 - Sorting and viewing data.
 - Database-like access: joins, groups, pivoting.

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 - Exception handling.
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 - Object oriented programming: concept of objects and classes.
 - Virtual environments.
 - Extensions with own C modules.
- Play around yourself, write code and discuss with your colleagues.

Practice Problems

Practice problems I

The following simple tasks will help you to familiarize yourself with Python and to recap some of the basics that have been introduced.

1. Implement a function with the signature `discrete_entr`

```
def discrete_entr(pX): pass
```

that calculates the entropy of the provided distribution `pX`. Take care of a proper error checking. The entropy is defined as

$$\sum_{x \in \text{supp}(P_X)} -P_X(x) \log_2(P_X(x)).$$

Practice problems II

2. Implement a function with the signature `discrete_cross_entr`

```
def discrete_cross_entr(pX, pY): pass
```

that calculates the cross-entropy of the distributions p_X and p_Y . Take care of a proper error checking and write a unit test. The cross entropy is defined as

$$\sum_{x \in \text{supp}(P_X)} -P_X(x) \log_2(P_Y(x)).$$

Practice problems III

3. Implement a function with the signature `discrete_kl_div`

```
def discrete_kl_div(pX, pY): pass
```

that calculates the Kullback-Leibler divergence of the distributions p_X and p_Y . Take care of a proper error checking and write a unit test. The Kullback-Leibler divergence is defined as

$$\sum_{x \in \text{supp}(P_X)} P_X(x) \log_2 \left(\frac{P_X(x)}{P_Y(x)} \right).$$

Practice problems IV

4. Implement a function with the signature `act_fct`

```
def act_fct(x, type_fct): pass
```

that returns the value of different activation functions evaluated at x depending on the `type_fct` parameter:

- Identity (`identity`): $y = f(x) = x$.
- Sigmoid (`sigmoid`): $y = f(x) = \frac{1}{1+e^{-x}}$.
- Tanh (`tanh`): $y = f(x) = \tanh(x)$.
- Rectified linear unit (`rect_lin_unit`): $y = f(x) = \max(0, x)$.